

# Indivisibilities in Investment and the Role of a Capacity Market

L

Nicolas Stevens

Join work with Yves Smeers & Anthony Papavasiliou

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# Motivations for the work

## Investment Problem

- Principle at the time of restructuring: **market will solve the investment problem**
- Then the “**missing money**” problem arises and questioned the ability of the market to foster sufficient investments
- This problem has generated a considerable literature on the respective merits of different **market designs** (CRM, CfD, PPA, etc)

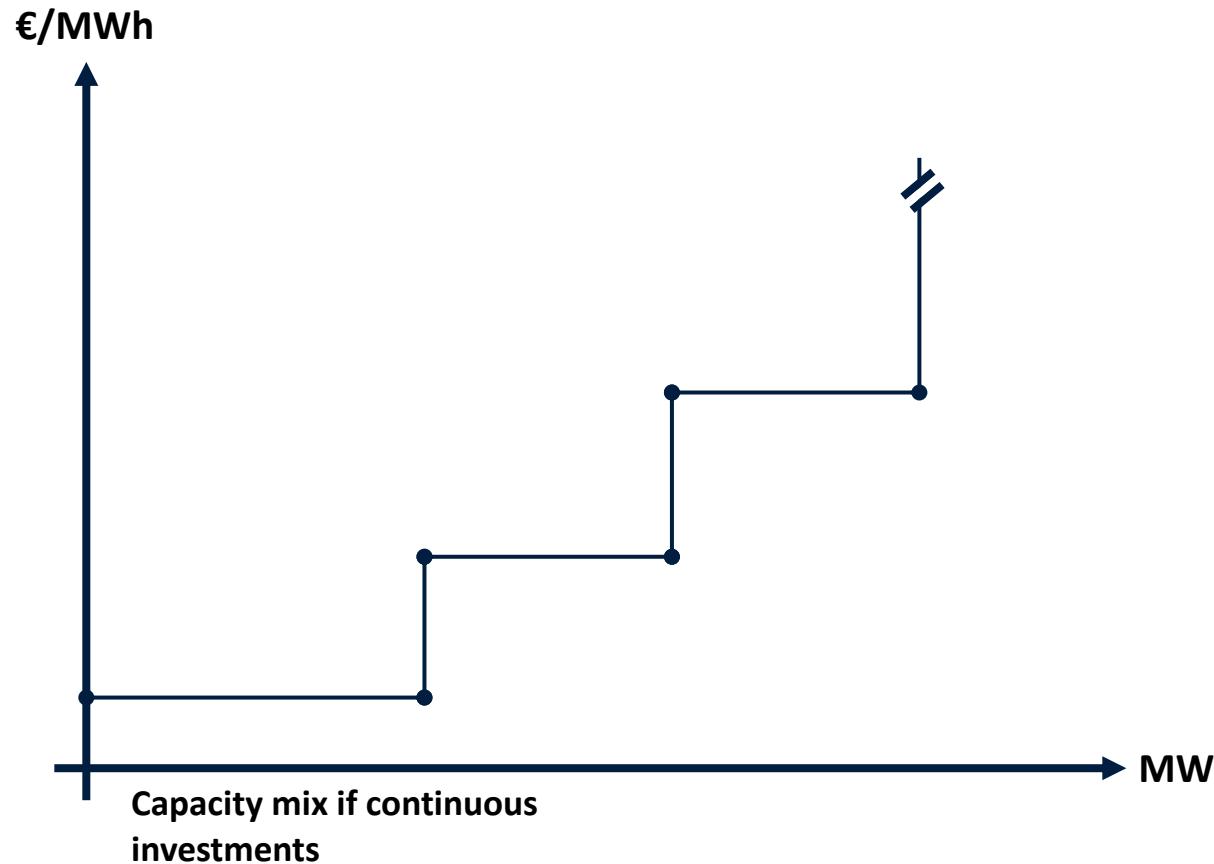
## Indivisibility Problem

- It was quickly recognized that generation plants have **short-term “indivisibilities”** (start-up, etc.)
- These required some **public coordination** (design of pricing scheme, side payments)
- Indivisibilities also have a **long-term dimension**:
  - **Large fundamentally indivisible projects** (nuclear units, offshore wind island, etc.)
  - **Economies of scale**, learning by doing

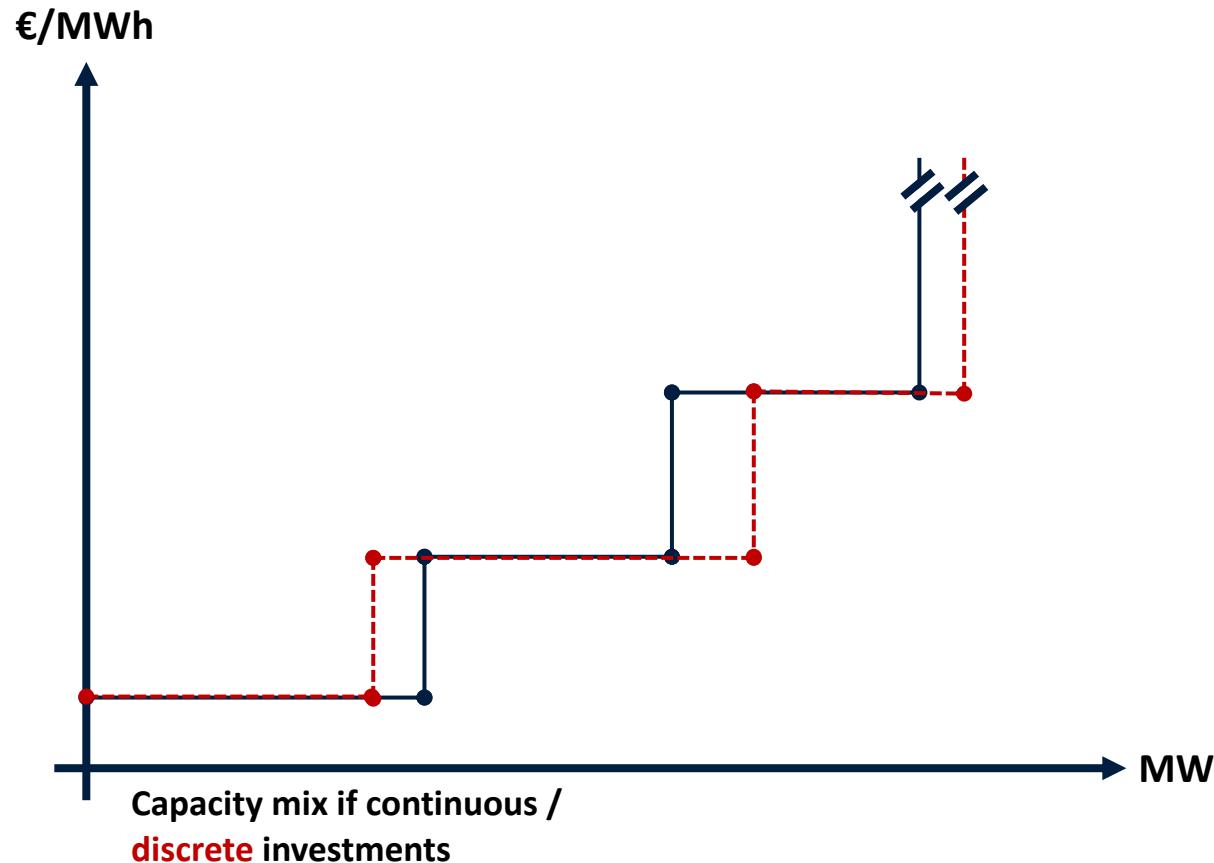
**Objective of the work**—Explore the problem of **capacity expansion with discrete variables** (using the market to drive investment) and explore analogies with **missing money**

