Chart Parsing

Lecture #6

Introduction to Natural Language Processing CMPSCI 585, Fall 2007

University of Massachusetts Amherst



Andrew McCallum

(agglomeration of slides from Jason Eisner)

Today's Main Points

- Hand back In-class Exercise #2
- Apologies: HW #1 not completed by grader.
 I'm giving you an extra day; now due Friday.
- Motivations and applications of Parsing.
- Dynamic Programming for Parsing: CYK
 - Some hands-on practice
- Discuss Programming Assignment #3 "Implement CYK and build a grammar"

Programming languages

```
assert (p + *p < pend);</pre>
for (c = 0; c < 256; c++)
  if (c / 8 < *p && (p[1 + (c/8)] & (1 << (c % 8)))) {
    /* Are we starting a range? */
    if (last + 1 == c &&! inrange) {</pre>
        putchar ('-');
        inrange = 1;
     /* Have we broken a range? */
     else if (last + 1 != c && inrange) {
        putchar (last);
        inrange = 0;
     if (! inrange)
        putchar (c);
                                    Easy to parse.
     last = c;
```

Designed that way!

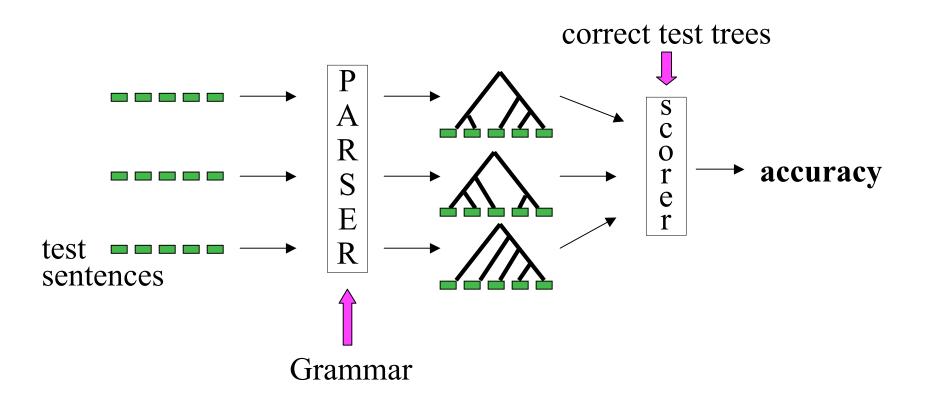
Andrew McCallum, UMass Amherst

Natural languages

```
printf "/charset %s", re_opcode t *p - 1 == charset not ? "^" : ""; assert p + *p < pend; for c = 0; c < 256; c++ if c 7 8 < *p && p1 + c/8 & 1 << c % 8 Are we starting a range? if last + 1 == c &&! inrange putchar '-'; inrange = 1; Have we broken a range? else if last + 1 != c && inrange putchar last; inrange = 0; if ! inrange putchar c; last = c;
```

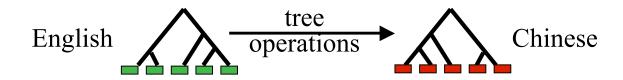
- No {} () [] to indicate scope & precedence
- Lots of overloading (arity varies)
- Grammar isn't known in advance!
- Context-free grammar not best formalism

The parsing problem



Applications of parsing (1/2)

• Machine translation (Alshawi 1996, Wu 1997, ...)



Speech synthesis from parses (Prevost 1996)

The government plans to raise income tax.

The government plans to raise income tax the imagination.

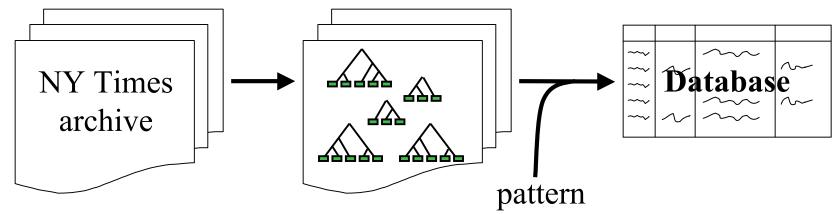
Speech recognition using parsing (Chelba et al 1998)

Put the file in the folder.

Put the file and the folder.

Applications of parsing (2/2)

- Grammar checking (Microsoft)
- Indexing for information retrieval (Woods 1997)
 ... washing a car with a hose ... vehicle maintenance
- Information extraction (Hobbs 1996) (Miller et al 2000)



Parsing State of the Art

- Recent parsers quite accurate, e.g.,
 - A Maximum-Entropy-Inspired Parser Eugene Charniak Proceedings of NAACL-2000.
 - Three Generative, Lexicalised Models for Statistical Parsing Michael Collins Proceedings of ACL, 1997.
- Most sentences parsed correctly, or with one error

Last class...

- We defined a CFG, where it sits in the Chomsky hierarchy
- Talked about parsing as search...
 ...through an exponential number of possible trees
- Gave examples of bottom-up and top-down search.
- Discussed problems:
 - Infinite loop with left-recursive rules
 - Much duplicated work in exponential space... backtracking

Dynamic Programming for Parsing

- Given CFG in Chomsky Normal Form, and an input string, we want to search for valid parse trees.
- What are the intermediate sub-problems?
- What would the dynamic programming table look like?

CKY algorithm, recognizer version

- Input: string of n words
- Output: yes/no (since it's only a recognizer)
- Data structure: n x n table
 - rows labeled 0 to n-1
 - columns labeled 1 to n
 - cell [i,j] lists possible constituents spanning words between i and j

CKY algorithm, recognizer version

- for i := 1 to n
 - Add to [i-1,i] all (part-of-speech) categories for the ith word
- for width := 2 to n
 - for start := 0 to n-width
 - Define end := start + width
 - for mid := start+1 to end-1
 - for every constituent X in [start,mid]
 - for every constituent Y in [mid,end]
 - for all ways of combining X and Y (if any)
 - Add the resulting constituent to [start,end] if it's not already there.

tin	ne	1	flies	2	like	3	an	4	arrow	5			_
	NF)	3										
	Vs	st	3										
0													
				NP	4								
1				VP	4								
2						Р							
2						V	5						
3									Det 1				
4											N	8	

