



LAUREA MAGISTRALE IN FISICA

# Particle Tracking through Machine Learning

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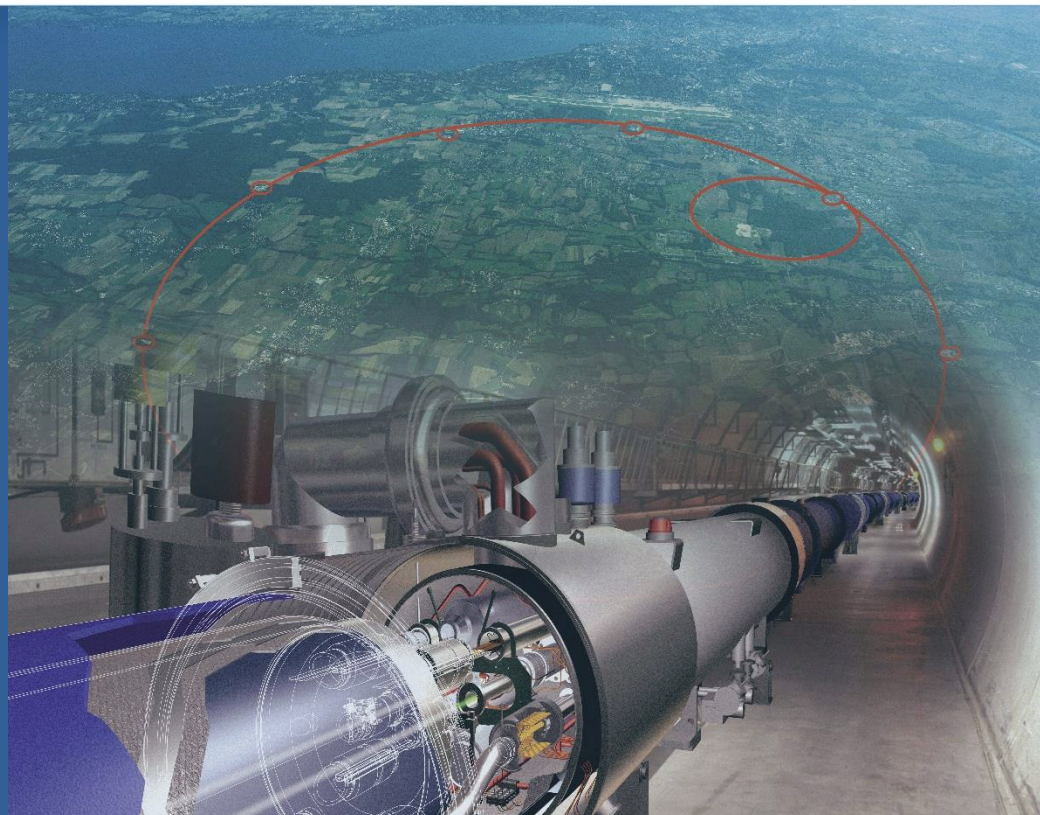
# Outline

- Introduction and Motivation
- The ATLAS experiment at CERN
- Deep Neural Network's architecture
- Results and Discussion
- Conclusion



# Introduction and Motivation

- Large Hadron Collider (LHC)
- Huge amount of data
- The tracking problem
- A Machine Learning approach



