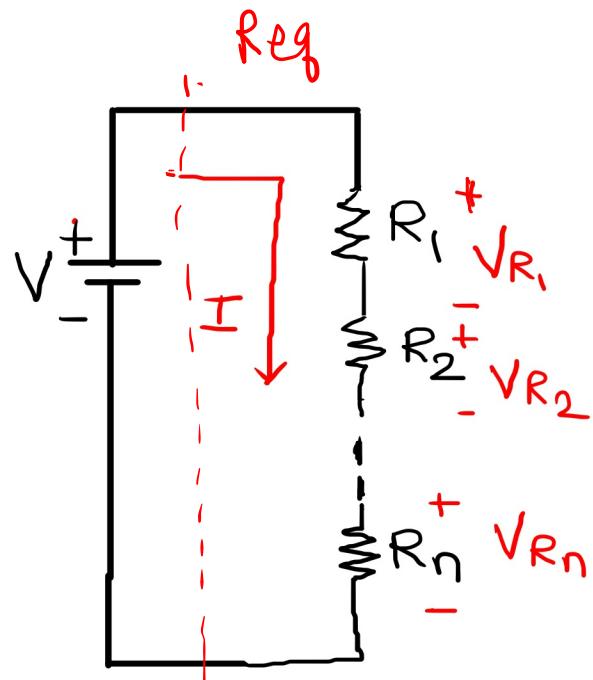


# Series Combination of Resistors (Current is same in all resistor)



Applying KVL

$$V - V_{R_1} - V_{R_2} - \dots - V_{R_n} = 0$$

$$V = V_{R_1} + V_{R_2} + \dots + V_{R_n}$$

$$V = I R_1 + I R_2 + \dots + I R_n$$

$$V = I (R_1 + R_2 + \dots + R_n)$$

$$\frac{V}{I} = R_1 + R_2 + \dots + R_n \text{ also } I = \frac{V}{R_1 + R_2 + \dots + R_n}$$

$$Req = R_1 + R_2 + \dots + R_n$$

$$Req = \sum_{i=1}^n R_i$$

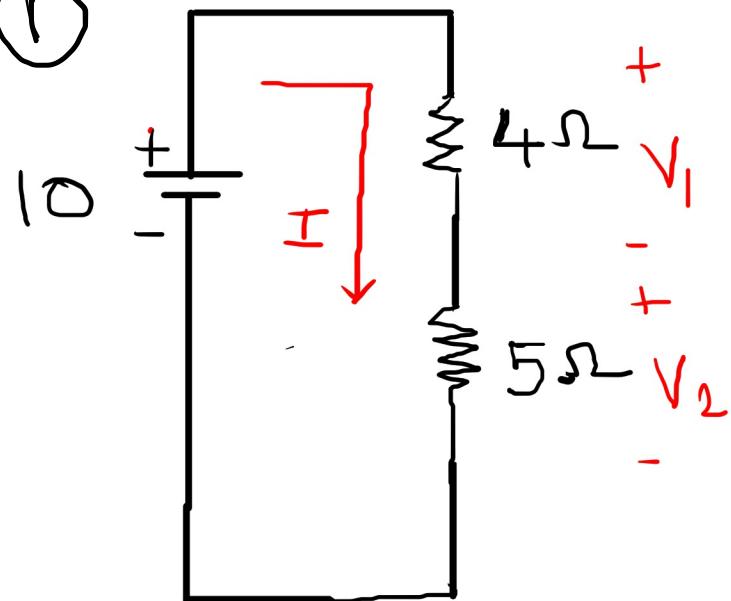
Voltage Division Formula

$$V_{R_1} = IR_1 = \frac{R_1 \times V}{R_1 + R_2 + \dots + R_n} , V_{R_2} = IR_2 = \frac{R_2 \times V}{R_1 + R_2 + \dots + R_n} \& V_{R_n} = IR_n = \frac{R_n \times V}{R_1 + R_2 + \dots + R_n}$$

Voltage across any resistor in a Series Combination = applied Voltage  $\times \left( \frac{\text{Resistance of the Same branch}}{\text{Sum of all resistances}} \right)$

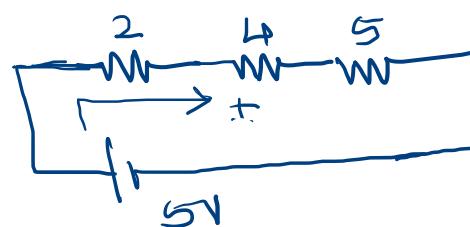
# Series Combination of Resistors (Current is same in all resistor)

①



$$V_1 = \frac{4}{4+5} \times 10 = \frac{40}{9}$$

②



$$V_2 = \frac{5}{5+4} \times 10 = \frac{50}{9}$$

$$V_{2\Omega} = \frac{2 \times 5}{2+4+5} = \frac{10}{11} \quad \checkmark$$

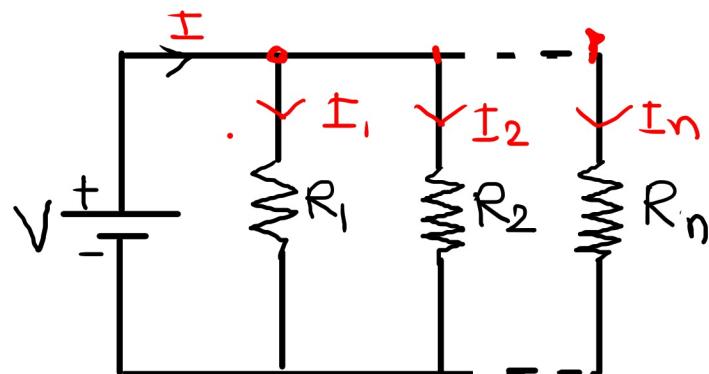
$$V_{4\Omega} = \frac{4}{2+4+5} \times 5 = \frac{20}{11} \quad \checkmark$$

$$V_{5\Omega} = \frac{5}{2+4+5} \times 5 = \frac{25}{11} \quad \checkmark$$

## Voltage Division Formula

Voltage across any resistor in a Series Combination = applied Voltage  $\times \left( \frac{\text{Resistance of Same branch}}{\text{Sum of resistances in Series}} \right)$

# Parallel Combination of Resistors (Voltage Across all resistors is Same)



Applying KCL

$$I = I_1 + I_2 + \dots + I_n$$

$$I = \left[ \frac{V}{R_1} + \frac{V}{R_2} + \dots + \frac{V}{R_n} \right] = V \left[ \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n} \right]$$

$$\frac{I}{V} = \left[ \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n} \right] = \frac{1}{R_{eq}}$$

Current Division formula

$$I_n = \frac{I \times \frac{1}{R_n}}{\frac{1}{R_{eq}}}$$

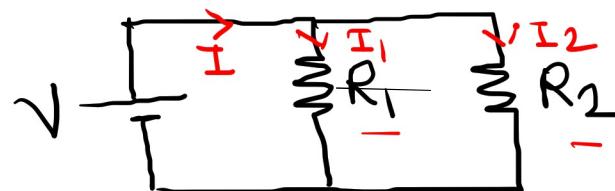
$$I_1 = \frac{V}{R_1} = \frac{1}{R_1} \left[ \frac{I}{\frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}} \right] = \left( \frac{\frac{1}{R_1} \times I}{\frac{1}{R_{eq}}} \right) = \left( \frac{\frac{1}{R_1} \times I}{\frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}} \right)$$

$$V = \frac{I}{\left[ \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n} \right]}$$

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}$$

For two Resistors in parallel

→



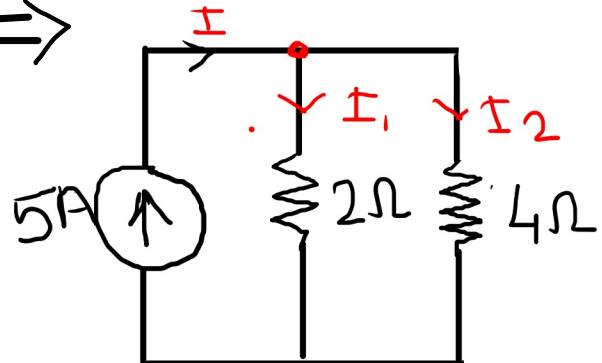
$$I_1 = \frac{\frac{1}{R_1} \times I}{\frac{1}{R_1} + \frac{1}{R_2}} = \frac{\frac{1}{R_1} \times I}{\frac{R_1 + R_2}{R_1 R_2}} = \frac{\frac{1}{R_1} \times I}{\frac{R_1 + R_2}{R_1 R_2}} = \frac{R_2 \times I}{R_1 + R_2}$$

Current Through a resistor (in parallel) = Total Current X (Resistance of other branch / Sum of Resistances combination of two resistors)

$$I_2 = \frac{\frac{1}{R_2} \times I}{\frac{1}{R_1} + \frac{1}{R_2}} = \frac{R_1 \times I}{R_1 + R_2}$$

## Parallel Combination of Resistors (Voltage Across all resistors is Same)

⇒

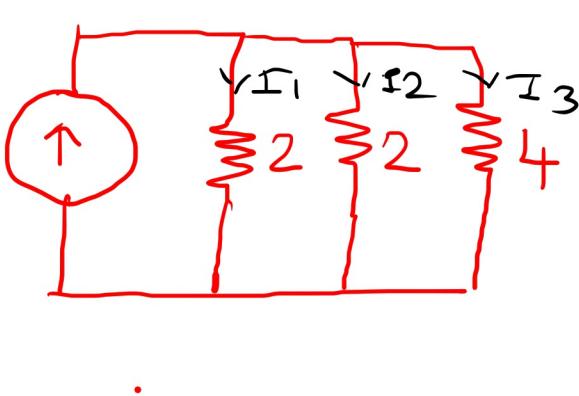


Current Division formula

$$I_1 = \frac{5 \times 4}{4+2} = \frac{20}{6}$$

$$I_2 = \frac{5 \times 2}{2+4} = \frac{10}{6}$$

⇒



$$I_1 = \frac{\frac{1}{2} \times 5}{\frac{1}{2} + \frac{1}{2} + \frac{1}{4}} \sim$$

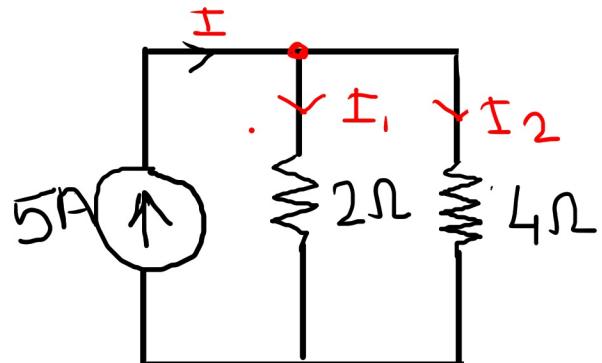
$$I_2 = \frac{\frac{1}{2} \times 5}{\frac{1}{2} + \frac{1}{2} + \frac{1}{4}} \sim$$

$$I_3 = \frac{5 \times \frac{1}{4}}{\frac{1}{2} + \frac{1}{2} + \frac{1}{4}} \sim$$

Current Through a resistor( in parallel combination of two resistors)

Total Current X (Resistance of other branch / Sum of Resistances)

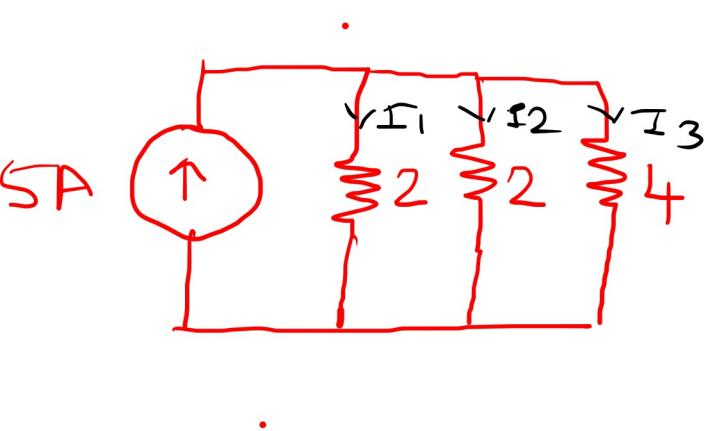
# Parallel Combination of Resistors (Voltage Across all resistors is Same)



Current Division formula

$$I_1 = \frac{5 \times 4}{4+2} = \frac{20}{6}$$

$$I_2 = \frac{5 \times 2}{2+4} = \frac{10}{6}$$



$$I_1 = \frac{\frac{1}{2} \times 5}{\frac{1}{2} + \frac{1}{2} + \frac{1}{4}} \sim$$

$$I_2 = \frac{\frac{1}{2} \times 5}{\frac{1}{2} + \frac{1}{2} + \frac{1}{4}} \sim$$

$$I_3 = \frac{5 \times \frac{1}{4}}{\frac{1}{2} + \frac{1}{2} + \frac{1}{4}} \sim$$

Current Through a resistor( in parallel combination of two resistors) =

Total Current X (Resistance of other branch / Sum of Resistances)

# Energy Sources

Voltage & Current Sources

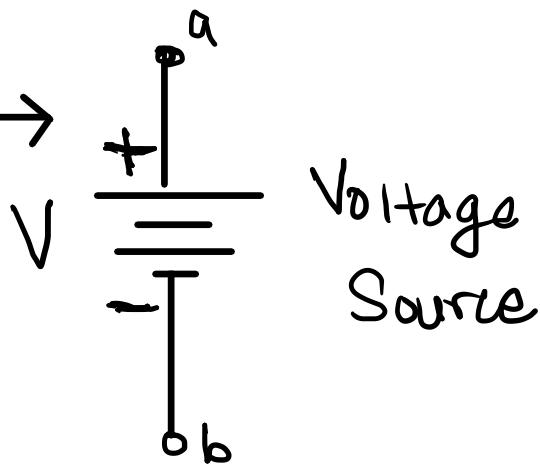
Direct Current (DC) Sources

$V_s$

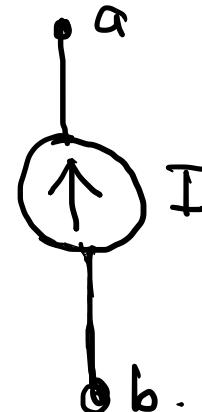
Alternating Current (AC) Sources

Ideal Vs Practical

Dependent Vs Independent



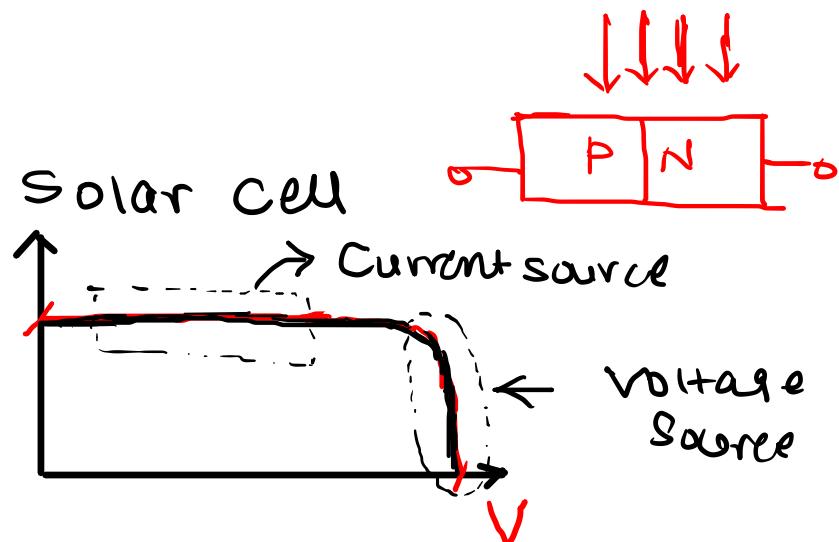
Voltage Source



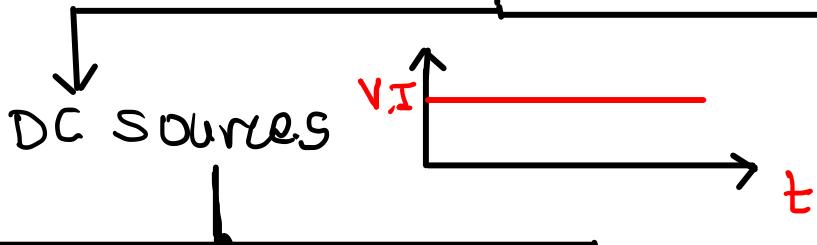
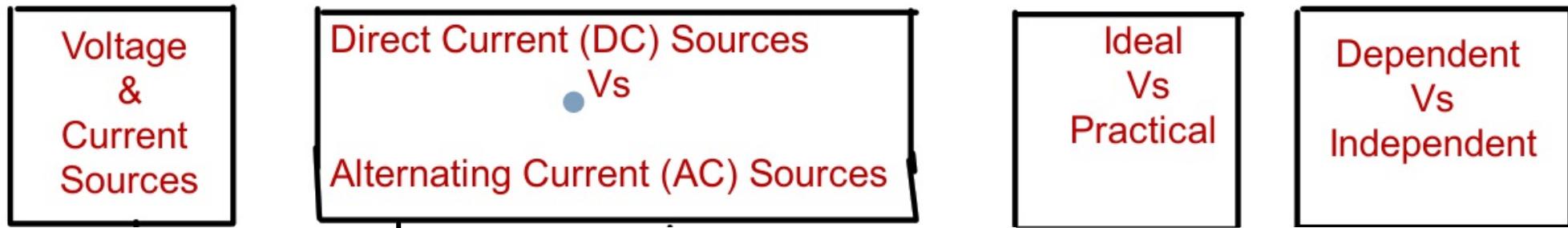
Current Source