 $NP \rightarrow time$

Vst → time

 $NP \rightarrow flies$

 $VP \rightarrow flies$

 $P \rightarrow like$

V → like

 $Det \rightarrow an$

 $N \rightarrow arrow$

 $1 S \rightarrow NP VP$

6 S \rightarrow Vst NP

 $2 S \rightarrow S PP$

1 $VP \rightarrow V NP$

2 $VP \rightarrow VP PP$

1 NP \rightarrow Det N

2 NP \rightarrow NP PP

3 NP \rightarrow NP NP

 $0 \text{ PP} \rightarrow \text{P NP}$

tin	ne 1	flies	2	like	3	an	4	arrow	5	_
	NP	3								
	Vst	3								
0										
			NP	4						
1			VP	4						
			VI	7						
					D					
2						2				
					V	5				
3								Det 1		
4									N 8	

 $6 S \rightarrow Vst NP$

 $2 S \rightarrow S PP$

1 $VP \rightarrow V NP$

 $2 \text{ VP} \rightarrow \text{VP PP}$

1 NP \rightarrow Det N

2 NP \rightarrow NP PP

3 $NP \rightarrow NP NP$

tin	ne 1	flies	2	like	3	an	4	arro)W	5		_
	NP	3	NP	10								
	Vst	3										
0												
			NP	4								
1			VP	4								
					Р							
2					V	5						
3								Det	1			
4										N	8	

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tin	ne	1	flies	2	like	3	an	4	arrow	5
	NP		3	NP	10					
	Vs	t	3	S	8					
0										
				NP	4					
1				VP	4					
_						Р	2			
2						V	5			
3									Det 1	
4										N 8

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ne 1	flies	2	like	3	an	4	arrow	5
NP	3	NP	10					
Vst	3	S	8					
		S	13					
		NP	4			-		
		VI	7					
				D	2	-		
				V	5			
							Det 1	
								N 8
	NP	NP 3	NP 3 NP	NP 3 NP 10 S 8 S 13	NP 3 NP 10 S 8 S 13	NP 3 NP 10 S 8 S 13 NP 4 VP 4 P 2	NP 3	NP 3

 $6 S \rightarrow Vst NP$

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ne	1	flies	2	like	3	an	4	arro	ow 5	5	
NF	•	3	NP	10							
Vs	t	3	S	8							
			S	13							
			NP	4							
			VP	4	-						
					Р	2					
					V	5		_ 			
								Det	1		
										N	8
	NF	NP	NP 3	NP 3 NP S S S	NP 3 NP 10 S 8 S 13	NP 3 NP 10 S 8 S 13 NP 4 P	NP 3 NP 10 S 8 S 13 NP 4 P 2	NP 3	NP 3 NP 10 S 8 S 13 NP 4 P 2 P 5 P 2 P 5	NP 3 NP 10 S 8 S 13 NP 4 P 2 P 2 V 5	NP 3 NP 10

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tin	ne	1	flies	2	like	3	an	4	arrow	5		_
	NP		3	NP	10							
	Vs	t	3	S	8							
				S	13							
0												
				NP	4							
1				VP	4	-						
						Р	2					
2						V	5		_			
3									Det 1		NP	10
4											N	8
												•

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tin	ne	1	flies	2	like	3	an	4	arrow	5		
	NP		3	NP	10							
	Vst		3	S	8							
				S	13							
0												
				NP	4							-
1				VP	4	-						
				VI	7							
						D	2					_
2							2		_			
						V	5					
3									Det 1	NP		
4										N	8	

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	NP	3	NP	10	_					
	Vst	3	S	8						
			S	13						
0										
1			NP	4	-			_		
•			VP	4						
					Р	2		_	PP	12
2					V	5				
3								Det 1	NP	10
4									N	8

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 $0 \text{ PP} \rightarrow \text{P NP}$

		ow 5	arro	4	an	3	like	2	flies	ne 1	tin
						_	10	NP	3	NP	
							8	S	3	Vst	
							13	S			
											0
			_			_	4	NP			
							4	VP			1
12	PP		_		2	Р					
16	VP				5	V					2
10	NP	1	Det								3
8	N										4
		1	Det								

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tin	ne 1	flies	2	like	3	an	4	arrov	v 5		_
	NP	3	NP	10	_						
	Vst	3	S	8							
			S	13							
0											
			ND	4							
1			NP	4	_			_			
•			VP	4							
_						2		_		PP	12
2					V	5				VP	16
3								Det '	1	NP	10
4										N	8
ı											

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	NP	3	NP	10	_			_			
	Vst	3	S	8							
			S	13							
0											
1			NP	4	_			_		NP	18
•			VP	4							
					Р	2		_		PP	12
2					V	5				VP	16
3								Det 1		NP	10
4										N	8
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NP 18	$\overline{}$
S 21	
PP 12	2
VP 16	
NP 10	,
N 8	
	PP 12 VP 16 NP 10

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	NP	3	NP	10				_			
	Vst	3	S	8							
			S	13							
0											
				_							
1			NP	4	_			_		NP	18
1			VP	4						S	21
										VP	18
					Р	2		_		PP	12
2					V	5				VP	16
3								Det 1		NP	10
4										N	8

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tin	ne 1	flies	2	like	3	an	4	arro	ow 5)	
	NP	3	NP	10	_			_			
	Vst	3	S	8							
			S	13							
0											
			ND							ND	40
1			NP	4	-			-		NP	18
•			VP	4						S	21
										VP	18
					Р	2		_		PP	12
2					V	5				VP	16
3								Det	1	NP	10
4										N	8
					1						

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tin	ne 1	flies	2	like	3	an	4	arrow	5		
	NP	3	NP	10	_			_		NP	24
	Vst	3	S	8							
			S	13							
0											
			NP	4						NP	18
1			VP	4	-			_		S	21
			VF	4							
									_	VP	18
					P	2		_		PP	12
2					V	5				VP	16
3								Det 1		NP	10
4										N	8

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NP					an	4	arrow	5		
INL	3	NP	10	_			_		NP	24
Vst	3	S	8						S	22
		S	13							
		ND	1					\dashv	ND	40
				 			_			18
		VP	4							21
									VP	18
				Р	2		_		PP	12
				V	5				VP	16
							Det 1		NP	10
									N	8
	Vst	Vst 3		S 13	NP 4 VP 4	NP 4 VP 4 P 2	NP 4 VP 4 P 2	NP 4 VP 4 P 2 V 5	S 13 NP 4 VP 4 P 2 V 5	NP 4

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tin	ne 1	flies	2	like	3	an	4	arrow	5		
	NP	3	NP	10	_			_		NP	24
	Vst	3	S	8						S	22
			S	13						S	27
0											
			\								10
1			NP	4	_			_		NP	18
I			VP	4						S	21
										VP	18
					Р	2		_		PP	12
2					V	5				VP	16
3								Det 1		NP	10
4										N	8
										_	