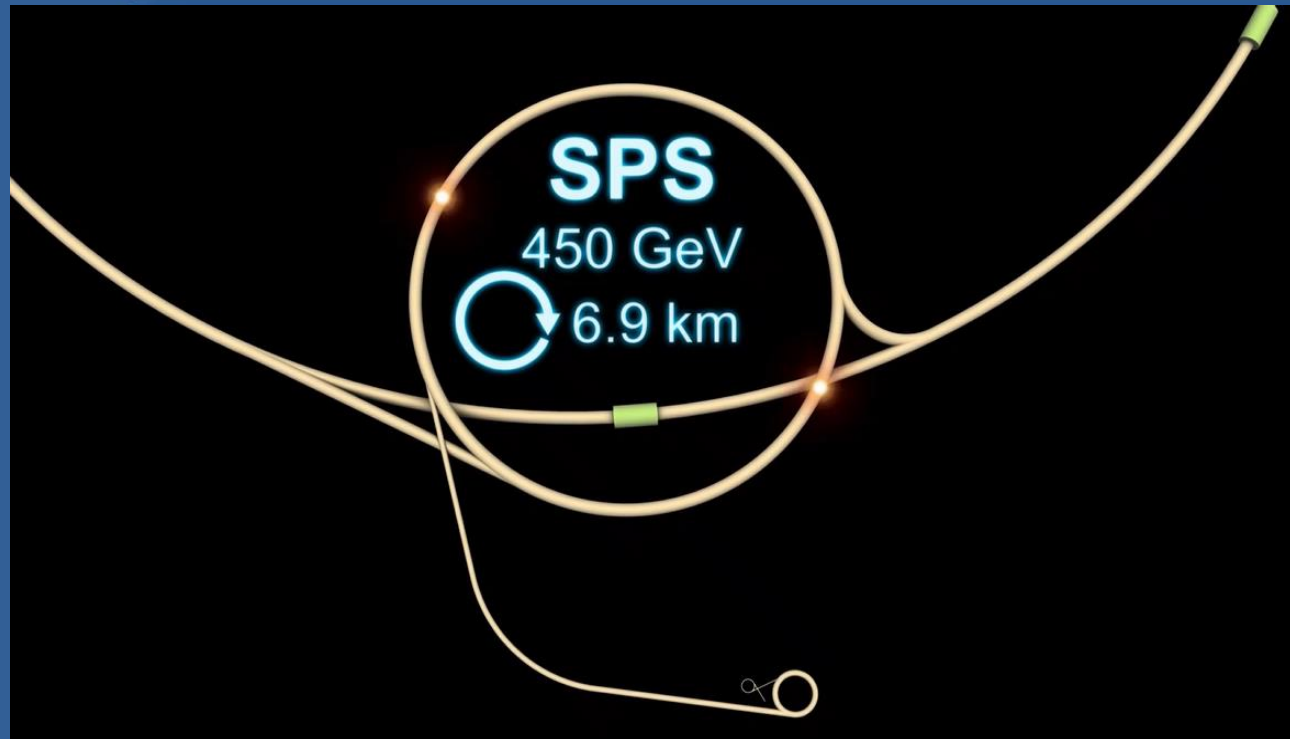
# The Standard Model

- It describes three of the four fundamental forces
- It classifies all known elementary particles
- Protons and neutrons are made up of up and down quarks
- It does not explain gravity and dark matter

QUARKS	mass → charge → spin →	$\approx 2.3 \text{ MeV}/c^2$ 2/3 1/2 <b>u</b> up	$\approx 1.275 \text{ GeV}/c^2$ 2/3 1/2 <b>c</b> charm	$\approx 173.07 \text{ GeV}/c^2$ 2/3 1/2 <b>t</b> top	0 0 1 <b>g</b> gluon	$\approx 126 \text{ GeV}/c^2$ 0 0 0 <b>H</b> Higgs boson
		$\approx 4.8 \text{ MeV}/c^2$ -1/3 1/2 <b>d</b> down	$\approx 95 \text{ MeV}/c^2$ -1/3 1/2 <b>s</b> strange	$\approx 4.18 \text{ GeV}/c^2$ -1/3 1/2 <b>b</b> bottom	0 0 1 <b><math>\gamma</math></b> photon	
		$0.511 \text{ MeV}/c^2$ -1 1/2 <b>e</b> electron	$105.7 \text{ MeV}/c^2$ -1 1/2 <b><math>\mu</math></b> muon	$1.777 \text{ GeV}/c^2$ -1 1/2 <b><math>\tau</math></b> tau	0 1 <b>Z</b> Z boson	
LEPTONS		$< 2.2 \text{ eV}/c^2$ 0 1/2 <b><math>\nu_e</math></b> electron neutrino	$< 0.17 \text{ MeV}/c^2$ 0 1/2 <b><math>\nu_\mu</math></b> muon neutrino	$< 15.5 \text{ MeV}/c^2$ 0 1/2 <b><math>\nu_\tau</math></b> tau neutrino	80.4 GeV/c <sup>2</sup> ±1 1 <b>W</b> W boson	GAUGE BOSONS

