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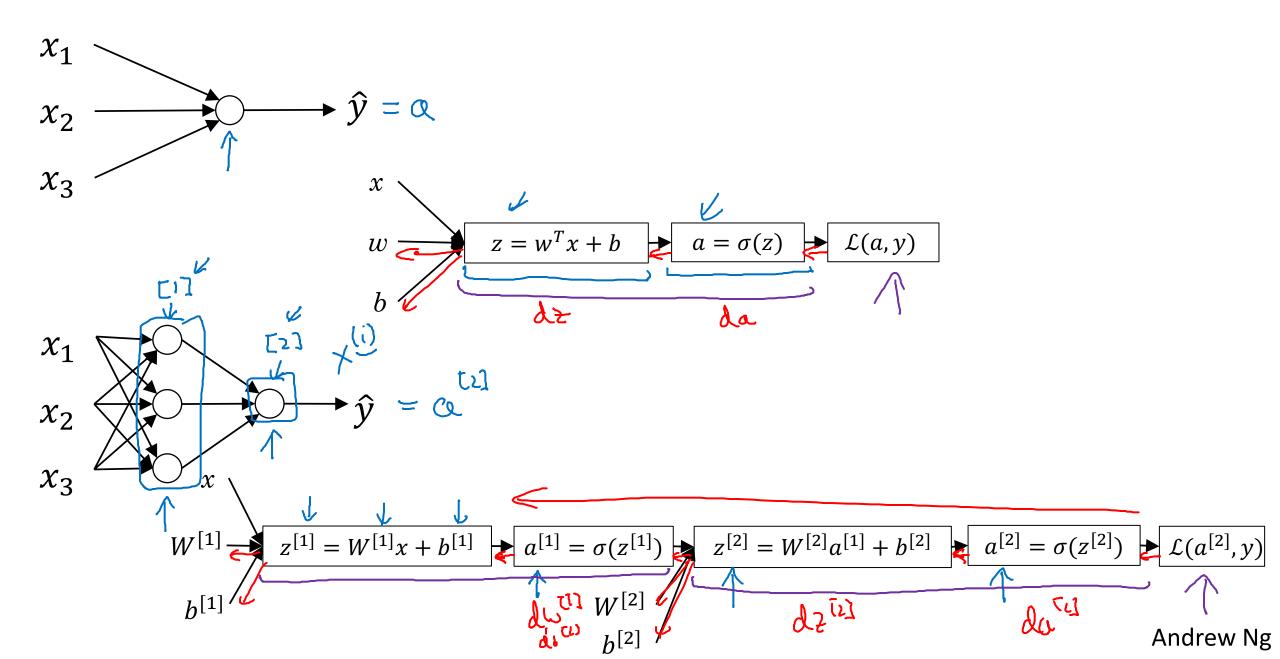
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One hidden layer Neural Network

Neural Networks Overview

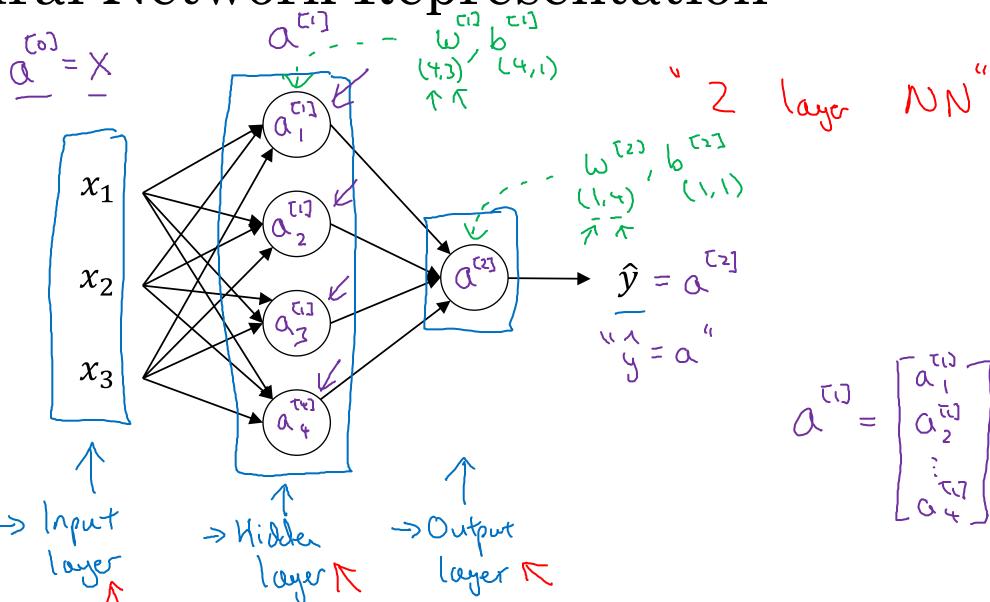
What is a Neural Network?





