

# CoEDSoc - Exam 15

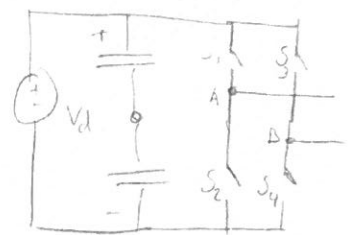
## Part 1 - Modulation

### 1. Single-phase analogue PWM technique

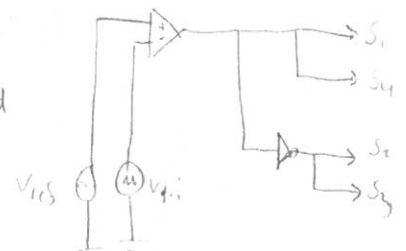
- A reference signal is generated and compared with a triangular carrier wave.



### H-Bridge



### Bipolar PWM

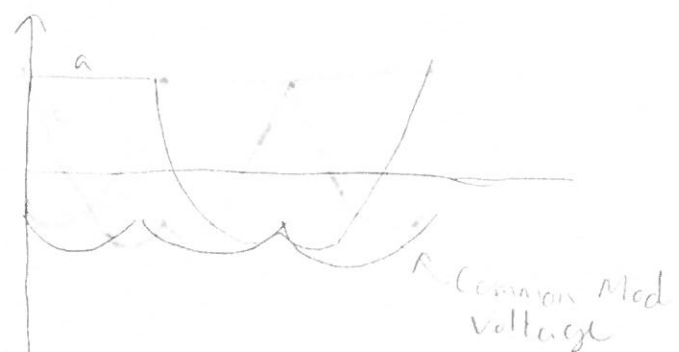
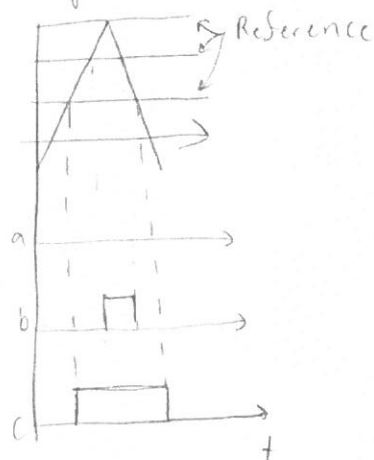


### 2. Discontinuous PWM (DPWM)

DPWM allows reducing the average switching, which is particular suitable for high-power inverters.

Considering similar switching frequency (same carrier frequency), DPWM gives a 1/3 reduction of the average switching frequency, thus reducing switching losses by 33%.

- Implementation DPWM:



## CoEDSaC - Exam 15

3- An electric drive switches from motor to generator

- What happens with the DC-link

- Energy will build up in the capacitor, if no precaution is taken and the capacitor limit are exceeded, this will damage the inverter.

- Reason

- This is caused by the fact that the motor is operating in generator mode.

4. - Limit the phenomena of 1.3

- Dissipative braking

- A resistor is set in parallel with the DC-link capacitor to dissipate the energy.

- Regenerative braking

- A 4-Quadrant Inverter is used to deliver energy back to the grid.

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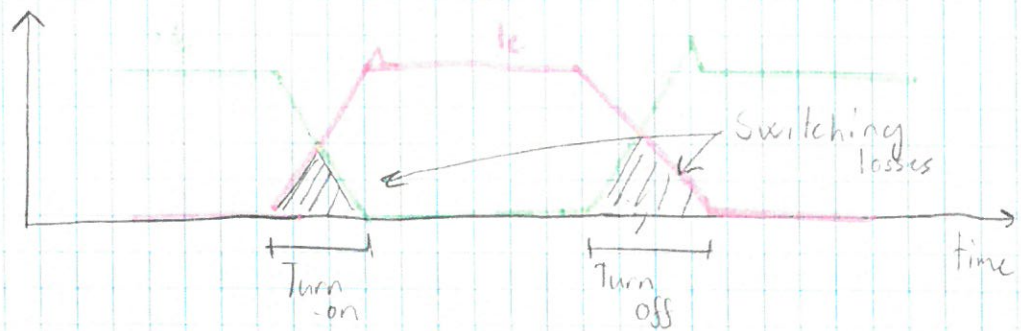
## 5. Comparison of Adjustable Frequency Drives.

