

# Written examination in Control of Electrical Drive Systems and Converters

8<sup>th</sup> semester

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- All usual helping aids are allowed, including text books, slides, personal notes, and exercise solutions.
  - Calculators and laptop computers are allowed, provided that all wireless and wired communication equipment is turned off.
  - Internet access is strictly forbidden.
  - Any kind of communication with other students is not allowed.
  - Remember to write your study number on **all** answer sheets.
  - The complete description of the solution of the questions must be attached separately.
  - Only results with a complete description of the solution will be taken into account.
  - All intermediate steps and calculations should be included in your answer sheets --- printing the final result is **NOT** sufficient.
  - This exam contains **3** parts. The percentage is indicated for every part.
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## Part 1 (50 %)

- 1.1 How is soft switching realized and what are the advantages and disadvantages compared to hard switching? Use also the switching trajectory in your explanation (10%)
- 1.2 How is three-phase PWM implemented in an analog application? (10%)
- 1.3 Discuss in detail Table 14-2 from the book 'Power Electronics Converters, Application and Design. N. Mohan, T.M. Undeland and W.P. Robbins (cover at least 6 parameters). (10%)

**Table 14-2 Comparison of Adjustable Frequency Drives**

<i>Parameter</i>	<i>PWM</i>	<i>Square Wave</i>	<i>CSI</i>
Input power factor	+	—	— —
Torque pulsations	++	—	—
Multimotor capability	+	+	—
Regeneration	—	—	++
Short-circuit protection	—	—	++
Open-circuit protection	+	+	—
Ability to handle undersized motor	+	+	—
Ability to handle oversized motor	—	—	—
Efficiency at low speeds	—	+	+
Size and weight	+	+	— —
Ride-through capability	+	—	—

- 1.4 What is discontinuous PWM and what are the advantages and disadvantages of such modulation techniques compared to ST-PWM? How can these be implemented? (20%)

For all questions: besides explaining with your own words, use also figures in your answers.

## Part 2 (30%)

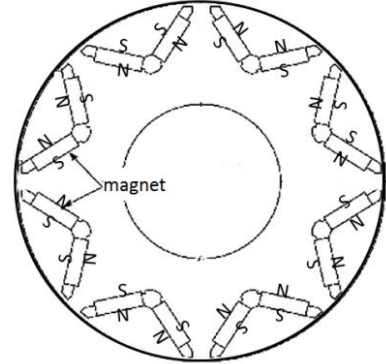
An interior permanent magnet machine's rotor is shown below. Modelled in a synchronously rotating dq-reference frame, we have:

$$\begin{aligned} u_q &= R i_q + p \lambda_q + \omega_r \lambda_d & \lambda_q &= (L_{ls} + L_{mq}) i_q = L_q i_q \\ u_d &= R i_d + p \lambda_d - \omega_r \lambda_q & \lambda_d &= (L_{ls} + L_{md}) i_d + \lambda_{mpm} = L_d i_d + \lambda_{mpm} \end{aligned}$$

The torque equation is

$$T_e = \frac{3}{2} p (\lambda_d i_q - \lambda_q i_d)$$

where  $p$  in the torque equation is the number of pole pairs and  $\lambda$  represents the flux linkage.



1. Please add the dq-reference frame to the rotor shown above, and explain why. The rotor is assumed to rotate in **clockwise** direction (*important to notice this!*).
2. Please determine for this rotor, if ( $L_d > L_q$ ) or ( $L_d < L_q$ ), and explain why. In the dq-frame you have drawn above, please indicate the desired location for the current vector (a rough indication with respect to the q-axis is enough), and explain why.
3. For field oriented control of PM machine, please give the control block diagram in order to control the d-axis current to follow a reference current command; add the back-EMF decoupling term to this control block diagram; simply the control block diagram considering back-EMF decoupling effects.
4. Please indicate the back-EMF term appearing in the q-axis voltage equation; what is the back-EMF decoupling term that should be introduced to the q-axis current regulation block diagram? Please use the machine equations to give mathematical proof that supports your statement.
5. Knowing  $R=0.2$  (Ohm),  $L_d = 2$  (mH). The inverter switches at 5 kHz and the equivalent delay the inverter introduces to the controller is considered to be 1.5/5000 (s). In the PI controller,  $K_p = 3$  and  $K_i = 100$ . Please calculate the bandwidth of this d-axis current control loop. Please give the bandwidth in Hz.

### Part 3 (20%)

The mathematical model of an induction machine may be expressed as:

The stator side:

$$u_{qs} = r_s i_{qs} + p \lambda_{qs} + \omega_e \lambda_{ds}$$

$$\lambda_{qs} = L_{ls} i_{qs} + L_m (i_{qs} + i_{qr})$$

$$u_{ds} = r_s i_{ds} + p \lambda_{ds} - \omega_e \lambda_{qs}$$

$$\lambda_{ds} = L_{ls} i_{ds} + L_m (i_{ds} + i_{dr})$$

The rotor side:

$$u_{qr} = r_r i_{qr} + p \lambda_{qr} + (\omega_e - \omega_r) \lambda_{dr} \quad \lambda_{qr} = L_{lr} i_{qr} + L_m (i_{qs} + i_{qr})$$

$$u_{dr} = r_r i_{dr} + p \lambda_{dr} - (\omega_e - \omega_r) \lambda_{qr} \quad \lambda_{dr} = L_{lr} i_{dr} + L_m (i_{ds} + i_{dr})$$

where  $\lambda$  represents the flux linkage. The voltage supplied to the rotor windings is zero, assuming it is a squirrel cage induction machine.

1. You will implement rotor-flux oriented control for this induction machine. Please give the stator, rotor voltage equations and the torque equation expressed in the rotor flux-oriented reference frame.
2. Please list the motor parameters needed in realization of the rotor-flux oriented FOC.
3. For the given induction machine listed below, please calculate the rated d-axis current reference value to be used in the rotor flux oriented FOC.

V. $\Delta/Y$	Hz	kW	rpm	A. $\Delta/Y$	COS $\phi$
230/400	50	0.3	905	1.9/1.1	0.64

Stator and rotor resistances

$$R_s = 26.5 \text{ (}\Omega\text{)}$$

$$R_r = 23.9 \text{ (}\Omega\text{)}$$

Stator and rotor self-inductances

$$L_s = 0.79 \text{ (H)}$$

$$L_r = 0.79 \text{ (H)}$$

Magnetization inductance

$$L_m = 0.71 \text{ (H)}$$