e.g. Electro-chemical cell

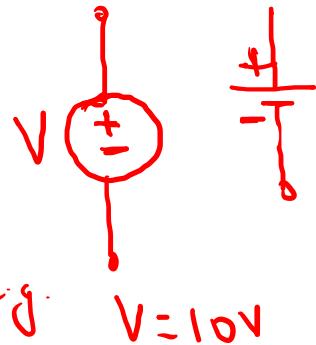
e.g. Solar cell



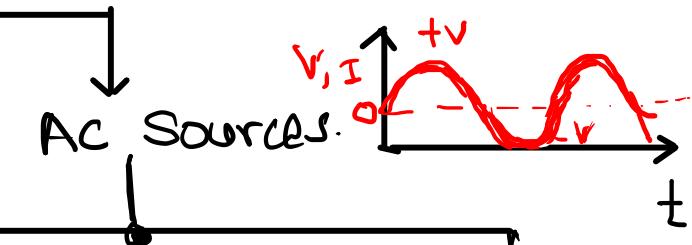
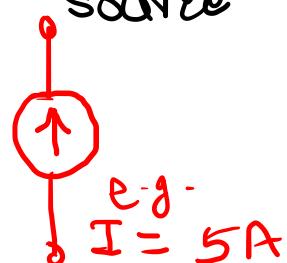
# Energy Sources



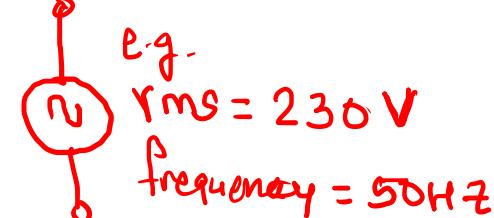
↓ Voltage source



↓ Current source



↓ Voltage source



↓ Current source

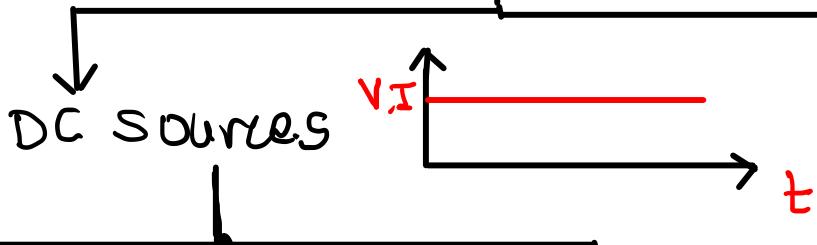
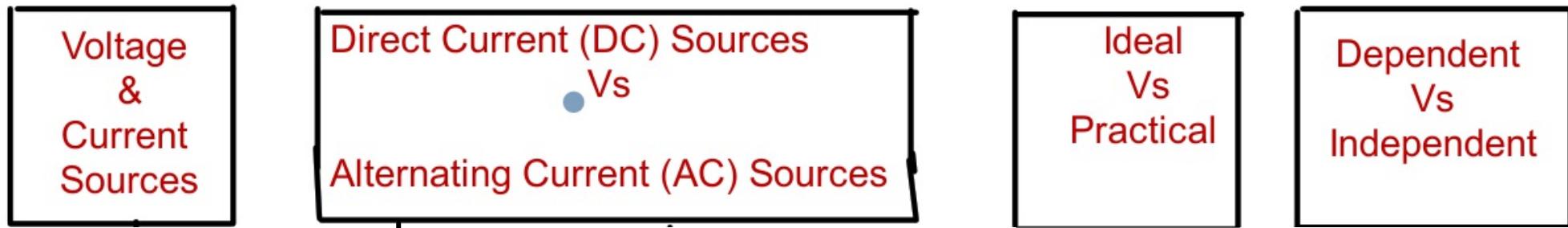


DC  
output  
( $5V, 12V$ )  
 $1A$

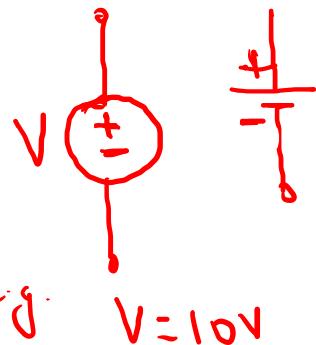
mobile / Laptop  
Battery charger

AC input ( $230V, 50Hz$ )

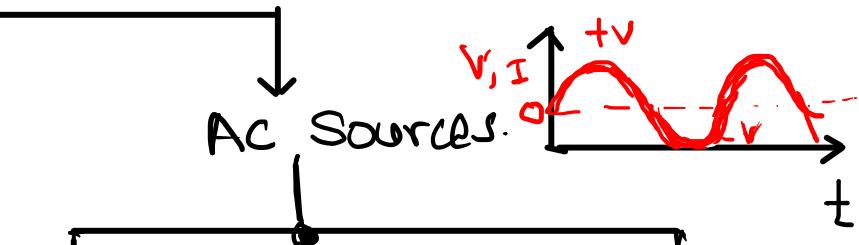
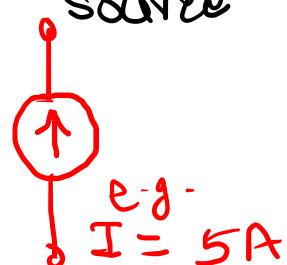
# Energy Sources



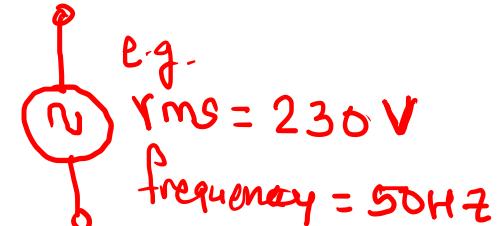
↓ Voltage source



↓ Current source



↓ Voltage source



↓ Current source



DC output  
(5V, 12V)  
1A

mobile / Laptop  
Battery charger

AC input (230V, 50Hz)

# Energy Sources

Voltage & Current Sources

Direct Current (DC) Sources

$V_s$

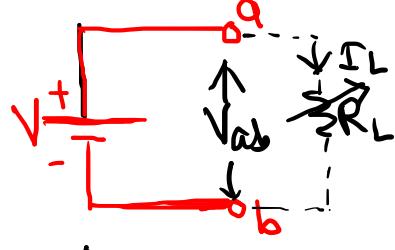
Alternating Current (AC) Sources

Ideal Vs Practical

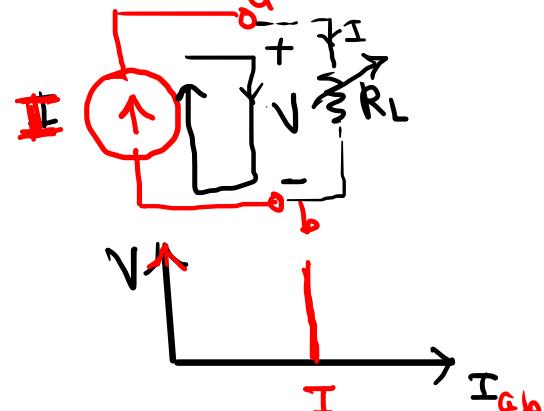
Dependent Vs Independent

Ideal

Voltage Source



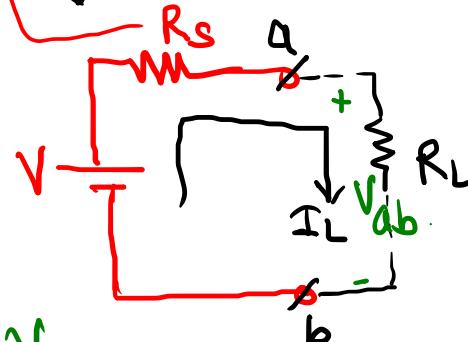
Current Source



Practical

Source resistance

Voltage source



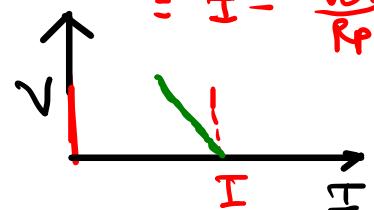
$$V_{ab} = V - I_L R_s$$

Current source



$$I_{ab} = I - I_p$$

$$= I - \frac{V_{ab}}{R_p}$$



# Energy Sources

Voltage & Current Sources

Direct Current (DC) Sources

$V_s$

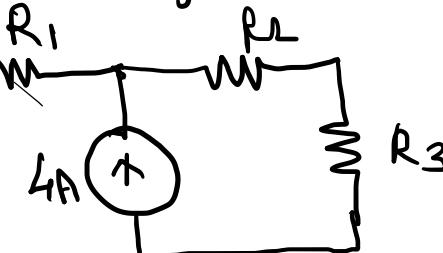
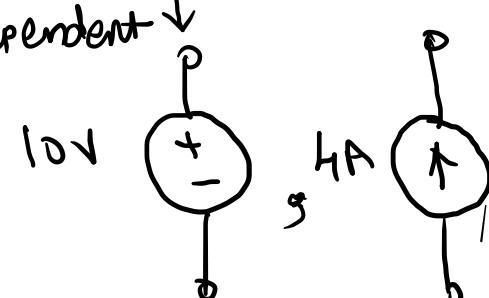
Alternating Current (AC) Sources

Ideal Vs Practical

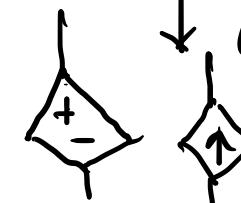
Dependent Vs Independent

(Uncontrolled)

Independent

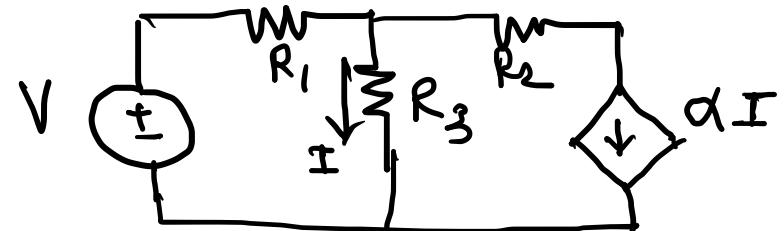


Independent (voltage/current) Source is the one whose value is independent of any other parameter in the network



Controlled / dependent

The value of source will depend on other parameters in the circuit.