	PWM	Square Wave	CSI
Power Factor S.p. 5/21 L4	Uses a capacitor, thus a smaller PF angle. Faster control ✓	Uses a capacitor, thus a smaller PF angle. Thyristor causes reactive P $\rightarrow$ don't switch when reverse ✓	Uses an inductor, ✓ where the motor already is inductive ✓
Torque Pulsation	Fast switching $\rightarrow$ Small V & I ripples. ✓	Slow switching $\rightarrow$ Larger V & I ripples $\propto I$ ✓	Thyristor can only be turned off, when $I = 0$ , i.e., only once per fundamental. $\leftrightarrow$
Regeneration	Needs a four quadrant inverter supplied by grid. ✓ $\leftrightarrow$		Has a large inductor, which can store a larger amount of energy than the DC-link capacitor ✓
Short circuit protection	Shorts the DC-link ✓ $\leftrightarrow$		The current is limited by the inductor ✓
Open circuit protection	Current stops slowing $\rightarrow$ No consequence ✓ $\leftrightarrow$		Overvoltage, caused by the energy stored in the inductor. ✓ - Current can't change instantaneously
Size and weight	Physically smaller than CSI ✓ $\leftrightarrow$		Large Inductor ✓
Multi Motor Capability	Voltage distributed equally across multiple motors. Same voltage on each ✓ $\leftrightarrow$		Current depends on the load, current divides.
Ride-through capability	Fast Control, can response to a drop in voltage ✓	Slow Switching cannot response ✓	Slow response $\rightarrow$ The large L can compensate for ✓

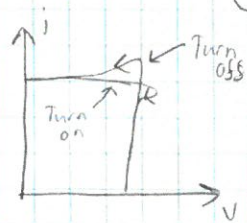


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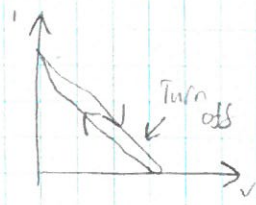
1.6 - MosFET / IGBT turn on/off.



- During turn on/off periods, switching losses appears.
- Since the switches are not ideal, the switching does not happen instantaneously.
- The switching trajectory



Hard switching



Soft switching.

So by soft switching the switching trajectory is increased.

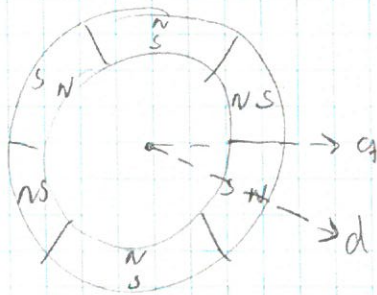
↳ This can be achieved by adding a snubber capacitor or a resonance tank.

# CoEDS a D - Exam 15

## Part 2 - PMSM

A 6-pole surface Mounted PMSM

### 2.1 - dq-reference frame



q leads d with  
 $90^\circ$  electrical  
 $\rightarrow 90^\circ / \hat{n}_{\text{pole pairs}}$

### 2.2 - Torque eq.

- Torque expressed by dq inductances and currents

$$T_e = \frac{3}{2} p (\lambda_{\text{mpm}} i_q + (L_d - L_q) i_d i_q)$$

// Since surface mounted,  $L_d = L_q$

$$T_e = \frac{3}{2} p (\lambda_{\text{mpm}} i_q)$$

- Determination of d- and q-axis current references for FOC:

$$i_{d,\text{ref}} = 0$$

$i_{q,\text{ref}}$  can be found either by:

$\chi (V_{\text{ref}} - \omega) \cdot \text{PI}$  - Through a speed loop or through a torque reference:

$$i_{q,\text{ref}}^* = \frac{2}{3} \frac{T_{e,\text{ref}}^*}{p \lambda_{\text{mpm}}}$$



