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Networks and Dragons: A data-driven approach to procedural dungeon generation

Angel Simeonov

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Supervisor: Dr. Rob Alexander

<insert dedication>

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Executive Summary

>At most two (2) pages, aimed a non-specialist, knowledgeable authorial peer. The summary must: –state the aim of the reported work, –motivate the work, –state methods used, –state results found, and –highlight any legal, social, ethical, professional, and commercial issues as appropriate to the topic of study (if none, then this should be explicitly stated).

1 Introduction

1.1 Role-playing games

Role-playing game (RPG) is a broad term encompassing a multitude of different games with often distinct mechanics and platforms of interaction (the media). The common factor between all RPGs is that the player(s) portray a fictional character and is involved in a fictional world (or a subset of one). The interaction of the players with this world is governed by rules, defined by the media. To better understand the structure of RPGs, we can view it in terms of two sets:

1. Rules defining how we play the game. Describe the allowed actions for the player at any given moment in the game.
2. Narrative elements. Provide the *purpose* of the players to interact with the fictional world.

The first set can be viewed as "How I interact with the environment" (functional) and the second as "What is the meaning of the environment" (narrative).

Computer RPGs like the Action RPG (ARPG) Legend of Zelda, Diablo, Fallout and many alike have both sets of rules defined by the game designers. A functional rule in an RPG like Skyrim is that you can attack with the left mouse button and a story element is that you are a Dragonborn with a quest. This quest is defined by the writers and designers of the game and as such exploring the narrative in a digital RPG can be comparable to an interactive reading of a fiction book. Good computer RPGs often have the ability to relax the narrative [1], allowing for the player to have more freedom in the exploration of the world and as such create the sensation that the player has some impact on this pre-programmed fictional environment.

The ability for a player to influence the narrative is one of the defining features of tabletop RPGs (TRPG a.k.a pen-and-paper PnP) like Dungeons and Dragons [2]. In them, the functional rules are usually defined by a rulebook (like the Player's Handbook) and players verbally describe their interactions with the environment. The narrative is an ever evolving

amalgam between the input of players and the Dungeon Master (DM). The DM's task is to create a narrative outline and guide the player interaction. Because of the verbal nature of the game, the narrative does not suffer the limitations of its digital counterparts. But because there are no hard constraints to how the narrative is told, the DM has the non-trivial task of introducing consistency and outlining a structure for the story that would result in a compelling and ideally immersive experience for the players. This is often achieved by focusing the adventure's act on a particular and detailed location. These locations are often referred to as Dungeons and in practice can be anything from the villain's mansion or a beast's cave to a city under siege. A good dungeon design is crucial for creating a compelling narrative. The creative task of making the Dungeon is a laborious process. To facilitate that, academics and various gaming communities have been exploring different ways of automating Dungeon creation. We will refer to this process as Procedural Dungeon Generation (PDG). Arguably the greatest problem posed by automating PDG is answering the question of "What is a compelling Dungeon?". In the next section we will review different generative methods for Dungeons and their associated limitations in an attempt to answer this question.

1.2 State of the Art Generative methods

1.2.1 Non-digital Generators

The designers of the classic PnP modules acknowledge the issue of Dungeon creation and often incorporate *Loot* or *Encounter* tables in the rule-books. The tables are a reference over a set of treasures or monsters respectively, which can be chosen by rolling the specified die **need figure of loot/encounter table**. As noted before, a PnP RPG can evolve rapidly outside the planned narrative structure prepared by the DM and a simple way to quickly define new adaptive story elements via a loot table can be useful. Some early modules even provided a step-by-step guide for creating a full campaign from the plot, villains' obsessions and story setting to the various encounters and and treasures [3] entirely based on randomised content tables. An issue arises when using loot tables when a randomly selected element from one table is contradicted by an item selected from another. **show an example from the ADND module**. It is up to the DM to resolve such disparities. As can be seen, this process although providing some degree of creative assistance, it does little to facilitate the laborious nature of creating elements for a compelling narrative. Furthermore, these methods pay no attention to providing guidance of what would mean a good Dungeon as they are occupied with solving global narrative questions. **Argue that DMs know what they want to do, they just need a facilitator**

that will create a dungeon based on their requirements ? citation needed for what people use dungeon generators for.