→ Current Controlled Current Source

# Energy Sources

Voltage & Current Sources

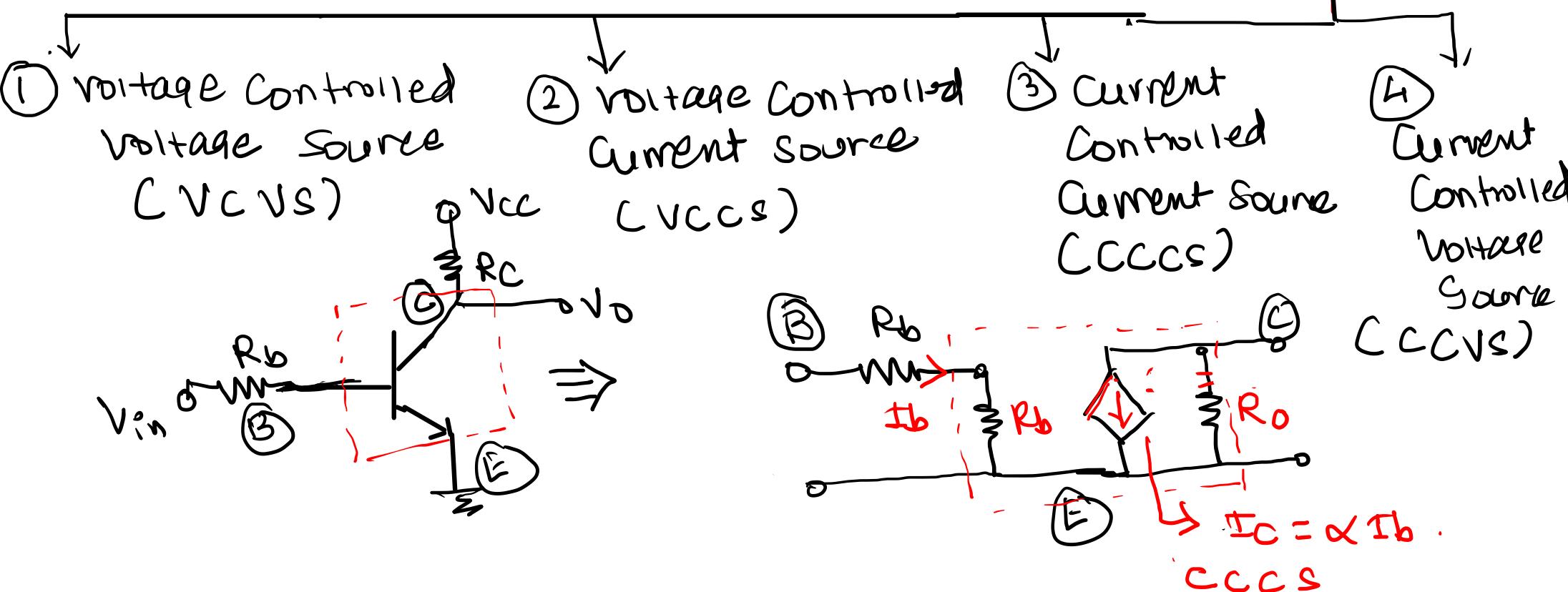
Direct Current (DC) Sources

$V_s$

Alternating Current (AC) Sources

Ideal Vs Practical

Dependent Vs Independent



# Energy Sources

Voltage & Current Sources

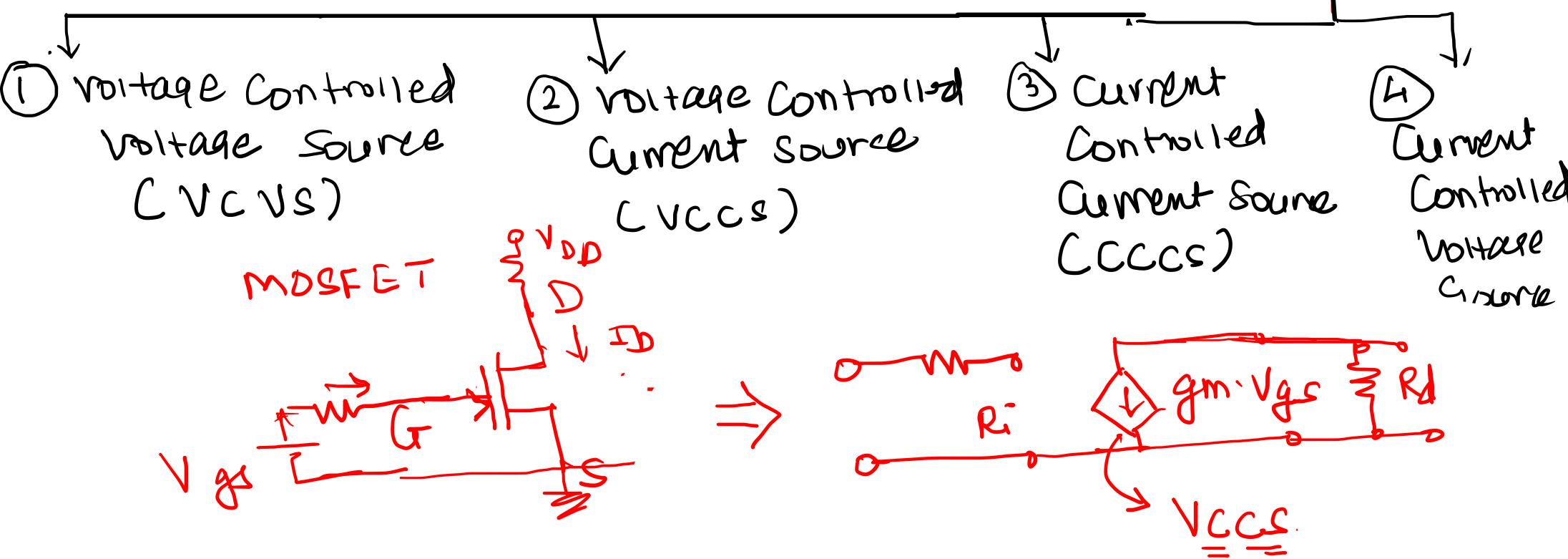
Direct Current (DC) Sources

$V_s$

Alternating Current (AC) Sources

Ideal Vs Practical

Dependent Vs Independent



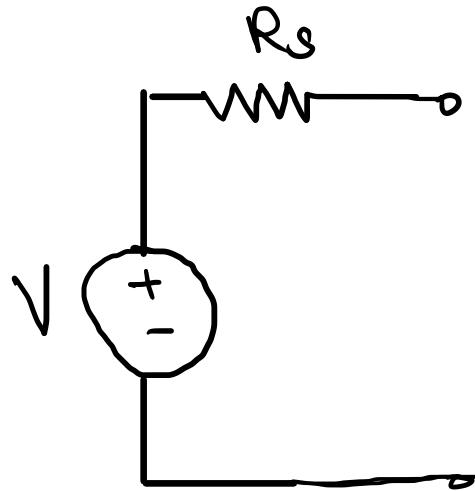
# Source Transformation

[ Transforming / Converting ]

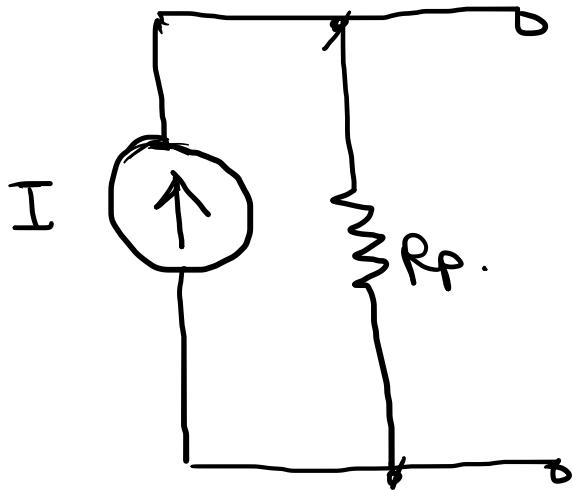
Voltage Source  $\rightarrow$  Current Source }

Current Source  $\rightarrow$  Voltage

SOURCE.

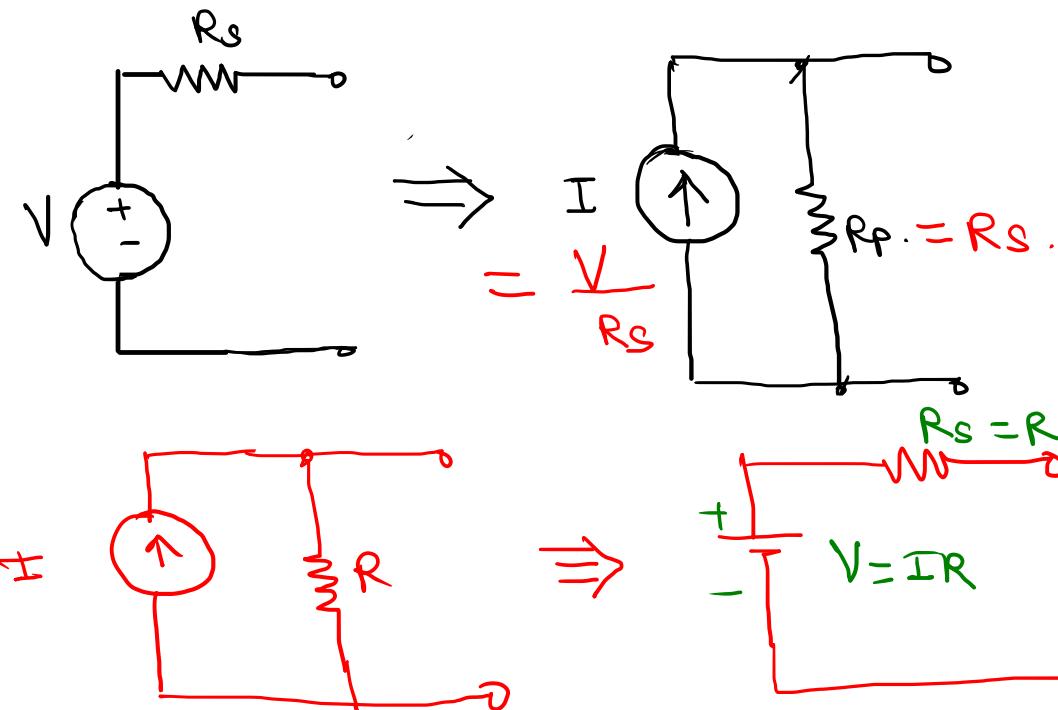


practical voltage  
source



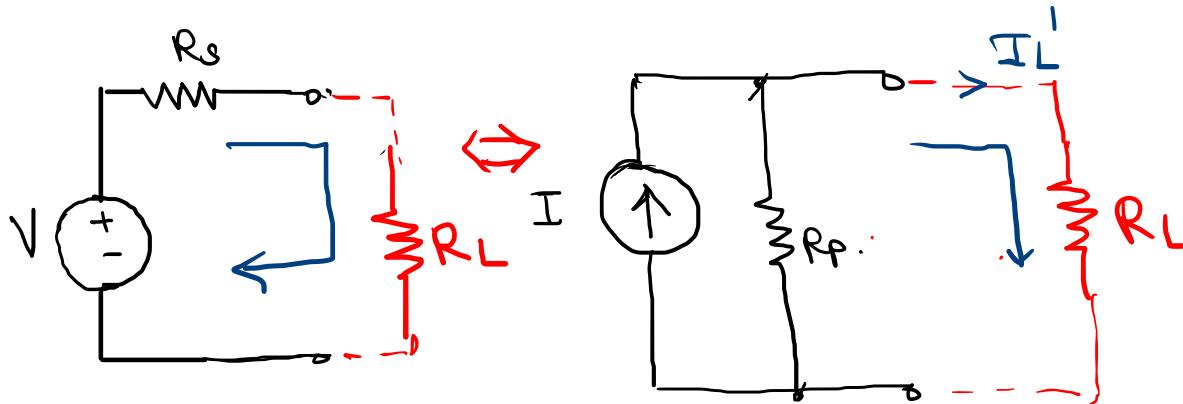
practical Current  
source.

# Source Transformation



- ⇒ Voltage source in series with resistance can be converted into equivalent current source in parallel with resistance
- ⇒ Current source in parallel with resistance can be converted into equivalent voltage source in series with resistance

# Source Transformation



$$I_L = \frac{V}{R_s + R_L}$$

$$I'_L = \frac{I \cdot R_s}{R_p + R_L}$$

To maintain electrical equivalence

$$I_L = I'_L$$

$$\frac{V}{R_s + R_L} = \frac{I \cdot R_s}{R_p + R_L}$$

$$V = I \cdot R_s \quad \text{So } I = \frac{V}{R_s}$$

$$R_s + R_L = R_p + R_L$$

$$R_s = R_p$$

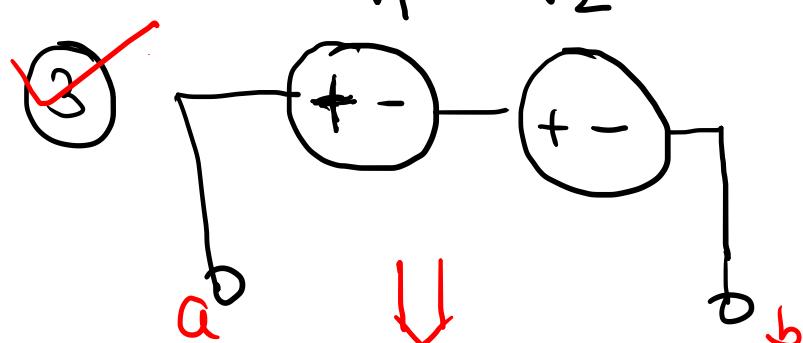
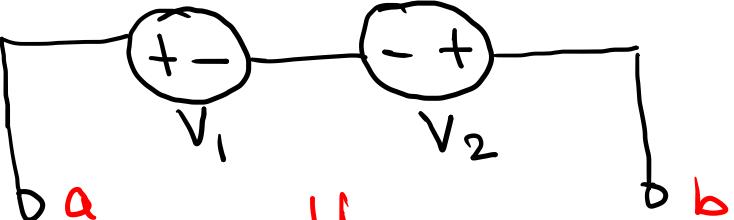
# Interconnection of energy sources

Voltage Source

Current Source

① ✓

In series



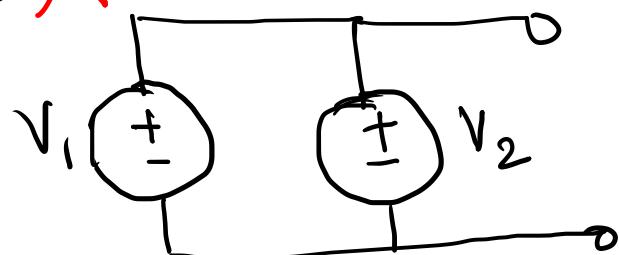
$$a \xrightarrow{+} \text{---} \xleftarrow{+} b$$