One hidden layer Neural Network

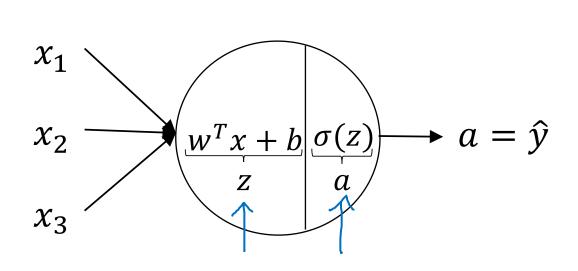
Neural Network Representation



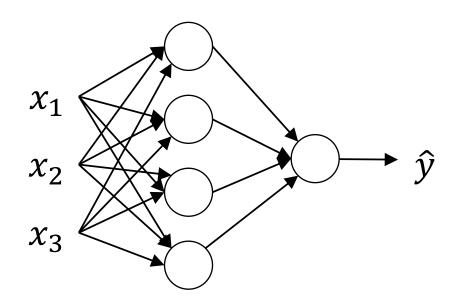


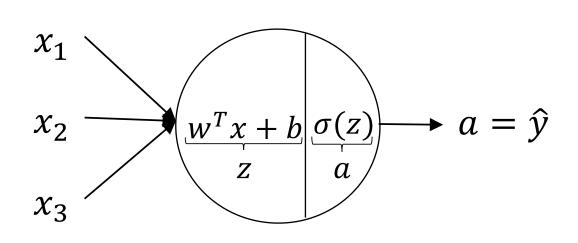
One hidden layer Neural Network

Computing a Neural Network's Output

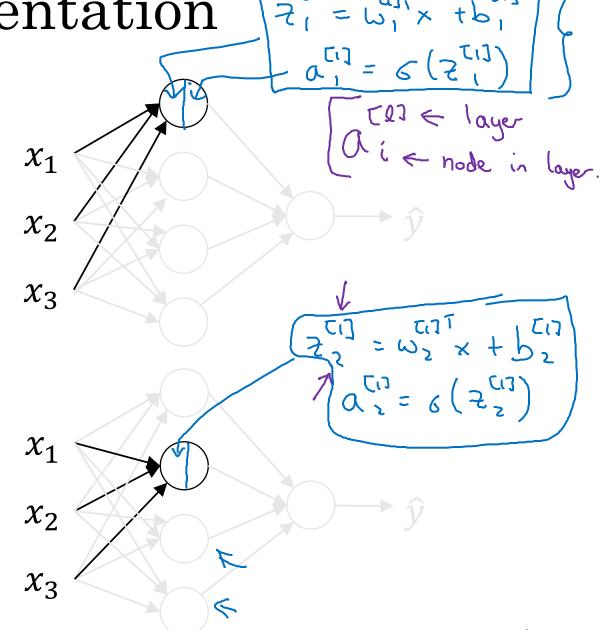


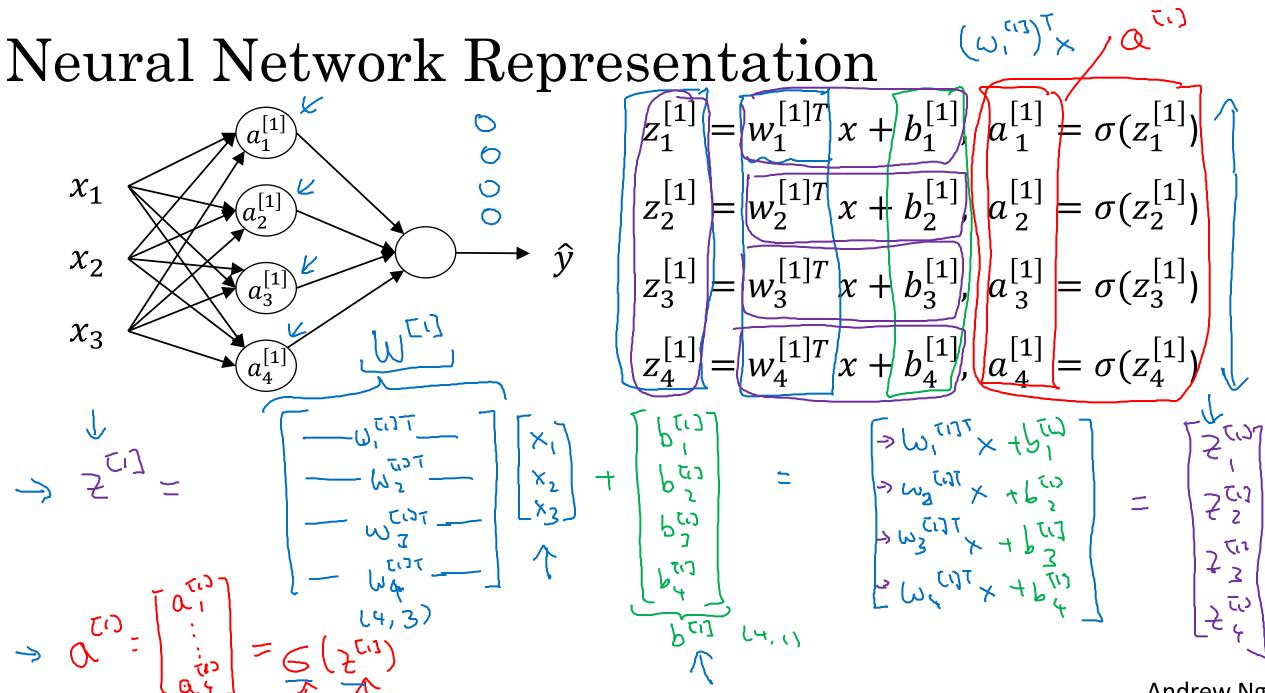
$$z = w^T x + b$$
$$a = \sigma(z)$$





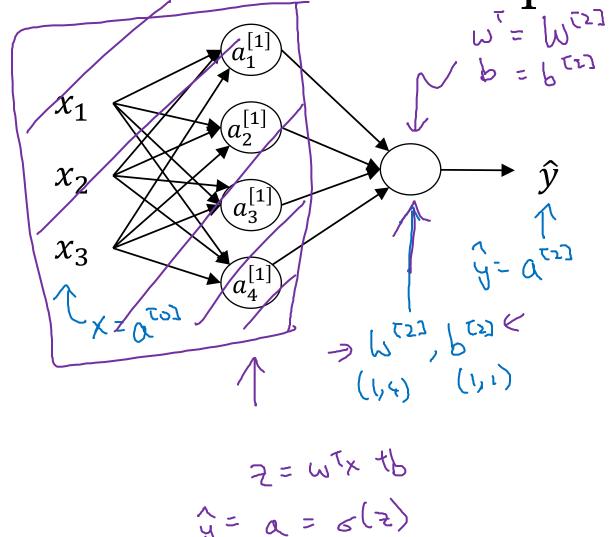
$$z = w^T x + b$$
$$a = \sigma(z)$$





Andrew Ng

Neural Network Representation learning



Given input x:

$$z^{[1]} = W^{[1]} + b^{[1]}$$

$$(4,1) = \sigma(z^{[1]})$$

$$(4,1) = (4,1)$$

$$z^{[2]} = W^{[2]} a^{[1]} + b^{[2]}$$

$$(1,1) = (1,4) + b^{[2]}$$

$$(1,1) = (1,4) + b^{[2]}$$

$$(1,1) = (1,4) + b^{[2]}$$

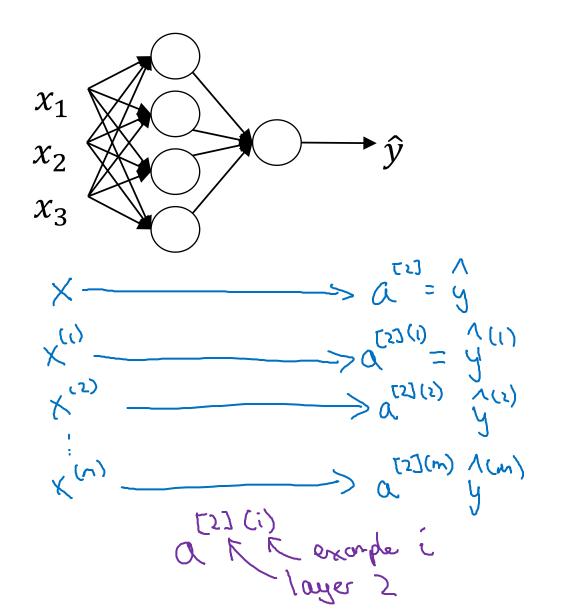
$$(1,1) = (1,1) + b^{[2]}$$

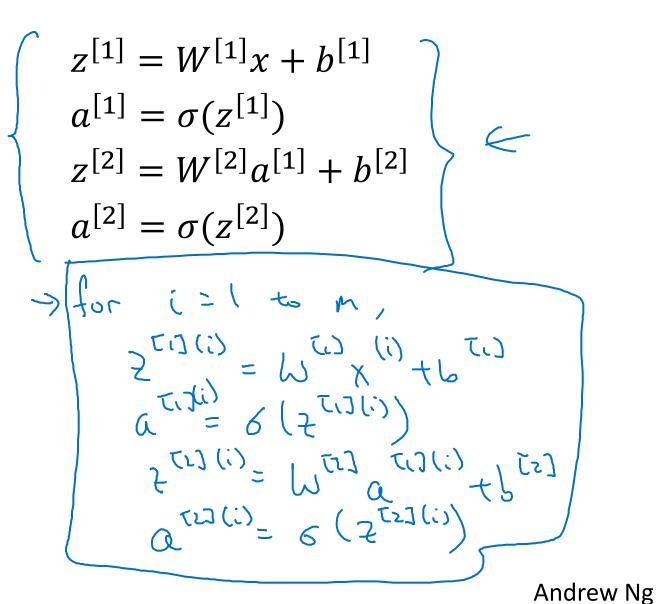


One hidden layer Neural Network

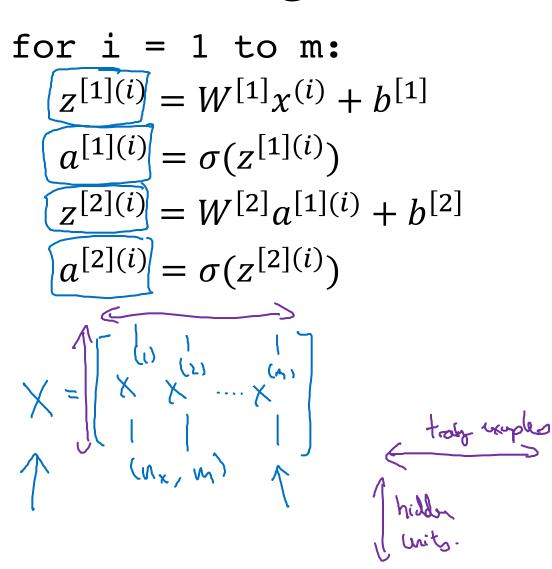
Vectorizing across multiple examples

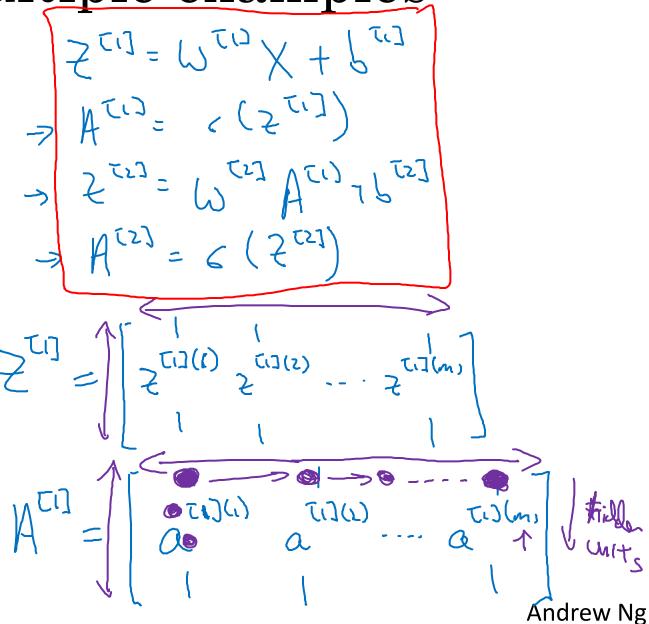
Vectorizing across multiple examples





Vectorizing across multiple examples



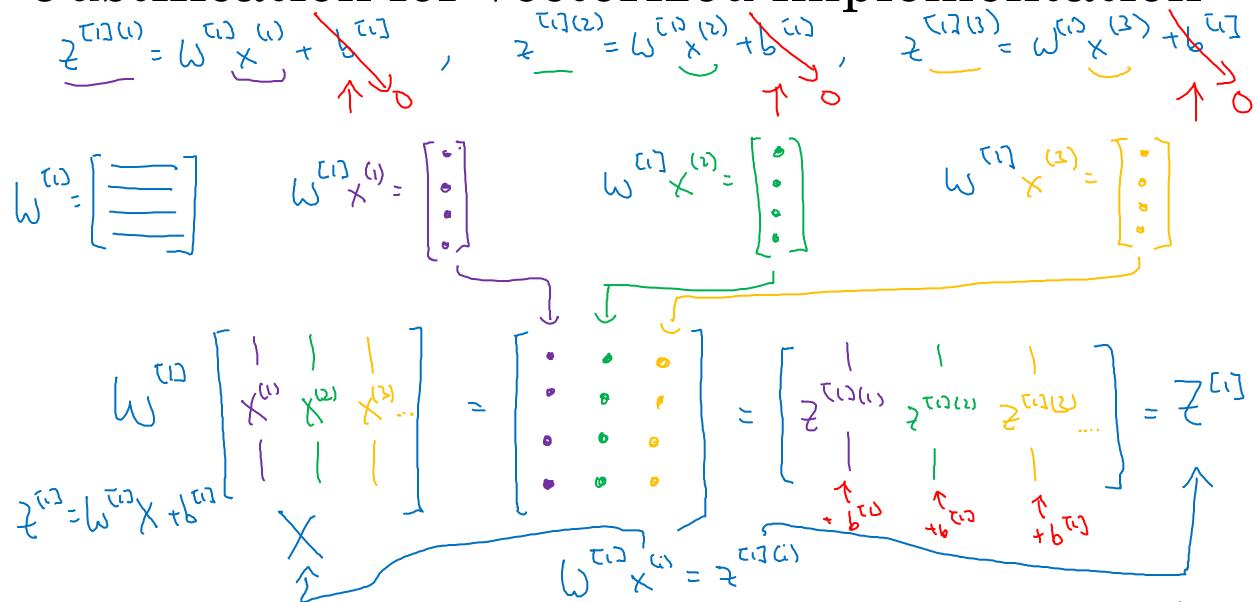




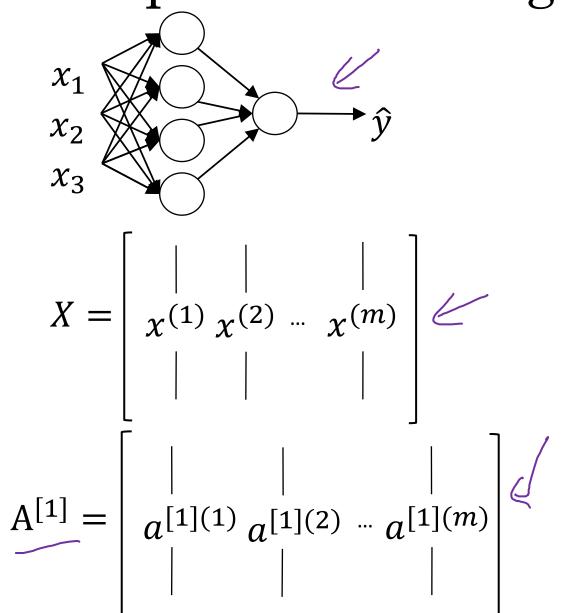
One hidden layer Neural Network

Explanation for vectorized implementation

Justification for vectorized implementation



Recap of vectorizing across multiple examples



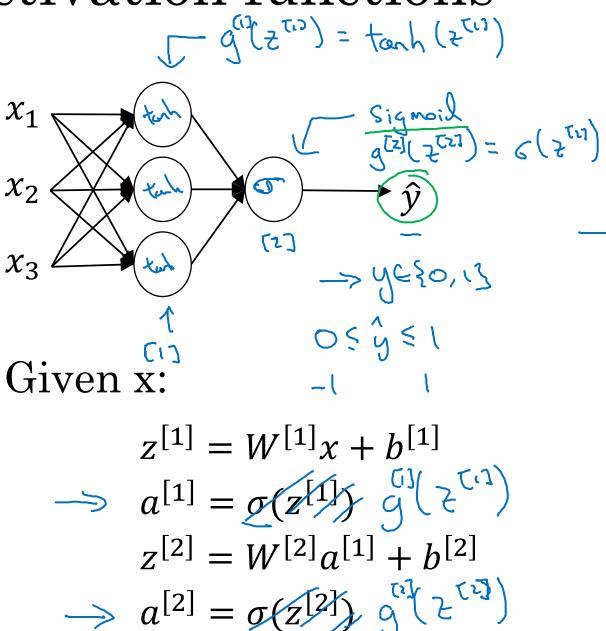
```
for i = 1 to m
                                     + z^{[1](i)} = W^{[1]}x^{(i)} + b^{[1]}
                                    \Rightarrow a^{[1](i)} = \sigma(z^{[1](i)})
                                  \Rightarrow z^{[2](i)} = W^{[2]}a^{[1](i)} + b^{[2]}
                            \Rightarrow a^{[2](i)} = \sigma(z^{[2](i)})
                                                                                                                                                                                                                      \chi = \alpha^{(0)} \quad \chi = \alpha^{(0)} \quad \chi^{(0)} = \alpha^{(0)
 Z^{[1]} = W^{[1]}X + b^{[1]} \leftarrow W^{[1]}X^{(0)} + b^{[1]}
         A^{[1]} = \sigma(Z^{[1]})
Z^{[2]} = W^{[2]}A^{[1]} + b^{[2]}
     A^{[2]} = \sigma(Z^{[2]})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Andrew Ng
```