1.2.2 Digital Generators

It is important to note that PnP RPGs and the various genres of computer RPGs although differing in the mechanisms of interaction, they share the same narrative goal [4]. Therefore we will not limit ourselves to looking only at existing tabletop solutions. Unlike the original non-digital generators, computerised ones rarely allow for human input in the middle of the process. A generative algorithm would provide a DM with an interface that takes a set of parameters and produce a template of a game. The degree of complexity of this template is naturally dependent on the complexity of the algorithm itself. Because they aim to exclude the human designer from the process, the digital generators tend to focus on creating elaborate Dungeon spaces and struggle providing coherent semantic content [5], [6].

Cellular Automata

Cellular automata (CA) utilises a procedural generation mechanism in which a $N \times M$ grid space is mutated incrementally by a set of agents**[citation needed for CA and fig. showing agents in action?]**. The implementation of these mutation operators define if the CA will simulate erosion [7] or man-made structures such as rooms and corridors. The latter is the case of the donjon dungeon generator [8]. Its simplicity and degrees of customisations of both layout and style has made donjon a popular generator choice with more than 2500 generated dungeons in the last 12 hours and 100 donations in the last 3 months **[[citation needed?]]**. Despite its popularity, donjon (as well as other CA) implores purely random generation techniques which are only evaluated based on a notion of the solvability of the level. The criteria for donjon's level is only if each room is reachable (i.e. there is a path to each room). As it can be observed, although we have control over the input parameters for the topological randomness, the semantic elements (the contents, rather than the structure) of the dungeon are entirely arbitrary and often contradictory **[[citation of brown and thrall or elaboration?]]**. In terms of the aforementioned solvability, when accounting for reachability donjon does not take in account the randomly allocated locked doors as the key allocation is left at the DM's discretion. That ultimately limits the usefulness of the tool and only provides a skeleton for the dungeon. All information generated about the monsters, treasures and other quest elements are discarded by the DM **[[citation needed on how people use dungeon generators]]**

Constraint Propagators

Constraint Satisfaction Problems (CSPs) define a discrete set of variables with corresponding constraints that restrict the possible variable instantiations **[[cn of CSPs]]**. Dungeon generation has been described as a CSP on occasions where the variables and constraints define the layout **[[cn]]**, contents **[[cn]]** or both layout and content **[[cn]]** of a dungeon. Constraint Propagation (CP) is a particular method proven useful for solving CSP in the context of dungeon level generation. The algorithm selects a set of possible values for a particular variable and *propagates* the result to the rest of the variables, adjusting their possible values accordingly. If the selected value narrows another variable's possible values to the empty set, we infer that this instantiation is suboptimal and we backpropagate to the last viable solution and retry. Furthermore it can be generalised that if an instantiation for all variables that does not narrow any variable to the empty set exists, the level is solvable. Utilising this formalisation of the *solvability* of a level we can populate a level with varying degrees of complexity from ensuring that keys are always spawned before the door that they must unlock to adjusting difficulty by measuring survivability metrics between rooms **[[cn]]**. Even though CPs have solved some problems of the completely random generators, formulating a numerical constraint for a narrative element can be difficult. The complication is both in the translation of a story element to a numerical representation and in the computational expense that comes with computing large amounts of permutations.

Binary Partitioning

Formal Languages

Data-driven approaches

1.3 Mission and Space

An attentive reader would have noted that distinguishing between the level layout and contents is a common occurrence in popular PDG algorithms. This discrimination was formalised by Dormans[9] in his definitions of *Mission* and *Space* in relation to the ARPG Legend of Zelda game series. The *Space* of a dungeon embodies its topological structure and can be encoded as an undirected cyclic graph where each vertex is a room and each edge is a door or corridor. The *Mission* is the set of narrative tasks the player must accomplish in order for him to complete the dungeon. It can be encoded as a directed graph where each vertex is the objective and the edge directions show the required sequence of completion. It is

clear to see that the gameplay experience is defined in the interaction of the two graphs. As noted by Dormans, a *Mission* mapped on different layouts will result in drastically different exploration patterns and it is by understanding the necessities of the two separate entities that we can model player experience better. Due to this separation we have seen advancements in generating adaptable to the player game environments [10] and even reverse engineering the creation of *Missions* and *Spaces* by learning structure from data [11].

1.4 Aim

The dungeon's topology (Space) and contents (Mission) are correlated and embody the narrative of the game. As we have seen, dungeon generators usually implore bottom up approaches in which they apply rules for topology and then introduce dungeon content in an attempt to provide the structure for a captivating narrative. The various algorithmic methods have clear strengths and shortcomings in achieving the complex goal of creating an interesting story. I want to argue that from these observations we can affirm that the ultimate *dungeon generator* is the human designer. Dungeons and therefore narratives produced by humans are the most compelling out of all created dungeons. As noted by others **[[cn]]**, if we implore a top-down approach of analysing what makes a good man-made dungeon, we could potentially achieve higher levels of narrative automation.

