

## APPENDIX

### A. Notations

$N$	Number of Prosumers
$P_i^P(t)$	Available production of agent i at time t
$P_i^D(t)$	Consumption of agent i at time t
$P_i(t) = P_i^P(t) - P_i^D(t)$	Available extra-production of agent i at time t
$WT_i$	Wind turbine set of agent i
$PV_i$	Solar array set of agent i
$DER_i = WT_i \cup PV_i$	DER of agent i
$\nu_i(t)$	wind speed (in $ms^{-2}$ ) at agent i's location and time t
$\Psi_i(t)$	solar irradiance (in $Wm^{-2}$ ) at agent i's location and time t
$\mathcal{F}_{WT}$	power curve for the wind turbines
$\mathcal{F}_{PV}$	power curve for the solar arrays
$P_S^{CRCT}$	Contract value of coalition S
$\phi \in [0, 1]$	Reliability Threshold
$P^{MIN}$	Minimum Contract value
$\alpha$	Parameter that controls the coalitions sizes
$\epsilon$	Correlation graph filtering threshold
$N_{COAL}$	Number of coalitions
$\mathcal{R}_S$	Resilience of coalition S
$\lambda$	unitary price rate for electricity
$\delta_S(i)$	marginal utility of agent i in coalition S
$\rho_{ij}$	Pearson's correlation coefficient between $P_i$ and $P_j$
$\Theta_k(G)$	set of non overlapping cliques of size k in graph G
$\mathcal{R}_S$	resilience of coalition S

## B. Algorithms

**Data:**  $P_i$  series,  
Grid policy  $(P^{MIN}, \phi)$ ,  
Desired number of coalitions  $N_{COAL}$ ,  
size of starting cliques  $k$   
**Result:**  $CS = \{S_1, \dots, S_{N_{COAL}}\}$   
Compute  $G_2^{\epsilon^*}$  ;  
Find the  $N_{COAL}$  cliques in  $G_2^{\epsilon^*}$  ;  
**while**  $\mathcal{U}(CS)$  is improving **do**  
    **for each clique do**  
        Find  $i^*$  ;  
        **if**  $\delta_{clique}(i^*) \geq 0$  **then**  
             $clique \leftarrow clique \cup \{i^*\}$  ;  
        **end**  
        **if**  $\exists j \in clique, s.t. \delta_{clique}(j) < 0$  **then**  
             $clique \leftarrow clique - \{j\}$  ;  
        **end**  
    **end**  
**end**  
**Algorithm 1:** Local greedy optimization algorithm

Figure ?? displays the evolution of the global utility and the number of involved agents during the course of the greedy algorithm ?? . The transition from an invalid to a valid coalitions is clearly visible on the blue diamond curve and occurs between iteration 10 and 15. After this transition, coalition's utilities improve slowly up to a maximum point.

## C. Net production series

Data were collected from [1] (data for the United States at [2]). The variables used in the simulation are :

- Average wind speed (in  $m.s^{-1}$ )
- Nebulosity (integer in  $[0, 8]$ )
- Temperature (in degree Celsius)

1) *Wind power curve:* Power curves are functions that, for a given type of generator, map some input quantity to the output power produced. For wind-turbines and solar arrays

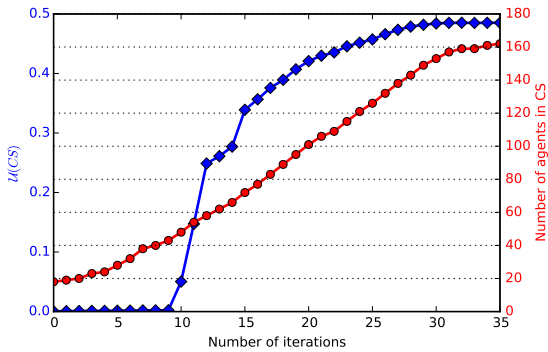


Figure 1: Evolution of the global utility  $\mathcal{U}(CS)$  (blue diamond curve, left axis) and the number of agents involved in the coalitions (red circle curve, right axis) during the greedy optimization of algorithm ??