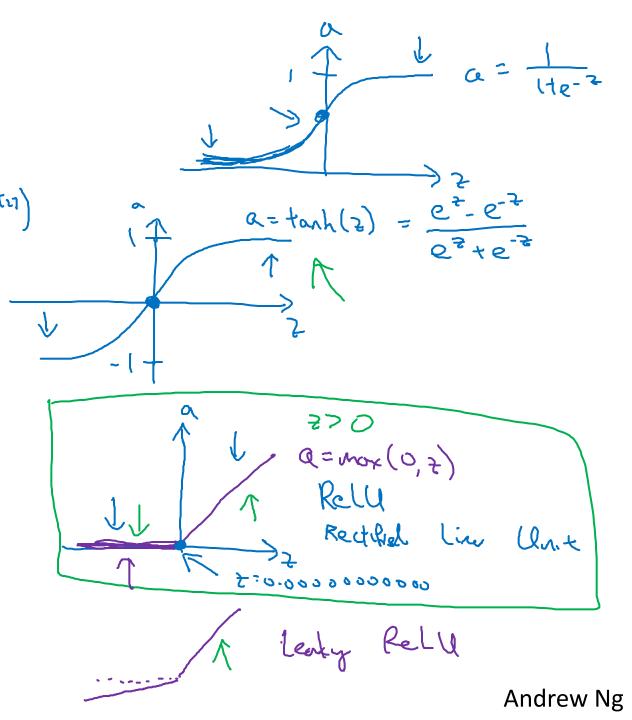


One hidden layer Neural Network

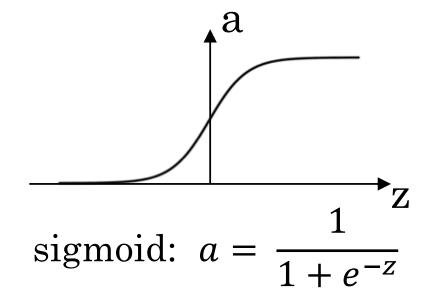
Activation functions

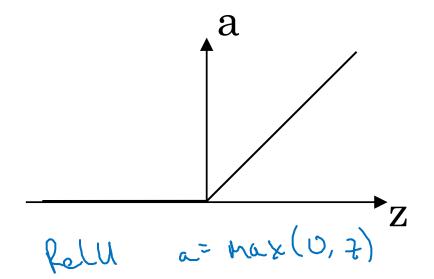
Activation functions

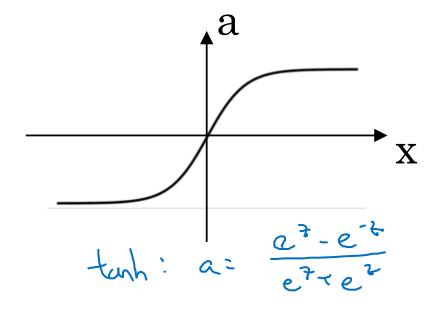


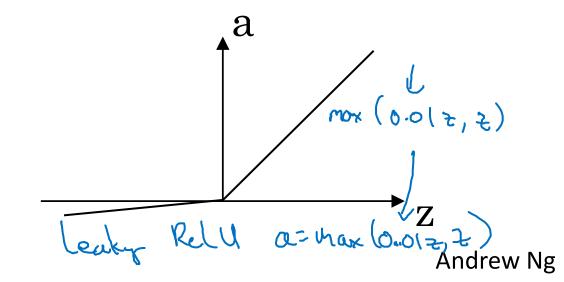


Pros and cons of activation functions







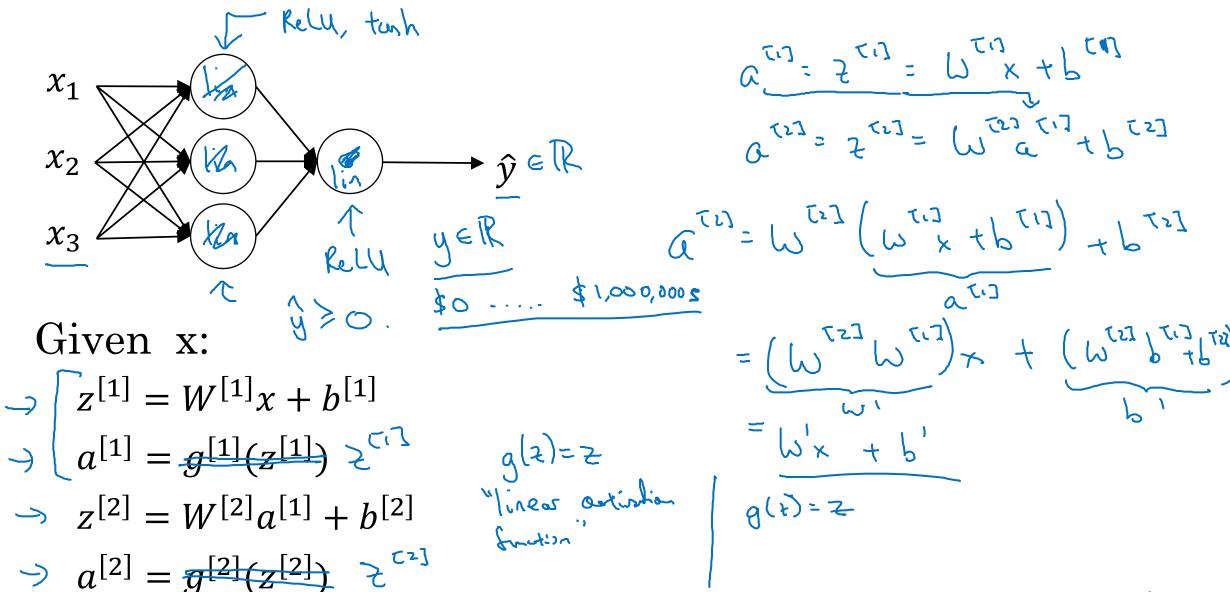




One hidden layer Neural Network

Why do you need non-linear activation functions?