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	NP	3	NP	10	_			_		NP	24
	Vst	3	S	8						S	22
			S	13						S	27
0											
-			ND	_	1					110	40
1			NP	4	_			_		NP	18
•			VP	4						S	21
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					Р	2		_		PP	12
2					V	5				VP	16
3								Det 1		NP	10
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	Vst	3	S	8						S	22
			S	13						S	27
0										NP	24
4			NP	4				_		NP	18
1			VP	4						S	21
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2					V	5				VP	16
3								Det 1		NP	10
4										N	8

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	NP	3	NP	10	_			_		NP	24
	Vst	3	S	8						S	22
			S	13						S	27
0										NP	24
										S	27
			NP	4	_					NP	18
1			VP	4						S	21
										VP	18
					Р	2		_		PP	12
2					V	5			,	VP	16
3								Det 1		NP	10
4										N	8

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	NP	3	NP	10	_			_		NP	24
	Vst	3	S	8						S	22
			S	13						S	27
0										NP	24
										S	27
										S	22
			NP	4	_			_		NP	18
1			VP	4						S	21
										VP	18
					Р	2		_		PP	12
2					V	5				VP	16
3								Det 1		NP	10
4										N	8

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	NP	3	NP	10	_			_		NP	24
	Vst	3	S	8						S	22
			S	13						S	27
0										NP	24
										S	27
										S	22
										S	27
				_							
4			NP	4	_			_		NP	18
1			VP	4						S	21
										VP	18
					Р	2		_		PP	12
2					V	5				VP	16
3								Det 1		NP	10
4										N	8

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 $2 \text{ VP} \rightarrow \text{VP PP}$

1 NP \rightarrow Det N

2 NP \rightarrow NP PP

 $3 \text{ NP} \rightarrow \text{NP NP}$

Follow backpointers

tin	ne 1	flies	2	like	3	an	4	arrow	5		_
	NP	3	NP	10	_			_		NP	24
	Vst	3	S	8						S	22
			S	13						S	27
0										NP	24
										S	27
										S	22
										S	27
4			NP	4	_			_		NP	18
1			VP	4						S	21
										VP	18
					Р	2		_		PP	12
2					V	5				VP	16
3								Det 1		NP	10
4										N	8

 $1 S \rightarrow NP VP$

6 S \rightarrow Vst NP

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1 $VP \rightarrow V NP$

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1 NP \rightarrow Det N

 $2 \text{ NP} \rightarrow \text{NP PP}$

3 NP \rightarrow NP NP

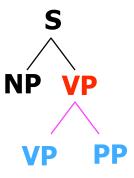
 $0 \text{ PP} \rightarrow \text{P NP}$



tin	ne 1	flies	2	like	3	an	4	arrow	5		
	NP	3	NP	10	_			_		NP	24
	Vst	3	S	8						S	22
			S	13						S	27
0										NP	24
										S	27
										S	22
										S	27
											4.0
4			NP	4	-			_		NP	18
1			VP	4						S	21
										VP	18
					Р	2		_		PP	12
2					V	5				VP	16
3								Det 1		NP	10
4										N	8

- $1 S \rightarrow NP VP$
- 6 S \rightarrow Vst NP
- $2 S \rightarrow S PP$
- 1 $VP \rightarrow V NP$
- 2 $VP \rightarrow VP PP$
- 1 NP \rightarrow Det N
- 2 NP \rightarrow NP PP
- 3 NP \rightarrow NP NP
- $0 PP \rightarrow P NP$

tin	ne 1	flies	2	like	3	an	4	arrow	5		_
	NP	3	NP	10	_			_		NP	24
	Vst	3	S	8						S	22
			S	13						S	27
0										NP	24
										S	27
										S	22
										S	27
4			NP	4	_			_		NP	18
1			VP	4						S	21
										VP	18
					Р	2		_		PP	12
2					V	5				VP	16
3								Det 1		NP	10
4										N	8



 $1 S \rightarrow NP VP$

6 S \rightarrow Vst NP

 $2 S \rightarrow S PP$

1 $VP \rightarrow V NP$

2 $VP \rightarrow VP PP$

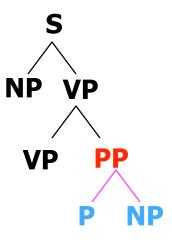
1 NP \rightarrow Det N

 $2 \text{ NP} \rightarrow \text{NP PP}$

3 NP \rightarrow NP NP

 $0 \text{ PP} \rightarrow \text{P NP}$

tin	ne	1	flies	2	like	3	an	4	arrow	5		
	NP)	3	NP	10	_			_		NP	24
	Vs	t	3	S	8						S	22
				S	13						S	27
0											NP	24
											S	27
											S	22
											S	27
				NP	4	_			_		NP	18
1				VP	4						S	21
											VP	18
						P	2		_		PP	12
2						V	5				VP	16
3									Det 1		NP	10
4											N	8



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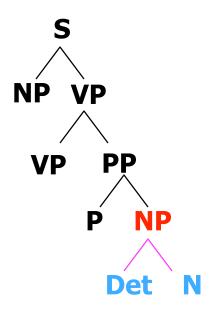
1 NP \rightarrow Det N

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 $0 \text{ PP} \rightarrow \text{P NP}$

tin	ne 1	flies	2	like	3	an	4	arrow	5		_
	NP	3	NP	10	_			_	NF	24	
	Vst	3	S	8					S	22	
			S	13					S	27	
0									NF	24	
									S	27	
									S	22	
									S	27	
4			NP	4	_			_	NF	18	
1			VP	4					S	21	
									VF	18	
					Р	2		_	PF	12	
2					V	5			VF	16	
3								Det 1	NF	10	
4									N	8	



 $1 S \rightarrow NP VP$

6 S \rightarrow Vst NP

 $2 S \rightarrow S PP$

1 $VP \rightarrow V NP$

2 $VP \rightarrow VP PP$

1 NP \rightarrow Det N

2 NP \rightarrow NP PP

3 NP \rightarrow NP NP

 $0 \text{ PP} \rightarrow \text{P NP}$

CMPSCI 585 In-class Exercise #3 Name: ______ Student ID: _____

Fill in the CYK dynamic programming table to parse the sentence below. In the bottom right corner, draw the two parse trees.

she	e ea	ats fis	sh wi		nop- icks
0	1	2	3	4	5
0	NP				
1					
2					
3					
4					

$S \rightarrow NP VP$	$NP \rightarrow she$
$NP \rightarrow NP PP$	$NP \rightarrow fish$
$VP \rightarrow V NP$	$NP \rightarrow fork$
$VP \rightarrow VP PP$	NP → chopsticks
$PP \rightarrow P NP$	V → eats
	$V \rightarrow fish$
	$P \rightarrow with$