**Data:** Agent set  $\mathcal{A}$ ,  
Desired number of coalitions  $N_{COAL}$ ,  
Maximum number of iterations  $Loop^{max}$   
**Result:**  $CS = \{S_1, \dots, S_{N_{COAL}}\}$   
 $N^{loop} \leftarrow 0$  ;  
 $CS^* \leftarrow \emptyset$  ;  
**while**  $N^{loop} < Loop^{max}$  **do**  
     $CS \leftarrow SelectRandomCS()$  ;  
    **if**  $\mathcal{U}(CS) > \mathcal{U}(CS^*)$  **then**  
         $CS^* \leftarrow CS$  ;  
    **end**  
     $N^{loop} \leftarrow N^{loop} + 1$  ;  
**end**  
**return**  $CS^*$   
**Algorithm 2:** Random algorithm

**Data:**  $P_i$  series,  
Desired number of coalitions  $N_{COAL}$ ,  
search step size  $\beta < 1$   
**Result:**  $CS = \{S_1, \dots, S_{N_{COAL}}\}$   
 $\epsilon \leftarrow 1$  ;  
 $CS \leftarrow \emptyset$  ;  
**while**  $|CS| < N_{COAL}$  **do**  
    Compute  $G_1^\epsilon$  ;  
     $CS \leftarrow computeClusters(G_1^\epsilon)$  ;  
    **if**  $|CS| = N_{COAL}$  **then**  
        **return**  $CS$  ;  
    **end**  
    **else**  
         $\epsilon \leftarrow \epsilon - \beta$  ;  
    **end**  
**end**  
**Algorithm 3:** Correlated algorithm

these functions are well studied and approximations have been proposed [3] [4], [5]. For the wind turbines, the power curve can be specified by 4 values :

- Cut-in-speed : The wind speed at which the turbine first starts to rotate and generates power.
- Rated-output-power : The maximum power that the turbine can generate.
- Rated-output-speed : The wind speed at which the turbine attains its rated output power.
- Cut-out-speed : The speed at which the turbine is turned off as not to damage the rotor.

The most interesting part is the increase of output power when the wind speed is in the cut-in-speed rated-output-speed range. Even if sometimes a simple linear model is used, the increase has been shown to be non linear and some more complex exponential fit can be found in the literature [3].

2) *Solar power curve:* The input quantity desired for our power curve model for solar arrays is a radiance in  $W.m^{-2}$ , which can be difficult to find in weather station available data. As we mainly collected nebulosity series, we used the Helios model described in [4], [5]. This model enabled us to compute perfect (clear blue sky situation) solar radiances at

some specific locations on earth and at given timestamps. As nebulosity is a measure of the sky cloudiness, we can use the nebulosity series as degradation factors on the clear blue sky model (see [4], [5] for more details) :

$$\begin{cases} \Psi_{real}(t) = \Psi_{perfect}(t)\eta(t) \\ \eta(t) = 1 - 0.75 \left( \frac{N(t)}{8} \right)^{3.4} \end{cases} \quad (1)$$

where  $\Psi_{perfect}(t)$  and  $\Psi_{real}(t)$  are respectively the clear blue sky and real radiances at time  $t$ ,  $\eta(t)$  is the degradation factor at time  $t$ , and  $N(t)$  is the nebulosity index at time  $t$ .

Once we have input data in the forms of radiances, we compute the production of a solar array with the following simplified power curve :

$$\mathcal{F}_{PV}(\Psi_{real}(t)) = S_{PV}\Psi_{real}(t)e_{PV} \quad (2)$$

where  $S_{PV}$  is the surface of the array, and  $e_{PV}$  is its efficiency. The very simple form of this power curve is due to some simplifications in order not to overload the model.

For instance, it does not take into account angles and orientations degradations. These could be incorporated if needed by changing the power curve in the simulations.