# Proton-Proton Collision

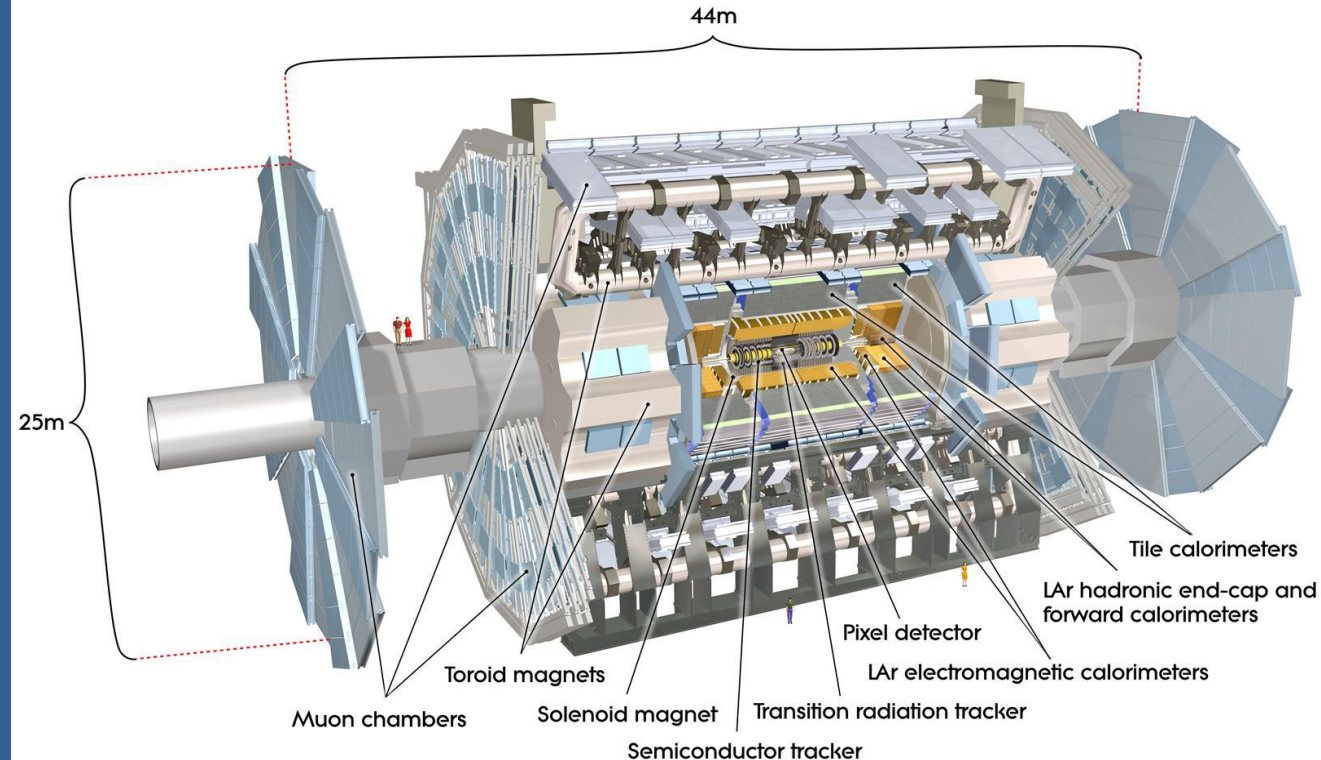
- Protons accelerate through the LHC
- After colliding many different particles are generated
- Particles pull away from the centre





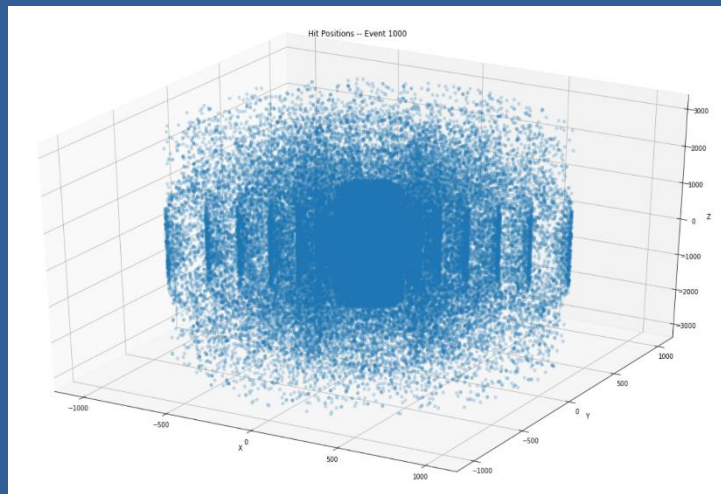
# ATLAS

- Protons collide in the middle
- Pixel detectors record the passage of particles
- Pixel detectors record the amount of energy lost by the particle