**Method**—Leverage the development on the “**pricing**” of **indivisibilities in unit commitment**

# Intuitive introduction to the research idea

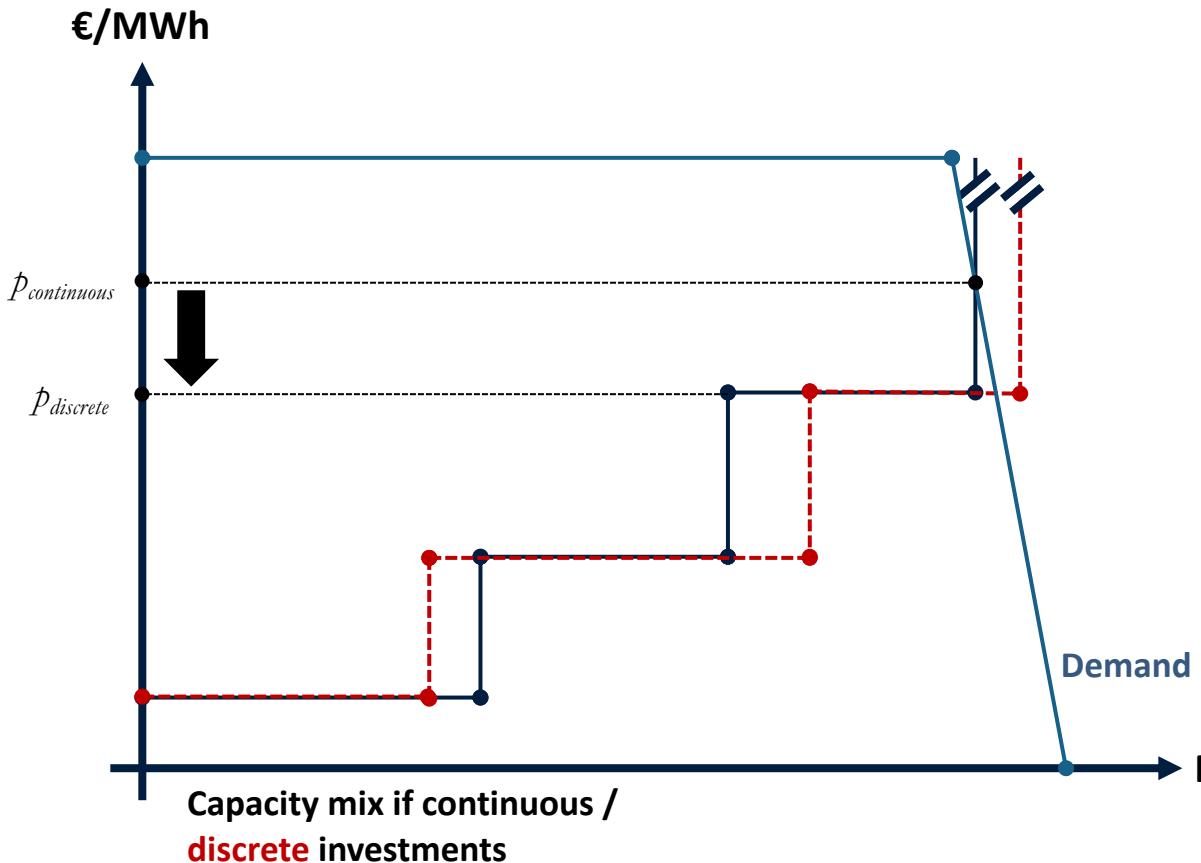


# Intuitive introduction to the research idea



- Lumpiness of investment may **disturb the capacity mix**, as compared with continuous investments
- This may impact the **total system cost** which will be higher than if investments were continuous

# Intuitive introduction to the research idea



- Lumpiness of investment may **disturb the capacity mix**, as compared with continuous investments
- This may impact the **total system cost** which will be higher than if investments were continuous
- But lumpiness may **also impact prices**: if leading to slight “over-investments” compared to the continuous case (given load curtailment is expensive), lumpiness may reduce the price (especially given load is inelastic )
- This may in turn lead to a kind of “**missing money**”
- Objectives** of the work
  - Model and theory** of this “missing money”
  - Analyze **numerically** the magnitude of it
  - Analyze **market solutions** to the problem (**CRM**)

## The long-term indivisibilities

- The continuous investment problem
- The lost opportunity cost under the discrete investment problem
- Illustration on a toy example

## Solution(s) to the indivisibilities

- Discriminatory payments
- Uniform price solution and capacity markets
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## Numerical Results

- ENTSO-E capacity expansion model
- Models and data description
- Results

## Conclusion

- Perspective for future research

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# The continuous investment problem

In the **continuous investment problem**, there exists a uniform energy price  $\pi_t$  with a welfare-maximizing allocation  $(d_t^*, x_g^*, q_{g,t}^*)$  that constitute a competitive equilibrium (Boiteux, 1949/1960)

$$\max_{q,x,d \geq 0} \quad \sum_t \Delta T_t V_t d_t - \sum_g \sum_t \Delta T_t MC_g q_{g,t} - \sum_g IC_g x_g \quad (1a)$$

Minimize total costs (operational + investment)

$$(\Delta T_t \pi_t) \quad d_t \leq \sum_g q_{g,t} \quad \forall t \quad (1b)$$

Market clearing constraint (supply = demand)

$$(\Delta T_t \mu_{g,t}) \quad q_{g,t} \leq x_g \quad \forall g, t \quad (1c)$$

Link between investment and operation

$$(\Delta T_t \eta_t) \quad d_t \leq D_t \quad \forall t \quad (1d)$$

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Investment in g

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| Production of g in t   | Investment in g |   |
|--|-----------------|---|
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Consumption in t

Production of g in t

Investment in g

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# The discrete investment problem

The discrete investment problem **turns the investment decisions into binary variables**: investment into lumps of capacity  $P_{g,i}^{max}$

$$\max_{q,x,d} \sum_t \Delta T_t V_t d_t - \sum_{g \in \mathcal{G}} \left( \sum_t \Delta T_t MC_g q_{g,t} + \sum_i x_{g,i} IC_{g,i} \right) \quad (3a)$$

$$\sum_{g \in \mathcal{G}} q_{g,t} \geq d_t \quad \forall t \in \mathcal{T} \quad (3b)$$

$$q_{g,t} \leq \sum_i P_{g,i}^{max} x_{g,i} \quad \forall g \in \mathcal{G}, t \in \mathcal{T} \quad (3c)$$

$$q_{g,t} \geq 0 \quad \forall g \in \mathcal{G}, t \in \mathcal{T} \quad (3d)$$

$$x_{g,i} \in \{0, 1\} \quad \forall g \in \mathcal{G}, i \quad (3e)$$

$$0 \leq d_t \leq D_t \quad \forall t \in \mathcal{T} \quad (3f)$$

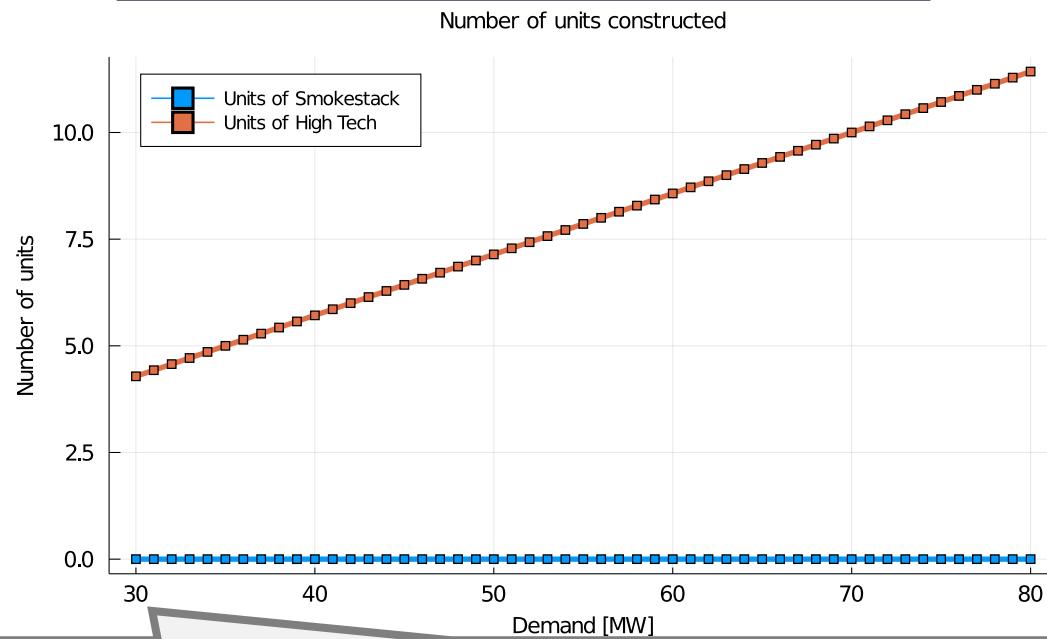
# Illustration on a numerical example (Scarf, 1994)

|            | Capacity [MW] ( $P^{max}$ ) | Investment Cost ( $IC$ ) | Marginal Cost ( $MC$ ) |
|------------|-----------------------------|--------------------------|------------------------|
| Smokestack | 16                          | 53                       | 3                      |
| High Tech  | 7                           | 30                       | 2                      |