$$(v_1 - v_2)$$

$$a \xrightarrow{+} \text{---} \xleftarrow{+} b$$

$$(v_1 + v_2)$$

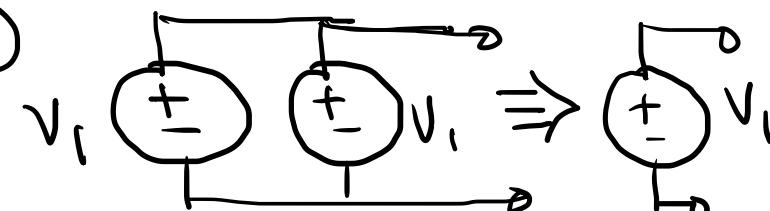
② ✗



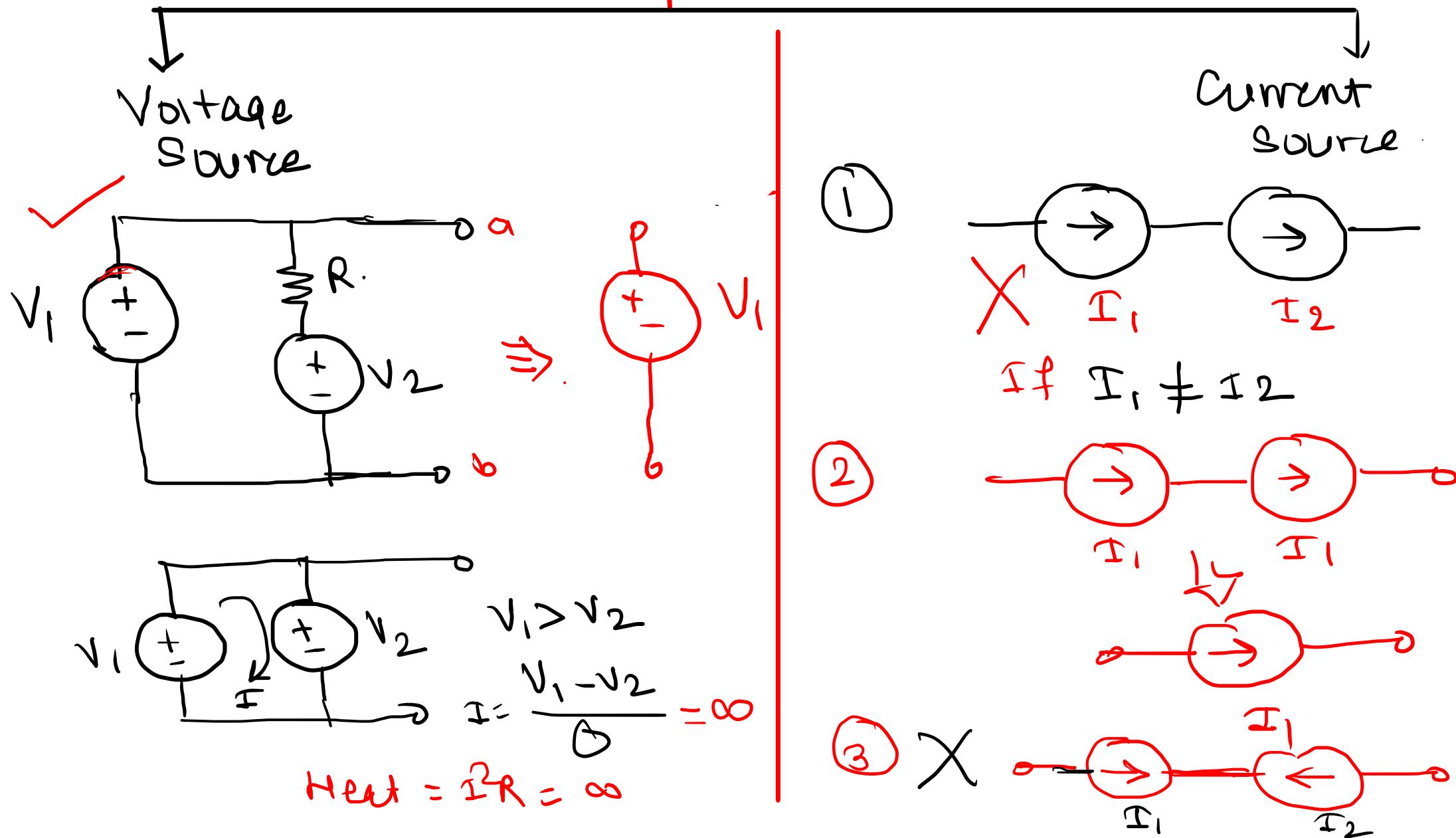
$$\Rightarrow \text{If } v_1 \neq v_2$$

$$\frac{v_1 - v_2}{0} = \infty$$

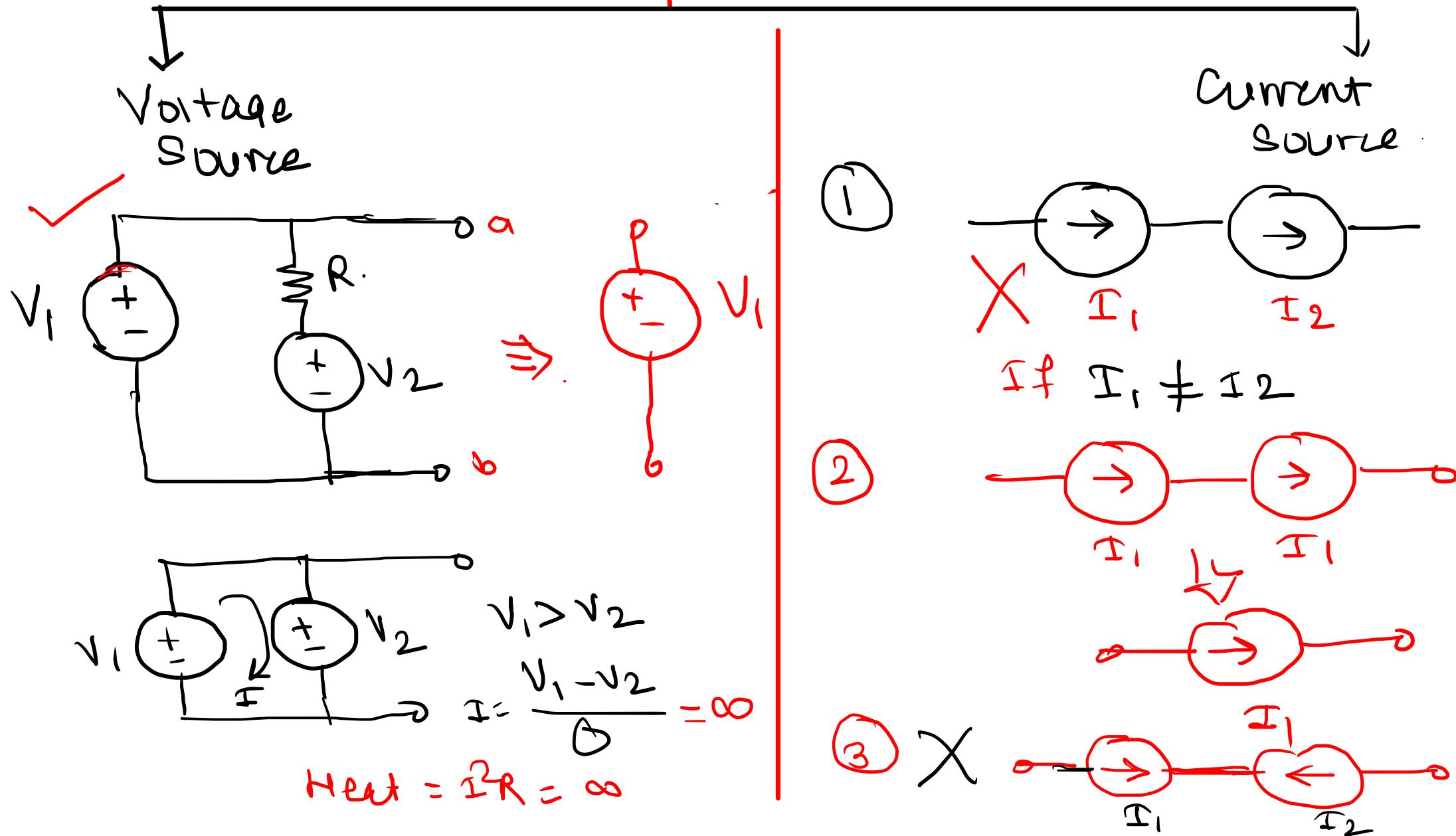
④



# Interconnection of energy sources

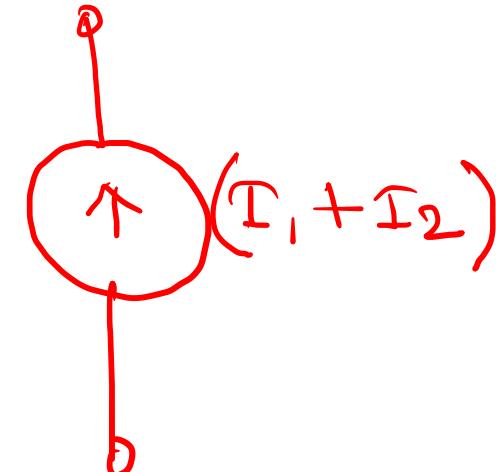
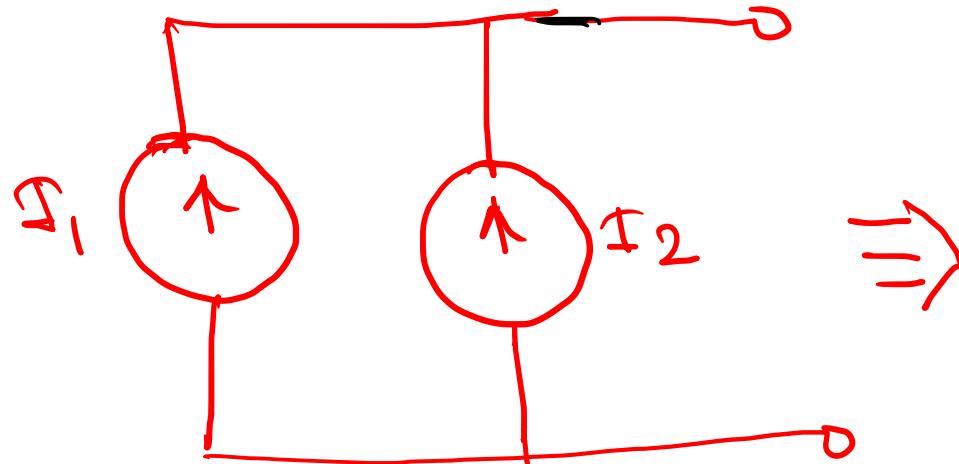


# Interconnection of energy sources



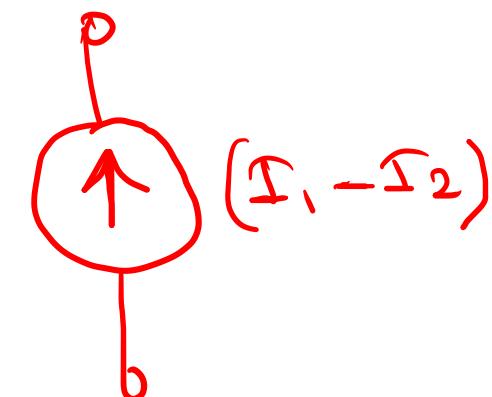
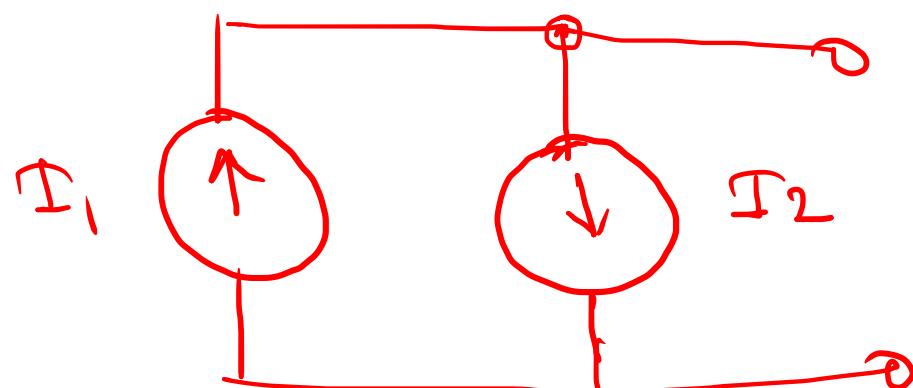
# Interconnection of energy sources

(3)

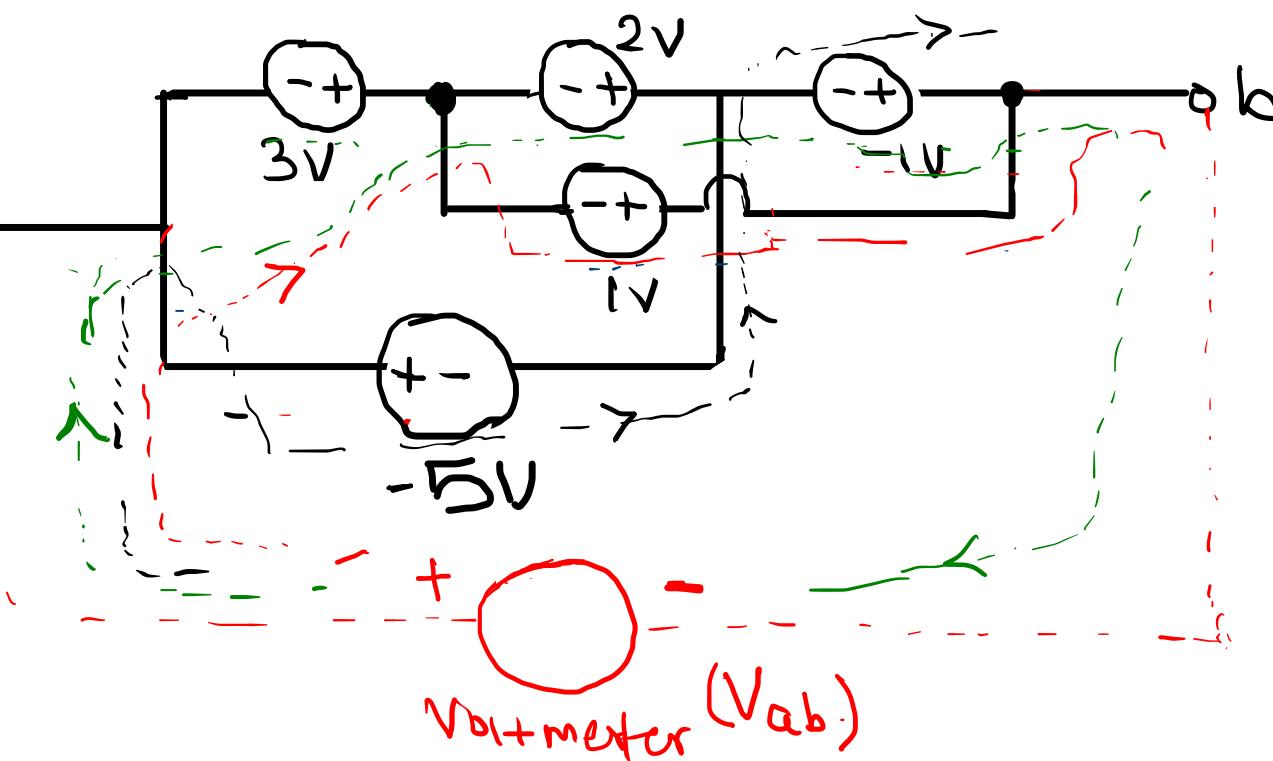
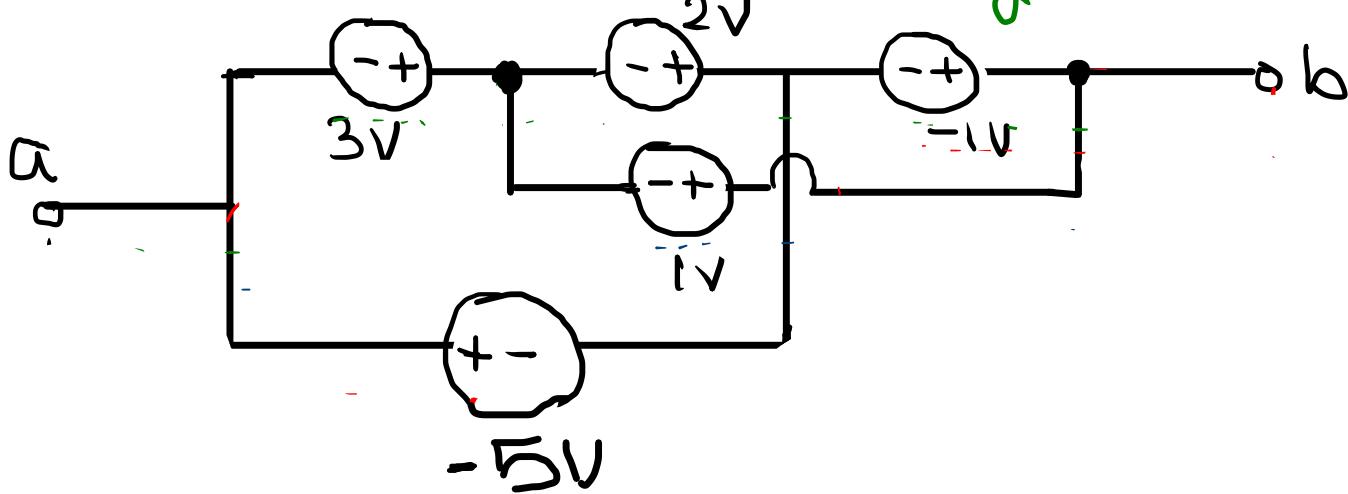


Current  
source

(4)



Q) Find  $V_{ab}$  in the following circuit.



