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# Functional modes and thermal B-factor predictions for multigenic structural analysis predicted from Alpha Fold

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## Abstract

Proteins are complex biomolecules that are critical to the functioning of living organisms. They are made up of sequences of amino-acids that fold into specific three-dimensional structures, which is highly related to their function. The process of protein folding is considered one of the most challenging problems in the field of biology and biochemistry, as it involves a delicate interplay of chemical and physical forces that determine the final shape of the protein. AlphaFold is a groundbreaking tool developed by DeepMind that uses artificial intelligence algorithms to predict 3D structure of proteins based on their amino-acid sequence. This tool has the potential to revolutionize the study of enzymes as it provides a fast and accurate way to predict the structure of molecules that have catalytic properties. The present work aims at using AlphaFold to study the catalytic properties of Glutathione Transferase (GST), especially from class  $\delta$  and  $\varepsilon$  of *drosophila melanogaster*, with the ultimate goal of being able to design brand new sequences for enzymes with improved catalytic efficiency.

In addition to using AlphaFold for the generation of 3D structures, molecular dynamics simulations can also be performed based on these structures. It allows to predict some of their potential behaviour and study various factors that may influence the function of the protein, such as thermal fluctuations or protein-ligand interactions. Simulating these processes gives a deeper understanding of how proteins function and allows to identify areas for further investigation and improvements.



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Proteins are biological macromolecules that perform a large variety of functions in living cells comprising biochemical (enzymes), structural, mechanical, and signaling functions. They consist of chains composed of 20 different amino-acids. To perform their functions, proteins interact with small molecules referred to as ligands, which are able to bind to a protein with high affinity and specificity [1]. These protein/ligand interactions are crucial in biology, particularly in the context of drug design [2]. Since proteins interact with a broad range of drugs, it is of particular interest to study the mechanisms of binding of ligands to proteins and its impact on the structural dynamics to gain insights into (i) phenomena involved in the biological process and related to diseases [3] (misfolding, aggregation), and (ii) discovery, design, and development of new drugs [4]. The experimental structural data (e.g., X-ray crystallography, NMR, or cryo-EM) provide key structural information of the ligand-bound and ligand-unbound (APO) proteins [5]. Nevertheless, the static information is not always sufficient for understanding protein–ligand binding mechanisms, especially when pockets are highly flexible and contain several binding sites. Therefore, molecular dynamics (MD) and Normal Mode Analysis (NMA) are powerful tools that provide a description of the dynamics and structures of protein–ligand systems with a high spatial and temporal resolution.

## 1.1 Glutathione Transferase

Glutathione transferases (GSTs) belong to a ubiquitous superfamily of enzymes that metabolize a broad range of reactive toxic compounds by catalyzing the conjugation of reduced tripeptide glutathione ( $\gamma$ -Glu-Cys-Gly; named GSH) to the electrophilic center of a second substrate [6–8], the reactivity of GSH being due to the thiol group SH of the cysteine residue. The conjugation reaction occurs spontaneously but GST accelerates it dramatically. This process of detoxification protects cells against damages caused by both exogenous and endogenous molecules. GSTs were first discovered in liver cells [9], and since then, they have been found to exhibit ligand-binding properties for a large variety of compounds, which are not always their enzymatic substrates [10]. Therefore, GSTs participate in diverse biological processes, making them multifunctional proteins. Moreover, GSTs are classified into three families according to their location in the cell: cytosolic, mitochondrial, and microsomal, which is not evolutionarily related to the two other classes [11]. First-discovered and most-abundant cytosolic GSTs are divided into 13 classes based on homology of their sequences. Members of the same cytosolic class have at least 40% of sequence identity, while members of different classes must have at most 25% of sequence identity. Even if they present a low homology with the cytosolic GST, mitochondrial GSTs can be considered as a particular class of GSTs (Kappa). Among the 42 GSTs identified in *Drosophila melanogaster*,  $\delta$  and  $\epsilon$  are the largest classes, with 25 members [12]. In their catalytic cycle, the GSH usually binds in a specific set of amino-acids called G-site and the hydrophobic xenobiotic in the so-called H-site. Interactions between insects and plant's chemicals lead to a major driving force in herbivorous insect evolution, hence this encourages the study of insect GSTs to understand how spontaneous mutations modify the stability, selectivity and the catalytic efficiencies of this enzyme superfamily.