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Continuous investment



Smooth investment decisions

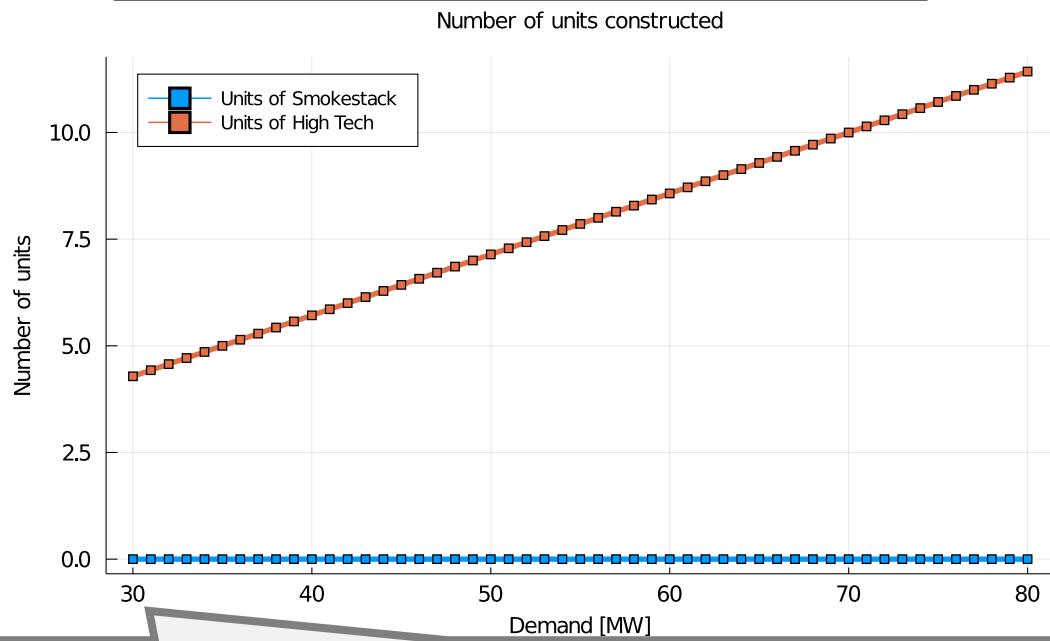
+ A long-term competitive equilibrium exists

(price=6.3125€/MWh) → both technologies have incentives to implement the efficient outcome

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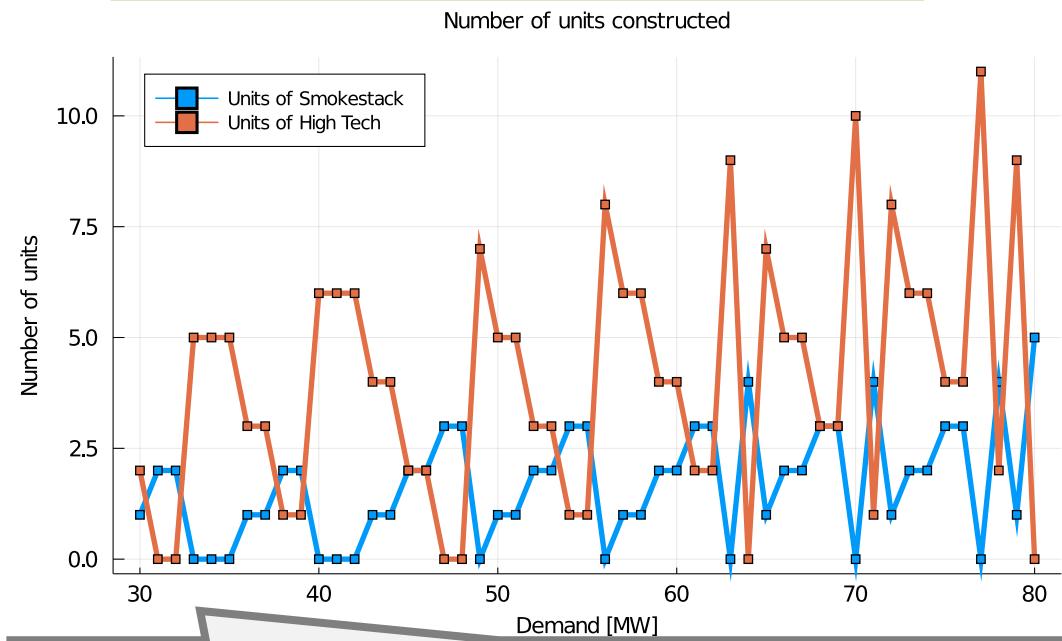


Smooth investment decisions

+ A long-term competitive equilibrium exists

(price=6.3125€/MWh) → both technologies have incentives to implement the efficient outcome

Discrete investment



Cycling effect

+ A long-term competitive equilibrium does NOT exists

→ There will be incentives to deviate from efficient outcome

# Long-term Lost Opportunity Costs

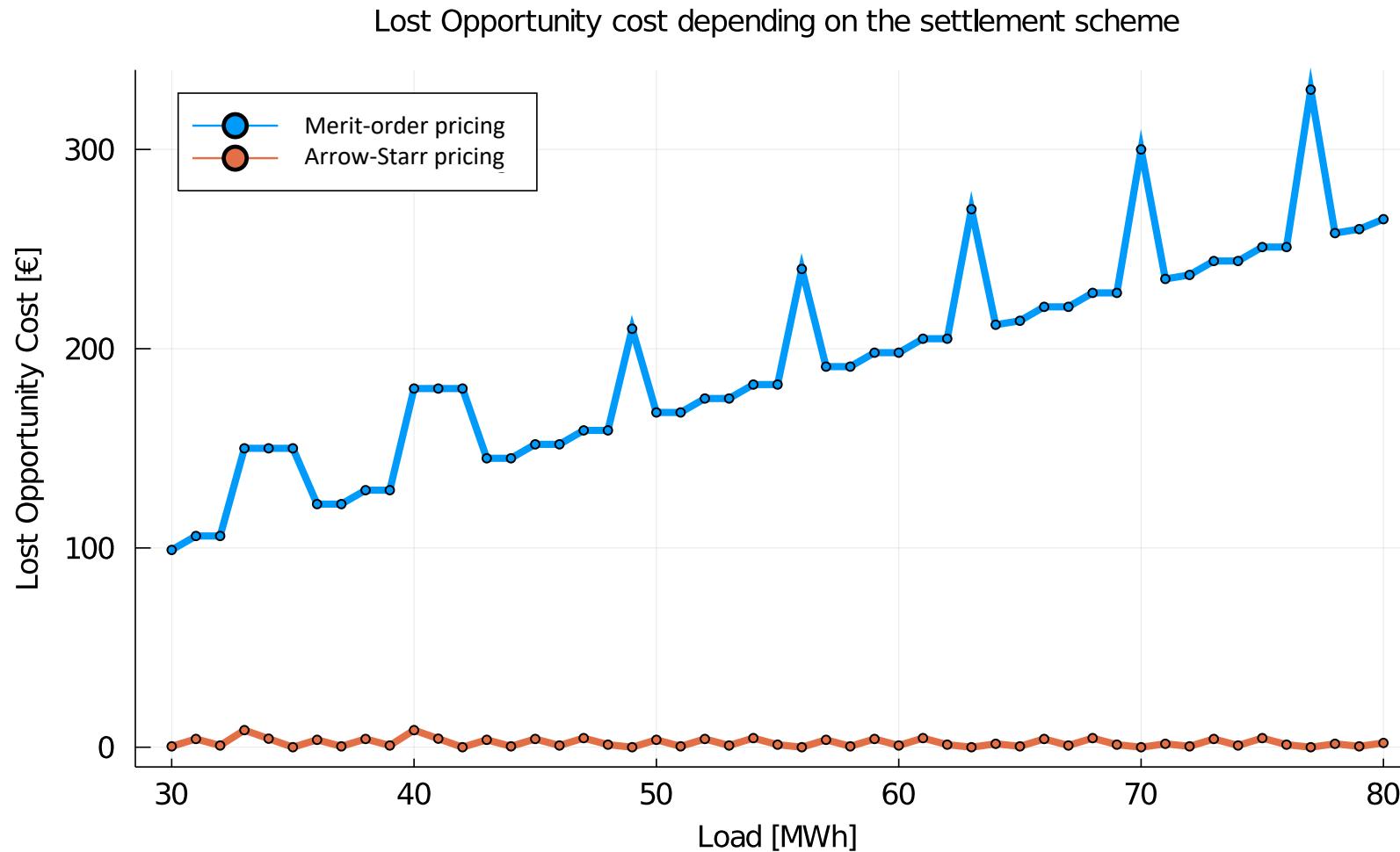
**Definition 5** (Long-term Lost Opportunity Cost) The lost opportunity cost (*LOC*) is the difference between the selfish maximum profit under self-scheduling and the as-cleared profit (with allocation  $(q^*, x^*, d^*)$ ) under price  $\pi$ . For each supplier  $g$ , it is expressed as:

$$0 \leq LOC_g(\pi) = \overbrace{\max_{(q,x)_g \in \mathcal{X}_g} \mathcal{P}_g(q, x, \pi)}^{\text{selfish maximum profit}} - \overbrace{\mathcal{P}_g(q^*, x^*, \pi)}^{\text{as-cleared profit}} \quad (7)$$

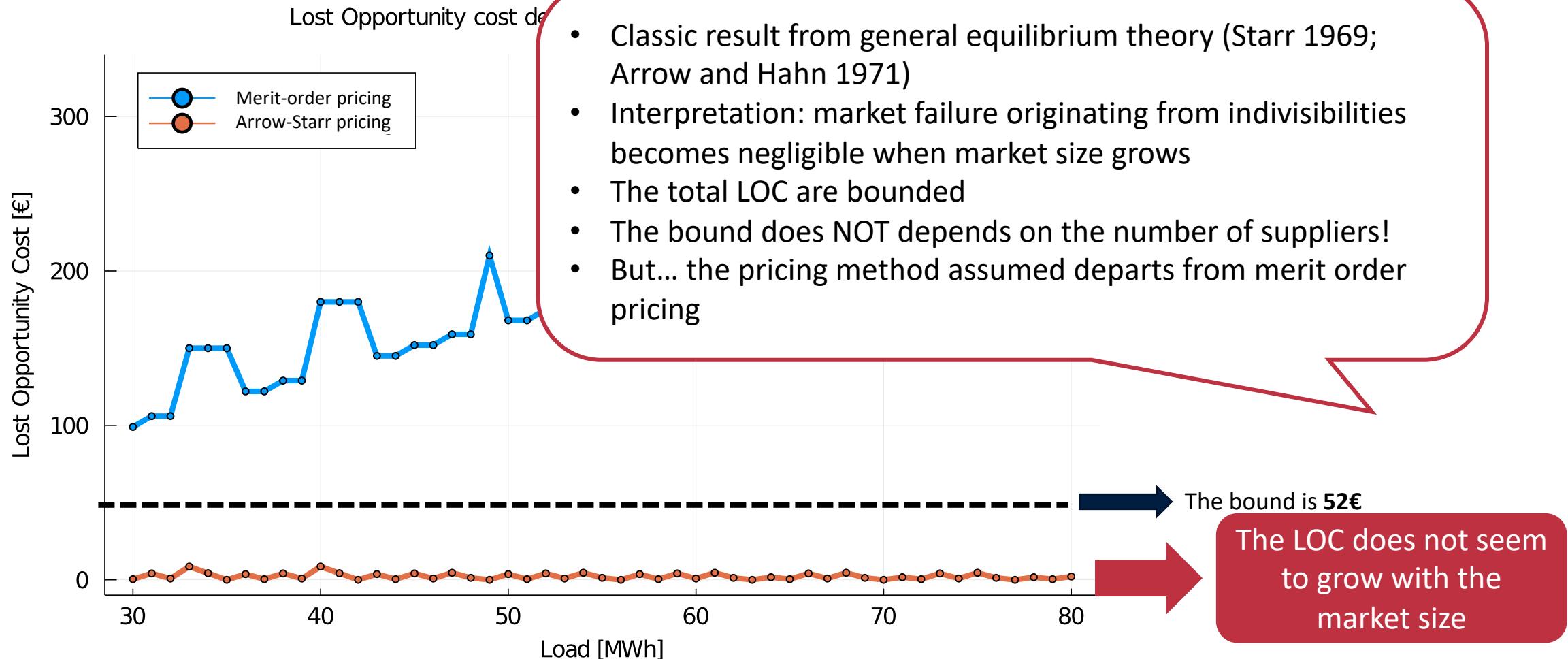
Intuitively, given the market price, some agents will :

- Either have the incentive to exit the market (facing a **revenue shortfall**)
- Or have the incentive to build more than what is socially optimum (facing a **foregone opportunity**)

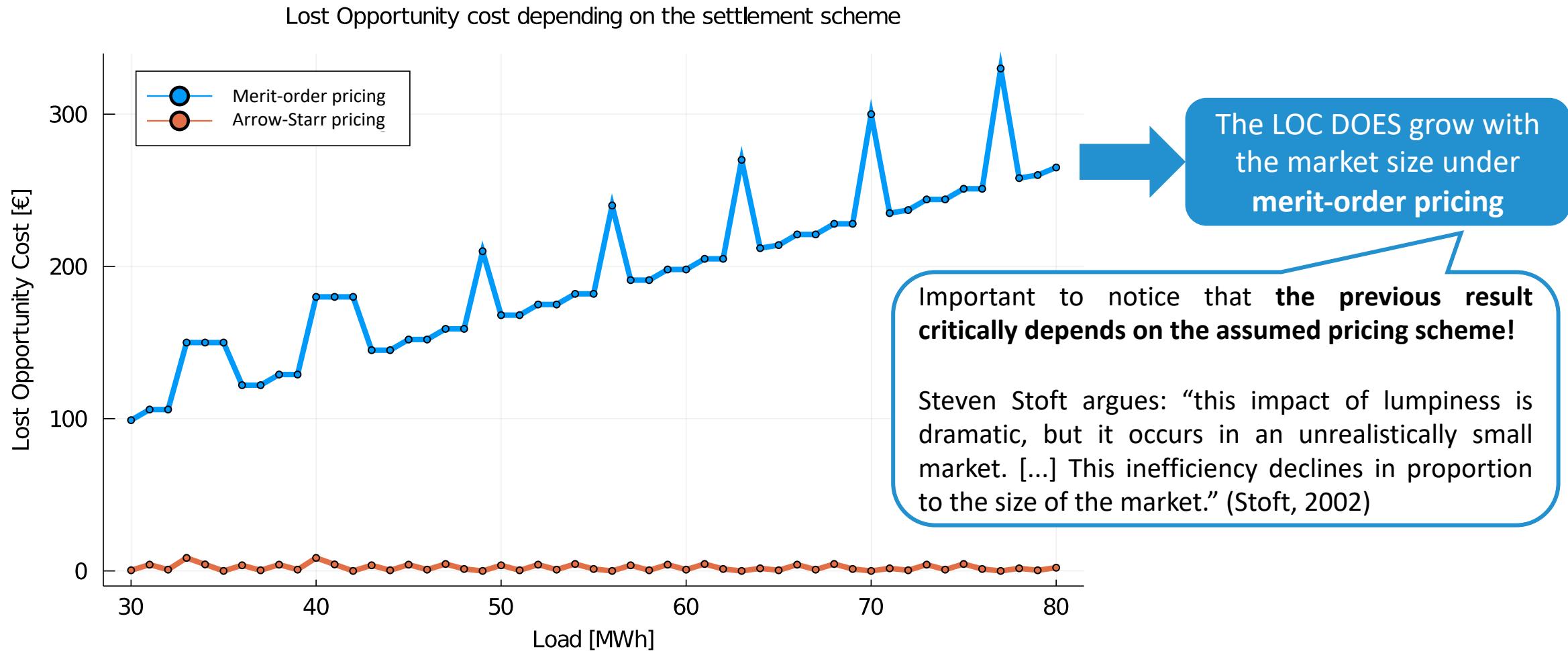
# Illustration on a numerical example



# Illustration on a numerical example



# Illustration on a numerical example



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# Market incompleteness: discriminatory prices solution

