







# A Tutorial Introduction to Maxima

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### **Outline**



#### Introduction

- Vectors
- Matrices and Linear Algebra

- Differential Calculus
- Taylor Series
- Symbolic Integration



(From the website) Maxima is a system for the manipulation of symbolic and numerical expressions, including differentiation, integration, Taylor series, Laplace transforms, ordinary differential equations, systems of linear equations, polynomials, sets, lists, vectors, matrices and tensors.



► Powerful Computer Algebra System (CAS) combining symbolic, numerical, and graphical capabilities



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- Cousin of the commercial Macsyma CAS (currently available without support)



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- ► Powerful Computer Algebra System (CAS) combining symbolic, numerical, and graphical capabilities
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- Cousin of the commercial Macsyma CAS (currently available without support)
- Completely Free and Open Source Software, written in LISP
- ▶ Fully customizable and extensible



#### maxima Native CLI

```
maxima 80x24

* ~ maxima

Maxima 5.37.2 http://maxima.sourceforge.net subme.meca
using Lisp GNU Common Lisp (GCL) GCL 2.6.12
Distributed under the GNU Public License. See the file COPYING. macscard.pdf
Dedicated to the memory of William Schelter.
The function bug report() provides bug reporting information.

(%i1) A:matrix([1,2,3],[2,3,1],[4,3,5]);

[1 2 3 ]
[2 3 1]
[3 ]
[4 3 5 ]
[4 3 5 ]

(%i2) gamma:alpha+beta;
(%o2)
Divers

Divers

Divers

Maxima 80x24

**The maxima 80x24

**The
```



maxima Native CLI xmaxima History:)



maxima Native CLI xmaxima History :) wxmaxima Wxwidgets



maxima Native CLI xmaxima History :) wxmaxima Wxwidgets imaxima Emacs!



maxima Native CLI xmaxima History:) wxmaxima Wxwidgets imaxima Emacs!

```
(%12) A:matrix([1,2,3],[2,3,1],[3,2,4]):
      gamma:alpha+beta:
(%01) 2 3 1
      3 2 4
(%o2) B+a
```

# Maxima Init File



- ▶ By default, the variable "maxima\_userdir" stores the user directory (in Linux it is /.maxima")
- You will have to create this directory and a file "maxima-init.mac" inside it
- ► Try adding "disp("Greetings!")\$" in the file and fire up maxima

# **Command Summary**



disp display string to stdout describe,? describe maxima command or variable apropos,?? inexact search for maxima command or variable

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#### **Basics**

**Plotting** 

Solving Equations

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# Symbolic Manipulations

# Some basics



- ► Statements terminated by a ";"
- Suppress output by terminating with a \$
- ► Variable assignment with ":"
- ► Function declaration with ":="
- ▶ Note: "=" is a symbol, not an operator!
- Lists indices go as 1,2,3,...
- "nouns" and "verbs"

# Some basics



– Maxima

$$diff(sin(x^2),x);$$

$$2x\cos x^2$$

$$\frac{e^{-x} \left( (e^{2x} - 1) \cos x + (e^{2x} + 1) \sin x \right)}{4}$$

# **Basic Arithmetic**



### **Handling literals**

— Maxima

- Maxima

$$expand((1/2+sqrt(2/3))^2);$$

$$\left(\frac{1}{2} + \frac{\sqrt{2}}{\sqrt{3}}\right)^2$$

$$\frac{\sqrt{2}}{\sqrt{3}} + \frac{11}{12}$$

### **Basic Arithmetic**



#### Handling literals

Maxima

```
expand((1/2+sqrt(2/3))^2), numer;
```

1.733163247594392

```
fpprec:20;
bfloat(expand(
  (1/2+sqrt(2/3))^2));
```

Maxima

1.7331632475943926994B0



# **Handling Symbolics**

– Maxima

$$(x+3*y+x^2*y)^3;$$

$$\left(x+3y+x^2y\right)^3$$

— Maxima

expand(
$$(x+3*y+x^2*y)^3$$
);

$$x^{6}y^{3} + 9x^{4}y^{3} + 27x^{2}y^{3} + 27y^{3} + 3x^{5}y^{2} + 18x^{3}y^{2} + 27xy^{2} + 3x^{4}y + 9x^{2}y + x^{3}$$



### **Handling Symbolics**

- Maxima expand(subst([x=5/y],

$$(x+3*y+x^2*y)^3);$$

— Maxima -

factor( $27*y^3+810*y+8100/y +2700/y^3$ );

$$27y^3 + 810y + \frac{8100}{y} + \frac{27000}{y^3}$$

$$\frac{27 \, (100 + 300 \, y^2 + 30 \, y^4 + y^6)}{y^3}$$



### **Handling Symbolics**

— Maxima

$$\left[y = -\sqrt{10}\,i, y = \sqrt{10}\,i\right]$$



### **Handling Symbolics**

— Maxima

$${\tt solve([x+y+z=4,y+z-2*x=5,z=4*x-3*y+t,t+y=z],[x,y,z,t]);}$$

$$\left[ \left[ x = -\frac{1}{3}, y = -\frac{1}{3}, z = \frac{14}{3}, t = 5 \right] \right]$$



# **Handling Symbolics**

$$sum(1/n^2,n,0,N);$$

$$\sum_{n=0}^{N} \frac{1}{n^2}$$

$$\frac{1}{13168189440000}$$

# **Commands Summary**



diff symbolic differentiation integrate symbolic integrations numer numerical result fpprec (variable) set floating point precision bfloat floating point representation expand expression factor factor expression subst substitute for variables solve solve system