Fill in the CYK dynamic programming table to parse the sentence below. In the bottom right corner, draw the two parse trees.

she	e ea	ats fis	sh wi		nop- icks
0	1	2	3	4	5
0	NP		S NP,VP		S NP VP
1		V	VPVNP		VP V NP VP VP PP
2			NP V		NP NP PP
3				Р	PP _{PNP}
4					NP

$S \rightarrow NP VP$	$NP \rightarrow she$
$NP \rightarrow NP PP$	$NP \rightarrow fish$
$VP \rightarrow V NP$	$NP \rightarrow fork$
$VP \rightarrow VP PP$	NP → chopsticks
$PP \rightarrow P NP$	$V \rightarrow eats$
	$V \rightarrow fish$
	$P \rightarrow with$

Homework #3

- Implement CYK
- Create a grammar
- Experiment with it...
- Due Thursday.

Dynamic Programming Parsing 2

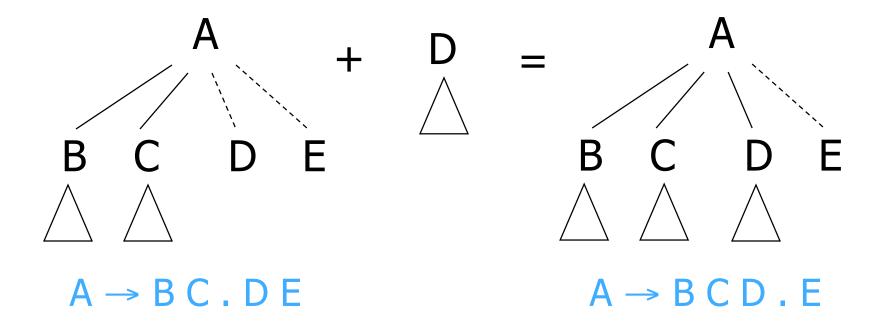
- How about a dynamic programming solution for arbitrary CGF grammars?
- (Grammars not in Chomsky Normal Form.)

Earley Parser (1970)

- Nice combination of
 - dynamic programming
 - incremental interpretation
 - avoids infinite loops
 - no restrictions on the form of the context-free grammar.
 - $A \rightarrow B C the D of$ causes no problems
 - O(n³) worst case, but faster for many grammars
 - Uses left context and optionally right context to constrain search.

Overview of the Algorithm

- Finds constituents and partial constituents in input
 - A → B C . D E is partial: only the first half of the A



Overview of the Algorithm

- Proceeds incrementally left-to-right
 - Before it reads word 5, it has already built all hypotheses that are consistent with first 4 words
 - Reads word 5 & attaches it to immediately preceding hypotheses.
 Might yield new constituents that are then attached to hypotheses immediately preceding them ...
 - E.g., attaching D to A → B C . D E gives A → B C D . E
 - Attaching E to that gives A → B C D E.
 - Now we have a complete A that we can attach to hypotheses immediately preceding the A, etc.

The Parse Table

- Columns 0 through n corresponding to the gaps between words
- Entries in column 5 look like (3, NP → NP . PP)

(but we'll omit the \rightarrow etc. to save space)

- Built while processing word 5
- Means that the input substring from 3 to 5
 matches the initial NP portion of a NP → NP PP rule
- Dot shows how much we've matched as of column 5
- Perfectly fine to have entries like (3, VP → is it . true that S)

The Parse Table

- Entries in column 5 look like (3, NP → NP . PP)
- What will it mean that we have this entry?
 - Unknown right context: Doesn't mean we'll necessarily be able to find a VP starting at column 5 to complete the S.
 - Known left context: Does mean that some dotted rule back in column 3 is looking for an S that starts at 3.
 - So if we actually do find a VP starting at column 5, allowing us to complete the S, then we'll be able to attach the S to something.
 - And when that something is complete, it too will have a customer to its left ...
 - In short, a top-down (i.e., goal-directed) parser: it chooses to start building a constituent not because of the input but because that's what the left context needs. In **the spoon**, won't build **spoon** as a verb because there's no way to use a verb there.
 - So any hypothesis in column 5 *could* get used in the correct parse, if words 1-5 are continued in just the right way by words 6-n.

Earley's Algorithm, recognizer version

- Add ROOT → . S to column 0.
- For each j from 0 to n:
 - For each dotted rule in column j, (including those we add as we go!) look at what's after the dot:
 - If it's a word w, SCAN:
 - If w matches the input word between j and j+1, advance the dot and add the resulting rule to column j+1
 - If it's a non-terminal X, PREDICT:
 - Add all rules for X to the bottom of column j, wth the dot at the start: e.g. X → . Y Z
 - If there's nothing after the dot, ATTACH:
 - We've finished some constituent, A, that started in column I<j. So for each rule in column j that has A after the dot: Advance the dot and add the result to the bottom of column j.
- Output "yes" just if last column has ROOT → S.
- NOTE: Don't add an entry to a column if it's already there!

Summary of the Algorithm

- Process all hypotheses one at a time in order.
 (Current hypothesis is shown in blue.)
- This may add new hypotheses to the end of the to-do list, or try to add old hypotheses again.
- Process a hypothesis according to what follows the dot:
 - If a word, scan input and see if it matches
 - If a nonterminal, predict ways to match it
 - (we'll predict blindly, but could reduce # of predictions by looking ahead k symbols in the input and only making predictions that are compatible with this limited right context)
 - If nothing, then we have a complete constituent, so attach it to all its customers

A Grammar

 $S \rightarrow NP \ VP$ $NP \rightarrow Papa$ $NP \rightarrow Det \ N$ $N \rightarrow caviar$ $NP \rightarrow NP \ PP$ $N \rightarrow spoon$ $VP \rightarrow V \ NP$ $V \rightarrow ate$ $VP \rightarrow VP \ PP$ $P \rightarrow with$ $PP \rightarrow P \ NP$ $Det \rightarrow the$ $Det \rightarrow a$

An Input Sentence

Papa ate the caviar with a spoon.

initialize 0 ROOT . S Remember this stands for $(0, ROOT \rightarrow . S)$ 0 ROOT . S 0S.NPVP

predict the kind of S we are looking for

Remember this stands for $(0, S \rightarrow . NP VP)$

0
0 ROOT . S
0 S . NP VP
0 NP . Det N
0 NP . NP PP
0 NP . Papa

predict the kind of NP we are looking for (actually we'll look for 3 kinds: any of the 3 will do)

0
0 ROOT . S
0 S . NP VP
0 NP . Det N
0 NP . NP PP
0 NP . Papa
0 Det . the
0 Det . a

predict the kind of Det we are looking for (2 kinds)

0 ROOT.S 0S.NPVP 0 NP . Det N 0 NP . NP PP 0 NP . Papa 0 Det . the 0 Det . a

predict the kind of NP we're looking for

but we were already looking for these so don't add duplicate goals! Note that this happened when we were processing a left-recursive rule.

