



POLITECNICO
MILANO 1863

SCUOLA DI INGEGNERIA INDUSTRIALE
E DELL'INFORMAZIONE

Formal Analysis of Search-and-Rescue Scenarios

Project for Formal Methods for Concurrent and Realtime
Systems course

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Academic Year: 2023-24

Abstract

This document presents a formal model implemented with Uppaal of search-and-rescue scenarios. Inside a rectangular map of arbitrary size, civilian *survivors* have to be brought to safety by either reaching an exit or being assisted by *first-responders*. *Drones* surveys the area and coordinate the rescue efforts by instructing *survivors* on what to do. The model then undergoes formal verification to highlight key behavioral aspects and identify optimal configurations for maximizing *survivor* safety.

Contents

Abstract	2
1 High Level Model Description	3
1.1 Model Assumptions	3
2 Model Description and Design Choices	4
2.1 State and Parameters Representation	4
2.1.1 Map Representation	4
2.2 Synchronization and Message Passing	5
2.3 Templates	5
2.3.1 Survivor	5
2.3.2 First-responder	6
2.3.3 Drone	6
2.3.4 Initializer	6
2.4 Design Choices	6
3 Properties	6
4 Conclusion	7

1 High Level Model Description

The model adopted for the search-and-rescue mission involves 3 different types of agents: *survivors*, *first-responders* and *drones*. They are placed in different numbers inside a rectangular map, where exits (i.e. safe zones reached by survivors to get to safety) and fires are fixed in placed from the beginning of the scenario.

The key characteristics of the agents are these:

- **Survivors:** Can be in 3 different states, depending whether they find themselves near a fire or if they are following instructions
 - **In-need** (i.e. near a fire): They cannot move and needs to be assisted. After T_v time units, they became a casualty
 - **Busy:** The survivor is following an instructions and can be either assisting directly or contacting a *first-responder* to get help
 - **Moving:** When survivors are not near a fire or busy enacting some instruction, they can move towards an exit to get to safety following some *moving policy*
- **First-responders:**
 - **Assisting:** When a survivor *in-need* is within a 1-cell range, the *first-responder* will assist them for T_{fr} time units. After that, the assisted survivor is considered safe
 - **Moving:** When free from other tasks, the *first-responder* can move following some *moving policy*
- **Drones:** They survey their surroundings, limited by the field of view N_v of the sensors, and following a pre-determined path moving 1 cell at each time step. When two survivors, one *in_need* and one free, are detected the drone can instruct the free survivor to assist the *in_need* directly or to contact a *first-responder*

1.1 Model Assumptions

To simplify the model described in the assignment, the following assumptions have been made:

- The map is a 2D grid with a fixed number of rows and columns, and fires and exits are static (i.e. they won't change during simulation)
- Movements from one cell to another allows for diagonal movements. Therefore, the distance can be easily computed as the maximum between the difference of the x and y coordinates
- Movements of *survivors* and *first-responders* towards a human target (e.g. a *survivor* goes to a *first-responder*), are modeled with a wait state, where the agents remains idle for the duration of the movement, and then with a change in coordinates. This reduces the complexity of the model, lowering the number of states of the simulation and thus speeding up the verification process
- Drones know the global position of all the *first-responders* and their status, at any given time. This allows them to instruct *survivors* to contact the nearest *first-responder*
- All *survivors* know the location of the exits and can determine the nearest one
- *survivors* cannot start the simulation inside a fire cell

2 Model Description and Design Choices

2.1 State and Parameters Representation

Each agent type (*survivor*, *first-responder*, *drone*) is represented by an automaton, called **template** in Uppaal. These templates are characterized by many different parameters, and are implemented in Uppaal in the following way:

- The template signature (the parameters list) contains only one constant parameter, the agent id, annotated with a custom type defined as an integer with the range of possible ids (e.g. `typedef int[0, N_DRONES-1] drone_t;`). This way, by listing the template names in the *System declarations* (`system Drone, Survivor, FirstResponder;`), Uppaal can automatically generate the right number of instances of each template;
- The other agents' parameters (e.g. N_v , N_r , T_{zr} , etc.) are defined in constant global arrays (e.g. `const int N_v[drone_t] = {1, 1};`). Each template instance can then index these arrays with its own id as an index for these arrays (e.g. `N_v[id]`).

This setup allows to easily define the simulation parameters all inside the *Declarations* section, thus without modifying neither the templates nor the *System declarations*, and to easily assign different parameters to each template instance.