# CoEDS a C - Exam 15/6

2.3 - The machine shaft speed

$$\omega_r = 377 \text{ rad/s}$$

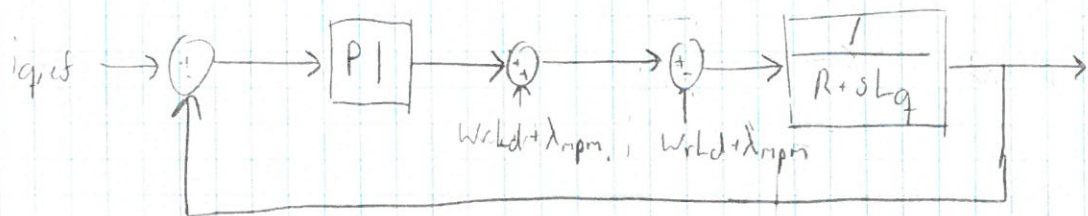
$$\omega_{r, \text{shaft}} = \omega_r / p$$

$$\omega_{r, \text{shaft}} = \frac{377 \text{ rad/s}}{3} \cdot \frac{60}{2\pi} = 1200 \text{ rpm}$$

2.4 - Tune the current loop PI parameters at zero speed (Recommended):

- At zero speed there is no coupling i.e. the back EMF is zero.

2.5 - Control Block Diagram for the q-axis



Since  $u_q = R i_d + p \lambda_d + \omega_r (L_d i_d + \lambda_{mpm})$ . -- No coupling.

Open Loop Transfer Function:

$$G(s) = \frac{k_p}{L_d} \cdot \frac{s + k_i}{s} \cdot \frac{1}{s + R/L_d}$$

$$= \frac{k_p s + k_i}{L_d s^2 + s R}$$

$$= \frac{1}{L_d} \frac{k_p s + k_i}{s^2 + \frac{R}{L_d} s}$$

$$= \frac{k_p}{L_d} \frac{s + \frac{k_i}{k_p}}{s^2 + \frac{R}{L_d} s}$$

# CoEDS a C · Exam 16

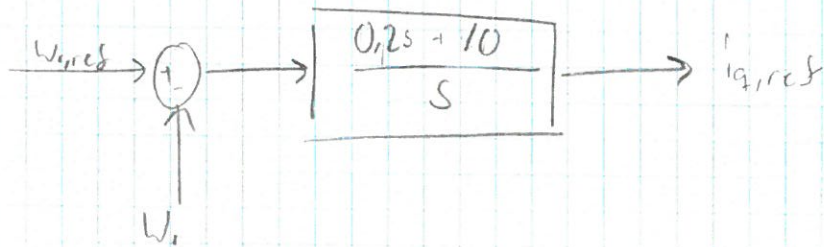
## 2.6 - Step

The motor is running at 1000 rpm

$$k_p = 0,2, \quad k_i = 10$$

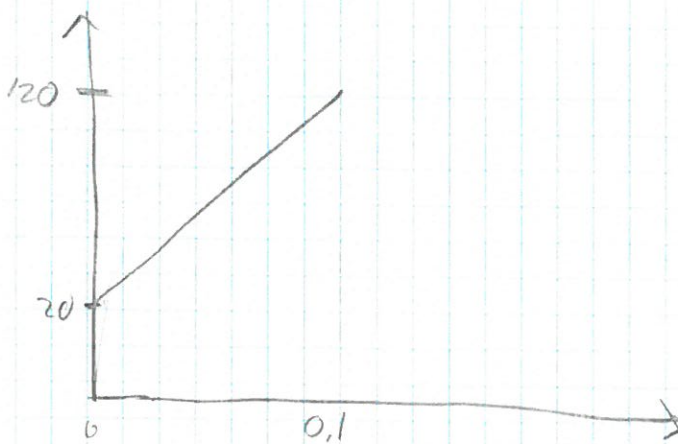
A new speed reference of 1100 rpm is introduced:

- The change in q-current reference command for the next 0,1 s:



$$i_{q,ref,init} = (1100 - 1000) \cdot 0,2 = 20 \text{ A, at } t=0$$

$$i_{q,ref,final} = (1100 - 1000) \cdot 0,2 + 10 \int_0^{0,1} 100 \, dt = 120 \text{ A, at } t=0,1$$