Using KVL

$$V_{ab} + 3 + 2 + (-1) = 0$$

$$V_{ab} + 4 = 0$$

$$\boxed{V_{ab} = -4V}$$

OR

$$V_{ab} + 3 + 1 = 0$$

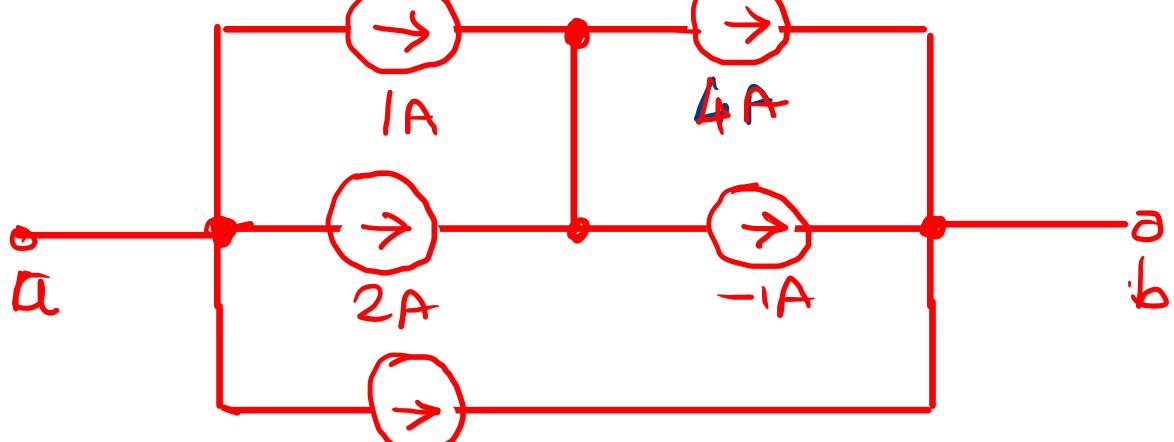
$$\boxed{V_{ab} = -4V}$$

$$V_{ab} - (-5) + (-1) = 0$$

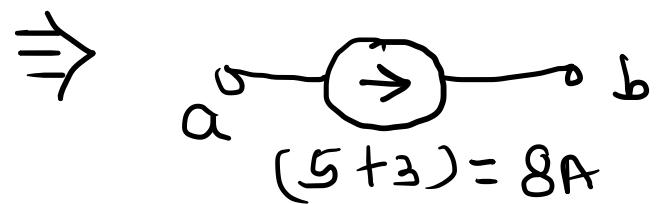
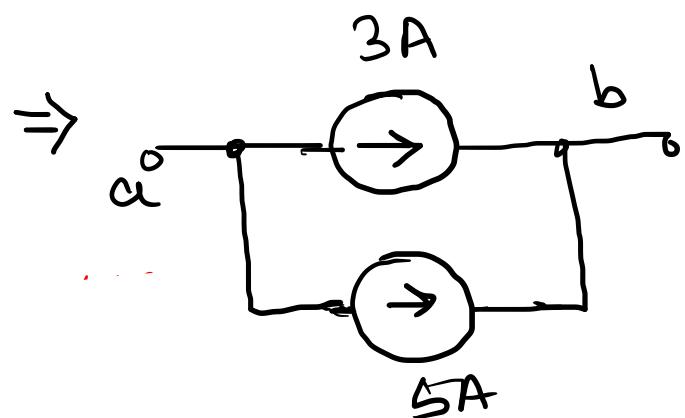
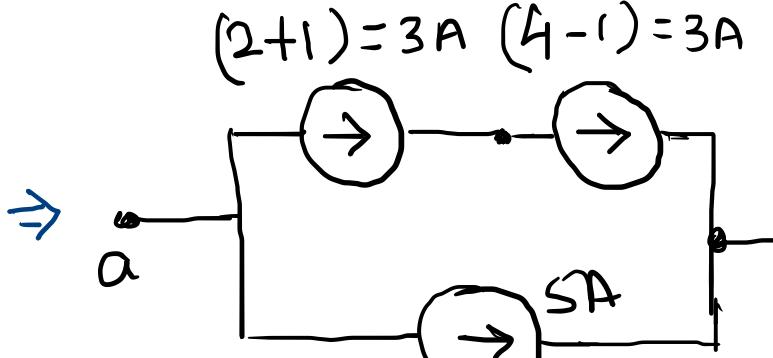
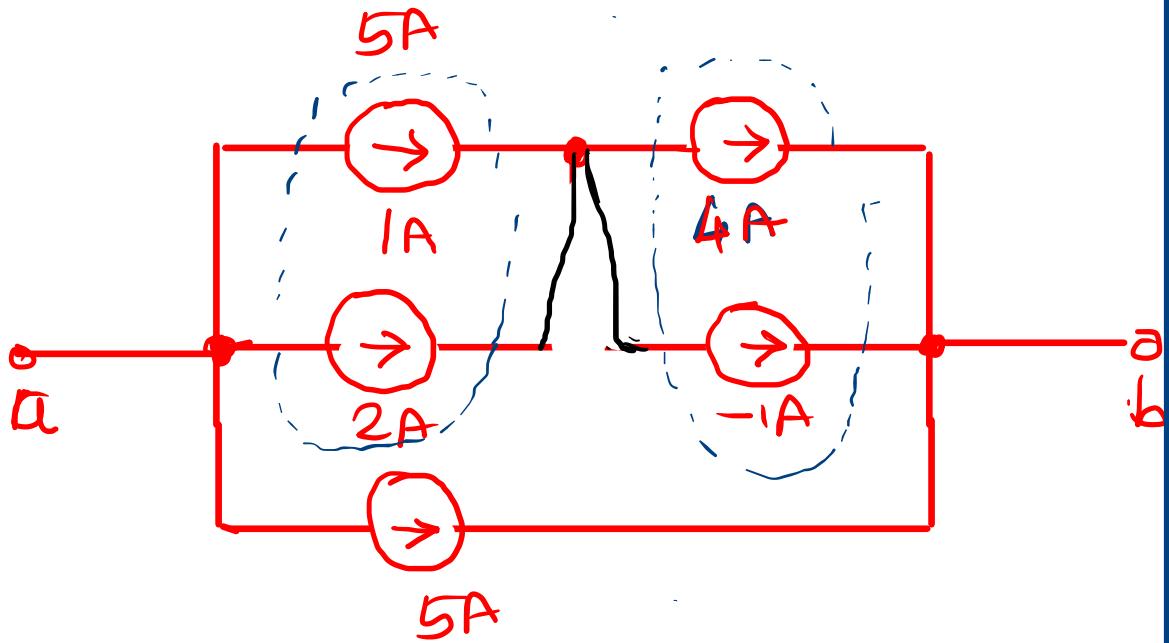
$$V_{ab} + 5 - 1 = 0$$

$$\boxed{V_{ab} = -4V}$$

② Find  $I_{ab}$

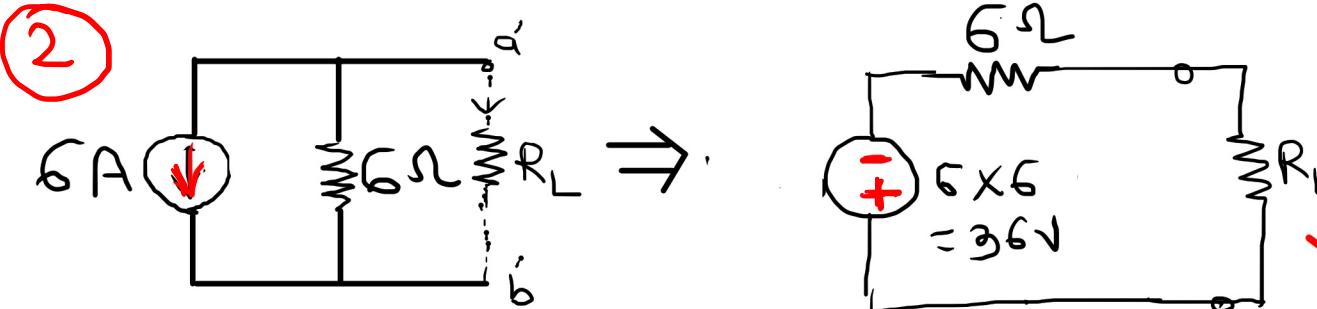
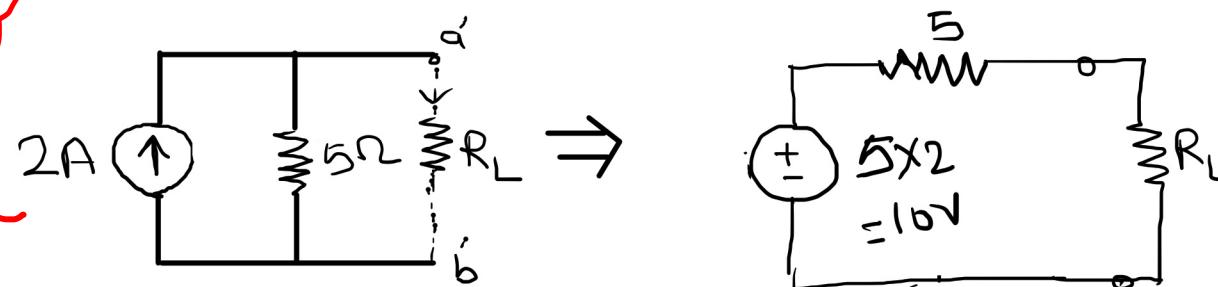
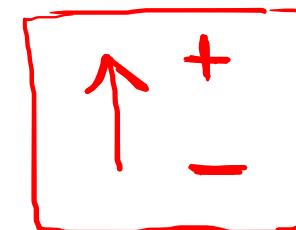
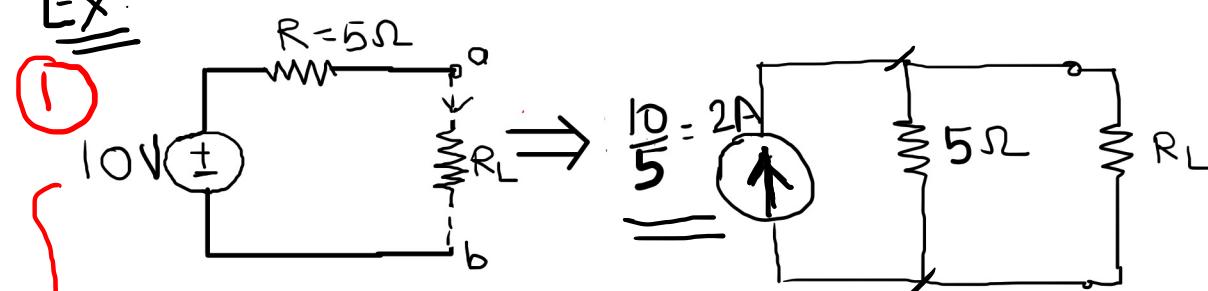


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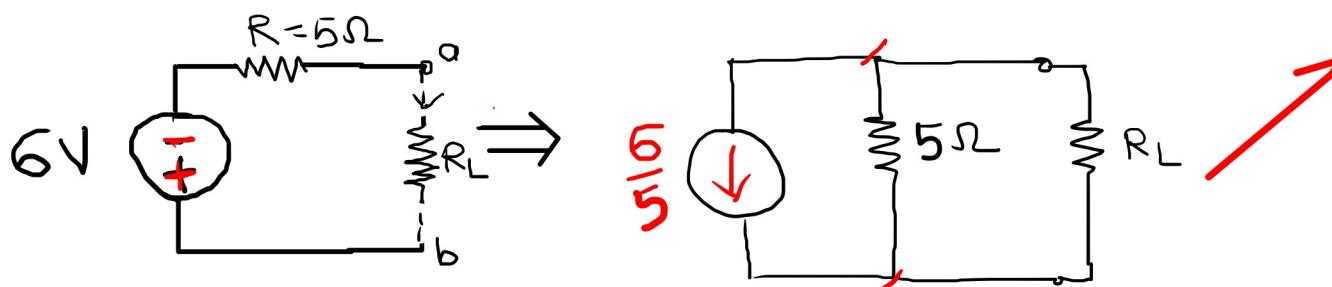


# Source Transformation Examples

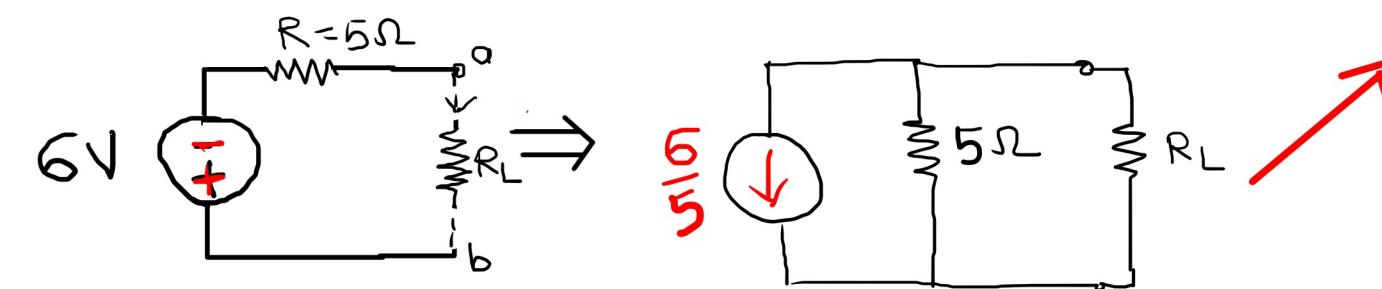
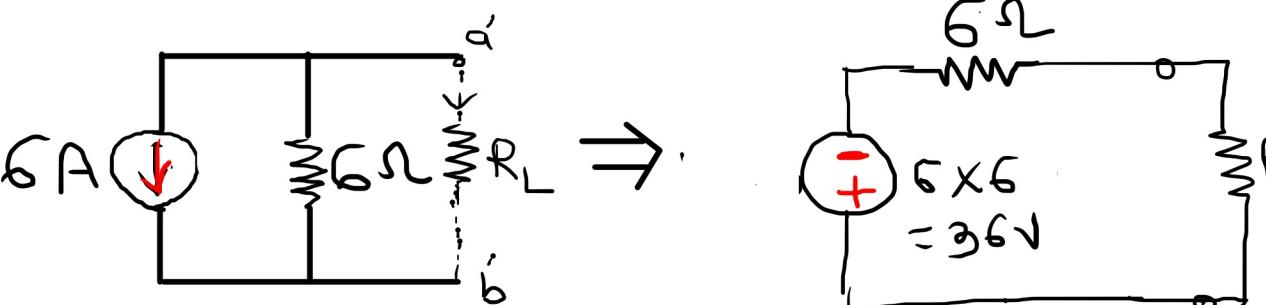
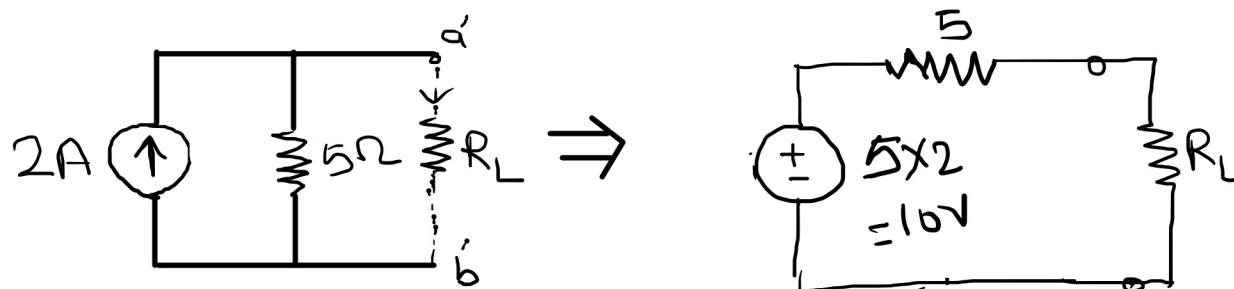
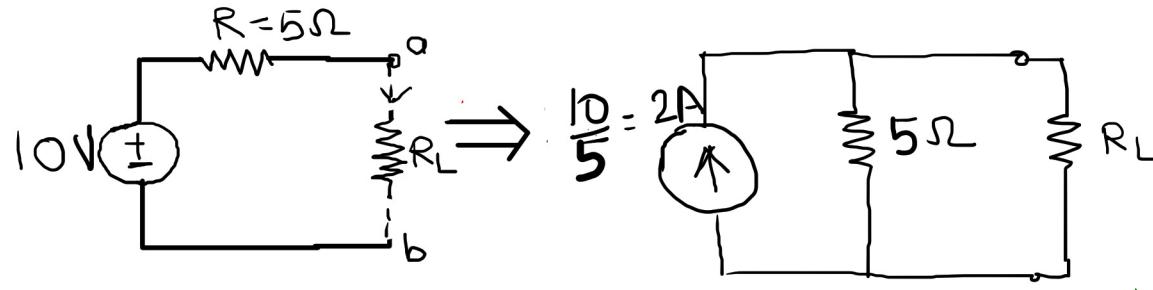
Ex.