3) *Consumption*: Modeling electric consumption has already been widely tackled in the literature. Models can be basically divided into two main categories : Top-down and bottom-up approaches. Top-down techniques take aggregated consumption data as inputs and try to estimate individual consumption patterns while bottom-up methods use a fine modeling of users consumptions as to obtain realistic aggregated consumption curves. In this paper, we used a bottom-up model since the end user, or relatively small aggregations of end users, are in our interest. The main objective was to capture both daily patterns and seasonal variations of the consumptions. We assumed an additive model where the consumption of an agent is the sum of a seasonal heating term that depends on the outside temperature and an electronic consumption term that only depends on the hour of the day. By denoting  $\tau(t)$  the outside temperature at timestamp  $t$ , we can express the consumption  $P_i^D(t)$  of agent  $i$  at time  $t$  :

$$P_i^D(t) = \mathcal{F}_i^{heat}(\tau(t), t) + \mathcal{F}_i^{elec}(t) \quad (3)$$

where  $\mathcal{F}_i^{heat}(\tau(t), t)$  is the power curve that maps the temperature to a heating consumption, and  $\mathcal{F}_i^{elec}(t)$  computes the consumption of agent  $i$  (other than heating) at a given hour of the day. In the simulation, all agents have a desired inside temperature  $T_i$ , supposed to be a constant for simplification. By using thermodynamic laws  $\mathcal{F}_i^{heat}(\tau(t), t)$  can be approximated by :

$$\mathcal{F}_i^{heat}(\tau(t), t) = \frac{B_i}{R_i} [T_i - \tau(t)] \quad (4)$$

where  $B_i$  is the surface of thermal exchanges for agent  $i$  and  $R_i$  is their thermal resistance. We denote by  $\Omega_i$  the

maximum consumption possible for agent  $i$ , which is basically the sum of all its appliances powers. We also denote by  $\omega_i(t) = \{\omega_i(t_0), \dots, \omega_i(t_{24})\}$  the vector of the average fraction of  $\Omega_i$  used for each hour. We can therefore write :

$$\mathcal{F}_i^{elec}(t) = \Omega_i(\omega_i(t) + \epsilon) \quad (5)$$

where  $\epsilon$  is a noise term. The vector  $\omega_i(t)$  enables us to easily differentiate agent consumption behaviors. Business or residential areas for instance can be easily distinguished with this kind of model.

#### D. Resilience algorithm

The following algorithm (see algorithm ??) explains the process through which the resilience of a coalition structure is explored. For a given coalition structure, we consider random failures of physical components of the agents. This results in the agent being unable to support its coalition. Therefore, the agent is simply removed from the coalition, which impacts the coalition's production. Eventually, after some number of agent failures, some coalitions might not be sufficiently stable and productive to fulfill the market's constraints. In this case, the coalition fails, and is removed from the market.

**Data:**  $CS = \{S_1, S_2, \dots, S_k\}$  Coalition structure ;

$pool = \cup_{k \in N_{COAL}} S_k$  ;

**while**  $pool \neq \emptyset$  **do**

    Select randomly agent  $i$  from pool;

$i$  fails  $\Rightarrow$  Remove  $i$  from its coalition :

$S_k \leftarrow S_k - \{i\}$  ;

$pool = pool - \{i\}$ ;

**if**  $Pr[P_{S_k} < P^{MIN}] > \phi$  **then**

$S_k$  fails  $\Rightarrow$  Remove  $S_k$  from the market

**end**

**end**

**Algorithm 4:** Random failures algorithm

#### REFERENCES

- [1] "Infoclimat." [Online]. Available: <http://www.infoclimat.fr>
- [2] "National Centers for Environmental Information." [Online]. Available: <http://www.ncdc.noaa.gov/>
- [3] M. Lydia, S. S. Kumar, a. I. Selvakumar, and G. E. Prem Kumar, "A comprehensive review on wind turbine power curve modeling techniques," *Renewable and Sustainable Energy Reviews*, vol. 30, pp. 452–460, 2014.
- [4] C. Piedallu and J.-C. G  gout, "Multiscale computation of solar radiation for predictive vegetation modelling," *Annals of Forest Science*, vol. 64, no. 8, pp. 899–909, 2007.
- [5] C. Piedallu and J.-C. G  gout, "Efficient assessment of topographic solar radiation to improve plant distribution models," *Agricultural and Forest Meteorology*, vol. 148, no. 11, pp. 1696 – 1706, 2008.