## Lab 2 – Design of Experiments

Short course on Statistical modelling for optimization

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The first half of this lab session is dedicated to designing the best possible DoE. In the second one, we will run the actual experiments.

## 1 Design of experiments

The aim of this section is to define a DoE of 40 points over  $(0,1)^4$  that shows good space filling properties and good projection properties. Some useful functions (such as discrepancy, minimax, maximin, IMSE) are provided in the file lab2.py. The file SobolSequence.py will also be of particular interest to generate low discrepancy sequences.

- **Q1.** Write a function that implements a Latin Hypercube Design. The function should take as parameters the number of points n and the dimension d. It should return a np.array with shape (n, d).
- **Q2.** Write a function that returns a Centroidal Voronoi Tesselation. You may use a k-means or a McQueen algorithm. The inputs and outputs should be as in Q1.
- **Q3.** Generate various DoE using the functions you just wrote (you may also consider SobolSequence).
- **Q4.** Choose your favourite DoE using the various space filling criteria. Do not forget to test the projections on some variables. Justify your choice in the report.

## 2 Running the experiments

- **Step 1.** Convert your DoE on  $(0,1)^4$  to the hyper-rectangle you defined during the last lab session.
- **Step 2.** If you have changed the parameterization of the problem, convert the set of points to the initial space  $w_l$ ,  $w_w$ ,  $t_l$ ,  $a_l$ . You should obtain a np.array of shape (40,4). The following constrains on the design should be respected:  $w_l + t_l + a_l \le 31.6cm$ ,  $a_l > 2.5cm$ ,  $t_l > 2.5cm$  and  $w_w < 10.1$ .

- **Step 3.** Execute the function writeLaTeX for your design. It will generate a file 'helicopter.tex'.
- **Step 4.** Run a latex compiler to transform the .tex file into a pdf. Note that the compiler must be able to deal with ps-pictures and LaTeX->PS->pdf is recommended.
- **Step 5.** Print the pdf document and start making the helicopters! Use two paper-clips to fix the 'arms' on the 'tail'. These paper-clips are important, they also give stability to the helicopter.
- **Step 6.** Go to the launching area and throw each helicopter 3 times. Record carefully each falling time.