- **What is broken** by the presence of indivisibilities in the investment decisions **is the possibility to achieve a perfect coordination** of private agents solely by means of a **uniform energy price signal**
- A purely **decentralized market** do not lead to a welfare-maximizing investment
- **O'Neill (2005)** : mitigate the LOC by **extending the set of commodities**
  - Two commodities : energy and capacity
  - Uniform price of energy & discriminatory prices for capacities
  - O'Neill shows that this is a market equilibrium

# Uniform capacity price solution?

- Motivation: Capacity markets are currently a much debated topic in power system economics
- Can we find a **uniform (capacity) price** way to mitigate the LOC?

**Definition** (Profit Under Energy and Capacity prices). *The agent  $g$  is assumed to maximize its selfish profit function  $\mathcal{P}_g$  defined as follows:*

$$\max_{\substack{(c,p,x)| \\ (5c), (5d) \\ (5e)}} \mathcal{P}_g(c, p, x, \pi^E, \pi^C) = \max_{\substack{(c,p,x)| \\ (5c), (5d) \\ (5e)}} \left\{ \sum_t \pi_t^E p_{g,t} + \pi^C \sum_i P_{g,i}^{max} x_{g,i} - \sum_t MC_g p_{g,t} - \sum_i IC_{g,i} x_{g,i} \right\} \quad (18)$$

# Uniform price capacity market

## *The capacity auction model*

**Definition 10** (Discrete Capacity Auction) The capacity auction minimizes the cost of satisfying the inelastic capacity demand  $C^{min}$ :

$$\min_x \sum_{g \in \mathcal{G}} \left( \sum_{i \in \mathcal{I}_g} x_{g,i} IC_{g,i} - \sum_{i \in \mathcal{I}_g} P_{g,i}^{max} x_{g,i} \sum_{t \in \mathcal{T}_g} \Delta T_t (\pi_t^M - MC_g) \right)$$

Agents' bids: investment cost – profit from energy market

$$(\pi^C) \quad \sum_{g \in \mathcal{G}} \sum_{i \in \mathcal{I}_g} P_{g,i}^{max} x_{g,i} \geq C^{min}$$

“Market clearing constraint”: capacity target set by the SO

$$x_{g,i} \in \{0, 1\} \quad \forall g \in \mathcal{G}, i \in \mathcal{I}_g$$

→ **Theorem:** the capacity price resulting from the above auction (under some assumptions), reduces the Lost Opportunity Cost (LOC) of the market agents

# Illustration on a numerical example



The LOC are mitigated by  
the uniform capacity price  
...but not reduced to 0

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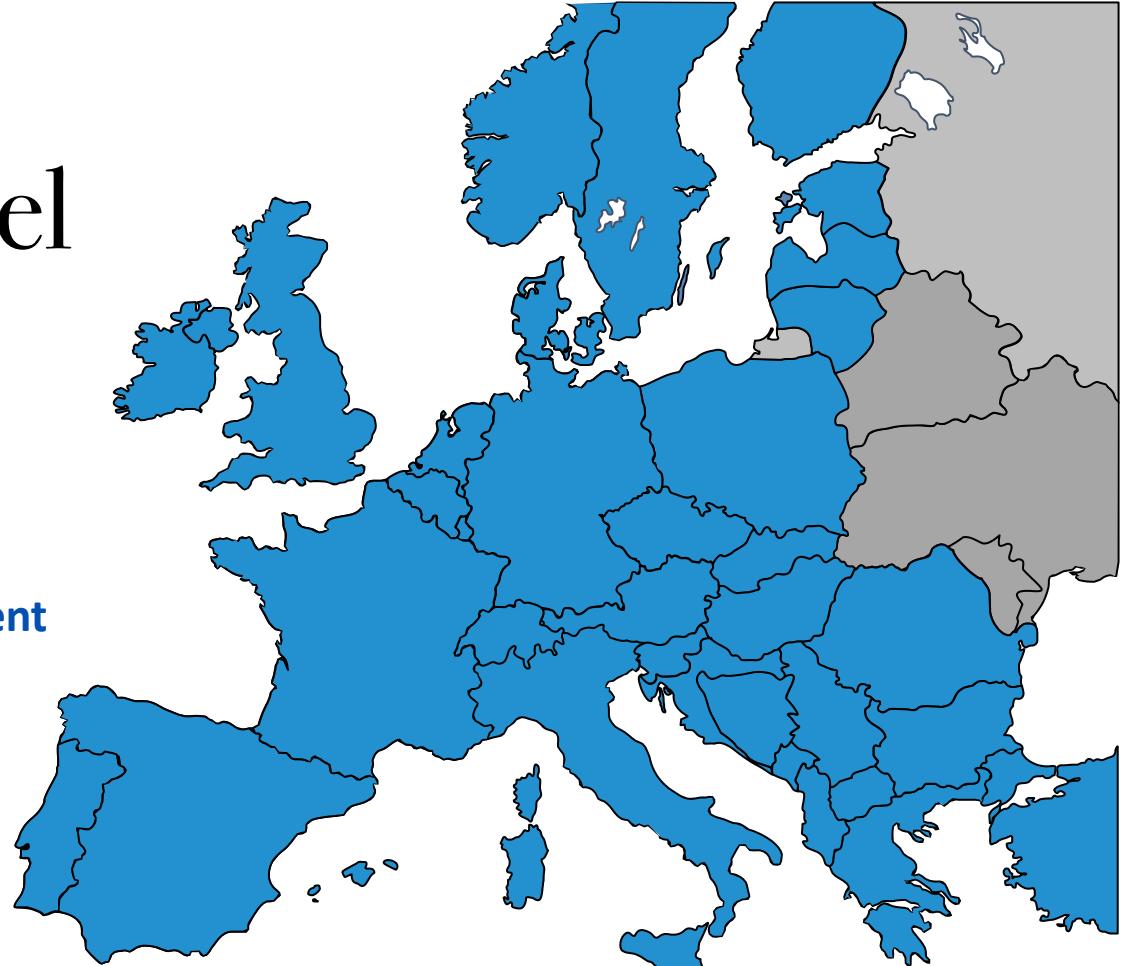
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# EU Capacity expansion model

- To what extend does this theoretical problem materialize in big (realistic) systems?
- Based on ENTSO-E data ([European Resource Adequacy Assessment \(ERRA\)\\*](#))
- Both operations and **investment decisions are convex** in ERRA (essentially for computational reasons)
- Our **objectives**:
  - Simulate the continuous model
  - Simulate the discrete model
  - Simulate the capacity market as previously described



## KEY FIGURES\*

- Geographical ext.: **37** countries
- Bidding Zones: **56**
- Target year: **2025**
- Num. of Techno.: **20**

# EU Capacity expansion model

- **Minimization of total cost** (investment + operational costs),  
Load curtailment valued at VOLL
- **Operational constraints** (all convex sources of production):
  - Thermal production
  - Batteries (load shifting)
  - Demand response (load shedding)
  - 4 types of hydro power plants
- **Network constraints:** convex, mainly cross-border ATC lines
- **Investment decisions:**
  - Investment in **new** MW of production units  
→ essentially unlimited
  - Retirement of **existing** MW of production units  
→ limited for many technologies