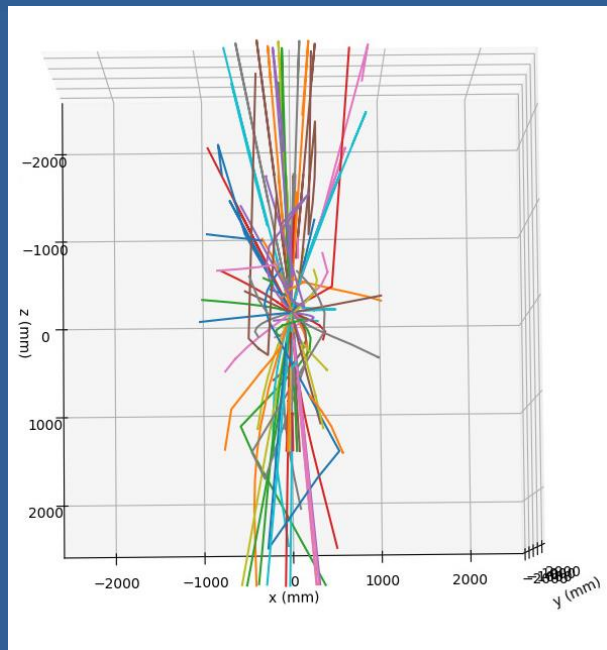




# Track Particle



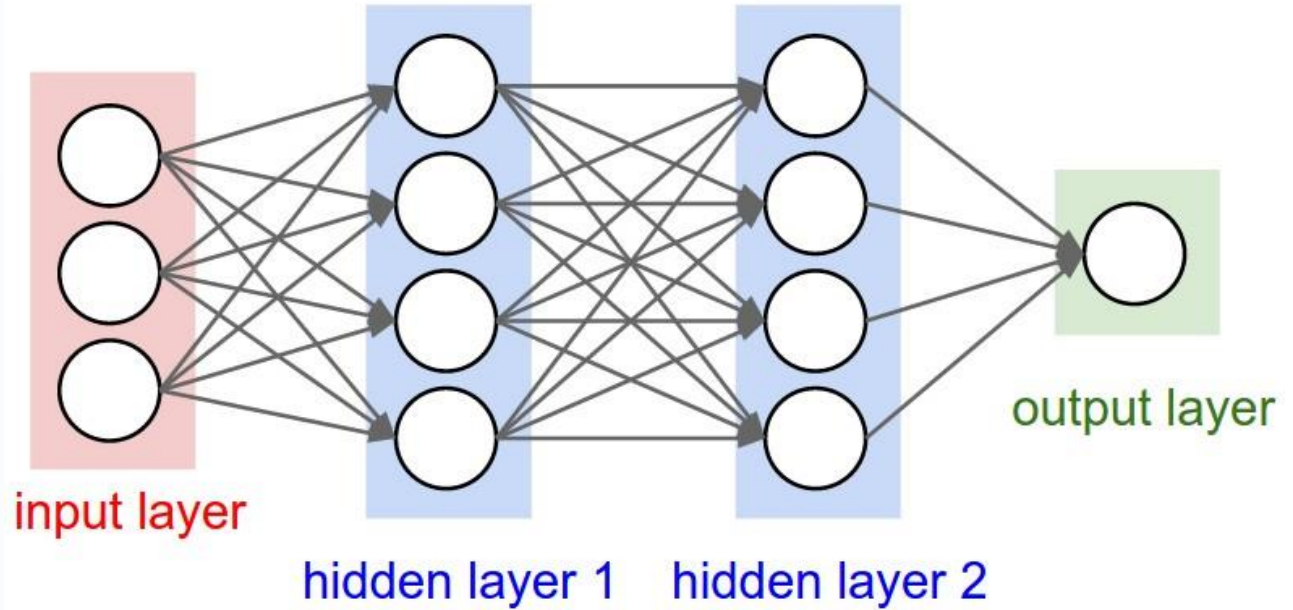
How to  
reconstruct all  
trajectories?



Input: dataset recorded by detectors

Output: predicted trajectories by the DNN

# Neural Network



Flow of activation





# Training Process

Target Function

$$y = f^*(\underline{x}) , \underline{x} \in \mathbb{R}^d$$

Approximating Function

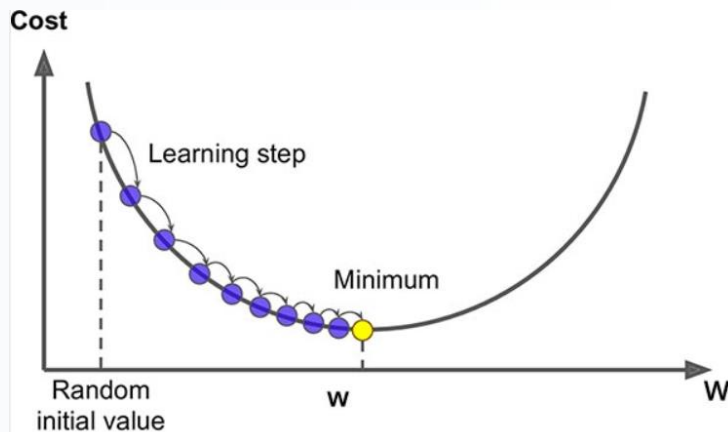
$$\tilde{y}(\underline{x}) = \underline{w} \cdot \underline{x} + b , \underline{w} \in \mathbb{R}^d , b \in \mathbb{R}$$