## 1.2 AlphaFold

X-ray diffraction is a powerful experimental technique that have been used extensively to determine the three-dimensional structures of proteins. In this technique, a crystal of the protein is bombarded with X-rays, and the resulting diffraction pattern is used to determine the position of atoms within the protein. Over the years, X-ray diffraction experiments have played a pivotal role in determining the structures of tens of thousand of proteins, which are deposited in the Protein Data Bank (PDB). However, this experimental process can be time-consuming and technically challenging. Moreover, compared to the vast number of known protein sequences, the ensemble of solved structure is insignificant. In 2021, DeepMind [13] used machine learning approaches with the AlphaFold program. It uses computational models to predict the 3D structures of proteins based on it amino-acid's sequence with a high accuracy. In the field of de novo design of enzymes, AlphaFold has the potential to revolutionize the way we consider the design process, allowing to predict 3D structures that have not yet been experimentally characterized.

In addition to the initial AlphaFold program, DeepMind developped several other tools that have further expanded the capacities of protein structure predictions. One such tool is AlphaFold-multimer[14], which allows predictions for the structure of protein complexe such as homodimers. An other one is AlphaFill[15], which predict the positions of ligands, small molecules that bind to protein such as Glutathione. All together, these tools represent a major step forward in the field of protein study and will be at the root of the present work.

## 1.3 Goals



## 2.1 Multiple Sequence Alignment

Multiple sequence alignment (MSA) is a fundamental technique in bioinformatics used to compare and analyze the similarities and differences between multiple biological sequences. These sequences can be DNA, RNA, or protein sequences and can come from various species or different regions of the same genome. By aligning these sequences, it is possible to identify conserved regions that are important for function or evolution, as well as unique features that differentiate the sequences. In this study, we focus on a set of 25 GSTs sequences related to each other through evolution. Each sequence has a different length, making the alignment process especially useful. Through this analysis, we aim to identify regions of conservation and divergence between the sequences (see exemple below). Our first task was to use MSA to predict both the position of the interface of dimerization and the binding site of the set of GST sequence. The stability of the dimer structure is dependent on the interactions at this interface. Therefore, understanding the location and conservation of the dimer interface can provide insights into the stability of the dimer structure and the mechanisms of the biological activity. On the other hand, the binding site is the specific location on the enzyme where a substrate or ligand binds and interacts. The catalytic efficiency of the enzyme is related to the binding site because it determines the specificity and strength of the substrate-enzyme interaction. Therefore, understanding the location and conservation of the binding site is essential for elucidating the function and mechanism of action of the enzyme.

Each cell in the MSA matrix corresponds to a particular amino acid at a particular position in a particular sequence. We refer to the position in the MSA matrix as the MSA index. The MSA index allows us to compare the amino acid residues at each position across all the sequences in the alignment. We focused on highlighting residues that are known to be part of the dimer interface or binding site. By doing so, we can compare these residues across all sequences and identify any conserved or variable regions.

## 2.2 Anisotropic Network Model

As seen in the introduction, the AlphaFold program allows for the prediction of protein structures with remarkable accuracy. These structures have the potential to be used in a wide range of applications, including molecular dynamics simulations. In this work, we aim to use AlphaFold-predicted structures as input for the Anisotropic Network Model (ANM) to study protein dynamics. Specifically, we will compare the results obtained from the ANM simulations using AlphaFold structures with those obtained using experimentally determined structures. More precisely, we will use the ANM to predict the thermal B-factors of the studied structures[16], which are important indicators of protein flexibility and stability. The insights gained from this study will contribute to the ongoing efforts to develop computational tools for protein structure analysis and facilitate a deeper understanding of protein dynamics and function. To achieve these goals, it is necessary to provide a detailed description of the

ANM and its underlying mathematical principles. The ANM is a widely used method for studying the collective motions and dynamics of proteins based on their structure. It models the protein as a network of connected nodes and springs (representing covalent and non-covalent interactions between them).