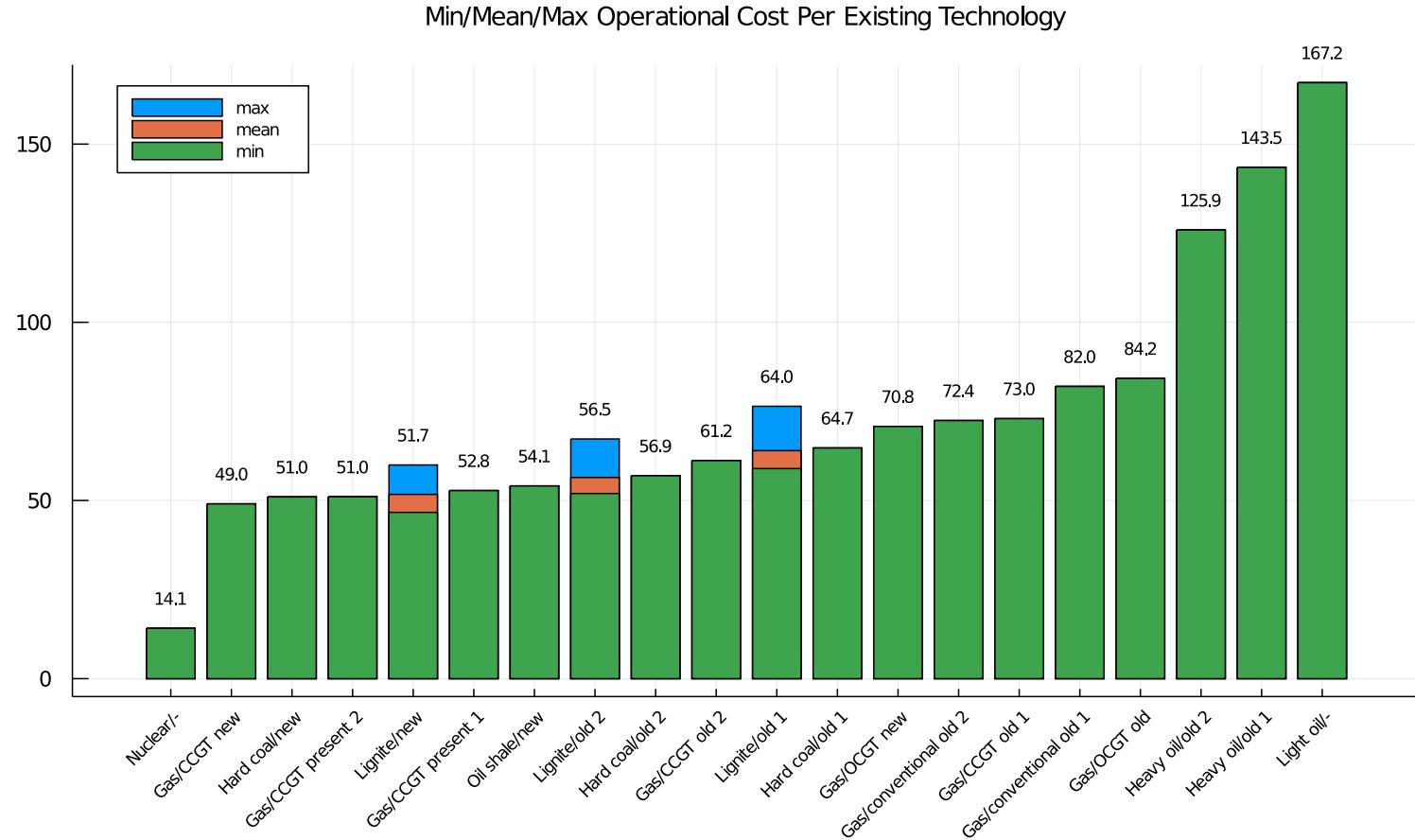


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# The EU input data

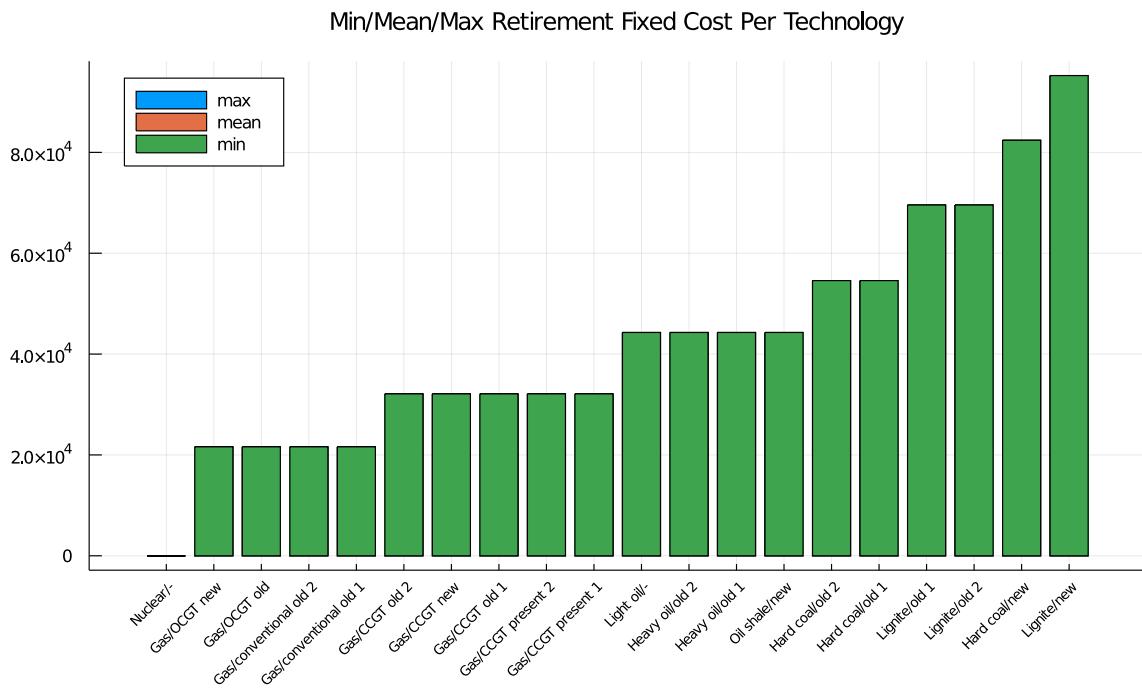
## *Merit order (Operational cost) of the entire system*



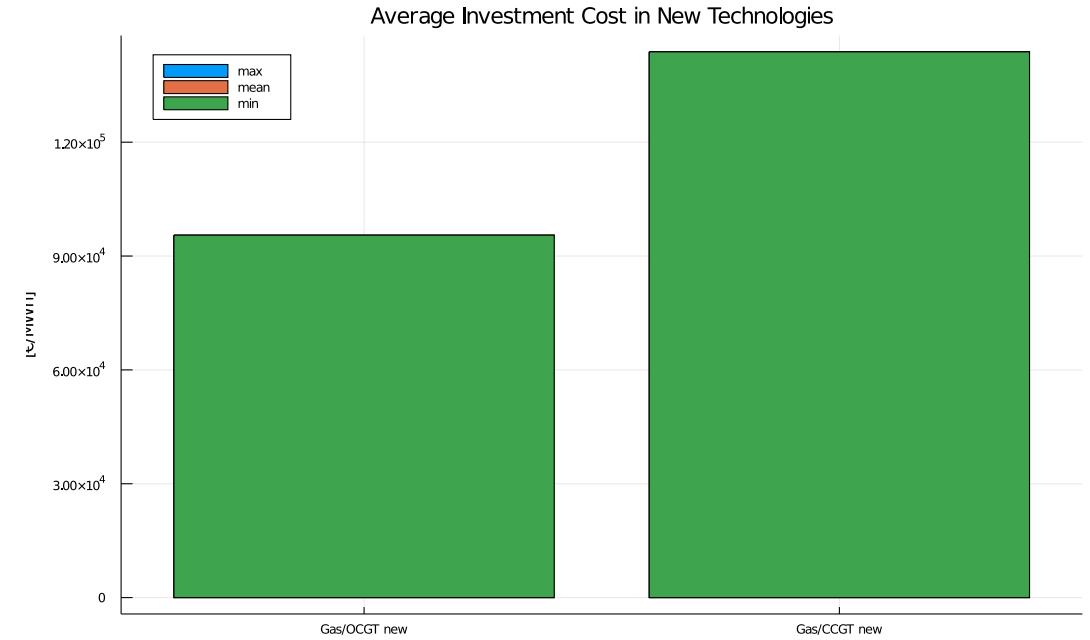
# The EU input data

## *Fixed costs*

### Retirement of **Existing** installed capacity



### Investments in **New** installed capacity



# The results

|                | Total Cost |          |      |
|----------------|------------|----------|------|
|                | Cont.      | Disc.    | Inc. |
| ...<br>1989    | 7.385e10   | 7.409e10 | 0.3% |
| ...<br>2014    | 7.228e10   | 7.258e10 | 0.4% |
| ...<br>Average | 7.637e10   | 7.657e10 | 0.3% |