Loss Function

$$L(\underline{x}^{(i)}, y^{(i)}) := (\tilde{y}(\underline{x}^{(i)}) - y^{(i)})^2$$

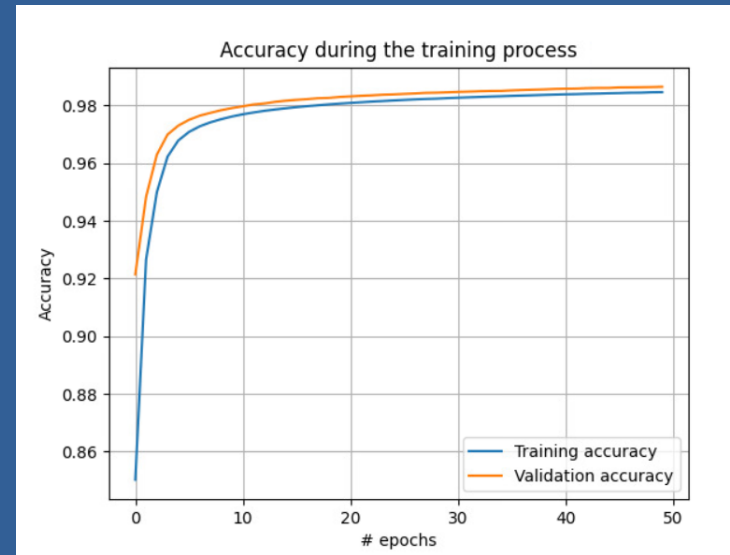
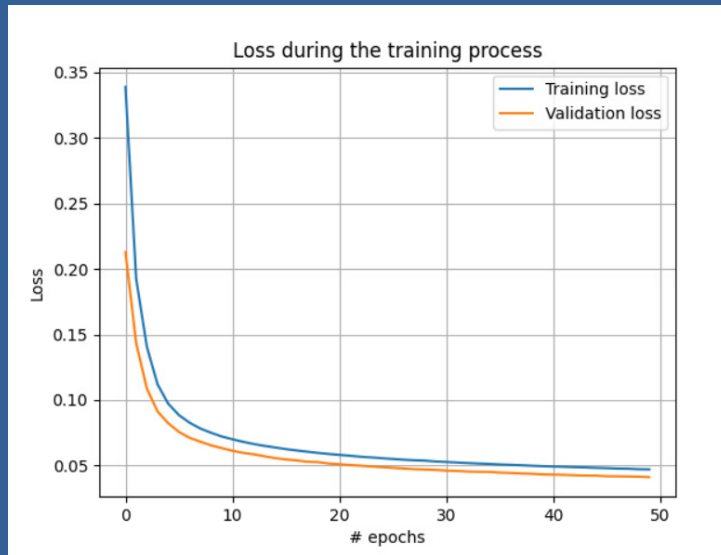
Best Parameters

$$\theta^* := \operatorname{argmin}_{\Theta} L(D, \theta)$$



# Training vs Validation

Validation set is often used to estimate how well the model has been trained





# Tracking Particles' Neural Network

- Input: couple of points
- Number of neurons: 2200
- Number of layers: 5
- Output: 1 if points belong to the same trajectory, 0 otherwise



Points are gathered  
in lists



Each list describes a  
**TRAJECTORY**





# Error Measure

How do we determine if the predicted trajectory is good?