Note the direction of  
current source &  
polarity of voltage source

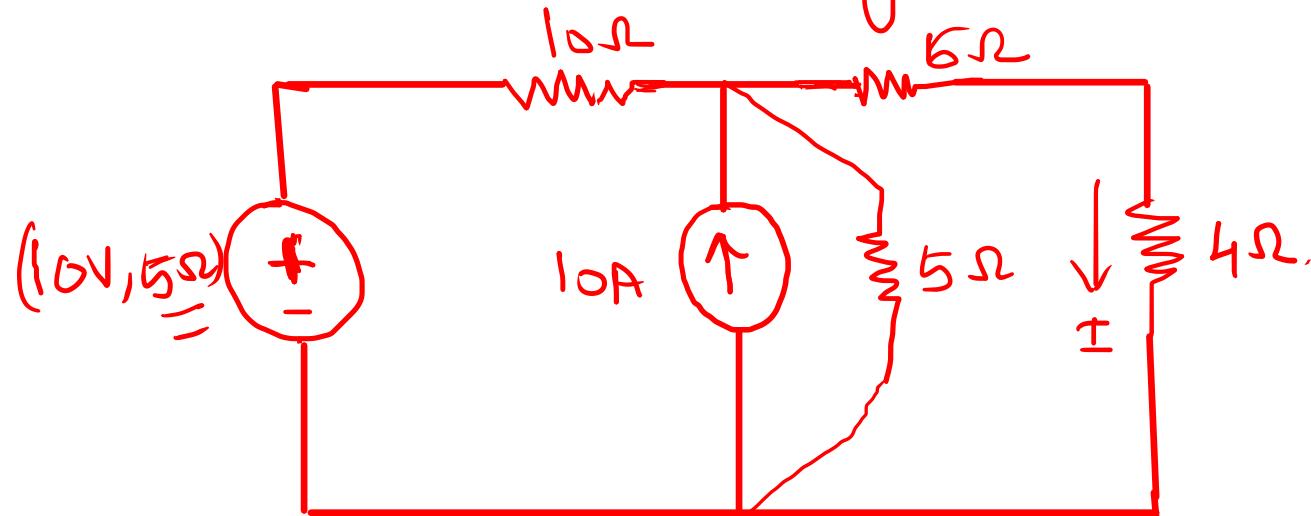


# Source Transformation Examples

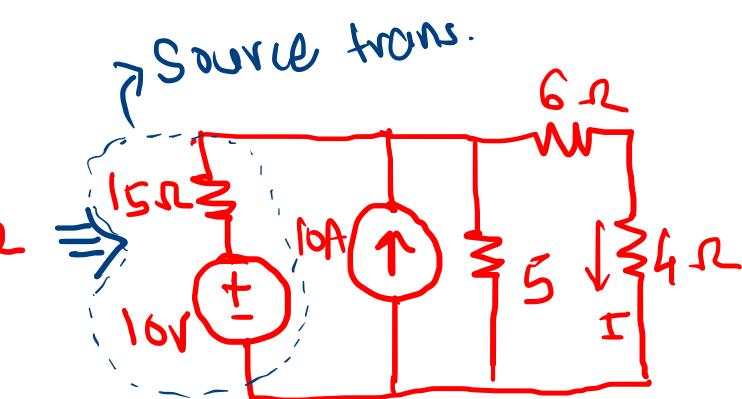
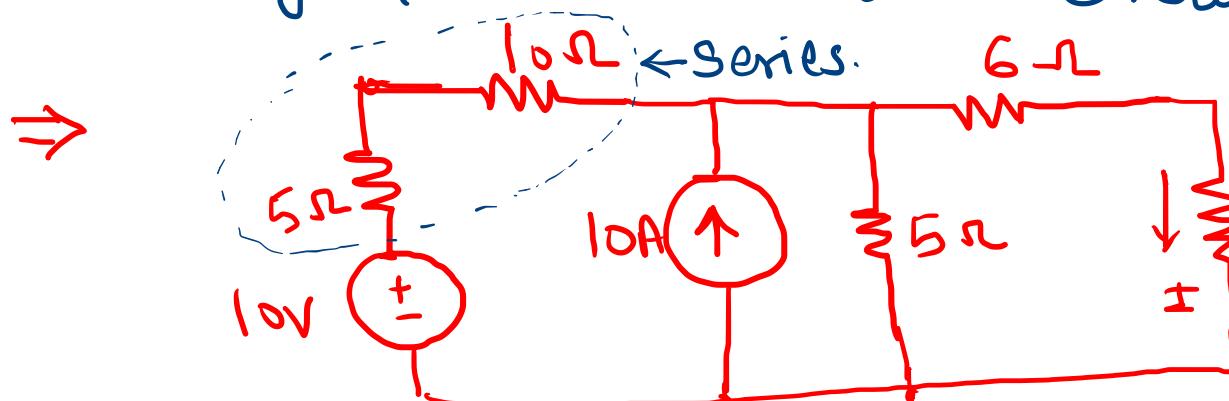


Note the direction of  
current source &  
polarity of voltage source

⇒ Find Current  $I$  using source transformation.

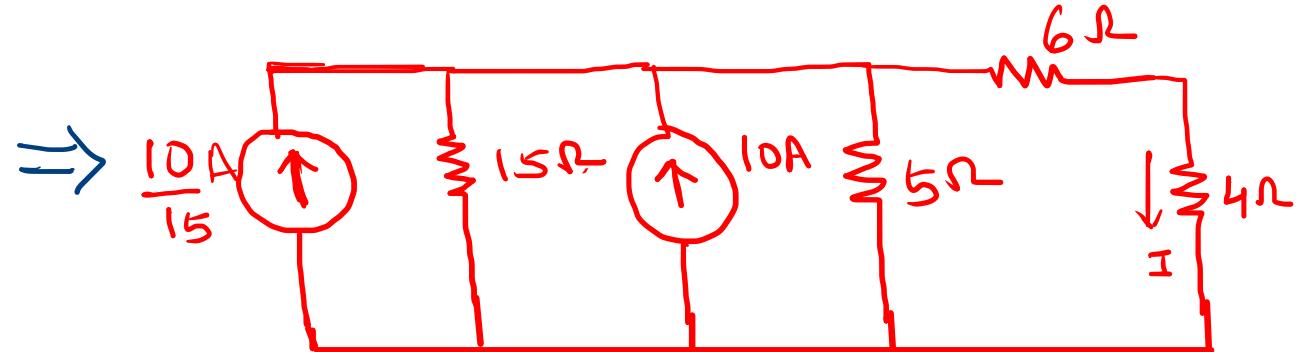
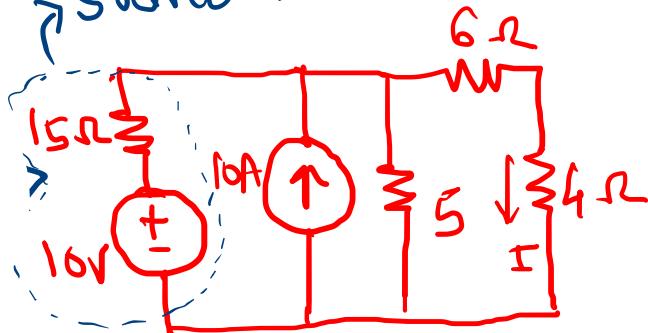


Note: Never take resistance for Source transformation across which (through which) the voltage (current) to be found.  
(e.g.  $4\Omega$  resistor in above circuit)



→ Find Current  $I$  using source transformation.

Source trans.



$$(0.67A \parallel 10A)$$

$$(10 + 0.67 = 10.67A \uparrow)$$

Source trans.

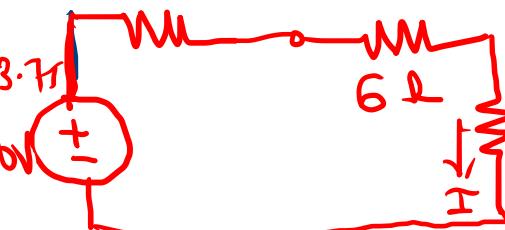


$$(15\Omega \parallel 5\Omega) \quad \frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} = \frac{R_1 + R_2}{R_1 R_2}$$

$$R_{eq} = \frac{R_1 R_2}{R_1 + R_2} = \frac{15 \times 5}{15 + 5} = \frac{75}{20} \Omega$$

$$R_{eq} = 3.75\Omega$$

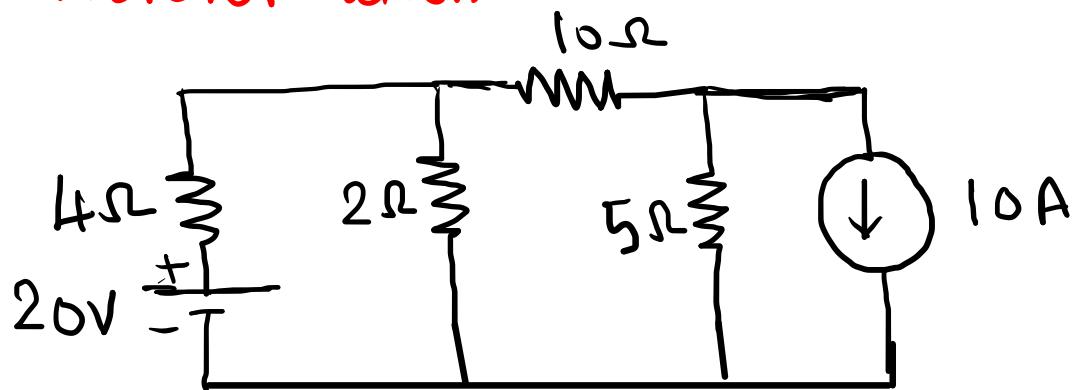
$$10.67 \times 3.75$$



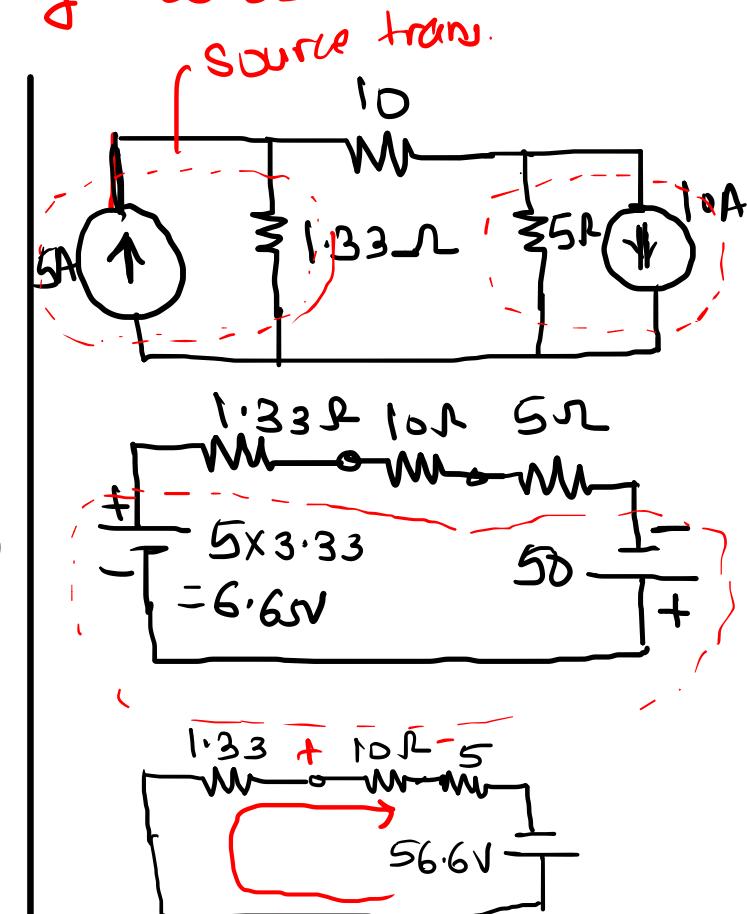
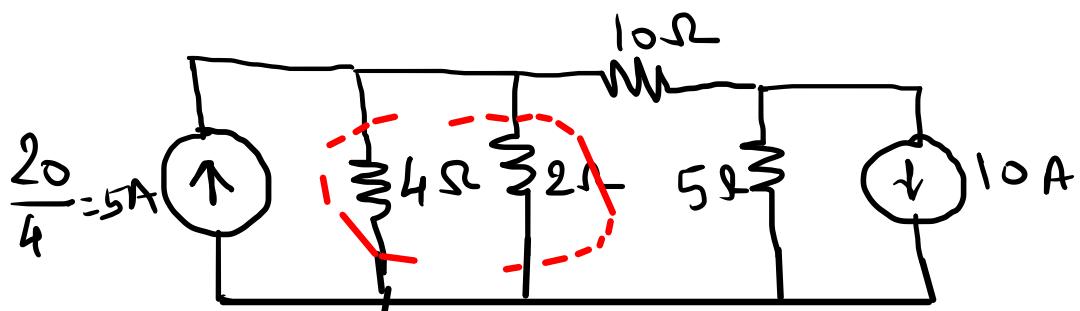
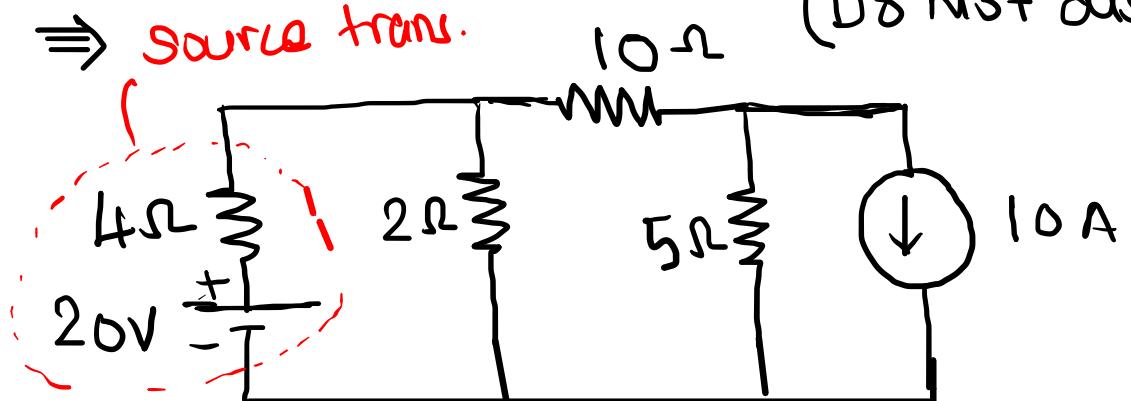
$$I = \frac{40}{(3.75 + 6 + 4)}$$

$$I = \frac{40}{13.75} = 2.91A$$

Ex(2) Find voltage across  $10\Omega$  resistor using Source transformation



⇒ **Source trans.** (Do Not disturb  $10\Omega$ )



Using Voltage division formula.

