Lab 3 – Gaussian Process Regression

Short course on Statistical modelling for optimization

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The aim of this lab session is to obtain the best possible GPR model for the data that has been collected yesterday during lunch time.

GPR with GPy

GPy is a python package for Gaussian process models. If you have not already installed it on your computer, we advise that you download the developers version on github https://github.com/SheffieldML/GPy/tree/devel and follow the instructions.

- **Q1.** Import the data you have generated and choose your favourite parametrization. You may also rescale the data.
- **Q2.** The code for creating and optimizing a basic GP model is already given in the python script. Read it carefully to understand each line signification.
- **Q3.** Since you have two (or three) observations for each design point, does-it make sense to use leave-one-out to asses the prediction quality? Modify the leaveOneOut function accordingly.
- **Q4.** Write a function that computes the standardised LOO residuals and that compare them to the $\mathcal{N}(0,1)$ distribution.
- **Q5.** Compute the Q^2 and look at the standardized residuals of your first model. Is it convincing?
- **Q6.** Try various models and select the best one. When building the models, you may consider changing:
 - the kernel (try various ones and sums of kernels)
 - the way kernel parameters are estimated (optimization staring point, boundaries, ...)
 - the way you take the noise into account (fixed, estimated)
 - ...