

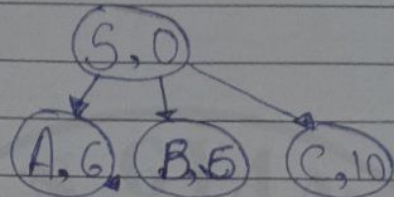
Q1.

1.1]

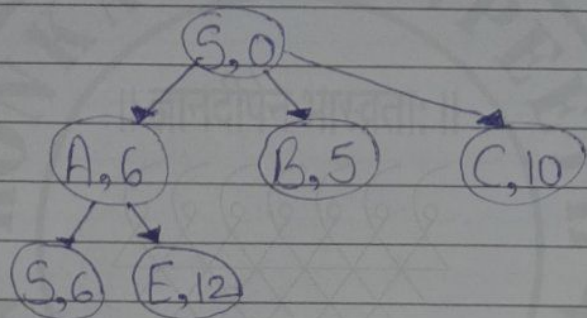
→ Step 0:

(S,0)

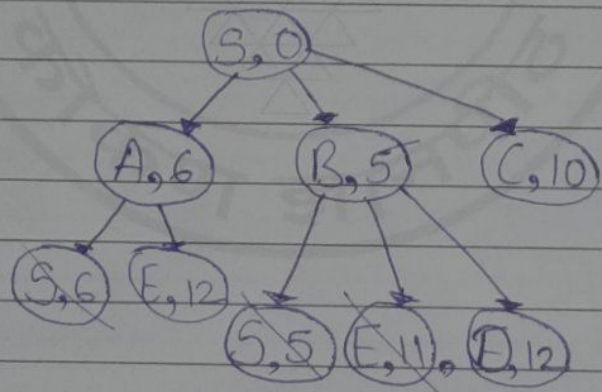
Step 1:



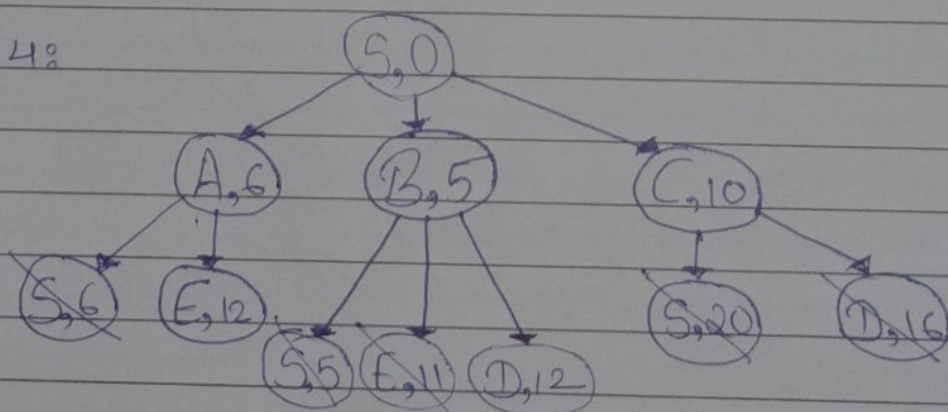
Step 2:



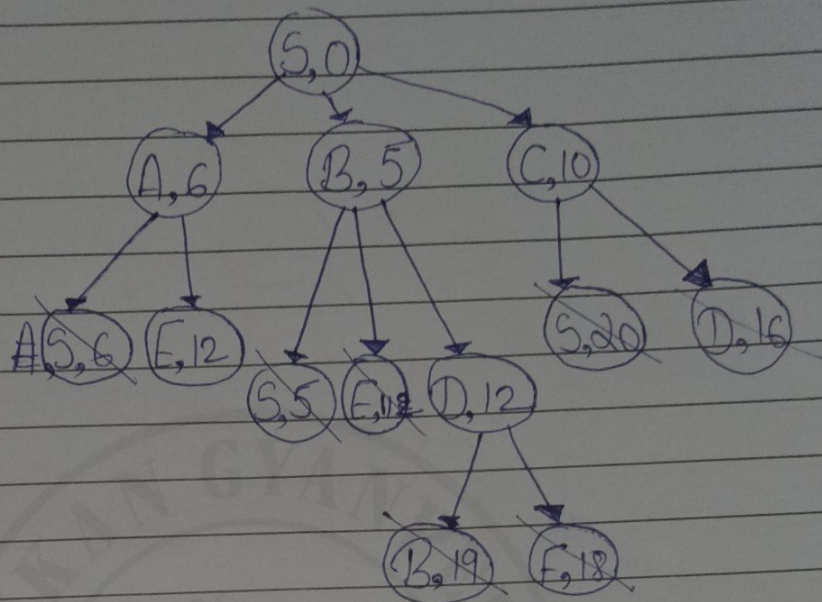
Step 3:



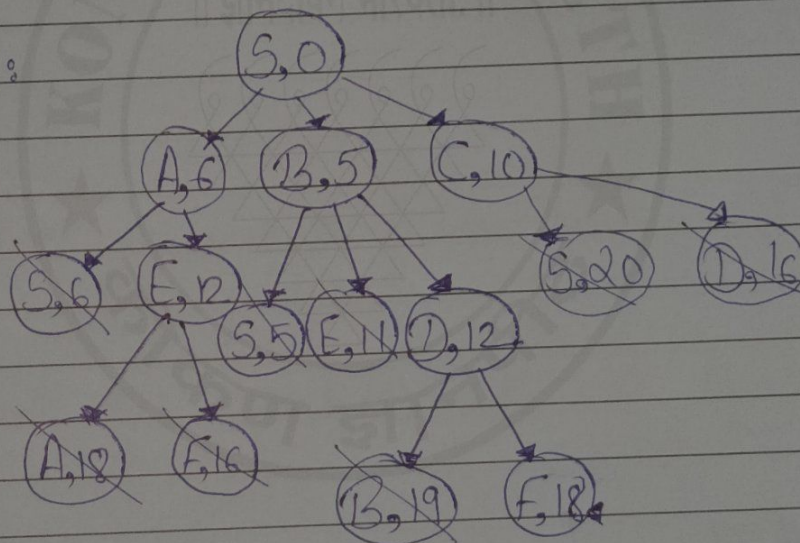
Step 4:



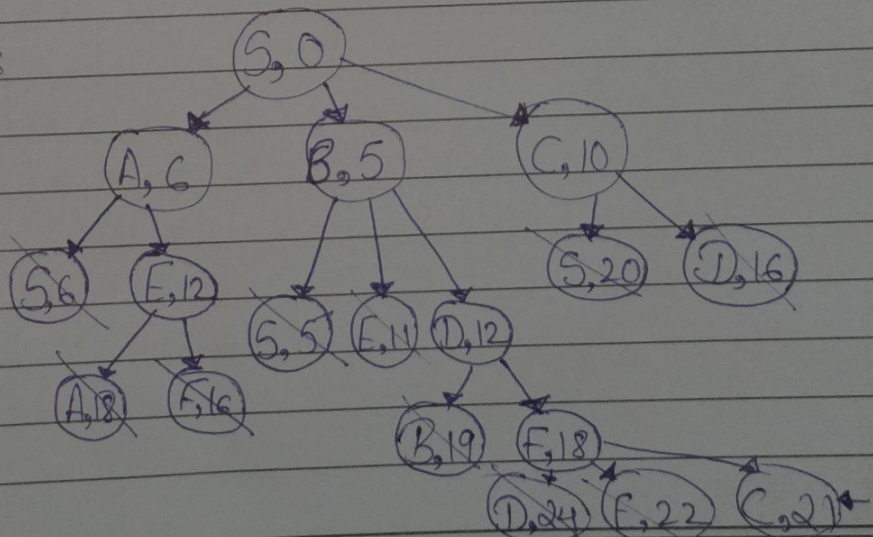
Step 5:



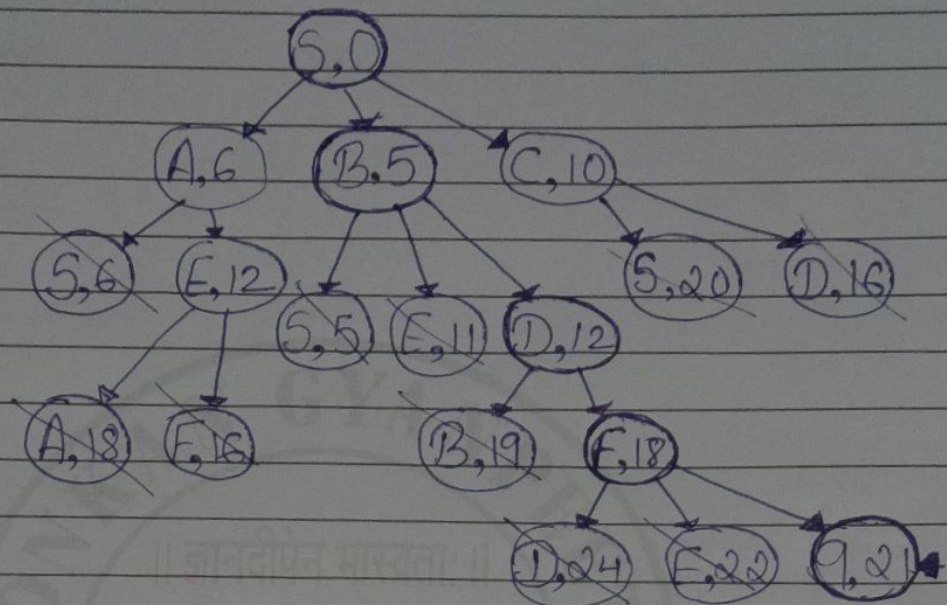
Step 6:



Step 7:



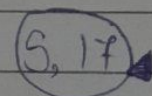
Step 8:



1.4

Initialization : Compute f-score for S & put in it the openlist.