0 Pap	a 1
0 ROOT . S	0 NP Papa .
0 S . NP VP	
0 NP . Det N	
0 NP . NP PP	
0 NP . Papa	scan:
0 Det . the	
0 Det . a	

0 Papa	a 1	
0 ROOT . S	0 NP Papa .	
0 S . NP VP		
0 NP . Det N		
0 NP . NP PP		
0 NP . Papa		
0 Det . the	scan: f	ailure
0 Det . a		

0 Pap	a 1	
0 ROOT . S	0 NP Papa .	
0 S . NP VP		
0 NP . Det N		
0 NP . NP PP		
0 NP . Papa		
0 Det . the		
0 Det . a	scan	: failure

0 Papa 1		
0 ROOT . S	0 NP Papa .	
0 S . NP VP	0 S NP . VP	
0 NP . Det N	0 NP NP . PP	
0 NP . NP PP		
0 NP . Papa		
0 Det . the		
0 Det . a		

attach the newly created NP (which starts at 0) to its customers (incomplete constituents that *end* at 0 and have NP after the dot)

a 1
0 NP Papa .
0SNP.VP
0 NP NP . PP
1 VP . V NP
1 VP . VP PP

0 Papa 1		
0 ROOT . S	0 NP Papa .	
0 S . NP VP	0SNP.VP	
0 NP . Det N	0 NP NP . PP	
0 NP . NP PP	1 VP . V NP	
0 NP . Papa	1 VP . VP PP	
0 Det . the	1 PP . P NP	
0 Det . a		

0 Papa	a 1
0 ROOT . S	0 NP Papa .
0 S . NP VP	0SNP.VP
0 NP . Det N	0 NP NP . PP
0 NP . NP PP	1 VP . V NP
0 NP . Papa	1 VP . VP PP
0 Det . the	1 PP . P NP
0 Det . a	1 V . ate

0 Papa	a 1
0 ROOT . S	0 NP Papa .
0 S . NP VP	0SNP.VP
0 NP . Det N	0 NP NP . PP
0 NP . NP PP	1 VP . V NP
0 NP . Papa	1 VP . VP PP
0 Det . the	1 PP . P NP
0 Det . a	1 V . ate

0 Papa	a 1
0 ROOT . S	0 NP Papa .
0 S . NP VP	0SNP.VP
0 NP . Det N	0 NP NP . PP
0 NP . NP PP	1 VP . V NP
0 NP . Papa	1 VP . VP PP
0 Det . the	1 PP . P NP
0 Det . a	1 V . ate
	1P. with

0 Papa	a 1 ate	2	
0 ROOT . S	0 NP Papa .	1 V ate .	
0 S . NP VP	0SNP.VP		
0 NP . Det N	0 NP NP . PP		
0 NP . NP PP	1 VP . V NP		
0 NP . Papa	1 VP . VP PP		
0 Det . the	1 PP . P NP		
0 Det . a	1 V . ate	scan: suc	ccess!
	1 P . with		

0 Papa	a 1 ate	2	
0 ROOT . S	0 NP Papa .	1 V ate .	
0 S . NP VP	0 S NP . VP		
0 NP . Det N	0 NP NP . PP		
0 NP . NP PP	1 VP . V NP		
0 NP . Papa	1 VP . VP PP		
0 Det . the	1 PP . P NP		
0 Det . a	1 V . ate		
	1 P . with	scan: failu	ıre

0 Papa	a 1 ate	2
0 ROOT . S	0 NP Papa .	1 V ate .
0 S . NP VP	0SNP.VP	1 VP V . NP
0 NP . Det N	0 NP NP . PP	
0 NP . NP PP	1 VP . V NP	
0 NP . Papa	1 VP . VP PP	
0 Det . the	1 PP . P NP	
0 Det . a	1 V . ate	
	1 P . with	

attach

0 Papa	a 1 ate	2
0 ROOT . S	0 NP Papa .	1 V ate .
0 S . NP VP	0SNP.VP	1 VP V . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa
0 Det . the	1 PP . P NP	
0 Det . a	1 V . ate	
	1P. with	

0 Papa	a 1 ate	2
0 ROOT . S	0 NP Papa .	1 V ate .
0 S . NP VP	0 S NP . VP	1 VP V . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the
0 Det . a	1 V . ate	2 Det . a
	1 P . with	

predict (these next few steps
should look familiar)

0 Papa	a 1 ate	2
0 ROOT . S	0 NP Papa .	1 V ate .
0 S . NP VP	0SNP.VP	1 VP V . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the
0 Det . a	1 V . ate	2 Det . a
	1 P . with	

0 Papa	a 1 ate	2
0 ROOT . S	0 NP Papa .	1 V ate .
0 S . NP VP	0SNP.VP	1 VP V . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the
0 Det . a	1 V . ate	2 Det . a
	1 P . with	

scan (this time we fail since Papa is not the next word)

0 Papa	a 1 ate	2 the	3	
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	
0 S . NP VP	0SNP.VP	1 VP V . NP		
0 NP . Det N	0 NP NP . PP	2 NP . Det N		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP		
0 NP . Papa	1 VP . VP PP	2 NP . Papa		
0 Det . the	1 PP . P NP	2 Det . the	scan: suc	cess!
0 Det . a	1 V . ate	2 Det . a		
	1P. with			

0 Papa	a 1 ate	2 the	3
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .
0 S . NP VP	0SNP.VP	1 VP V . NP	
0 NP . Det N	0 NP NP . PP	2 NP . Det N	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa	
0 Det . the	1 PP . P NP	2 Det . the	
0 Det . a	1 V . ate	2 Det . a	
	1 P . with		

0 Papa	a 1 ate	2 the	3
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N
0 NP . Det N	0 NP NP . PP	2 NP . Det N	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa	
0 Det . the	1 PP . P NP	2 Det . the	
0 Det . a	1 V . ate	2 Det . a	
	1 P . with		

