

## Homework 6 Solutions

### 1. Two Positive Lens Configuration

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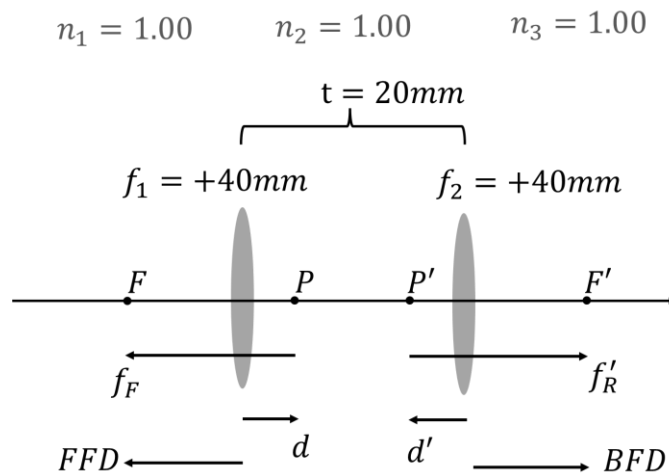
Find the location of the planes P, P', F, F' in addition to the BFD and FFD for a two positive lens configuration. You must use Gaussian reduction.

$$f_1 = +40\text{mm}$$

$$f_2 = +40\text{mm}$$

$$t = 20\text{mm}$$

Assume this configuration is in air with  $n = 1.00$ .



$$\varphi = \varphi_1 + \varphi_2 - \varphi_1 \varphi_2 t$$

$$\varphi = \frac{1}{+40\text{mm}} + \frac{1}{+40\text{mm}} - \frac{1}{+40\text{mm}} \cdot \frac{1}{+40\text{mm}} \cdot 20\text{mm} = 0.0375 \text{ mm}^{-1}$$

$$f_E = \frac{1}{0.0375\text{mm}^{-1}} = 26.67\text{mm}$$

$$f_F = -f_E = -26.67\text{mm}$$

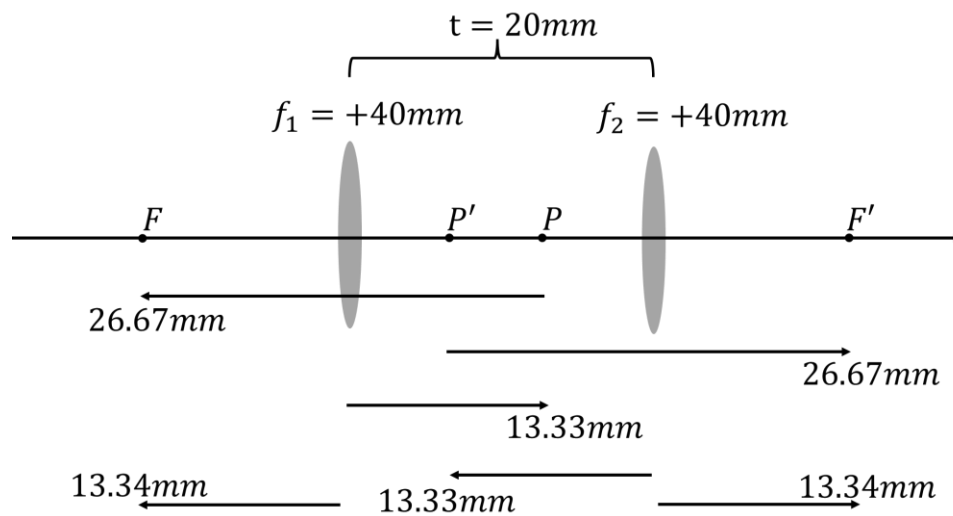
$$f'_R = +f_E = 26.67\text{mm}$$

$$d = n\delta = +n \frac{\varphi_2}{\varphi} \frac{t}{n} = +\frac{\varphi_2}{\varphi} t = 13.33\text{mm}$$

$$d' = n\delta' = -n \frac{\varphi_1}{\varphi} \cdot \frac{t}{n} = -\frac{\varphi_1}{\varphi} \cdot t = -13.33\text{mm}$$