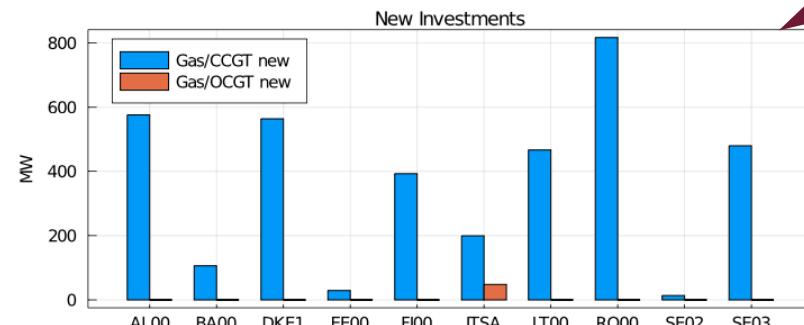
1

In terms of TOTAL COST, the inclusion of lumpiness of investment leads to an increase of +0.3%.

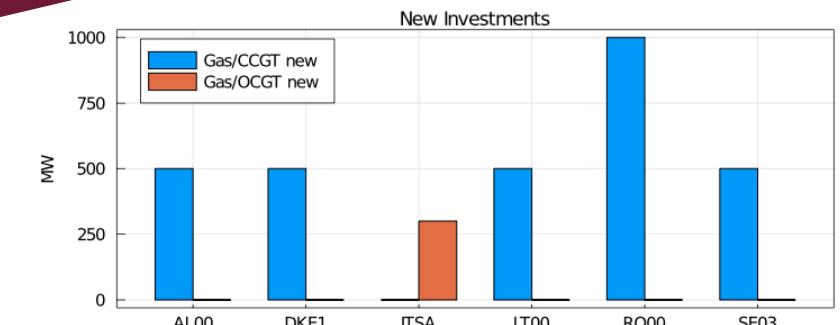
Simulations performed over 31 net load scenarios

# The results

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| 2014    | 7.228e11   |          |      |
| ...     |            |          |      |
| Average | 7.637e11   |          |      |



(a) Continuous model



(b) Discrete model

2

It also leads to some rearrangement in terms of commissioning / decommissioning decisions

**Fig. 5:** Commissioning decisions under the continuous and discrete model for the scenario 2014.

# The results

3

The essential difference with the continuous case is that the agents now have incentives to deviates from the welfare-maximizing investment!

|          |                | Without capacity market |             |         | With capacity market |         |           |
|----------|----------------|-------------------------|-------------|---------|----------------------|---------|-----------|
|          |                | New units               | Exist units | Total   | Inelastic            | Elastic | No Coord. |
| 1989     | <i>LOC</i>     | 3.534e8                 | 1.376e8     | 4.91e8  | 4.863e8              | 6.354e8 | 1.144e9   |
|          | $RS^{\in LOC}$ | 1.802e7                 | 0.0         | 1.802e7 | 1.335e7              | 4.154e7 | 3.244e7   |
|          | <i>FO</i>      | 3.354e8                 | 1.376e8     | 4.73e8  | 4.73e8               | 5.939e8 | 1.111e9   |
| 2014     | <i>LOC</i>     | 1.052e8                 | 3.202e8     | 4.254e8 |                      |         |           |
|          | $RS^{\in LOC}$ | 6.925e7                 | 3.171e8     | 3.864e8 |                      |         |           |
|          | <i>FO</i>      | 3.599e7                 | 3.061e6     | 3.905e7 |                      |         |           |
| ...      |                |                         |             |         |                      |         |           |
| Averages |                |                         |             |         |                      |         |           |
|          | <i>LOC</i>     | 6.528e8                 | 4.754e8     | 1.128e9 | 7.0e8                | 9.149e8 | 1.404e9   |
|          | $RS^{\in LOC}$ | 9.598e7                 | 3.477e8     | 4.437e8 | 1.463e7              | 2.29e7  | 2.385e7   |
|          | <i>FO</i>      | 5.568e8                 | 1.277e8     | 6.846e8 | 6.854e8              | 8.92e8  | 1.38e9    |

The **LOC are significant** although we are considering a large system: among all the possible commissioning (resp. decommissioning) decisions, **11% (resp. 10%)** face a positive LOC.

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| ...      |                |                         |             |         |   |         |           |
| 2014     | <i>LOC</i>     | 1.052e8                 | 3.202e8     | 4.254e8 | There are some plants that should be constructed/not retired while loosing money: |         |           |
|          | $RS^{\in LOC}$ | 6.925e7                 | 3.171e8     | 3.866e8 | • 67% of effective commissioning come with a RS                                   |         |           |
|          | <i>FO</i>      | 3.599e7                 | 3.061e6     | 3.96e7  | • On average, RS stands for 22% of the investment cost.                           |         |           |
| ...      |                |                         |             |         |   |         |           |
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There are some agents that are willing to build more capacity than what is socially optimum to construct. Concretely, some technologies have a non-zero profit: they earn a “discreteness rent” of 3740 €/MW/year (for a 500MW CCGT it means **1.87 M€/year**)

# The results

The capacity price, compared to the sole energy remuneration, allows to **reduce the shortfall of revenue** for both the new and existing plants, **without increasing the opportunity costs.**

4

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| 1989     | $LOC$          | 3.534e8                 | 1.376e8     | 4.91e8  | 4.863e8  | 6.354e8 | 1.144e9   |
|          | $RS^{\in LOC}$ | 1.802e7                 | 0.0         | 1.802e7 | 1.335e7  | 4.154e7 | 3.244e7   |
|          | $FO$           | 3.354e8                 | 1.376e8     | 4.73e8  | 4.73e8   | 5.939e8 | 1.111e9   |
| ...      |                |                         |             |         |  |         |           |
| 2014     | $LOC$          | 1.052e8                 | 3.202e8     | 4.254   | On average, the inclusion of a CRM:  |         |           |
|          | $RS^{\in LOC}$ | 6.925e7                 | 3.171e8     | 3.864   | <ul style="list-style-type: none"> <li>Reduces by 40% the LOC</li> <li>Reduces by 95% the Revenue Shortfall</li> </ul> |         |           |
|          | $FO$           | 3.599e7                 | 3.061e6     | 3.905   |  |         |           |
| ...      |                |                         |             |         |  |         |           |
| Averages |                | 6.528e8                 | 4.754e8     | 1.128e9 | 7.0e8  | 9.149e8 | 1.404e9   |
|          |                | $LOC$                   |             |         |  |         |           |
|          |                | 9.598e7                 | 3.477e8     | 4.437e8 | 1.463e7  | 2.29e7  | 2.385e7   |
|          |                | $FO$                    |             |         |  |         |           |
|          |                | 5.568e8                 | 1.277e8     | 6.846e8 | 6.854e8  | 8.92e8  | 1.38e9    |

# The results

The **capacity price**, compared to the sole energy remuneration, allows to **reduce the shortfall of revenue** for both the new and existing plants, **without increasing the opportunity costs.**