# CoEDSAC - Exam 15

## Part 3 - Induction Motor

### 1 - Rotational Speed

$$f_{\text{supply}} = 50 \text{ Hz}$$

#### - Rotor field

$$\omega_{r,el} = \omega_s - \omega_{sc} \quad , \quad \omega_{sc} = s \cdot \omega_s$$

so if  $s = 0$  (No-Slip, i.e. no load)

$$\omega_{r,el} = 50 \cdot 2\pi = 314,15 \text{ rad/s}$$

#### - Stator field:

$$\omega_s = f_s \cdot 2\pi$$

$$\omega_s = 50 \text{ Hz} \cdot 2\pi = 314,15 \text{ rad/s}$$

#### - Air gap field:

$$\omega_{sc} = \omega_s - \omega_{r,el}$$

so if  $s = 0$

$$\omega_{sc} = 0 \text{ rad/s.}$$

### 2 - Rotor Flux Oriented Field Oriented Control

#### - Torque eq.

$$\tau = \frac{3}{2} p \frac{L_m}{L_r} \text{Im}(\bar{i}_{qds} \cdot \bar{\lambda}_{qdr})$$

|| since  $\bar{\lambda}_{qdr} = \lambda_{dr} = \lambda_r$

$$\tau = \frac{3}{2} p \frac{L_m}{L_r} (i_{qs} \cdot \lambda_r)$$



# CoEDSAC - Exam 15

## 3 - RFO FOC

- Derive an expression linking rotor flux magnitude and stator d-axis current:

As  $\lambda_{dr} = 0$  and  $\lambda_{dr} = \lambda_r$

From rotor side:

$$\lambda_{dr} = L_r i_{dr} + L_m (i_{ds} + i_{dr}), \quad L_r + L_m = L_r$$

$$\lambda_r = L_r + L_m i_{ds}$$

and

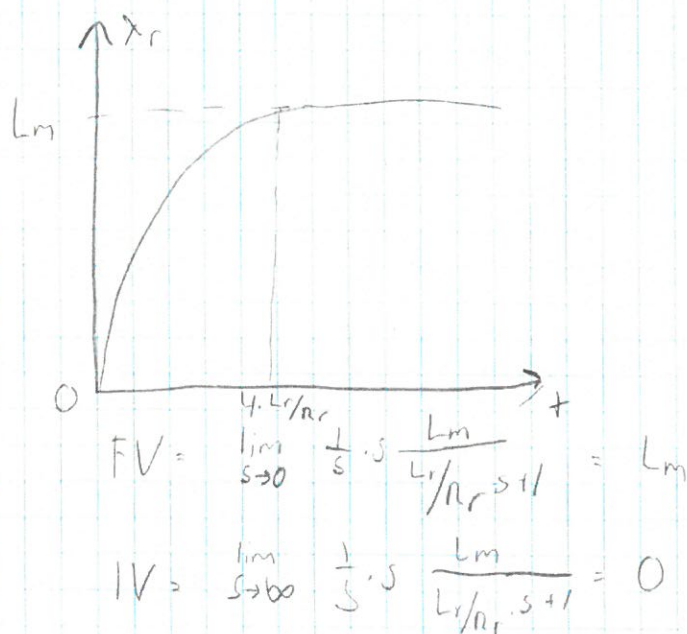
$$0 = R_r i_{dr} + p \lambda_{dr}$$

Thus:

$$\left(1 + \frac{L_r}{R_r} p\right) \lambda_r = L_m i_{ds}$$

$$\Downarrow \quad \frac{\lambda_r}{i_{ds}} = \frac{L_m}{\frac{L_r}{R_r} s + 1}, \quad \approx \frac{L_r}{R_r}$$

- Step



## CoEDSAL - Exam 15

### 4 - Types of FOC:

- Rotor-flux oriented FOC is the simplest

- Motor Parameters needed

- $R_r$ ,  $R_s$ ,  $L_{ls}$ ,  $L_{lr}$ ,  $L_m$ ,  $\phi_{kr}$ ,  $V_{k0}$ :

Lecture 1, slide 14