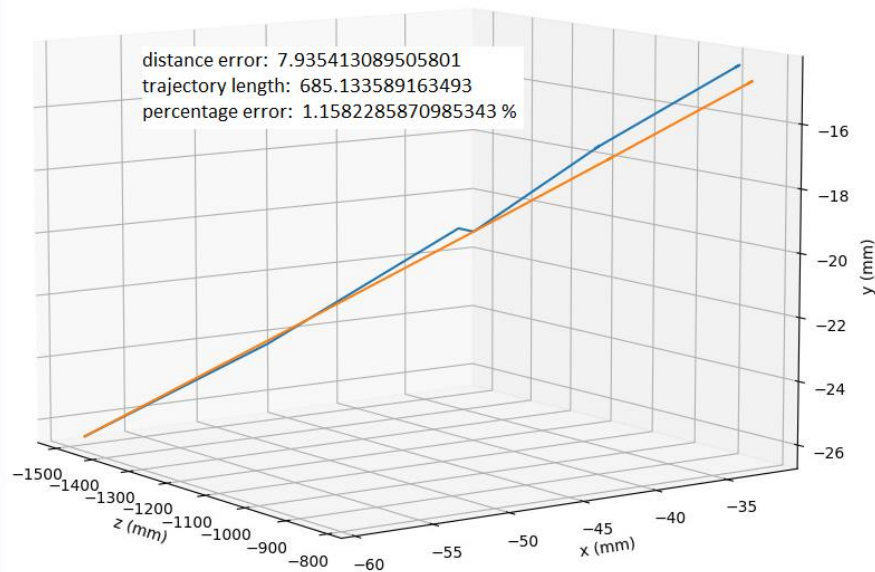
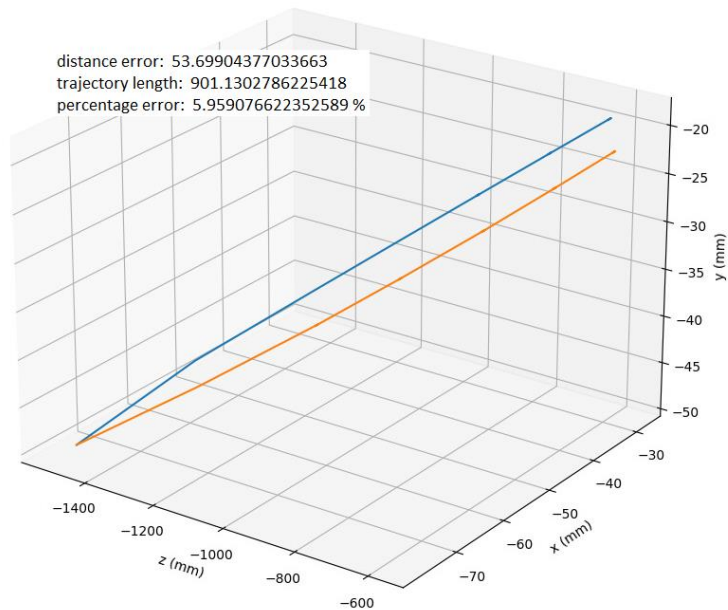


ERROR = sum of all minimum distances between  
reconstructed points and real trajectory



$$\text{PERCENTAGE ERROR} = \frac{\text{ERROR}}{\text{LENGTH OF TRAJECTORY}}$$

# Reconstructed vs Real trajectory



BLUE= reconstructed

ORANGE = real

# Models

Name	Event A (%)	Event B (%)	Event C (%)	Event D (%)	Average (%)
<b>basic10</b>	31,19	29,02	24,03	22,52	26,69
<b>100ev_32k</b>	4,79	12,24	7,29	5,79	7,52
<b>100ev_2k</b>	5,56	11,11	8,62	5,09	7,59
<b>best80</b>	2,99	4,49	6,88	1,86	4,05

4 different model applied to 4 different collisions' events  
produce the above results