2.1.1 Map Representation

Despite each agent holding internally its own position, a global representation of the map is needed for agents who require to know the state of other agents (e.g. drones need to know the position of *first-responders* to instruct *survivors* to contact them).

The map is represented as a 2D grid of cells, with each cell indicating which type of human agent is within (drones positions are not needed, so they are not included in this representation). This choice is made to avoid each agent holding a reference to all other agents, which would make the model more complex and harder to maintain.

When one agent changes position, it updates the map accordingly. For example, when a *survivor* moves, it empties the cell it was occupying and fills the new cell with its type.

```
void move(int i, int j) {
    set_map(pos, CELL_EMPTY);
    pos.x += i;
    pos.y += j;
    set_map(pos, CELL_SURVIVOR);
}
```

```
// Map cell status enumeration
const int CELL_EMPTY = 0;
const int CELL_FIRE = 1;
const int CELL_EXIT = 2;
const int CELL_FIRST_RESP = 3;
const int CELL_SURVIVOR = 4;
const int CELL_ZERO_RESP = 5;
const int CELL_IN_NEED = 6;
const int CELL_ASSISTED = 7;
const int CELL_ASSISTING = 8;

typedef int[0, 8] cell_t;

// Map array
cell_t map[N_COLS][N_ROWS];
```

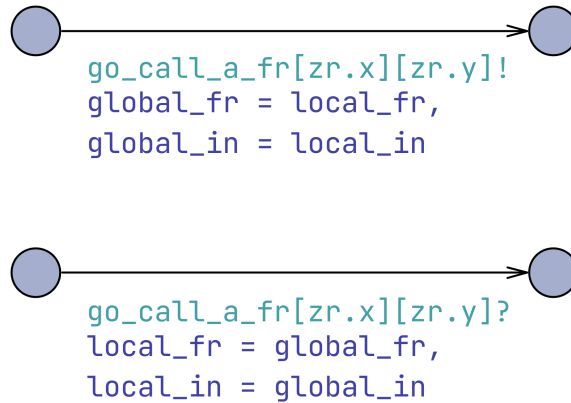
2.2 Synchronization and Message Passing

Between the different agents, there are some interactions that require a way to pass a payload. For example, when a *survivor* is instructed by a *drone* to contact a *first-responder*, the *survivor* must receive from the *drone* both the positions of the *first-responder* and that of the one *in-need* to assist.

This synchronization with message passing is implemented via Uppaal's built-in channels, augmented with global variables used to temporarily store the payload. The channels themselves are 2D matrices to allow targeting a specific agent. Each agent can trigger a channel at a given coordinate or listen at a channel on its own current position.

Following the previous example, the synchronization follows these steps:

1. The *drone* saves the positions of the target *first-responder* and *in-need* in two global variables and then triggers the channel at the coordinates of the targeted *survivor*.
2. The *survivor*, upon receiving the signal through the channel, reads the global variables to get the positions of the *first-responder* and *in-need*.



2.3 Templates

2.3.1 Survivor

At the beginning of the simulation, *survivors* position themselves in the map; if they are near a fire they become *in_need* otherwise they are considered *survivors*.

1. *in_need*: The survivor cannot move and needs to be assisted. After T_v time units near a fire, they became a casualty, if assisted in time they are considered safe. In both cases they leave the simulation freeing the map cell they were occupying.
2. *survivors*: The survivor moves towards an exit following a *moving policy*. If they are within a 1-cell range from an exit they are considered safe and leave the simulation freeing the map cell they were occupying. In this state they can receive instructions from the drone to either assist a *in_need* survivor or to contact a *first-responder* to get help.
 - Assisting a *in_need* survivor: The survivor “moves” towards the *in_need* survivor by staying in the same cell for the time needed to reach the *in_need* (the distance

between the two). The survivor “assist” the *in_need* by waiting T_{zr} . After that the survivor is considered safe and leaves the simulation.

- Calling a First responder: The survivor “moves” towards the *first-responder* by staying in the same cell for the time needed to reach the *first-responder* (the distance between the two). The survivor “calls” the *first-responder* that will assist the *in_need* survivor. When the *first-responder* ends the assist the survivor is considered safe and leaves the simulation.

At the end of the simulation all survivors are either safe or casualties.

2.3.2 First-responder

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2.3.3 Drone

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2.3.4 Initializer

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2.4 Design Choices

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3 Properties

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4 Conclusion

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