Deery made the first steps by manually analysing submissions to the One Page Dungeon Contest *OPDC* [12] to extract a graph grammar for Mission generation [13]. The Mission graph was then mapped to a physical Space in a 1:1 ratio. The result was that each room was limited to a single Mission element. It is trivial to see that the originals in OPDC do not impose such a restriction. One room can have multiple Mission elements (e.g. the key to unlocking the door is on the bandit's waist, Key + Encounter). Furthermore, Deery's approach was to manually look at 10 competition winners and heuristically extract the grammar rules, which he highlights that they do not capture all the possible patterns. An automated approach to learning would potentially solve that issue. Programmatically learning a level from data has been an object of interest for computer based RPGs [11], but has not been applied to PnP RPGs, presumably because of the lack of a consistent dataset.

In this paper we will investigate if applying a data-driven approach to learning the Space of the dungeon can produce a map that is undistinguishable from human-made dungeon topologies. We will define a meaningful

set of features to be extracted from the OPDC dataset and use those features as random variables defining an Inference (Bayesian) Network. Subsequently we compare different network structures and learning algorithms and internally assess which model has the greatest statistical predictive capabilities using various scoring rules. We will use the best model to generate a dungeon and conclude with a user study to externally validate how well the generator has approximated human-made dungeon topologies.

2 Bayesian Inference Networks

What are Bayesian networks? Bayesian Networks *BNs* [14] (also referred to as Inference Networks, Belief Networks, Directed Acyclic Graph (DAG) Models and others) are a graphical probabilistic model in which vertices are random variables *RVs* whose edges indicate causal beliefs. *BNs* assert that our domain is defined in terms of a joint probability distribution $PD\ P(X_1, \dots, X_n)$ over a set of *RVs* X , each of which has a set of potential values it can take $X_i(\Omega) = \{x_1, \dots, x_j\}$ with an associated *PD*. The network structure shows how the full join distribution factorises given the causal dependencies. This property gives us a way to encode our prior domain knowledge about the relationships between our *RVs*. Once we have encoded our knowledge about the *RV* interaction, using a *BN* as an inference tool is a matter of querying with a conditional set of *RVs* and noting how the *CPTs* change given our new knowledge. In practice, conditioning is done by *observing* (i.e. instantiating) an *RV* to be a particular value. Extracting information from our newly formed conditional distributions is done by sampling. Sampling involves simulating our network with respect to the observations in order to obtain point estimates. The sampling methodology will be discussed in 3.3.

To contextualise the inference process, we can look into Summerville's work on the Legend of Zelda dungeons [11]. After annotating the dungeon maps with elements of both Mission and Space (total number of rooms, treasures, monsters, critical path *CP*, etc.), he extracts features for the *BN* by parsing them as *RVs*. If we condition on total number of rooms (i.e. observe $P(NumRooms = n) = 1$), the *PD* for the possible *CP* would reflect our new knowledge. Most likely the *CPs* that are greater than the total number of rooms would be impossible $P(CriticalPathLength > n \mid NumRooms = n) \rightarrow 0$, which is logical. Then by sampling the network we can get a point estimate for critical path length given that number of rooms in the dungeon. This *observe-then-infer* process can be done with any permutation of our *RVs*.

Why use Bayesian networks? The reasoning behind choosing *BNs* is that the probabilistic causal structures have been shown to perform well in capturing properties from data for PDG tasks in ARPGs [11], [15]. Furthermore they give us a natural description about the dependencies in our model, which can be used as a supplemental analysis tool for

investigating human-made dungeons. As a PDG tool itself, the *observe-then-infer* pattern gives the user precise control over the desired properties of his dungeon without loss of automation. If a user observes a dungeon with 5 rooms and critical path of length of 3, they will be guaranteed in the final product. This solves the problem previous graph grammar data-driven approaches encountered, whereby the dungeon size input was used as an approximation for the actual number of rooms in the dungeon [13].

The downside of BNs is that their generalisation capabilities are highly dependent on the availability of data. If conditioning on an undefined set (e.g. there was never a data entry that showed a 5 room dungeon with CP of 3), the inference will fail. A proposed way to solve this issue is by creating artificial data entries for the undefined cases. We will use linear interpolation due to its simplicity and the fact it has been shown to produce good results in general [16] and exceptional results on small datasets [17]. This can potentially solve the problems of undefined dungeons within the range of sizes of our dataset, but it cannot extrapolate to infer arbitrarily large dungeons. We would argue that that generalisation is not necessary as we are trying to capture properties of One-Page dungeons which are designed to be small enough to be fit in a single gameplay session.