### 2.2.1 Theory

Let  $\vec{r}_i$  being the position of the node  $i$  and  $M_i$  it's mass. In the ANM, each node is assumed to be at the bottom of an harmonic potential, since interactions are modeled by connections between nodes, the force matrix is obtained by computing the mass-weighted Hessian matrix

$$\hat{H}_{ij} = -\frac{\Gamma_{ij}\gamma}{\sqrt{M_i M_j}} \frac{\vec{R}_{ij} \vec{R}_{ij}^T}{R_{ij}^2} \quad (2.1)$$

where  $\gamma$  is the spring constant used to model interactions between nodes,  $\vec{R}_{ij} = \vec{R}_j - \vec{R}_i$  and  $\Gamma$  is the contact matrix. In the case were  $i = j$ , the force matrix is computed so that the self interacting term is the response to all the applied forces.

$$\hat{H}_{ii} = -\sum_{j \neq i} \hat{H}_{ij} \quad (2.2)$$

$\Gamma_{ij}$  is the contact matrix that allow or not two nodes to be interacting with each other. The normal modes and eigenfrequencies are given by the diagonalization of the mass-weighted Hessian matrix.

$$\hat{H} \vec{e}_k = \tilde{\omega}_k^2 \vec{e}_k \quad (2.3)$$

It is important to make some remarks at this point, first in the equation (2.1)  $\hat{H}_{ij}$  is actually a three by three matrix. It means that the overall  $\hat{H}$  will be a square matrix of dimension  $d = 3N$  with  $N$  the number of considered nodes. Since the diagonalization algorithms have a complexity of  $O(d^3)$ , it means that the computation time will highly depends on the choosen set of nodes. Second, the masses of the nodes are expressed in  $\text{g.mol}^{-1}$  to avoid numerical errors in the diagonalization. Expressing  $\gamma$  in  $\text{kcal.mol}^{-1} \cdot \text{\AA}^{-2}$ , it means that the eigenvalues  $\tilde{\omega}_k^2$  are expressed in  $\text{kcal.g}^{-1} \cdot \text{\AA}^{-2}$  which is directly proportional to a squared frequency  $\omega^2 = 4.184 \times 10^{26} \text{ s}^{-2}$ . Thermal B-factors of the node  $i$  is directly proportionel to the mean squared fluctuations of the node's position  $\sigma^2(\vec{R}_i)$  and can be computed from the normal modes using the following

$$\beta_i = \frac{8\pi^2}{3} \frac{k_B T}{M_i} \sum_k \frac{|\vec{e}_{k,i}|^2}{\tilde{\omega}_k^2} \quad (2.4)$$

where  $\vec{e}_{k,i}$  contains the elements of  $\vec{e}_k$  related to the node  $i$ .  $\beta_i$  is expressed in  $m^2$  but will always be converted in  $\text{\AA}^2$  because of conventions and usual order of magnitude.

Ever since the beginning, we were talking in a very abstract way about "nodes". In this work, we did consider several ensembles of nodes, namely the amino-acid's center of mass (COM), the heavy atom's position (ATM) and the atom's position (ATM+H). This allowed us to analyse structures with a various number of node. When available, we compared the values computed with the various ANMs with X-ray based measurement in term of pearson correlation.

$$\mathcal{R} = \frac{\sum_i (\beta_i - \langle \beta \rangle) (B_i - \langle B \rangle)}{\sqrt{\sum_i (\beta_i - \langle \beta \rangle)^2} \sqrt{\sum_j (B_j - \langle B \rangle)^2}} \quad (2.5)$$

The values of  $\mathcal{R}$  are between  $-1$  and  $1$  and gives the linear correlation between predicted and measured B-factors. A coefficient of  $1$  is associated to a perfect correlation whereas a coefficient of  $0$  means that there is basically no links between prediction and experiment. Eventually, a negative value of  $\mathcal{R}$

means that there is a correlation with opposite sign and would be interpreted as a result even worst than no correlation. Note that we need to consider the same ensemble of points for  $\beta_i$  and  $B_i$ .

The thermal fluctuation of the nodes is not the only informations one can get from normal modes, indeed fluctuations of the  $\vec{R}_{ij}$  vector can also be an interesting metric to analyse as it represents the relative motion of nodes within a given mode.

$$d_{ij} = k_B T \sum_k \frac{1}{\omega_k^2} \left( \frac{\vec{e}_{k,j}}{\sqrt{M_j}} - \frac{\vec{e}_{k,i}}{\sqrt{M_i}} \right)^2 \quad (2.6)$$

Such metric is especially interesting to study as it provide insights about the fluctuations of a mode with respect to another and allow to identify pairs of nodes involved in specific functional modes.