Activation function





One hidden layer Neural Network

Derivatives of activation functions

Sigmoid activation function

$$g(z) = \frac{1}{1 + e^{-z}}$$

$$g(z) = \frac{1}{1 + e^{-z}}$$

$$a = g(z) = \frac{1}{1 + e^{-z}}$$

$$\frac{1}{1 + e^{-z}}$$

$$= \frac{1}{1 + e^{-z}}$$

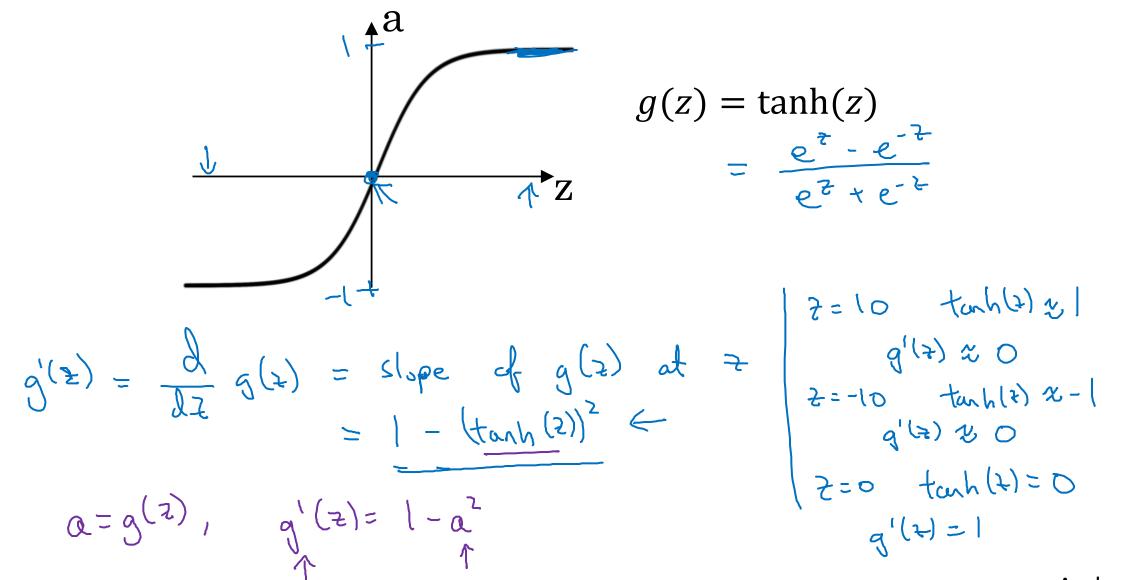
$$\frac{1}{1 + e^{-z}}$$

$$= \frac{1}{1 + e^{-z}}$$

$$\frac{1}{1 + e^{-z}}$$

$$\frac$$

Tanh activation function

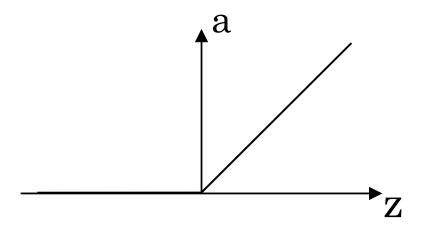


ReLU and Leaky ReLU

Sigmoide Perfetta per probabilità, ma inefficiente nelle reti profonde.

Tanh Migliore della sigmoide perché centrata in zero, ma soffre ancora del vanishing gradient.

ReLU La più usata oggi, perché è veloce e permette di allenare reti profonde. Leaky ReLU Versione migliorata della ReLU che evita il problema dei neuroni morti.

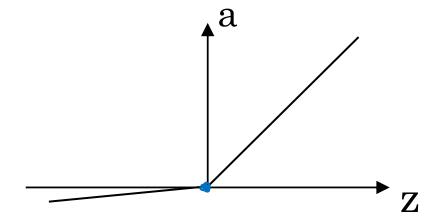


ReLU

$$g(t) = mox(0, t)$$

$$\Rightarrow g'(t) = \begin{cases} 0 & \text{if } t < 0 \\ 1 & \text{if } t > 0 \end{cases}$$

$$\Rightarrow g'(t) = \begin{cases} 0 & \text{if } t > 0 \\ 1 & \text{if } t > 0 \end{cases}$$



Leaky ReLU

$$g(z) = mox(0.01z, z)$$

 $g'(z) = \{0.01 \text{ if } z < 0 \text{ or } \}$



One hidden layer Neural Network

Gradient descent for neural networks

Gradient descent for neural networks

Porometers:
$$(D_1)$$
 (D_2) (D_3) (D_4) (D_4)

Formulas for computing derivatives

Formal propagation!

$$Z^{(1)} = U_{(1)}X + U_{(1)}$$

$$Z^{(1)} = U_{(1)}X + U_{(1)}$$

$$Z^{(2)} = U_{(2)}Y + U_{(1)}$$

$$Z^{(2)} = U_{(2)}Y + U_{(1)}$$

$$Z^{(2)} = U_{(2)}Y + U_{(1)}Y + U_{(2)}Y + U_{($$

Back propagation:

$$Az^{[i]} = A^{[i]} = Y$$

$$Az^{[i]} = \frac{1}{m} Az^{[i]} A^{[i]} T$$

$$Ab^{[i]} = \frac{1}{m} np. Sum (Az^{[i]}, anais = 1, keepdans = 1 ne)$$

$$Az^{[i]} = \frac{1}{m} np. Sum (Az^{[i]}, anais = 1, keepdans = 1 ne)$$

$$Az^{[i]} = U^{[i]} Az^{[i]} + g^{[i]} (Z^{[i]}) (n^{[i]}, m)$$

$$Az^{[i]} = \frac{1}{m} Az^{[i]} \times T$$

$$Az^{[i]} \times T$$

$$Ab^{[i]} = \frac{1}{m} np. sum (Az^{[i]}, ani = 1, keepdins = True)$$

$$Andrew Andrew Andrew$$

Andrew Ng

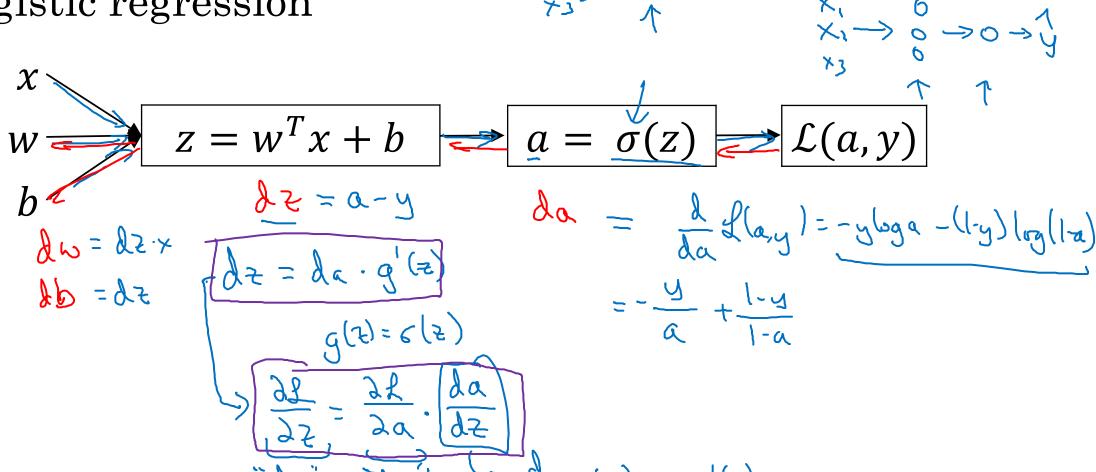


One hidden layer Neural Network

Backpropagation intuition (Optional)

Computing gradients

Logistic regression



Neural network gradients $z^{[2]} = W^{[2]}x + b^{[2]}$ du = de a Tos > db (2) = dz (2) K $\left(\begin{array}{ccc} n & \zeta & \zeta & \zeta & \zeta \end{array} \right)$

Summary of gradient descent

$$dz^{[2]} = a^{[2]} - y$$
 $dW^{[2]} = dz^{[2]}a^{[1]^T}$
 $db^{[2]} = dz^{[2]}$
 $dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$
 $dW^{[1]} = dz^{[1]}x^T$
 $db^{[1]} = dz^{[1]}$

Vectorized Implementation:

$$z^{(1)} = \omega^{(1)} \times + b^{(1)}$$