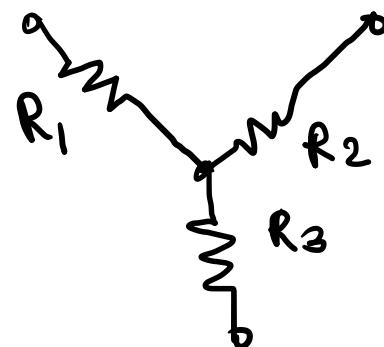
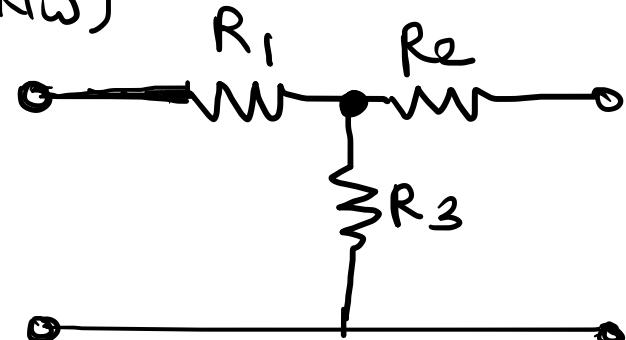
$$V_{10\Omega} = \frac{10 \times 56.6}{1.33 + 10 + 5}$$

$$V_{10\Omega} = (34.69)V$$

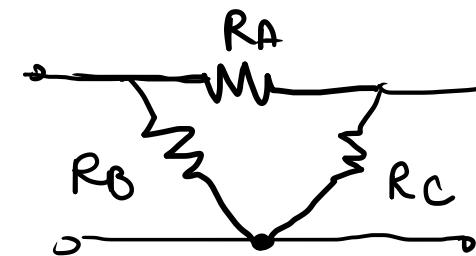
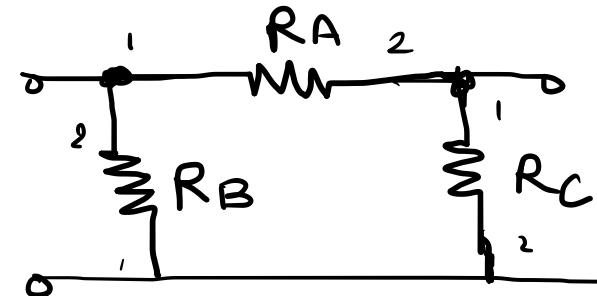
## Resistive network simplification using star-delta transformations

- ① Series Combination of resistors  $\Rightarrow$  Equivalent Reg =  $R_1 + R_2 + \dots + R_n$
- ② Parallel Combination of resistors  $\Rightarrow \frac{1}{R_{\text{eq}}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}$

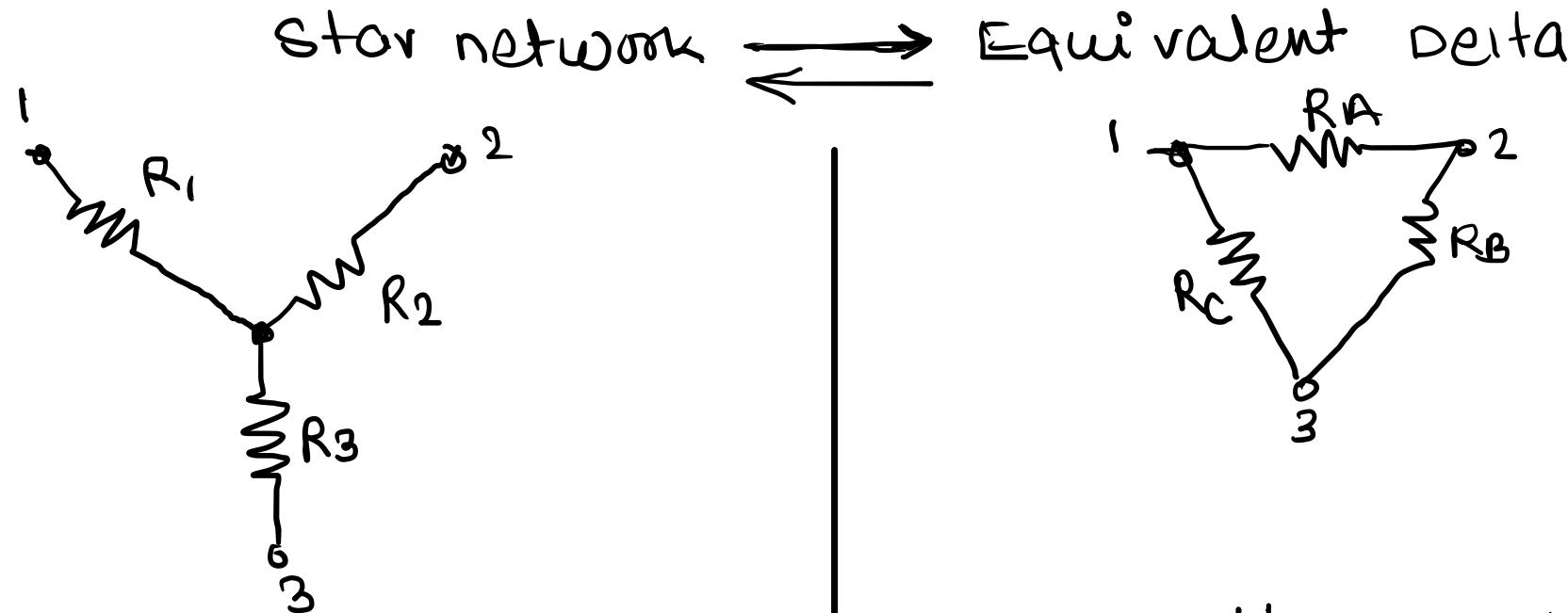
$\Rightarrow$  Star Network ( $\gamma$ )  
(T-NW)



$\Rightarrow$  Delta Network ( $\pi$ )  
(Mesh network)



## Resistive network simplification using star-delta transformations



$$R_{12Y} = R_1 + R_2$$

$$R_{23Y} = R_2 + R_3$$

$$R_{31Y} = R_1 + R_3$$

$$R_{12\Delta} = R_A \parallel (R_B + R_C)$$

$$R_{23\Delta} = R_B \parallel (R_A + R_C)$$

$$R_{31\Delta} = R_C \parallel (R_A + R_B)$$

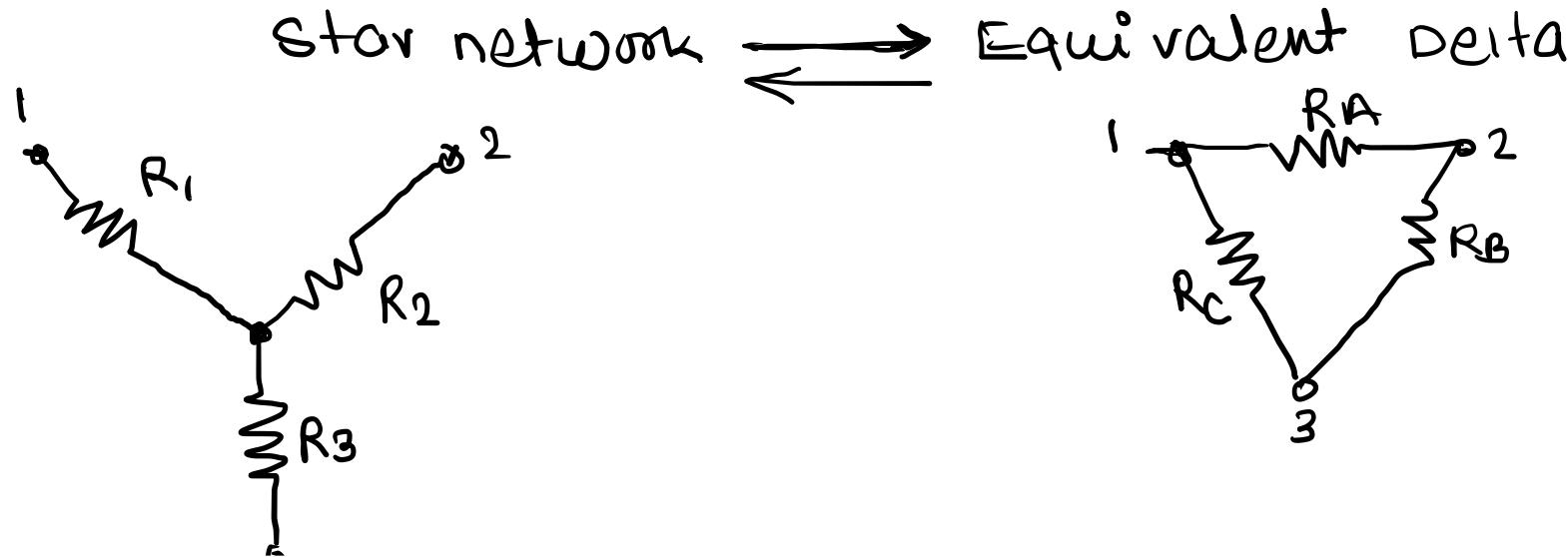
TWO NETWORKS WILL BE EQUIVALENT WHEN

$$R_{12Y} = R_{12\Delta}$$

$$R_{23Y} = R_{23\Delta}$$

$$R_{31Y} = R_{31\Delta}$$

## Resistive network simplification using star-delta transformations



Delta  $\rightarrow$  Star network

$$R_1 + R_2 = R_A \parallel (R_B + R_C)$$

$$R_1 + R_2 = \frac{R_A (R_B + R_C)}{R_A + R_B + R_C} \quad \text{--- (1)}$$

$$R_2 + R_3 = \frac{R_B (R_A + R_C)}{R_A + R_B + R_C} \quad \text{--- (2)}$$

$$R_3 + R_1 = \frac{R_C (R_A + R_B)}{R_A + R_B + R_C} \quad \text{--- (3)}$$

Equation (1) + (2) - (3)

$$R_1 + R_2 + R_3 - R_3 - R_1$$

$$= \frac{R_A (R_B + R_C)}{R_A + R_B + R_C}$$

## Resistive network simplification using star-delta transformations

Delta  $\rightarrow$  Star network

$$R_1 + R_2 = R_A \parallel (R_B + R_C)$$

$$R_1 + R_2 = \frac{R_A(R_B + R_C)}{R_A + R_B + R_C} \quad \text{--- (I)}$$

$$R_2 + R_3 = \frac{R_B(R_A + R_C)}{R_A + R_B + R_C} \quad \text{--- (II)}$$

$$R_3 + R_1 = \frac{R_C(R_A + R_B)}{R_A + R_B + R_C} \quad \text{--- (III)}$$

Adding (I) + (II) - (III)

$$\cancel{R_1 + R_2 + R_2 + R_3 - R_3 - R_1} = \frac{R_A(R_B + R_C) + R_B(R_A + R_C) - R_C(R_A + R_B)}{R_A + R_B + R_C}$$

$$2R_2 = \frac{\cancel{R_A R_B + R_A R_C} + R_A R_B + \cancel{R_B R_C} - \cancel{R_A R_C} - \cancel{R_B R_C}}{R_A + R_B + R_C}$$

$$2R_2 = \frac{\cancel{2 R_A R_B}}{R_A + R_B + R_C}$$

$$R_2 = \frac{R_A R_B}{R_A + R_B + R_C}$$

## Resistive network simplification using star-delta transformations

Delta  $\rightarrow$  Star network

$$R_1 + R_2 = R_A \parallel (R_B + R_C)$$

$$R_1 + R_2 = \frac{R_A(R_B + R_C)}{R_A + R_B + R_C} \quad \text{--- (I)}$$

$$R_2 + R_3 = \frac{R_B(R_A + R_C)}{R_A + R_B + R_C} \quad \text{--- (II)}$$

$$R_3 + R_1 = \frac{R_C(R_A + R_B)}{R_A + R_B + R_C} \quad \text{--- (III)}$$

Adding  $(\textcircled{I}) + (\textcircled{\text{III}}) - (\textcircled{\text{II}})$

$$2R_1 = \frac{2R_A \cdot R_C}{R_A + R_B + R_C}$$

$$R_1 = \frac{R_A R_C}{R_A + R_B + R_C}$$

Simplifying  
 $(\textcircled{\text{II}}) + (\textcircled{\text{III}}) - (\textcircled{I})$

$$2R_3 = \frac{2R_B R_C}{R_A + R_B + R_C}$$

$$R_3 = \frac{R_B R_C}{R_A + R_B + R_C}$$

## Resistive network simplification using star-delta transformations

Star  $\rightarrow$  Delta

$$R_1 = \frac{RA RC}{RA + RB + RC}$$

$$R_2 = \frac{RA RB}{RA + RB + RC}$$

$$R_3 = \frac{RB RC}{RA + RB + RC}$$

$$R_1 R_2 = \frac{RA^2 RB RC}{(RA + RB + RC)^2}$$

$$R_2 R_3 = \frac{RA^2 RB RC}{(RA + RB + RC)^2}$$

$$R_3 R_1 = \frac{RA RB R_C^2}{(RA + RB + RC)^2}$$

$$\sum R = R_1 R_2 + R_2 R_3 + R_3 R_1 = \frac{RA^2 RB RC + RA^2 RB RC + RA RB^2 RC}{(RA + RB + RC)^2}$$

$$\sum R = \frac{RA RB RC (RA + RB + RC)}{(RA + RB + RC)^2}$$

$$\sum R = \frac{RA RB RC}{RA + RB + RC} \quad \text{--- } (4)$$

$$\frac{\sum R}{R_1} = \frac{\cancel{RA RB RC}}{\cancel{(RA + RB + RC)}} \times \frac{\cancel{(RA + RB + RC)}}{\cancel{RA RC}} = RB$$

$$\frac{\sum R}{R_2} = \frac{\cancel{RA RB RC}}{\cancel{RA + RB + RC}} \times \frac{\cancel{(RA + RB + RC)}}{\cancel{RA \cdot RB}} = RC$$

$$\frac{\sum R}{R_3} = \frac{\cancel{RA RB RC}}{\cancel{RA + RB + RC}} \times \frac{\cancel{(RA + RB + RC)}}{\cancel{RB \cdot RC}} = RA$$

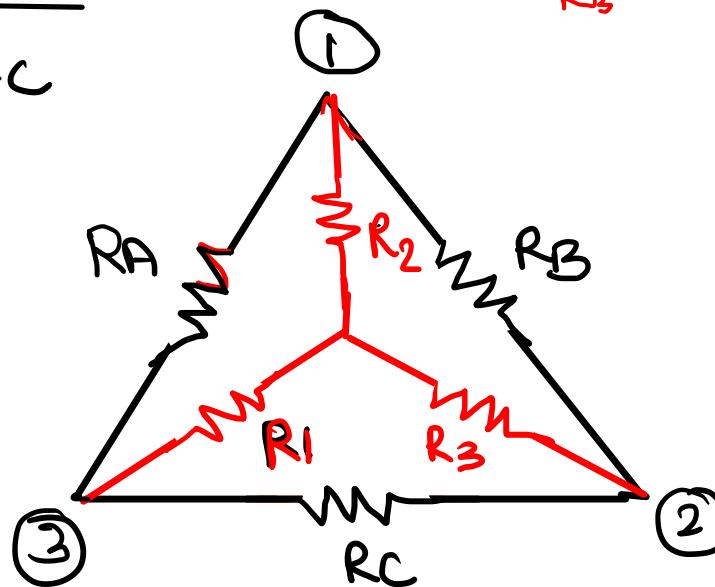
# Resistive network simplification using star-delta transformations