F-score S : $f(S) = h(S) = 17$



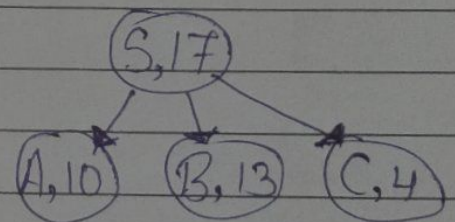
Step 1:

F-score of successors

$$f(A) = h(A) = 10$$

$$f(B) = h(B) = 13$$

$$f(C) = h(C) = 4$$

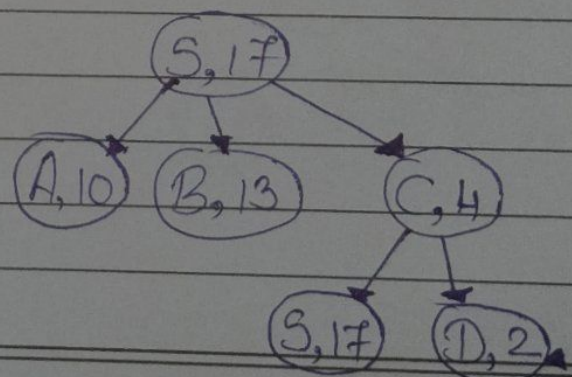


Step 2:

F-score of successors

$$f(S) = h(S) = 17$$

$$f(D) = h(D) = 2$$



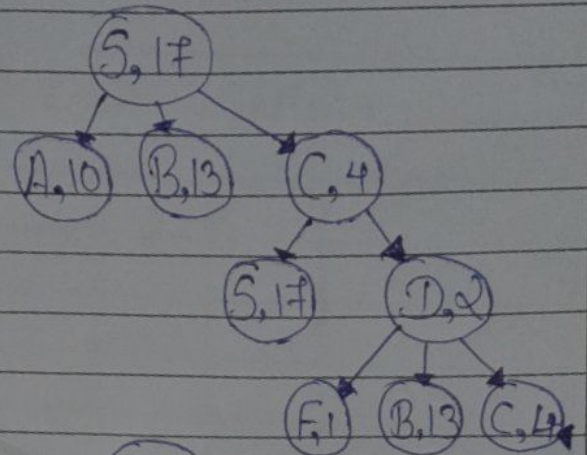
Step 3:

F-score of successor

$$f(A) = h(A) = 4$$

$$f(B) = h(B) = 13$$

$$f(F) = h(F) = 1$$



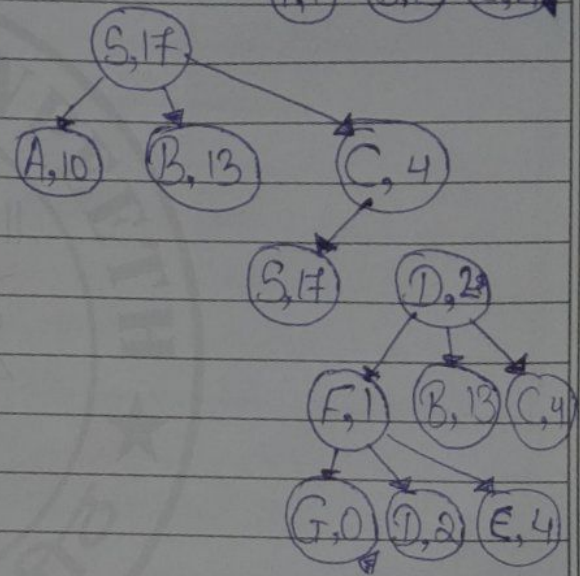
Step 4:

F-score of successor

$$f(D) = h(D) = 2$$

$$f(E) = h(E) = 4$$

$$f(G) = h(G) = 0$$

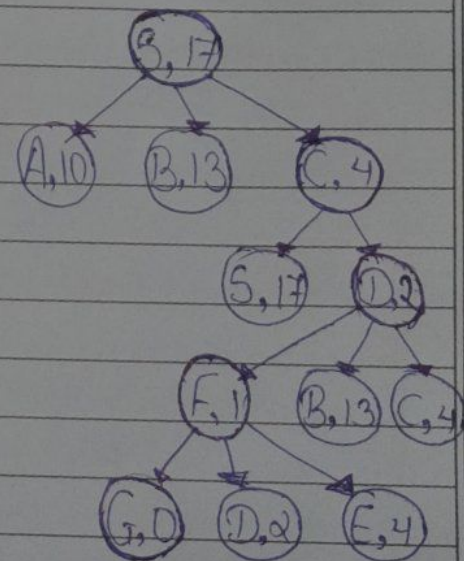


Step 5:

Solution is:

$S \rightarrow C \rightarrow D \rightarrow F \rightarrow G$ with

$$\text{Solution cost} = 10 + 6 + 6 + 3 = 25$$



Q2 Consider following instance of 8 puzzle problem.

8	7	6	-	8	7
2	1	5	2	1	6
3	4	-	3	4	5

Initial configuration

Goal configuration

Consider Heuristic functions defined below:

h_1 : Misplaced tiles count except space

h_2 : Correctly placed tiles count except space

h_3 : Sum of manhattan distance between current and correct position of all tiles except space.

a) In 8 puzzle problem we are concerned with getting to goal configuration within least number of steps. All moves are thus equally costly. Define $g(n)$ in your own words. What will be cost of 6 step solution to some arbitrary 8 puzzle instance?

→ The lowest path cost $g(n)$ can be the cost to reach the goal configuration in least steps: -

In our case, we can reach the final configuration in at least 4 moves: UP, ~~UP~~ DOWN, UP, UP, LEFT, LEFT

Since all moves are equally costly, we compute $g(n)$ as: -

$$g(n) = 1 + 1 + 1 + 1$$

$$g(n) = 4.$$

Consider the following arbitrary 8 puzzle instance which gives solution in 6 steps:

8	7	6
2	1	5
-	3	4

The solution can be represented as:-

$\{\{8, 7, 6\}, \{2, 1, 5\}, \{-, 3, 4\}\} \rightarrow \{\{8, 7, 6\}, \{2, 1, 5\}, \{3, -, 4\}\} \rightarrow$
 $\{\{8, 7, 6\}, \{2, 1, 5\}, \{3, 4, -\}\} \rightarrow \{\{8, 7, 6\}, \{2, 1, -\}, \{3, 4, 5\}\} \rightarrow$
 $\{\{8, 7, -\}, \{2, 1, 6\}, \{3, 4, 5\}\} \rightarrow \{\{8, -, 7\}, \{2, 1, 6\}, \{3, 4, 5\}\} \rightarrow$
 $\{\{-, 8, 7\}, \{2, 1, 6\}, \{3, 4, 5\}\}$

Since all the moves are equally costly, the cost would be.

$$g(n) = 6$$

[illegible]

8	7	6
2	1	5
3	4	-

Initial Configuration

LEF 7

UF

8	7	6
2	1	5
3	-	4

8	7	6
2	1	-
3	4	5

LEFT

VP

RIGHT

UP

LEFT

DOWN↑

8	7	6
2	1	5
-	3	4

8	7	6
2	-	5
3	1	4

8	7	6
2	1	5
3	4	-

8	7	-
2	1	6
3	4	5

8	7	6
2	-	1
3	4	5

8	7	6
2	1	5
3	4	-

LEFT

DOWN

8	-	7
2	1	6
3	4	5

8	7	6
2	1	-
3	4	5

LEFT

- DOWN

RIGHT

-	8	7
2	1	6
3	4	5

8	1	7
2	-	6
3	4	5

8	7	-
2	1	6
3	4	5

Final configuration

e)

→ For $i=1$, $n = \text{initial state}$

$h_1(\text{initial}) = \text{Misplaced tiles count except space}$

$$h_1(\text{initial}) = 4$$

$n = \text{goal state}$

$$h_1(\text{goal}) = 0$$

For $i=2$, $n = \text{initial state}$

$h_2(\text{initial}) = \text{Correctly replaced tiles count except space}$

$$h_2(\text{initial}) = 4$$

For $n = \text{goal state}$

$$h_2(\text{goal}) = 8$$

For $i=3$, $n = \text{initial state}$

$h_3(\text{initial}) = \text{Sum of translation manhattan distance between current \& correct position of all tiles except space.}$

$$h_3(\text{initial}) = 0 + 0 + 0 + 0 + 1 + 1 + 1 + 1 \\ = 4$$

For $n = \text{goal state}$

$$h_3(\text{goal}) = 0$$