$$z^{(1)} = g^{(1)}(z^{(1)})$$

$$z^{(1)} = \left[z^{(1)}(z^{(1)})\right]$$

$$z^{(1)} = \left[z^{(1)}(z^{(1)})\right]$$

$$z^{(1)} = \left[z^{(1)}(z^{(1)})\right]$$

$$z^{(1)} = \left[z^{(1)}(z^{(1)})\right]$$

$$z^{(1)} = g^{(1)}(z^{(1)})$$

Summary of gradient descent

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$$dW^{[1]} = dz^{[1]}x^T$$

$$db^{[1]} = dz^{[1]}$$

$$dz^{[2]} = a^{[2]} - y$$

$$dW^{[2]} = dz^{[2]}a^{[1]^T}$$

$$db^{[2]} = dz^{[2]}$$

$$dz^{[2]} = \frac{1}{m}dz^{[2]}A^{[1]^T}$$

$$dz^{[2]} = \frac{1}{m}np. sum(dz^{[2]}, axis = 1, keepdims = True)$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dW^{[1]} = dz^{[1]}x^T$$

$$dy^{[1]} = dz^{[1]}x^T$$

$$dy^{[1]} = \frac{1}{m}dz^{[1]}x^T$$

$$dy^{[1]} = \frac{1}{m}dz^{[1]}x^T$$

$$dy^{[1]} = \frac{1}{m}dz^{[1]}x^T$$

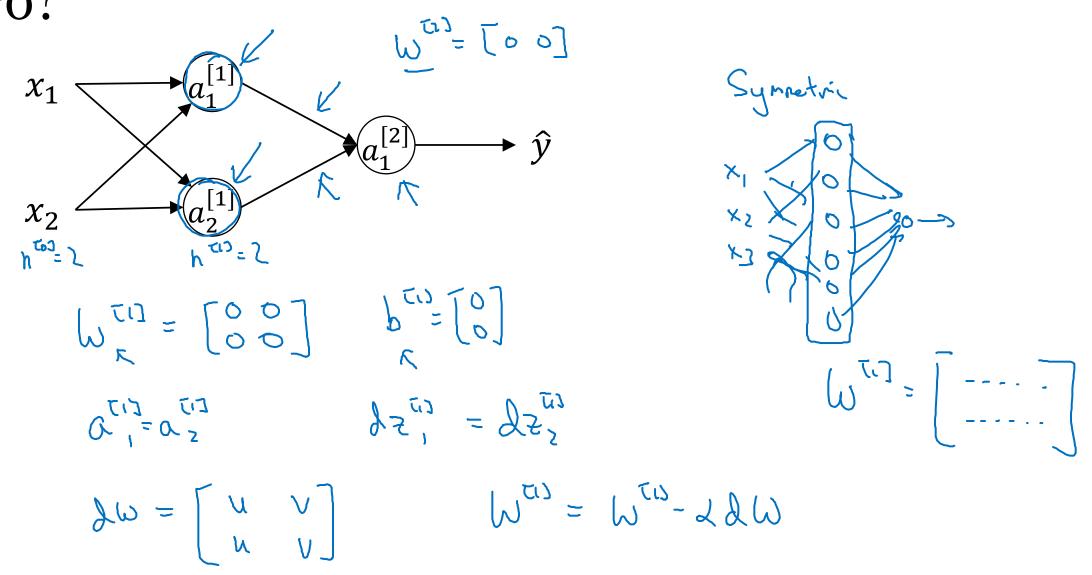
$$dy^{[1]} = \frac{1}{m}np. sum(dz^{[1]}, axis = 1, keepdims = True)$$



One hidden layer Neural Network

Random Initialization

What happens if you initialize weights to zero?



Random initialization