Delta  $\rightarrow$  Star

$$R_1 = \frac{RA \cdot RC}{RA + RB + RC}$$

$$R_2 = \frac{RA \cdot RB}{RA + RB + RC}$$

$$R_3 = \frac{RB \cdot RC}{RA + RB + RC}$$



Star  $\rightarrow$  Delta

$$\sum R = \frac{RA \cdot RB \cdot RC}{RA + RB + RC} \quad \text{--- (4)}$$

$$\frac{\sum R}{R_1} = \frac{RA \cdot RB \cdot RC}{(RA+RB+RC)} \times \frac{(RA+RB+RC)}{RA \cdot RC} = RB$$

$$\frac{\sum R}{R_2} = \frac{RA \cdot RB \cdot RC}{RA+RB+RC} \times \frac{(RA+RB+RC)}{RA \cdot RC} = RC$$

$$\frac{\sum R}{R_3} = \frac{RA \cdot RB \cdot RC}{RA+RB+RC} \times \frac{(RA+RB+RC)}{RB \cdot RC} = RA$$

$$RA = \frac{\sum R}{R_3}$$

$$RB = \frac{\sum R}{R_1}$$

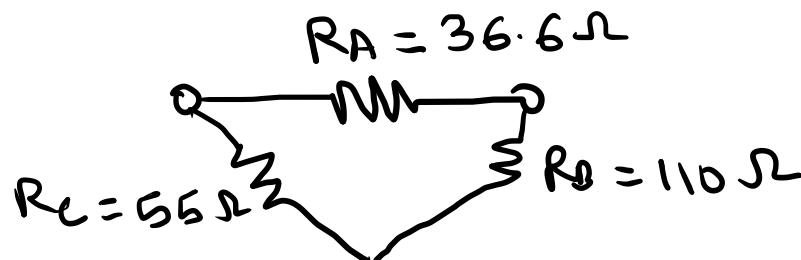
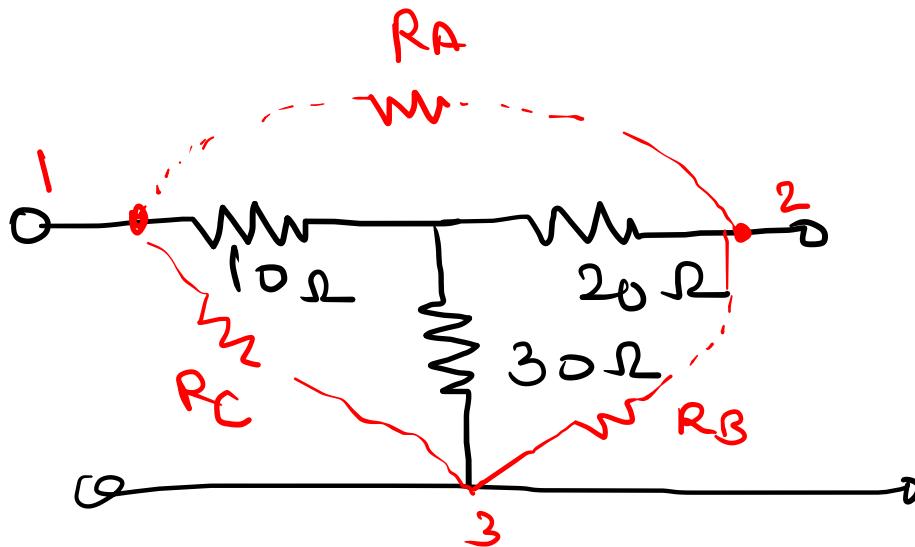
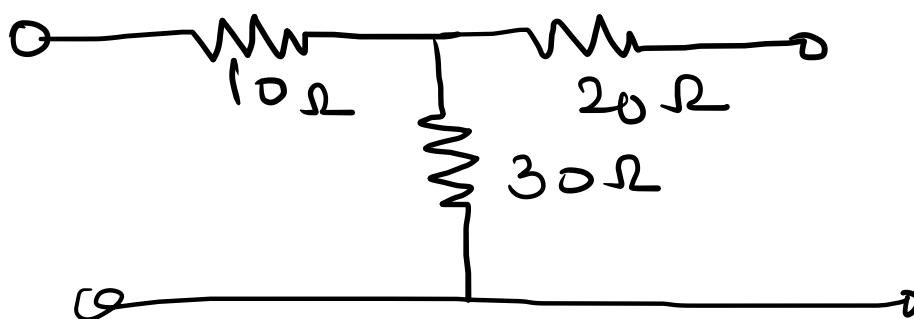
$$RC = \frac{\sum R}{R_2}$$

$$\sum R = R_1 R_2 + R_2 R_3 + R_1 R_3$$

## Resistive network simplification using star-delta transformations

Ex. ①

Convert to equivalent delta



$$\sum R = R_1 R_2 + R_2 R_3 + R_3 R_1$$

$$\bar{\sum} R = 10 \times 20 + 20 \times 30 + 30 \times 10$$

$$\sum R = 200 + 600 + 300 = 1100$$

$$R_A = \frac{\sum R}{30} = \frac{1100}{30} = \frac{110}{3} = 36.66\Omega$$

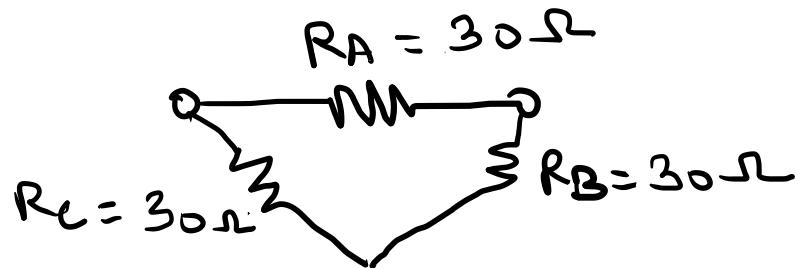
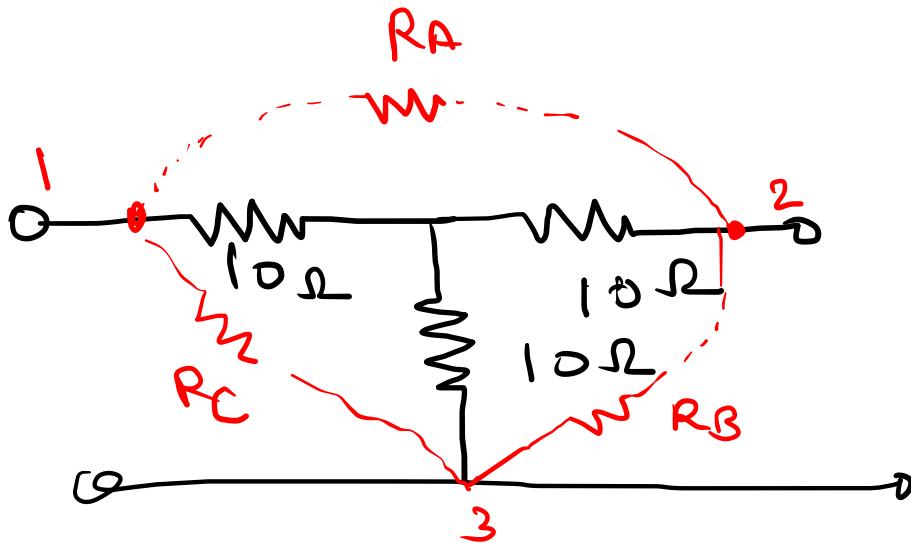
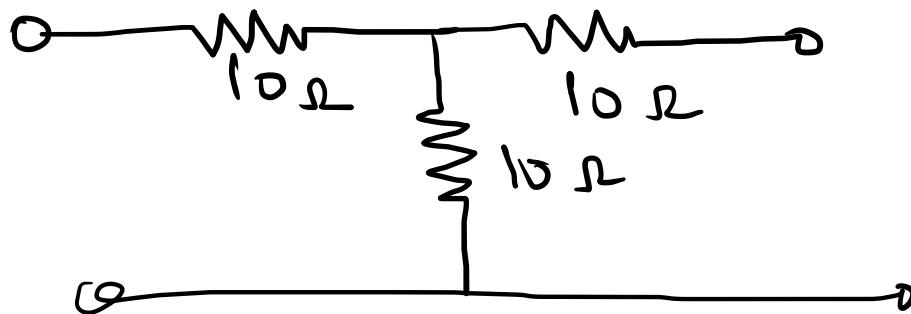
$$R_B = \frac{\sum R}{10} = \frac{1100}{10} = 110\Omega$$

$$R_C = \frac{\sum R}{20} = \frac{1100}{20} = 55\Omega$$

## Resistive network simplification using star-delta transformations

Ex. 11

Convert to equivalent delta



$$\sum R = R_1 R_2 + R_2 R_3 + R_3 R_1$$

$$\sum R = 10 \times 10 + 10 \times 10 + 10 \times 10 = 300$$

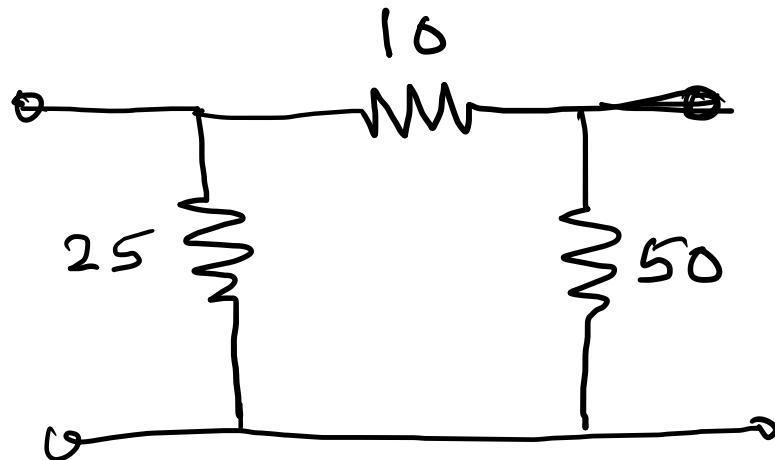
$$R_A = \frac{\sum R}{10} = \frac{300}{10} = 30\ \Omega$$

$$R_B = R_C = \frac{\sum R}{10} = 30\ \Omega$$

Delta resistances =  $3 \times$  Star resistance  
if all resistances in Star one same.

## Resistive network simplification using star-delta transformations

Ex. (1) Convert following network into equivalent star.

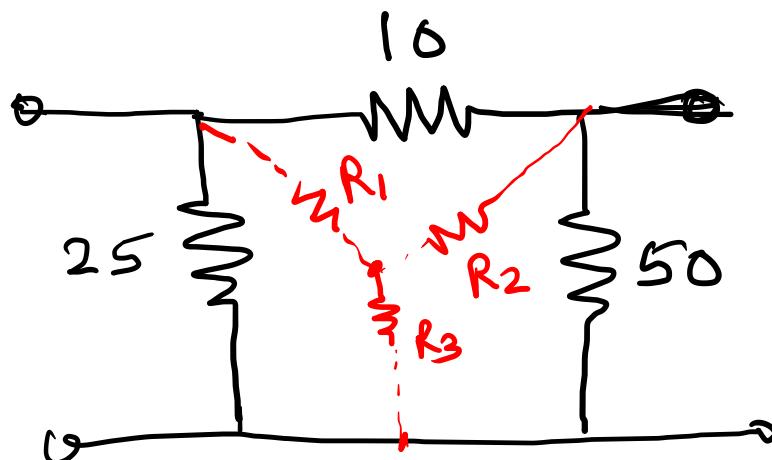


$$R_A + R_B + R_C = 10 + 50 + 25 = 85$$

$$R_1 = \frac{25 \times 10}{85} = 2.94 \Omega$$

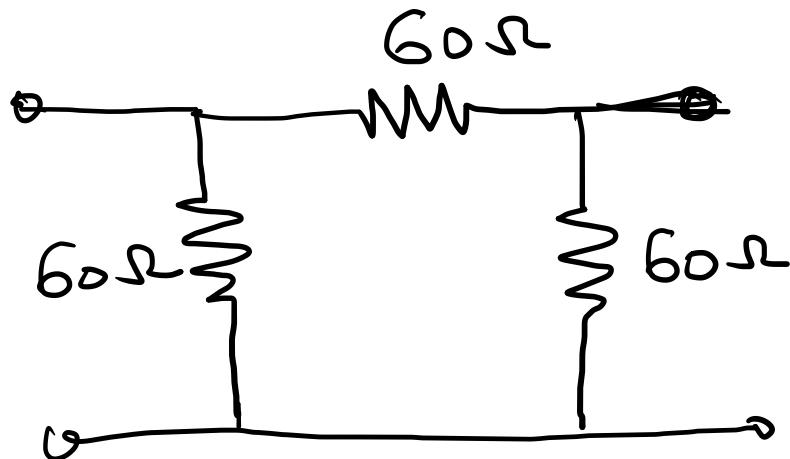
$$R_2 = \frac{10 \times 50}{85} = 5.88 \Omega$$

$$R_3 = \frac{25 \times 50}{85} = 14.7 \Omega$$



## Resistive network simplification using star-delta transformations

Ex N Convert following network into equivalent star.



$$R_A + R_B + R_C = 60 + 60 + 60$$

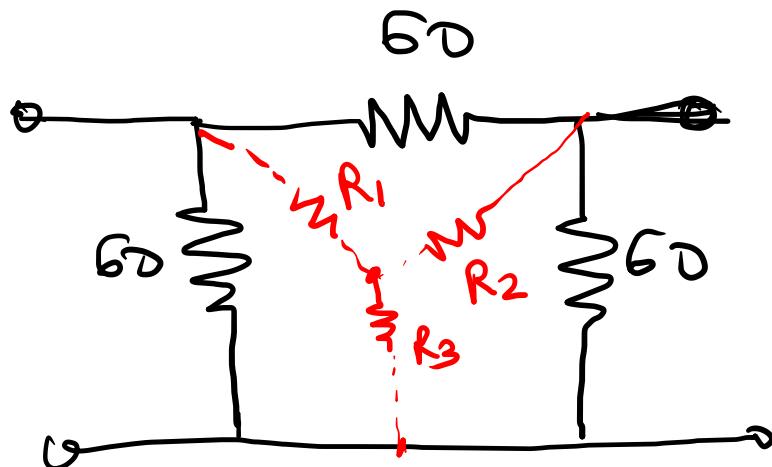
$$R_A + R_B + R_C = 180$$

$$R_1 = R_2 = R_3 = \frac{60 \times 60}{180}$$

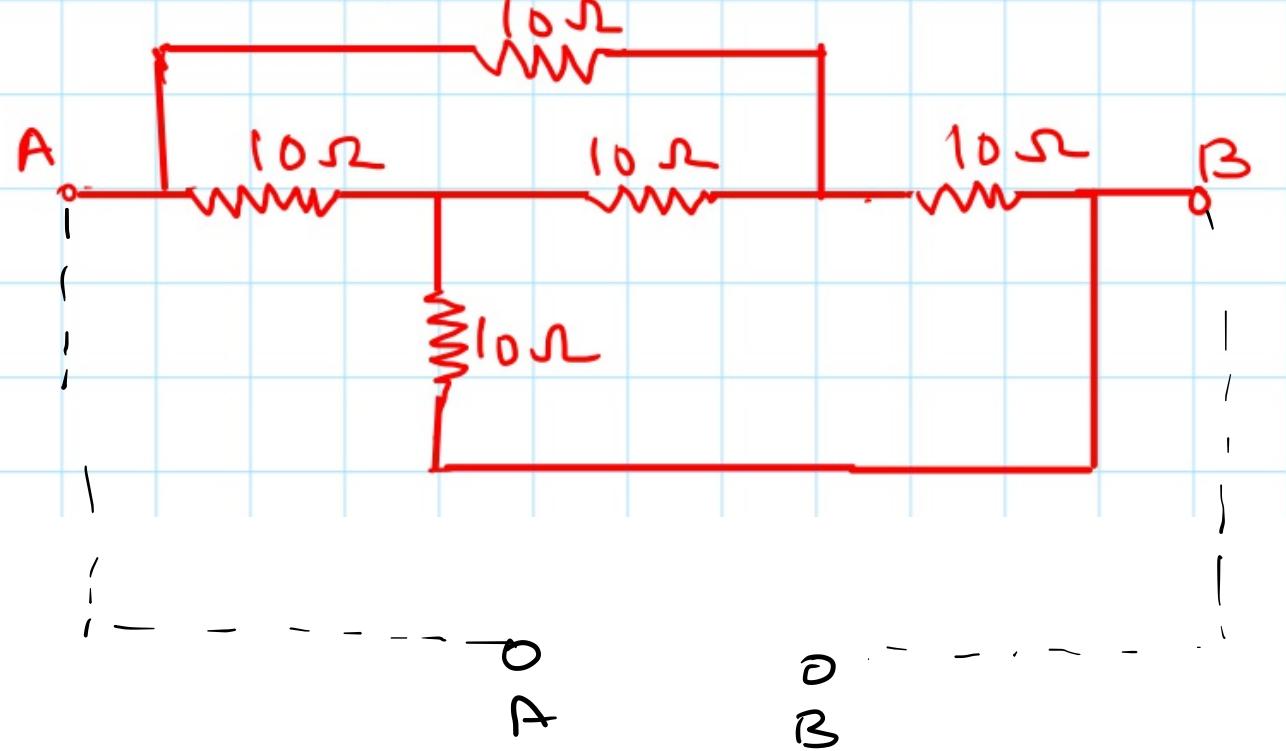
$$R_1 = R_2 = R_3 = 20\Omega$$

If all delta network resistances are same then

$$\text{Star equivalent} = \frac{1}{3} \times \text{Delta resistance}$$



Example: ② Find resistance  $R_{AB}$



Example ③ Find resistance  $R_{AB}$  in the following network