0 Papa	a 1 ate	2 the	3
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .
0 S . NP VP	0SNP.VP	1 VP V . NP	2 NP Det . N
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon
0 NP . Papa	1 VP . VP PP	2 NP . Papa	
0 Det . the	1 PP . P NP	2 Det . the	
0 Det . a	1 V . ate	2 Det . a	
	1 P . with		

0 Papa	a 1 ate	2 the	3 caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .
0 S . NP VP	0SNP.VP	1 VP V . NP	2 NP Det . N	
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	
0 NP . Papa	1 VP . VP PP	2 NP . Papa		
0 Det . the	1 PP . P NP	2 Det . the		
0 Det . a	1 V . ate	2 Det . a		
	1 P . with			

0 Papa	a 1 ate	2 the	3 caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .
0 S . NP VP	0SNP.VP	1 VP V . NP	2 NP Det . N	
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	
0 NP . Papa	1 VP . VP PP	2 NP . Papa		
0 Det . the	1 PP . P NP	2 Det . the		
0 Det . a	1 V . ate	2 Det . a		
	1 P . with			

0 Papa	a 1 ate	2 the	3 caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .
0 S . NP VP	0SNP.VP	1 VP V . NP	2 NP Det . N	2 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	
0 NP . Papa	1 VP . VP PP	2 NP . Papa		
0 Det . the	1 PP . P NP	2 Det . the		
0 Det . a	1 V . ate	2 Det . a		
	1 P . with			

attach

0 Papa	a 1 ate	2 the	3 caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .
0 S . NP VP	0SNP.VP	1 VP V . NP	2 NP Det . N	2 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		
0 Det . the	1 PP . P NP	2 Det . the		
0 Det . a	1 V . ate	2 Det . a		
	1 P . with			

attach
(again!)

0 Papa	a 1 ate	2 the	3 caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP
0 Det . a	1 V . ate	2 Det . a		
	1 P . with			

attach
(again!)

0 Papa	a 1 ate	2 the	3 caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP
	1 P . with			

0 Pap	a 1 ate	2 the	3 caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .
0 S . NP VP	0SNP.VP	1 VP V . NP	2 NP Det . N	2 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP
	1 P . with			0 ROOT S.

attach
(again!)

0 Papa	a 1 ate	2 the	3 caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .
0 S . NP VP	0SNP.VP	1 VP V . NP	2 NP Det . N	2 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP
	1 P . with			0 ROOT S.

0 Papa	a 1 ate	2 the	3 caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .
0 S . NP VP	0SNP.VP	1 VP V . NP	2 NP Det . N	2 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP
	1 P . with			0 ROOT S.
				4 P . with

0 Papa	a 1 ate	2 the	3 caviar	4
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .
0 S . NP VP	0SNP.VP	1 VP V . NP	2 NP Det . N	2 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP
	1 P . with			0 ROOT S.
				4 P . with

0 Papa	a 1 ate	2 the	3 caviar	4 with	5
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .
0 S . NP VP	0SNP.VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	
	1 P . with			0 ROOT S.	
				4 P . with	

0 Papa	a 1 ate	2 the	3 caviar	4 with	5
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .
0 S . NP VP	0SNP.VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	
	1 P . with			0 ROOT S.	
				4 P. with	

0 Papa	a 1 ate	2 the	3 caviar	4 with	5
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .
0 S . NP VP	0SNP.VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	
	1P. with			0 ROOT S.	
				4 P . with	

0 Papa	a 1 ate	2 the	3 caviar	4 with	5
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .
0 S . NP VP	0SNP.VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	5 Det . the
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	5 Det . a
	1P. with			0 ROOT S.	
				4 P. with	

0 Papa	a 1 ate	2 the	3 caviar	4 with	5
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .
0 S . NP VP	0SNP.VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	5 Det . the
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	5 Det . a
	1P. with			0 ROOT S.	
				4 P . with	

0 Papa	a 1 ate	2 the	3 caviar	4 with	5
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	5 Det . the
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	5 Det . a
	1 P . with			0 ROOT S.	
				4 P . with	

0 Papa	a 1 ate	2 the	3 caviar	4 with	5
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .
0 S . NP VP	0SNP.VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	5 Det . the
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	5 Det . a
	1P. with			0 ROOT S.	
				4 P. with	

е	2 the	3 caviar	4 with	5 a 6	
	1 V ate .	2 Det the .	3 N caviar .	4 P with .	5 Det a .
	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	
Р	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	
	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	
)	2 NP . Papa		0 S NP VP.	5 NP . Papa	
	2 Det . the		1 VP VP . PP	5 Det . the	
	2 Det . a		4 PP . P NP	5 Det . a	
			0 ROOT S.		
			4 P . with		

е	2 the	3 caviar	4 with	5 a 6	
	1 V ate .	2 Det the .	3 N caviar .	4 P with .	5 Det a .
	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	5 NP Det . N
Р	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	
	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	
)	2 NP . Papa		0 S NP VP.	5 NP . Papa	
	2 Det . the		1 VP VP . PP	5 Det . the	
	2 Det . a		4 PP . P NP	5 Det . a	
			0 ROOT S.		
			4 P. with		

e	2 the	3 caviar	4 with	5 a 6	
	1 V ate .	2 Det the .	3 N caviar .	4 P with .	5 Det a .
	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	5 NP Det . N
Р	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	6 N . caviar
	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	6 N . spoon
)	2 NP . Papa		0 S NP VP.	5 NP . Papa	
	2 Det . the		1 VP VP . PP	5 Det . the	
	2 Det . a		4 PP . P NP	5 Det . a	
			0 ROOT S.		
			4 P . with		

e	2 the	3 caviar	4 with	5 a 6	
	1 V ate .	2 Det the .	3 N caviar .	4 P with .	5 Det a .
	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	5 NP Det . N
Р	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	6 N . caviar
	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	6 N . spoon
)	2 NP . Papa		0 S NP VP.	5 NP . Papa	
	2 Det . the		1 VP VP . PP	5 Det . the	
	2 Det . a		4 PP . P NP	5 Det . a	
			0 ROOT S.		
			4 P . with		

е	2 the	3 caviar	4 with	5 a 6	spoon 7	
	1 V ate .	2 Det the .	3 N caviar .	4 P with .	5 Det a .	6 N spoon.
	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	5 NP Det . N	
Р	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	6 N . caviar	
	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	6 N . spoon	
)	2 NP . Papa		0 S NP VP.	5 NP . Papa		
	2 Det . the		1 VP VP . PP	5 Det . the		
	2 Det . a		4 PP . P NP	5 Det . a		
			0 ROOT S.			
			4 P. with			