### 2.2.2 Parametrization

In the Anisotropic network model as presented above, we consider two parameters namely the contact matrix  $\Gamma_{ij}$  and the spring constant  $\gamma$ . In order to get predictions that are physically relevant, it is necessary to compute the good parameters. Let us first consider the contact matrix. Given two nodes  $i$  and  $j$ , we will consider  $\Gamma_{ij} = 1$  if the distance  $|\vec{R}_{ij}|$  is smaller than the cut-off  $R_c$ . It is then necessary to find a good numerical value for  $R_c$ . Assuming an infinite cut-off, the structure will eventually be much more rigid that it needs to be, we then look for  $R_c$  as small as possible. We know that the eigenvalues are associated to frequencies for the collective modes. The six firsts modes should be global translations and rotations with a null frequency associated. In the case where  $R_c$  is too small, some other modes will have null eigenfrequencies with no physical justifications.  $R_c$  is then the smallest value that gives exactly 6 null eigenvalues for the Hessian. Eventually, in the equation (2.1)  $\gamma$  is a constant, it means that  $\tilde{\omega}_k^2 \propto \gamma$ . From the equation (2.4), one can show that  $\beta_i$  is inversly proportional to  $\gamma$  which is just a scaling factor. It can then be computed from comparitions with experimental measurments of thermal B-factors using least squared methods.

## 2.3 Molecular Dynamics

Molecular dynamics (MD) has emerged as a powerful computational tool for simulating molecular systems with exceptional precision. By numerically integrating the equations of motion for atoms and molecules, MD provides detailed information about the dynamic behavior and interactions within these systems. With its ability to capture the atomic-level motion and thermodynamics, MD offers insights into the structural changes, energetics, and properties of molecules under various conditions. Compared with ANM, MD stands out for its superior precision in capturing the dynamic behavior of molecular systems. For the purpose of this work, the amount of system to be studied is far too big (25 structures  $\times$  3 states in the catalytic cycle) and cannot be considered as an option. But considering it's accuracy, one can consider a sample of GSTs that will be simulated via MD.

MD consider interactions between atoms in a large variety of form. First, non-bonded interactions are considered with a lehnard-jones potential and electrostatic interactions.

$$V_{\text{non-bonded}}(\vec{r}_i) = \sum_j 4\epsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{R_{ij}} \right)^{12} - \left( \frac{\sigma_{ij}}{R_{ij}} \right)^6 \right] + \sum_j \frac{q_i q_j}{4\pi\epsilon_0 R_{ij}} \quad (2.7)$$

Interactions between bonded atoms are also described by the following.

$$V_{\text{bonded}}(\vec{r}_i) = \sum_{\text{bonds}} K_l (l - l_0)^2 + \sum_{\text{angles}} K_\theta (\theta - \theta_0)^2 + \sum_{\text{tortions}} K_\varphi [1 + \cos(n\varphi + \delta)] \quad (2.8)$$

The ensemble of parameters for those interactions are optimized and used by MD algorithms by the so called force fields. Since the potential consider interactions between all the atoms of the system, this kind of simulation is called All Atoms MD, in opposition to coarse grained MD that we wont discuss

here. Finally forces of interactions are obtained taking the gradient of the potential and the simulation is achieved by integration of the Newton's equation :

$$m \frac{d^2 \vec{r}_i}{dt^2} = -\vec{\nabla} V(\vec{r}_i) \quad (2.9)$$

From the time serie obtained, one can compute the associated Thermal B-Factors as mean squared fluctuations of the atom's position.

$$\beta_i = \frac{8\pi^2}{3} \langle \vec{R}_i^2 \rangle \quad (2.10)$$

Comparisons between such factors computed from MD and from ANM gives again extra informations about the precision of the considered models.