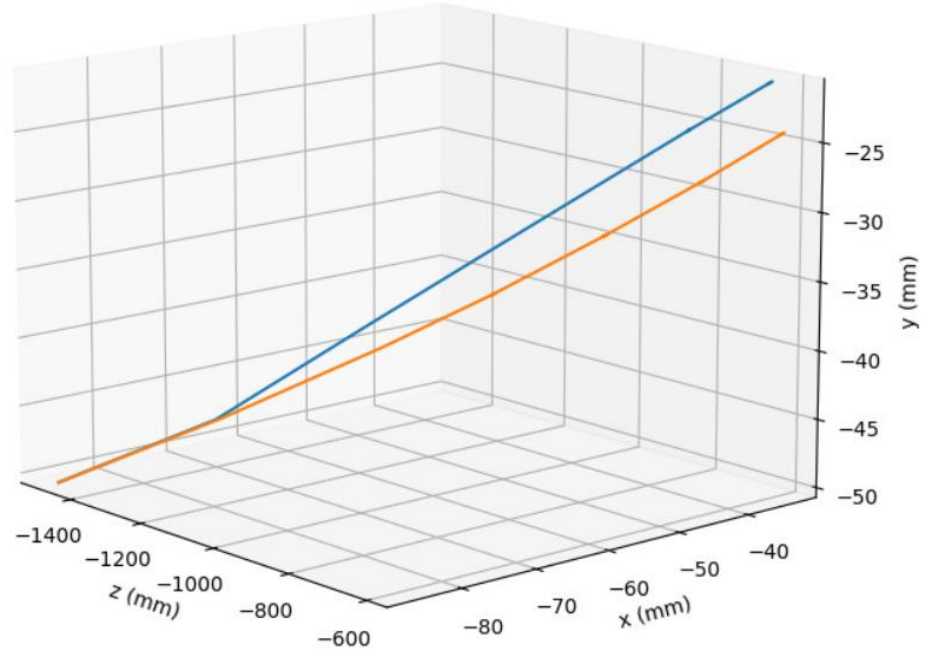
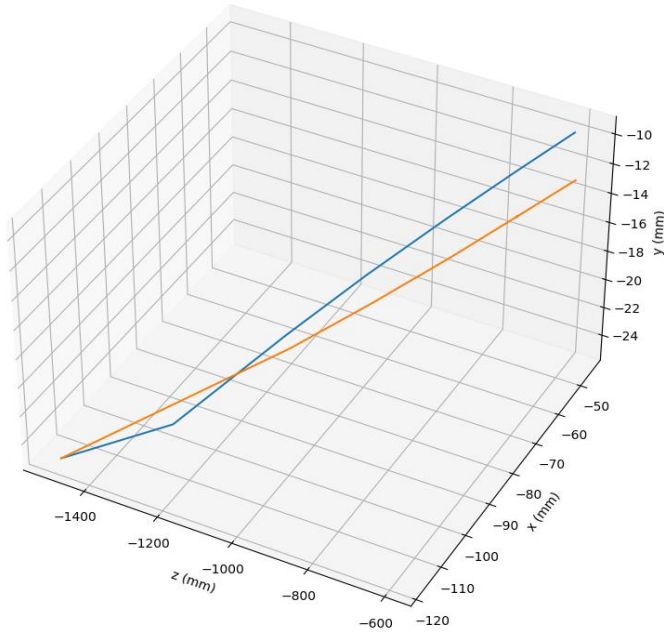
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Why is this the best model?

Difficult to answer; unbalanced dataset could be an explanation

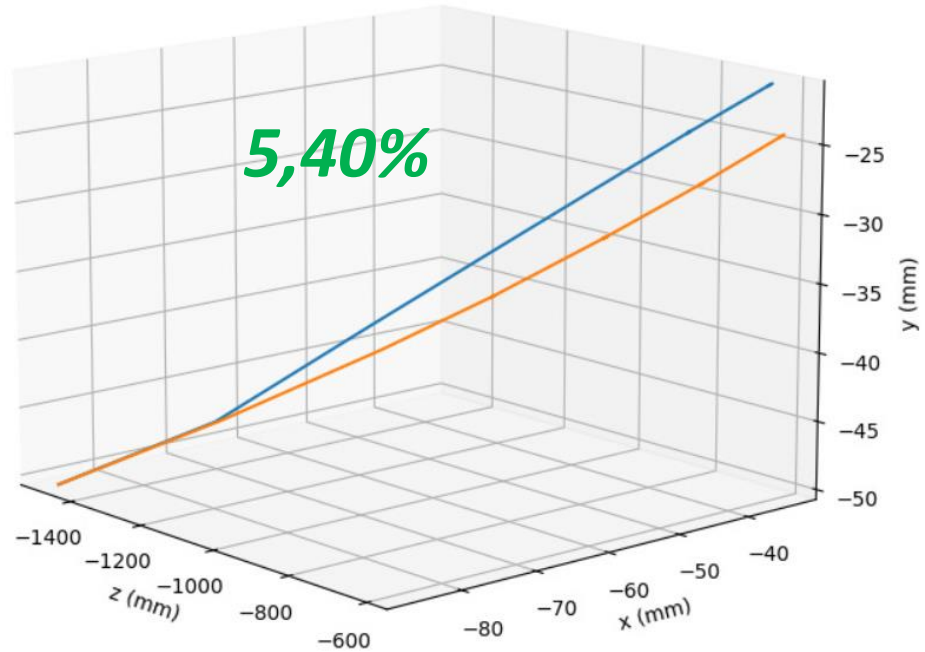
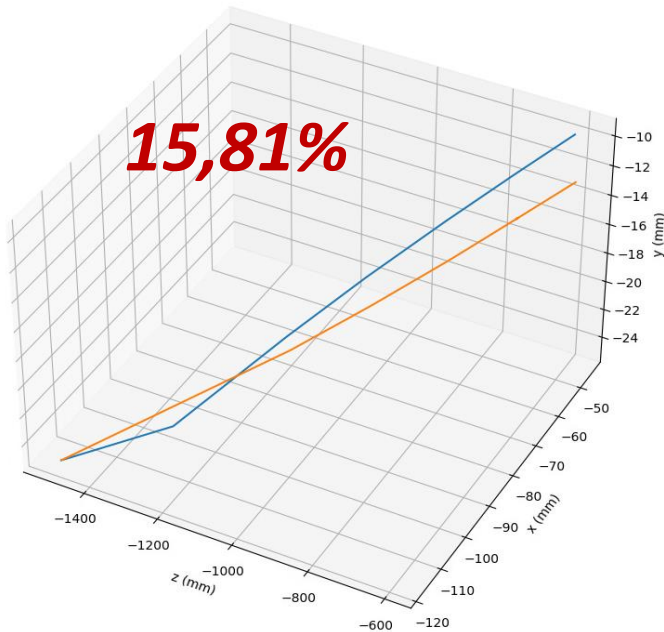
# Which one has the lowest error?