е	2 the	3 caviar	4 with	5 a 6	spoon 7	
	1 V ate .	2 Det the .	3 N caviar .	4 P with .	5 Det a .	6 N spoon.
	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	5 NP Det . N	5 NP Det N.
Р	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	6 N . caviar	
	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	6 N . spoon	
)	2 NP . Papa		0 S NP VP.	5 NP . Papa		
	2 Det . the		1 VP VP . PP	5 Det . the		
	2 Det . a		4 PP . P NP	5 Det . a		
			0 ROOT S.			
			4 P . with			

е	2 the	3 caviar	4 with	5 a 6	spoon 7	
	1 V ate .	2 Det the .	3 N caviar .	4 P with .	5 Det a .	6 N spoon .
	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	5 NP Det . N	5 NP Det N.
Р	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	6 N . caviar	4 PP P NP .
	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	6 N . spoon	5 NP NP . PP
)	2 NP . Papa		0 S NP VP.	5 NP . Papa		
	2 Det . the		1 VP VP . PP	5 Det . the		
	2 Det . a		4 PP . P NP	5 Det . a		
			0 ROOT S.			
			4 P . with			

0 Pap	a 1 ate	2 the	3 caviar	4 with a spoon	7	
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .		6 N spoon .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		
	1 P . with			0 ROOT S.		
				4 P . with		

0 Pap	a 1 ate	2 the	3 caviar	4 with a spoor	1 7	
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .		6 N spoon .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S.		
				4 P . with		

0 Pap	a 1 ate	2 the	3 caviar	4 with a spoor	1 7	
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .		6 N spoon .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S.		1 VP V NP .
				4 P . with		2 NP NP . PP

0 Pap	a 1 ate	2 the	3 caviar	4 with a spoor	n 7	
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .		6 N spoon .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S.		1 VP V NP .
				4 P . with		2 NP NP . PP
						0 S NP VP.
						1 VP VP . PP

0 Papa	a 1 ate	2 the	3 caviar	4 with a spoon 7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP
	1 P . with			0 ROOT S.
				4 P . with

	6 N spoon.
	5 NP Det N .
	4 PP P NP .
	5 NP NP . PP
	2 NP NP PP .
	1 VP VP PP .
	7 PP . P NP
	1 VP V NP .
	2 NP NP . PP
	0 S NP VP.
	1 VP VP . PP
	7 P . with
ı	

0 Papa	a 1 ate	2 the	3 caviar	4 with a spoon 7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP
	1 P . with			0 ROOT S.
				4 P . with

6 N spoon .
5 NP Det N .
4 PP P NP .
5 NP NP . PP
2 NP NP PP .
1 VP VP PP .
7 PP . P NP
1 VP V NP.
2 NP NP . PP
0SNPVP.
1 VP VP . PP
7 P . with

0 Papa	a 1 ate	2 the	3 caviar	4 with a spoor	n 7	
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .]	6 N spoon .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S.		1 VP V NP .
				4 P . with		2 NP NP . PP
						0 S NP VP.
						1 VP VP . PP
						7 P . with

0 Papa	a 1 ate	2 the	3 caviar	4 with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	6 N spo
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	5 NP D
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	4 PP P
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP N
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	2 NP N
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	1 VP V
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	7 PP . I
	1 P . with			0 ROOT S.	1 VP V
				4 P . with	2 NP N
					0 S NP
					1 VP V
					7 P . w
					0 ROO

6 N spoon .
5 NP Det N.
4 PP P NP .
5 NP NP . PP
2 NP NP PP .
1 VP VP PP .
7 PP . P NP
1 VP V NP .
2 NP NP . PP
0 S NP VP.
1 VP VP . PP
7 P . with
0 ROOT S.

0 Papa	a 1 ate	2 the	3 caviar	4 with a spoon	7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	6 N
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	5 NI
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	4 PF
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NI
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	2 NI
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	1 VI
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	7 PI
	1 P . with			0 ROOT S.	1 VI
				4 P . with	2 NI
					0 S
					1 VI
					7 P
					0 R

 6 N spoon .
5 NP Det N.
4 PP P NP .
5 NP NP . PP
2 NP NP PP .
1 VP VP PP .
7 PP . P NP
1 VP V NP .
2 NP NP . PP
0 S NP VP.
1 VP VP . PP
7 P . with
0 ROOT S.

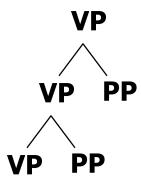
0 Papa	a 1 ate	2 the	3 caviar	4 with a spoor	n 7	
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .]	6 N spoon .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S.		1 VP V NP .
				4 P . with		2 NP NP . PP
						0 S NP VP.
						1 VP VP . PP
						7 P . with
						0 ROOT S.

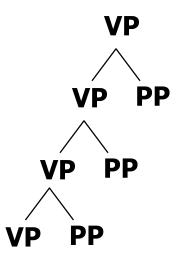
0 Papa	a 1 ate	2 the	3 caviar	4 with a spoor	n 7	
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .		6 N spoon .
0 S . NP VP	0SNP.VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S.		1 VP V NP .
				4 P . with		2 NP NP . PP
						0 S NP VP.
						1 VP VP . PP
						7 P . with
						0 ROOT S.

0 Papa	a 1 ate	2 the	3 caviar	4 with a spoor	n 7	
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .		6 N spoon .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S.		1 VP V NP .
				4 P . with		2 NP NP . PP
						0 S NP VP.
						1 VP VP . PP
						7 P . with
						0 ROOT S.

VP

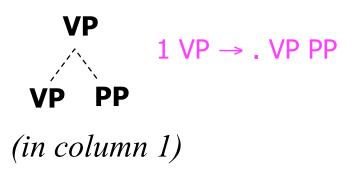


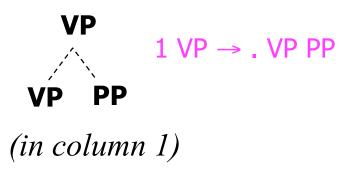


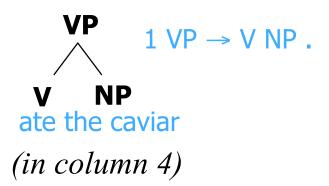


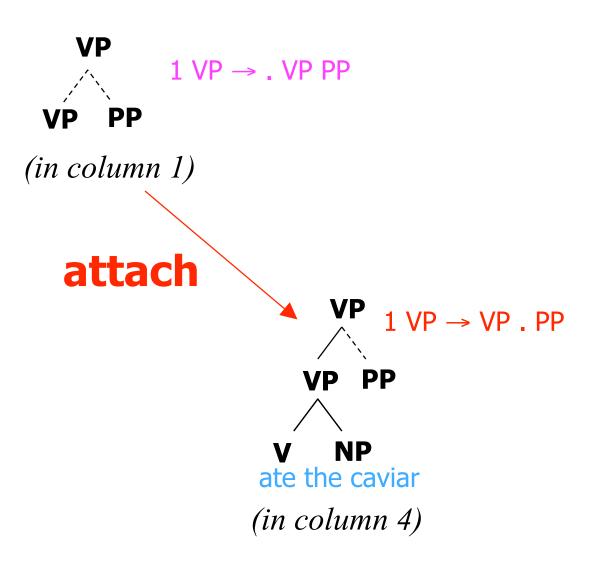
makes new hypotheses ad infinitum before we've seen the PPs at all