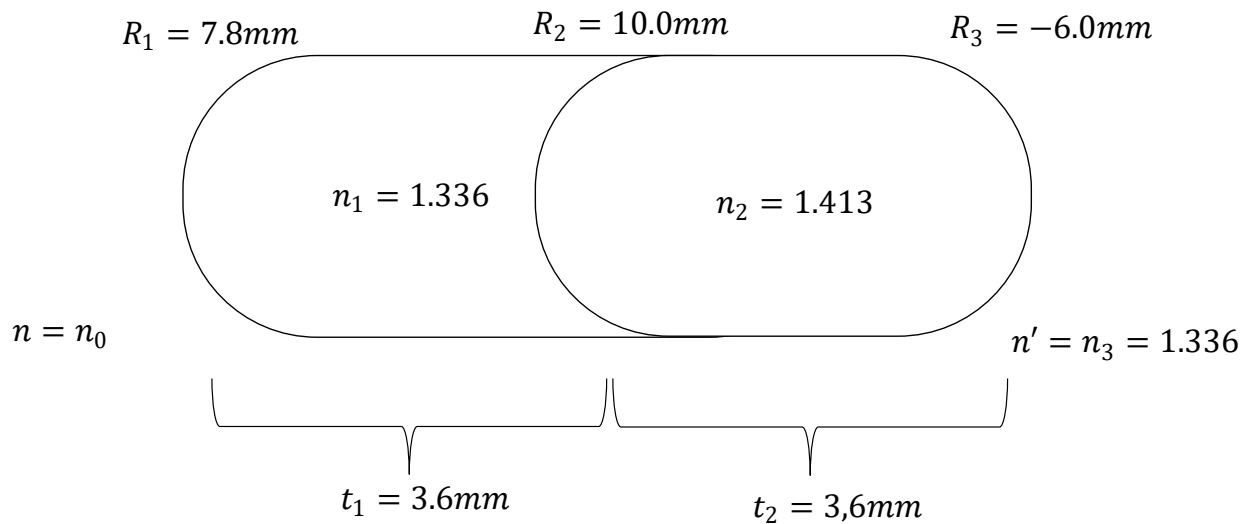
$$FFD = f_F + d = 13.34\text{mm}$$

$$BFD = f'_R + d' = 13.34\text{mm}$$



## 2. Eye Model

Using Gaussian reduction, determine the Gaussian properties (position of P and P' planes from vertices 1 and 3; F, F', N and N' planes from the P, P' planes) of an eye model. If the front of the eye is in air ( $n = 1.00$ ).



$$\varphi_n = (n_n - n_{n-1}) \cdot \frac{1}{R_n} = \frac{(n_n - n_{n-1})}{R_n}$$

$$\tau_n = \frac{t_n}{n_n}$$

$\varphi_1 = \frac{(1.336 - 1.00)}{7.8\text{mm}}$ $= 0.04308 \text{ mm}^{-1}$	$\varphi_2 = \frac{(1.413 - 1.336)}{10.0\text{mm}}$ $= 0.00770 \text{ mm}^{-1}$	$\varphi_3 = \frac{(1.336 - 1.413)}{-6.0\text{mm}}$ $= 0.01283 \text{ mm}^{-1}$
$\tau_1 = \frac{t_1}{n_1} = \frac{3.6\text{mm}}{1.336}$ $= 2.695 \text{ mm}$	$\tau_2 = \frac{t_2}{n_2} = \frac{3.6\text{mm}}{1.413}$ $= 2.548 \text{ mm}$	

Combining first two surfaces

$$\varphi_{12} = \varphi_1 + \varphi_2 - \varphi_1 \cdot \varphi_2 \cdot \tau_1 = 0.04988 \text{ mm}^{-1}$$

$$\delta_{12} = V_1 P_{12} = \frac{\varphi_2}{\varphi_{12}} \tau_1 = 0.4159 \text{ mm}$$

$$\delta'_{12} = V_2 P'_{12} = -\frac{\varphi_1}{\varphi_{12}} \tau_1 = -2.327 \text{ mm}$$

Reduced distance from  $P'_{12}$  to  $V_3$

$$\tau_{12-3} = P'_{12} V_3 = \tau_2 - \delta'_{12} = 4.875 \text{ mm}$$

$\varphi_{12} = 0.04988 \text{ mm}^{-1}$	$\varphi_3 = 0.01283 \text{ mm}^{-1}$
$\tau_{12-3} = P'_{12} V_3 = \tau_2 - \delta'_{12} = 4.875 \text{ mm}$	

Adding surface 3

$$\varphi = \varphi_{12} + \varphi_3 - \varphi_{12} \cdot \varphi_3 \cdot \tau_{12-3}$$

$$\varphi = 0.05960 \text{ mm}^{-1}$$

$$f_E = \frac{1}{\varphi} = 16.78 \text{ mm}$$

$$f_F = -n_0 f_E = -16.78 \text{ mm}$$

$$f'_R = n_3 f_E = 22.41 \text{ mm}$$

$$\delta_{12-3} = P_{12} P = \frac{\varphi_3}{\varphi} \cdot \tau_{12-3} = 1.050 \text{ mm}$$

$$\delta'_{12-3} = V_3 P' = -\frac{\varphi_{12}}{\varphi} \cdot \tau_{12-3} = -4.080 \text{ mm}$$

$$d = n_0 \delta = V_1 P = V_1 P_{12} + P_{12} P = 0.4159 + 1.050 = 1.4657 \text{ mm}$$

$$d' = n_3 \delta' = n_3 (V_3 P') = n_3 \delta'_{12-3} = -5.451 \text{ mm}$$

$$PN = f'_R + f_F = 22.41 - 16.78 = 5.64 \text{ mm}$$

$$P'N' = PN = 5.64mm$$

$$FFD = f_F + d = -16.78 + 1.47 = 15.31mm$$

$$BFD = f'_R + d' = 22.41 - 5.45 = 16.96mm$$

$$PP' = 3.6 + 3.6 - 1.47 - 5.45 = 0.28$$