### 3.1 Sequences and Static Structures

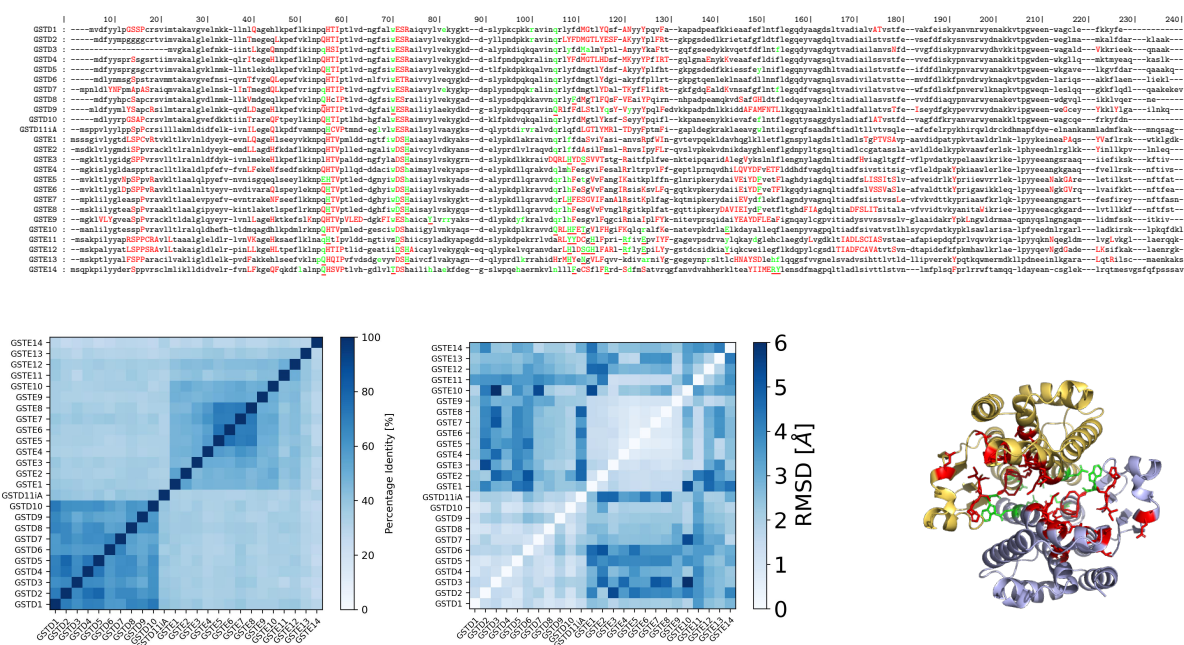


Figure 3.1: MSA & RMSD matrix of the considered GSTs

As a preliminary analysis, the 25 sequences of GSTs were aligned using MSA algorithms and structures were predicted using AlphaFold. The percent identity matrix has been computed and allow to show similarity between GSTs from a sequential point of view. The proteins from class  $\delta$  are all considered as part of the same cluster but for the  $\epsilon$  class, some variations pears and it seems that the class itself is very heterogene. MSA also allowed us to determine the conserved regions for the binding site (highlighted in green) and the structural differences based on the RMSD matrix. In the class  $\delta$ , the residues in a MSA index of 70 – 76 present a very high degree of conservation, and the same goes for the residues 204 – 210 in the class  $\epsilon$ . Conserved regions are a first probe for the common function of proteins, mainly catalyse in the case of GSTs. Moreover, the programm AlphaFill also allows to predict the position of ligands in the structures and thuss determine the residues involved in the protein/ligands binding. Here, it clearly appears that the ligands usually binds in the regions 55 – 58; 71 – 73; 111 – 121 with a high conservation but also in region 144 – 153 of class  $\epsilon$  with a much smaller conservation. From a geometrical point of view, the structures in class  $\delta$  are self similar (with RMSDs between 1 and 2 Å) and structures in class  $\epsilon$  are also self similar but with some exceptions like the GSTE10, GSTE13 and GSTE14 that can either be exceptions from a biological point of view or different because of the precision of the predictions of AlphaFold (with RMSDs  $\approx$  4 Å). Finally, the interface of dimerization looks well conserved from a positional point of view but also from a chemical

point of view, with a lot of chemically similar residues in the associated interfaces.