hypotheses try to predict in advance how many PP's will arrive in input

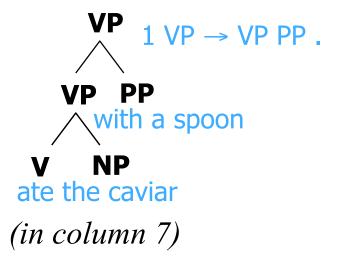




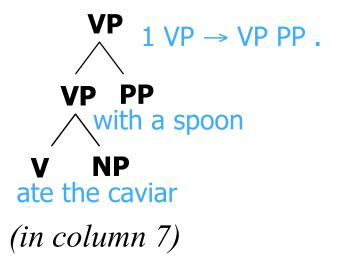


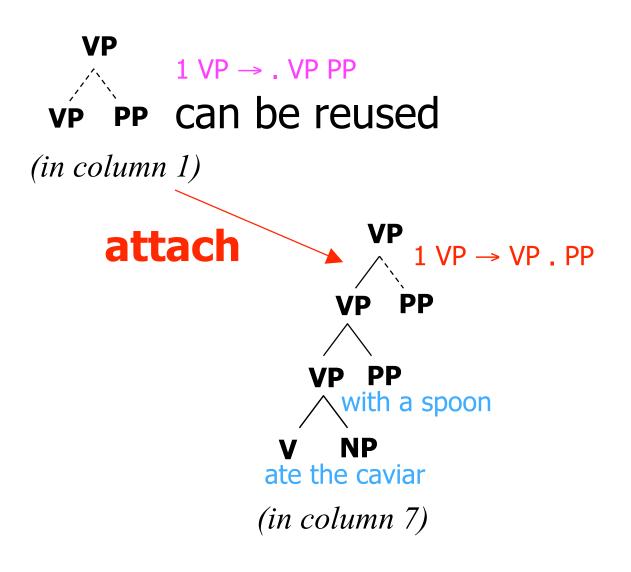


```
VP 1 VP \rightarrow . VP PP VP PP (in column 1)
```



```
VP
1 VP → . VP PP
vP PP can be reused
(in column 1)
```

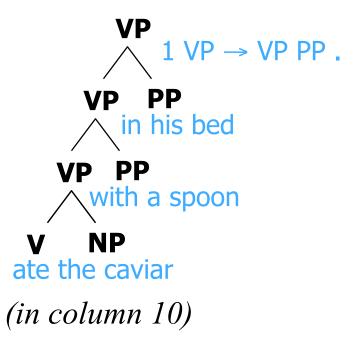




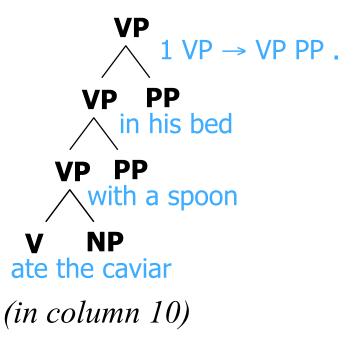
```
VP
1 VP → . VP PP

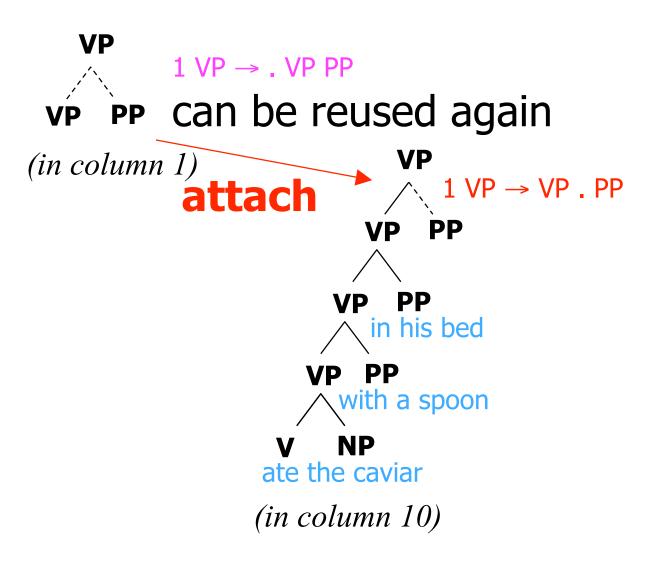
VP PP can be reused

(in column 1)
```



```
VP
1 VP → . VP PP
vP PP can be reused again
(in column 1)
```





0 Papa	a 1 ate	2 the	3 caviar	4 with a spoor	ո 7	
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .		6 N spoon.
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S.		1 VP V NP .
				4 P . with		2 NP NP . PP
						0 S NP VP.
						1 VP VP . PP
completed a VP in col 4						7 P . with
col 1 lets us use it in a VP PP structure				0 ROOT S.		

0 Papa	a 1 ate	2 the	3 caviar	4 with a spoon
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP
	1 P . with			0 ROOT S.
				4 P . with

completed that VP = VP PP in col 7 col 1 would let us use *it* in a VP PP structure can reuse col 1 as often as we need

6 N spoon. 5 NP Det N. 4 PP P NP. 5 NP NP . PP 2 NP NP PP. 1 VP VP PP 7 PP . P NP 1 VP V NP. 2 NP NP . PP 0 S NP VP. 1 VP VP . PP 7 P. with 0 ROOTS.

How to change the parser into a recognizer?

What's the Complexity?

What's the Complexity?

- How many state sets will there be?
 - Length of sentence, n
- How big can the state sets get?
 - Size of grammar, G, times n
- How long does it take to build a state set?
 - Scan
 - Constant time
 - Predict
 - Need to check for duplicates
 - Complete
 - Search previous state set, also check for duplicates, (Gn)²
- Total: O(n³)