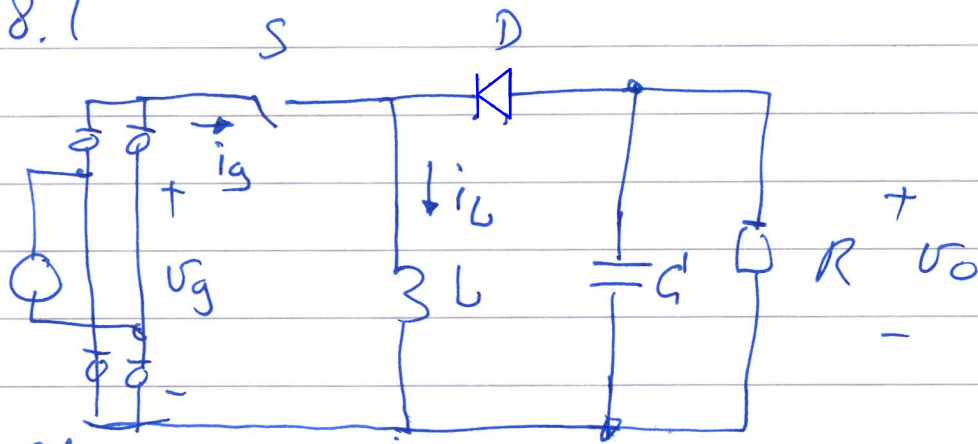


18.1

7/

a) (find $d, \langle i_L \rangle_{TS}$)

$$\frac{\langle v_o \rangle_{TS}}{\langle v_g \rangle_{TS}} = -\frac{d}{d'} \Rightarrow d = \frac{V_o}{V_o - \hat{V}_{ac} |\sin \omega t|}$$

$$d = \frac{1}{1 - \frac{\hat{V}_{ac}}{V_o} |\sin \omega t|}$$

$$\langle i_g \rangle_{TS} = d \langle i_L \rangle_{TS}$$

$$R_e = \frac{\langle v_g \rangle_{TS}}{\langle i_g \rangle_{TS}}$$

$$\langle i_L \rangle_{TS} = \frac{\langle i_g \rangle}{d}$$

$$\langle i_L \rangle_{TS} = \frac{\langle v_g \rangle_{TS}}{R_e d}$$

$$\langle i_L \rangle_{TS} = \hat{V}_{ac} |\sin \omega t| \cdot \frac{1}{\left(1 - \frac{\hat{V}_{ac}}{V_o} |\sin \omega t|\right)^2 R_e}$$

$$\langle i_L \rangle_{TS} = \hat{V}_{ac} |\sin \omega t| \left(1 - \frac{\hat{V}_{ac}}{V_o} |\sin \omega t|\right) \frac{1}{R_e}$$

b: For CCM is required.

$$\langle i_L \rangle_{T_s} > \Delta i_L$$

$$\Delta i_L = \frac{\langle v_g \rangle_{T_s} \cdot T_s d}{2L}$$

$$\langle i_L \rangle_{T_s} = \frac{\langle v_g \rangle_{T_s}}{R_e d}$$

So

$$\frac{\langle v_g \rangle_{T_s}}{R_e d} > \frac{\langle v_g \rangle_{T_s} \cdot T_s d}{2L}$$

$$\frac{1}{R_e \cdot d} > \frac{dT_s}{2L}$$

$$R_e < \frac{1}{d^2} \frac{1}{T_s} 2L$$

$$d = \frac{V_o}{V_o - v_g}$$

$$\underline{\underline{R_e < \left(\frac{V_o - v_g}{V_o} \right)^2 \frac{2L}{T_s}}}$$

$$\begin{aligned} \frac{V_o}{v_g} &= \frac{d}{1-d} \\ \frac{V_o}{v_g} (1-d) &= d \\ \frac{V_o}{v_g} - \frac{V_o}{v_g} d &= d \\ \frac{V_o}{v_g} &= \left(\frac{V_o}{v_g} + 1 \right) d \\ 1 &= \left(1 - \frac{v_g}{V_o} \right) d \\ 1 &= \frac{V_o - v_g}{V_o} d \end{aligned}$$

c)

Minimum Re_{crit} at $v_g = 0$

$$\text{So } \underline{Re} < \underline{\frac{2L}{Ts}} \Rightarrow ECM$$

Maximum Re_{crit} at $v_g = \overset{1}{V_{ac}}$

$$\underline{Re = \left(\frac{V_0 - V_{ac}}{V_{ac}} \right)^2 \frac{2L}{Ts}}$$

d)

$$R_{e \max} = \frac{132^2}{10} = 1742 \, \Omega$$

$$R_{e \min} = \frac{108^2}{100} = 117 \, \Omega$$

So CCM is obtained for:

$$L > R_e \frac{T_s}{2}$$

$$L > \frac{1742 \cdot \frac{1}{75e3}}{2} \Rightarrow \underline{L > 12 \text{ mH}}$$

So DCM is obtained for:

$$L < \frac{R_e T_s}{2} \left(\frac{\hat{V}_{ac}}{V_o - \hat{V}_{ac}} \right)^2$$

$$L < \frac{117 \cdot \frac{1}{75e3}}{2 \left(\frac{108}{120 - 108} \right)^2}$$

$$\underline{L < 125 \, \mu\text{H} \text{ at } 100\text{W} \text{ \& } 108\text{V}}$$