BLUE= reconstructed

ORANGE = real

# Average error is 4,05%

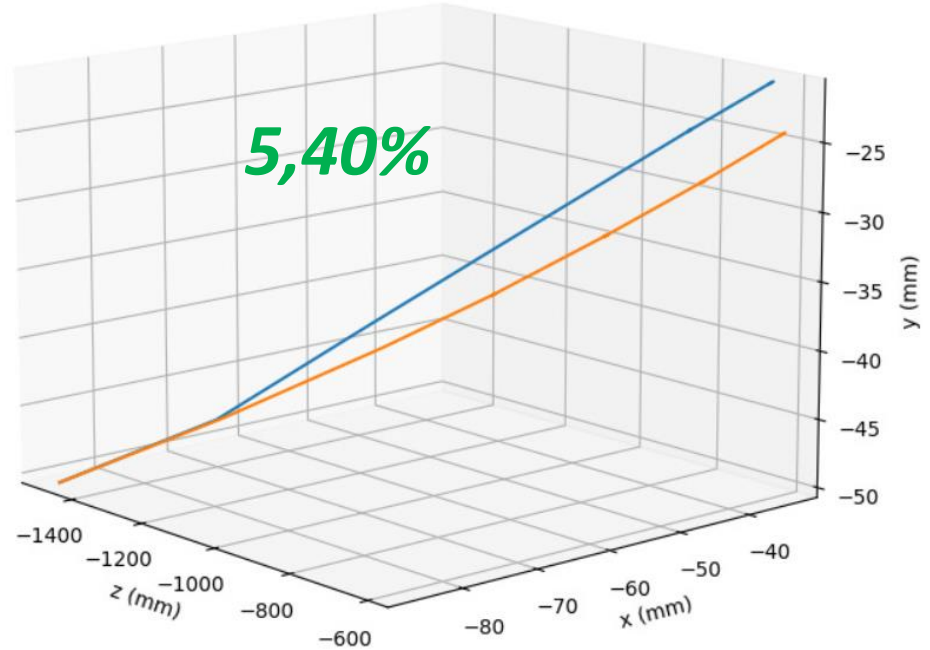
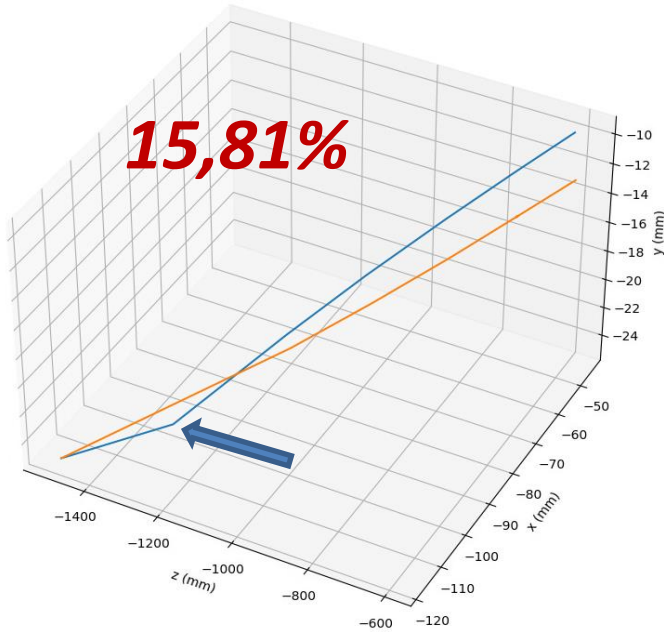


BLUE= reconstructed

ORANGE = real



# Model's predictions



Corner points should not be observed in real trajectories



# Conclusion & Future Works

We demonstrated how DNN can be useful for particles tracking problems, with errors lower than 5%.

Next Steps are:

- Prevent the neural network from violating physical laws
- Assert that each prediction does not violate any conservation law
- Try to estimate the charge of the particles