3 Methods and Implementation

3.1 Data acquisition

3.1.1 Data selection

Unsurprisingly the first priority of a data-driven method is the acquisition of a suitable dataset. The criteria we have chosen for our data is the following:

1. Data must be consistent. Dungeons have to be representatives of a similar and comparable category.
2. Data must be available under a research or similar open-source license.

The *OPDC* supplies a dataset that satisfies our requirements. All dungeons are in the same category of a one-session long dungeon and each dungeon is issued under Creative Commons CC license. Furthermore due to the fact that it is a competition, we have an exemplar answer of our main question "What makes compelling dungeon?" in the form of the competition winners. We apply the first filter and review only entries by competition winners. Due to the creative freedom the human designers have, it is naïve to assume that the dungeon Space is necessarily a dominant factor in all dungeons. In order to narrow down to dungeons that do have a consistent representation of Space as an important asset, we apply a second filter by omitting dungeons that have:

1. exclusively linear topologies
2. no map (no Space)
3. non-standard Space traversal (the map topology is ignored due to a functional mechanism e.g. time-travel, game of political control, etc.)
4. inconsistent map (our Space parameters are allowed to change e.g. intrigue campaigns where the objective constantly changes locations)
5. no goal defined by the designer (introduces the same problem as 4.)

3.1.2 Extracting Features

We will base our feature selection on the work done by Summerville [15] by selecting Space related parameters from his Extreme Sparse model due to its simplicity and effectiveness. We extract five parameters in two categories:

1. Dungeon (Global): total number of rooms and how many rooms are on the critical path
2. Room (Local): depth (how far away the room is from the entrance), critical path distance (how far away is the room from a critical path room, 0 indicates it is on the CP), total number of neighbours

Each global and local set of parameters is defined by the joint PDs respectively $P(\text{NumRooms}, \text{CPLength})$ and $P(\text{CPDistance}, \text{Depth}, \text{Neighbours})$. A full dungeon is therefore characterised by

$$P(\text{NumRooms}, \text{CPLength}) \prod_{i=1}^R P(\text{CPDistance}_i, \text{Depth}_i, \text{Neighbours}_i)$$

where R is the total number of rooms defined by the instantiation of *NumRooms*. To extract the five parameters the artistic and graphically rich textual representation of a dungeon in our dataset need to be transformed. Unfortunately automating feature extraction is very difficult due to the variant stylistic formatting and the prose like description of the tasks. Because of this, we establish a systematic way of manually annotating the Space of the dungeon as an abstract undirected graph from which we can calculate all the different parameters as shown in **[[insert figure of 2015 Sepulchre of the Abyss transcriptions]]**.

TODO: Filling in the data gaps. Linear interpolation and artificial datapoints

The final dataset is saved in a CSV format and consists of **[[size]]** organic entries and **[[synthetic]]** linearly interpolated entries for a total of **[[dungeon params]]** and **[[room params]]** with dungeon sizes ranging from **[[min]]-[[max]]** rooms.

3.2 Model selection

What we need to do to use Bayesian Networks? We need to define two key attributes of the BN:

1. The causal network's topology
2. Conditional probability tables *CPTs* for each RV

In this paper we will apply an empirical approach and evaluate different models in search of the model with highest statistical predictive capabilities. We will compare two structures with three CPT learning algorithms for a total of six models. The structures are the previously proposed Extreme Sparse model [15] (modified for Space only) and an automatically learned structure using the Tree Augmented Naïve Bayes. The CPT learning algorithms will be a simple joint occurrence count, Expectation Maximisation *EM* and Gradient Descent *GD*. Implementation of all BN related algorithms is done in the Netica Bayesian Network development software [18].

3.2.1 Bayesian Network topology

Summerville's Extreme Sparse Model *SESM*

In exploring data-driven PDG for the Legend of Zelda franchise, Summerville found out that when dealing with a small dataset (38 dungeons with 1031 rooms), the *SESM* is able to capture high level properties of both Mission and Space with the highest accuracy in respect to the learning criteria and the lowest complexity. Following our assertion that digital RPGs differ from PnP RPGs only in mechanisms of interaction, we will base one of our BN topologies on Summerville's work. In order to do so, we flatten down the graph to use only the Space parameters we have extracted from the OPDC data. We reconstruct the *SESM* in Netica and apply the `AbsorbNodes_bn` [19, pp. 62–63] which allows us to remove the unused Mission RVs by effectively setting them as constants and propagating any implied dependencies from the other nodes. In this way we remove the unused RVs and maintain the joint distribution dependencies between our Space parameters. The transformation can be seen in 3.1

Ignoring Mission parameters does reduce the dimensions of the model and can potentially reduce predictive capabilities.