4

|                |                | Without capacity market  |             |         | With capacity market |   |           |
|----------------|----------------|--|-------------|---------|----------------------|---|-----------|
|                |                | New units  | Exist units | Total   | Inelastic            | Elastic   | No Coord. |
| 1989           | $LOC$          | 3.534e8  | 1.376e8     | 4.91e8  | 4.86e8               | We made a sensitivity with two designs that depart from the ideal settings of our Proposition |           |
|                | $RS^{\in LOC}$ | 1.802e7  | 0.0         | 1.802e7 | 1.33e8               |   |           |
|                | $FO$           | 3.354e8  | 1.376e8     | 4.73e8  | 4.73e8               | 5.939e8   | 1.111e9   |
| 2014           | $LOC$          | If a CRM could mitigate the LOC stemming from indivisibilities, flaws in CRM design may also exacerbate the problem! |             |         | 2.678e8              | 1.328e9   |           |
|                | $RS^{\in LOC}$ |  |             |         | 4.362e7              | 3.012e7   |           |
|                | $FO$           |  |             |         | 2.242e8              | 1.297e9   |           |
| ...            |                |  |             |         |                      |   |           |
| Averages       |                | 6.528e8  | 4.754e8     | 1.128e9 | 7.0e8                | 9.149e8   | 1.404e9   |
| $LOC$          |                | 9.598e7  | 3.477e8     | 4.437e8 | 1.463e7              | 2.29e7  | 2.385e7   |
| $RS^{\in LOC}$ |                | 5.568e8  | 1.277e8     | 6.846e8 | 6.854e8              | 8.92e8  | 1.38e9    |
| ...            |                |  |             |         |                      |   |           |

## The long-term indivisibilities

- The continuous investment problem
- The lost opportunity cost under the discrete investment problem
- Illustration on a toy example

## Solution(s) to the indivisibilities

- Discriminatory payments
- Uniform price solution and capacity markets
- Illustration on a toy example

## Numerical Results

- ENTSO-E capacity expansion model
- Models and data description
- Results

## Conclusion

- Perspective for future research

# Conclusion

- We **identified and analyzed** a problem not extensively discussed in the literature—**the discrete investment problem**
- We characterized the **theoretical magnitude of the LOC** and we show how it depends of the pricing rule considered
- We have seen that a **CRM could play a role in mitigating the LOC**, provided that the capacity target is well-designed
- We make an assessment of this theoretical problem and solutions on (1) a **toy example** and (2) on a **realistic (European-wide) system** which suggest the relevance of both the problem and the solution

# Thank you!

Nicolas Stevens  
[nicolas.stevens@uclouvain.be](mailto:nicolas.stevens@uclouvain.be)

# Competitive Equilibrium

**Definition 4** (Competitive Walrasian Equilibrium) The allocation  $(q^*, x^*, d^*)$  together with the market price  $\pi$  constitute a competitive Walrasian equilibrium if

- (i) for each supplier  $g$ ,  $(q^*, x^*)_g$  optimizes its profit maximization problem (5) under price  $\pi$  ;  $d^*$  optimizes the load profit maximization problem (6) under price  $\pi$  ;
- (ii) the market clears ( $\sum_{g \in \mathcal{G}} q_{g,t}^* \geq d_t^* \quad \forall t \in \mathcal{T}$ ).

# Marginal / “Merit-order” pricing

**Definition 1** (Marginal Pricing) Let  $x^{**}$  be the values of the binary variables optimizing problem (3). The marginal prices are defined as the dual variables  $\pi^M$  obtained from solving the following (convex) problem, in which the variables  $x$  of problem (3) are fixed to  $x^{**}$ :

$$\max_{d,q} \sum_{t \in \mathcal{T}} \Delta T_t V_t d_t - \sum_{g \in \mathcal{G}} c_g((q, x^{**})_g) \quad (4a)$$

$$(\Delta T_t \pi_t^M) \sum_{g \in \mathcal{G}} q_{g,t} \geq d_t \quad \forall t \in \mathcal{T} \quad (4b)$$

$$(q, x^{**})_g \in \mathcal{X}_g \quad \forall g \in \mathcal{G} \quad (4c)$$

$$d \in \mathcal{X}_d \quad (4d)$$

# Convex Hull Pricing

**Definition 7** (Convex Hull Pricing) The convex hull prices  $\pi^{CH}$  are defined as the dual variables obtained from solving the following convex problem:

$$z_D^* = \max_{d, q, x} \sum_{t \in \mathcal{T}} \Delta T_t d_t V_t - \sum_{g \in \mathcal{G}} c_g((q, x)_g) \quad (9a)$$

$$(\Delta T_t \pi_t^{CH}) \sum_{g \in \mathcal{G}} q_{g,t} \geq d_t \quad \forall t \in \mathcal{T} \quad (9b)$$

$$(q, x)_g \in \text{conv}(\mathcal{X}_g) \quad \forall g \in \mathcal{G} \quad (9c)$$

$$d \in \mathcal{X}_d \quad (9d)$$

# New plants details

**Table 5:** Detailed analysis of agents incentives for the *new* plants (commissioning) for scenario 2014.

| Zone | Technology | Investment | Profit   | LOC     | $RS^{\infty LOC}$ | FO      |
|------|------------|------------|----------|---------|-------------------|---------|
| SE04 | CCGT new   | 0 × 500    | 0.0      | 3.05e6  | 0.0               | 3.05e6  |
| DKE1 | CCGT new   | 1 × 500    | -1.871e6 | 1.871e6 | 1.871e6           | 0.0     |
| LT00 | CCGT new   | 1 × 500    | 2.007e6  | 2.007e6 | 0.0               | 2.007e6 |
| AL00 | CCGT new   | 1 × 500    | -1.626e7 | 1.626e7 | 1.626e7           | 0.0     |
| FI00 | CCGT new   | 0 × 500    | 0.0      | 1.164e7 | 0.0               | 1.164e7 |
| EE00 | CCGT new   | 0 × 500    | 0.0      | 7.328e6 | 0.0               | 7.328e6 |
| RO00 | CCGT new   | 2 × 500    | -3.284e7 | 3.284e7 | 3.284e7           | 0.0     |
| SE02 | CCGT new   | 0 × 500    | 0.0      | 3.468e6 | 0.0               | 3.468e6 |
| SE01 | CCGT new   | 0 × 500    | 0.0      | 2.199e6 | 0.0               | 2.199e6 |
| SE03 | CCGT new   | 1 × 500    | 1.733e6  | 3.466e6 | 0.0               | 3.466e6 |
| ITSA | OCGT new   | 1 × 300    | -1.828e7 | 1.828e7 | 1.828e7           | 0.0     |
| LV00 | CCGT new   | 0 × 500    | 0.0      | 2.829e6 | 0.0               | 2.829e6 |

# Existing plant details

**Table 6:** Detailed analysis of agents incentives for *existing* plants (decommissioning) for scenario 2014 (sample).

| Zone | Technology     | In Place | Investment | Profit   | LOC      | $RS^{\epsilon LOC}$ | FO       |
|------|----------------|----------|------------|----------|----------|---------------------|----------|
| DKE1 | Light oil      | 529      | -2 × 100   | -2.871e6 | 2.618e6  | 2.618e6             | 0.0      |
| GR03 | Light oil      | 277      | -0 × 100   | -3.632e6 | 2.622e6  | 2.622e6             | 0.0      |
| PT00 | CCGT present 1 | 990      | -0 × 450   | -1.367e6 | 1.243e6  | 1.243e6             | 0.0      |
| HU00 | CCGT old 2     | 976      | -0 × 400   | -1.726e7 | 6.407e6  | 6.407e6             | 0.0      |
| BE00 | CCGT present 2 | 3550     | -0 × 450   | -6.709e6 | 5.953e6  | 5.953e6             | 0.0      |
| FR00 | CCGT present 2 | 5148     | -0 × 450   | -7.521e7 | 7.231e7  | 7.231e7             | 0.0      |
| UK00 | CCGT old 2     | 15010    | -3 × 400   | 3.173e7  | 2.757e6  | 0.0                 | 2.757e6  |
| UK00 | CCGT old 1     | 593      | -1 × 400   | 146800.0 | 303600.0 | 0.0                 | 303600.0 |
| RS00 | Lignite new    | 1106     | -0 × 300   | -2.863e7 | 2.33e7   | 2.33e7              | 0.0      |
| ES00 | CCGT present 1 | 24499    | -12 × 450  | -1.492e8 | 5.452e7  | 5.452e7             | 0.0      |