### 3.2 Dynamics from Normal Modes

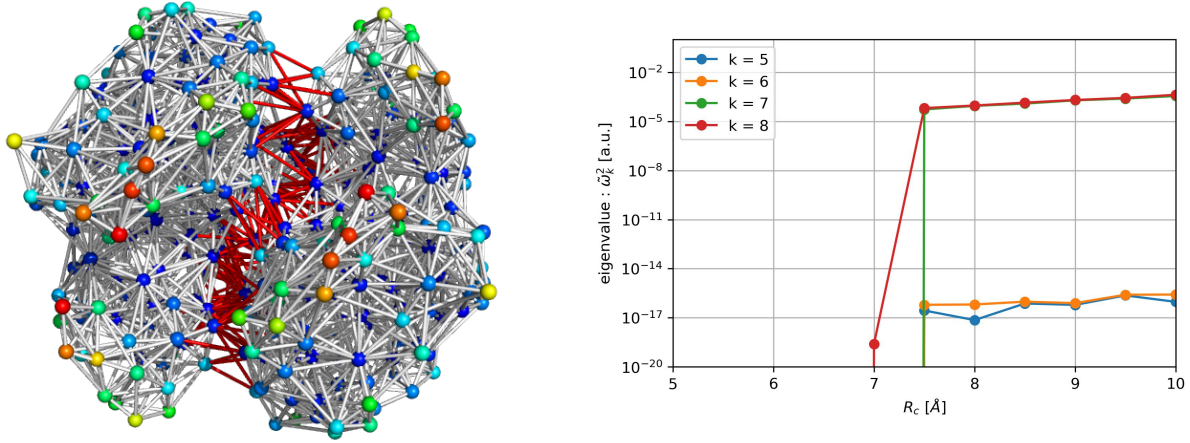


Figure 3.2: ANM-COM, cut-off parametrization

As presented before, this work aim at looking at the flexibility of the structures from ANM. A very first step is to decide of a set of parameters for the model. Let us first consider the GST-D1 structure predicted from AlphaFold. As seen in equation (2.1), the parameter  $R_c$  have a direct influence on the elements of the mass-weighted hessian  $\hat{H}$  and thus a direct influence on it's eigenvalues. The figure 3.2 gives a visual representation of the set of center of mass and gives the influence of  $R_c$ . Here, it clearly appears that the modes 5 and 6 are numerically nulls but the 7<sup>th</sup> mode gets non-null for cut-off above 7.5Å. This specific value then is the optimal value used for the computation of collective modes (2.3).

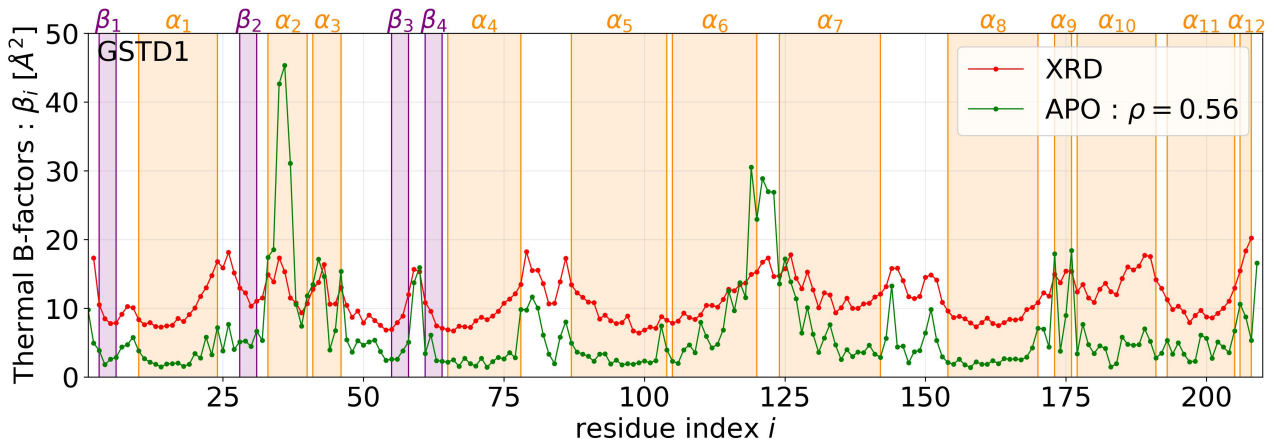


Figure 3.3: Thermal B-factors predictions for the AlphaFold's structure of GST-D1 and comparison with XRD experiment

From the expression (2.4), one can plot the predicted B-factors (green curve) as well as the results from X-ray diffraction (red curve). The coefficient  $\gamma$  used here is obtained using the least squared methods and gives a spring constant of 14 kcal.mol<sup>-1</sup>.Å<sup>-2</sup>. The actual precision of the measurment have been quantified based on the pearson correlation between the two series (2.5) and gives 56% which is a value that one can consider as descent !

### 3.3 Dynamics from Molecular Dynamics

### 3.4 Comparison between Structures





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