3 Methods and Implementation

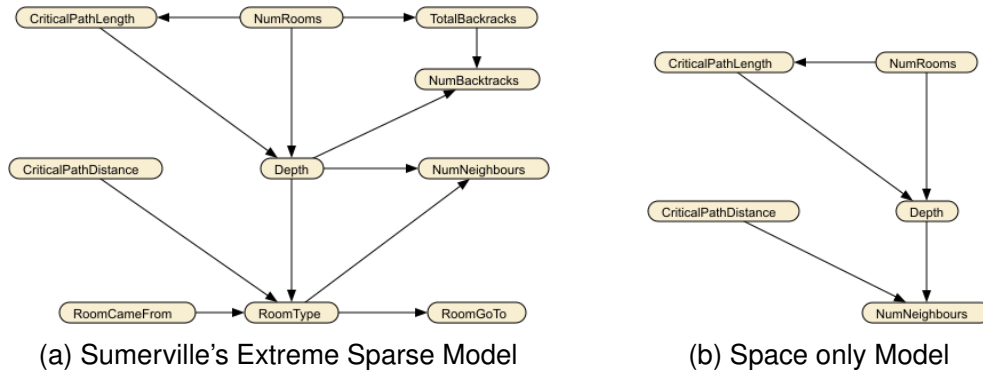


Figure 3.1: Bayesian Network topologies in Netica

TAN

3.2.2 Parameter Learning

Count

Expectation Maximisation EM

Gradient Descent GD

3.3 Implementation

Dungeon Sampling We can define characteristics of the desired dungeon by leveraging the inference nature of BNs. Generating a dungeon with five rooms is a matter of fixing (*observing*) the `NumRooms` parameter. The user can choose virtually any permutation of parameters to be fixed or inferred. For consistency purposes we are observing only the size of the dungeon via `NumRooms`.

Room Sampling

Converting from samples to Space

4 Results

	Count			EM			GD		
	log	quad	sphere	log	quad	sphere	log	quad	sphere
Extreme Sparse									
TAN									

Table 4.1: Structure and parameter learning comparison.

4.1 External Validation

5 Discussion

5.1 Critique

1. Data

- a) availability and extraction.
 - i. Could extend to include even non-winning entries for the sake of having a greater sample size. More datasets can be considered. We've use OPDC due to its CC license, but paid modules exist.
 - ii. Data extraction has been a manual process. Although due diligence is paid, noise introduced from human error is inevitable.

2. Method

- a) Cannot generalise to unseen cases. We can interpolate for missing data, but we cannot extrapolate. Argue that this is an issue of all ML approaches, not just BNets, because we're trying to capture properties of One-Page dungeon.
- b) This paper is considering only Space gen. A more robust approach would be needed to extract consistent and meaningful parameters for Mission. For Legend of Zelda there is a discrete subset of things you can do so that is why Mission extraction is possible. Deery has shown that formalising Mission in PnP RPG's is difficult due to the variant and creative nature of the human-made dungeons.

3. Validation

- a) We have decided to approach the external evaluation in a quantitative, rather qualitative measuring. That is due to the fact that conducting a study with a high environmental index is difficult due to multiple confound factors that are due to the nature of a tabletop RPG session. Not only does a one-session adventure usually take around 3 hours **[[cn]]**, but they are extremely variant between groups of players and DMs. An experiment that analyses how players use the generated dungeon rather

5 Discussion

than just discriminating between different dungeons topologies would give us more insight in the success of the recreation of a human-made dungeon.

6 Conclusion

6.0.1 Future Work

1. Rerun with more data (OPDC is conducted every year)
2. Automate the Feature Extraction process (OCR + NLP)
3. Incorporate Mission parameters as well
4. Analyse PnP specific dungeons and find more parameters that might be useful. E.g. size of rooms, multiple CPs,
5. Conduct a study with greater environmental impact (e.g. actually get people to play instead of using an aesthetics study)

A Some appendix

Use this section for graphical showing of the models. Nets, result tables (or tables should be inline?)

B Another appendix

Use this section for questionnaires and external validation support

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