### **Outline**



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#### Basics

# **Plotting**

Solving Equations

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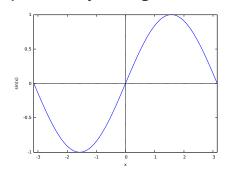
# Symbolic Manipulations

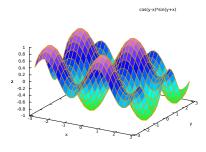


### **Explicit function plotting**

```
plot2d(sin(x),[x,-\%pi,\%pi]);
plot3d(sin(x+y)*cos(x-y),[x,-\%pi,\%pi],[y,-\%pi,\%pi])
```

### pointer: try adding "wx" as a prefix in wxmaxima



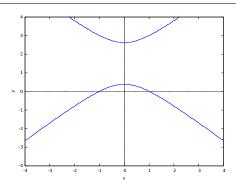




### Implicit plots

Maxima

```
load(implicit_plot);
implicit_plot(x^2=y^2-3*y+1,[x,-4,4],[y,-4,4],
[gnuplot preamble,"set\ zeroaxis"]);
```

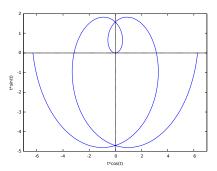




# parametric plots

Maxima

```
r(t):=t;
plot2d([parametric,r(t)*cos(t),r(t)*sin(t),
[t,-2*\%pi,2*\%pi],[nticks,80]],[x,-7,7]);
```





```
expr_1:cos(y)*(12.0+6*cos(x));

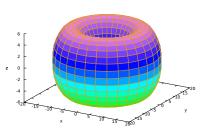
expr_2:sin(y)*(12.0+6*cos(x));

expr_3:6*sin(x);

plot3d([expr_1,expr_2,expr_3],

[x,0,2*\%pi],[y,0,2*\%pi],[gnuplot_pm3d,true]);
```

Parametric function

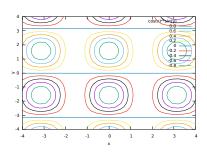




#### Misc

```
- Maxima
```

```
set_plot_option([gnuplot_preamble,"set\ cntrparam
levels\ 12"]);
contour_plot(sin(y)*cos(x)^2,[x,-4,4],[y,-4,4]);
```





#### Discontinuous function

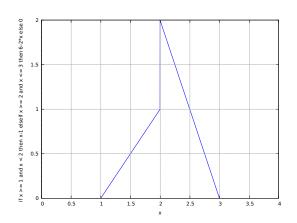
$$g(x) := \mathbf{if} \ x \ge 1 \land (x$$

$$< 2) \ \mathbf{then} \ x - 1 \ \mathbf{elseif} \ x$$

$$\ge 2 \land (x$$

$$\le 3) \ \mathbf{then} \ 6 - 2 x \ \mathbf{else} \ 0$$





# **Commands Summary**



```
plot2d 2d plots
    plot3d 3d plots
implicit_plot plotting implicit expressions
contour_plot contours
```

### **Outline**



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# **Plotting**

# Solving Equations

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# Symbolic Manipulations

# **Systems of equations**



Maxima

```
apropos("solve");
```

[baksolve, desolve, funcsolve, globalsolve, linsolve, linsolvewarn, linsolve\_by\_lu, linsolve\_params, solve, solvedecomposes, solveexplicit, solvefactors, solvenullwarn, solveradcan, solvetrigwarn, tmlinsolve]



#### linear systems

```
---- Maxima
```

```
eq1:x+y=8*a*x-z+4*5;\ eq2:y+z*\%pi=4*x;
eq3:x-y+z=4;
linsolve([eq1,eq2,eq3],[x,y,z]);
```

$$\[ x = -\frac{8 + 12\pi}{(4 + 4\pi) \ a - \pi - 4}, y = -\frac{32 + 8\pi + 16\pi a}{(4 + 4\pi) \ a - \pi - 4}, \\
z = \frac{16a - 40}{(4 + 4\pi) \ a - \pi - 4} \]$$



## Algebraic Equation (analytic solution)

--- Maxima

$$solve(a*x^2+b*x+c=0,x);$$

$$\[x = -\frac{b + \sqrt{b^2 - 4ac}}{2a}, x = \frac{\sqrt{b^2 - 4ac} - b}{2a}\]$$



#### Substitute values

— Maxima

```
sol:solve(a*x^2+b*x+c=0,x);
radcan(subst([a=1,b=2,c=3],sol[1]));
```

$$x = -\sqrt{2}i - 1$$



## System of algebraic equations

Maxima

$$f(x):=x^2-1;$$
  
solve([f(x/y)=0,f(x\*y)=0],[x,y]);

$$f(x) := x^2 - 1$$

$$\begin{split} & \left[ \left[ x = -1, y = 1 \right], \left[ x = 1, y = -1 \right], \left[ x = -i, y = -i \right], \left[ x = i, y = i \right], \left[ x = -i, y = i \right], \left[ x = i, y = -i \right], \left[ x = -1, y = -1 \right], \left[ x = 1, y = 1 \right] \right] \end{split}$$

Maxima



#### Polynomials & Numerical solutions

```
allroots(x^5+x^2-x+8=0);
```

Maxima

```
 \begin{aligned} [x &= 0.9189543576112322 \, i + 1.179427901164746, \\ x &= 1.179427901164746 - 0.9189543576112322 \, i, \\ x &= 1.427958893635229 \, i - 0.3522627040736663, \\ x &= -1.427958893635229 \, i - 0.3522627040736663, \\ x &= -1.65433039418216] \end{aligned}
```



## **Checking Solution**

— Maxima

```
f(x):=x^3+x^2-x+8 sol:allroots(f(x))$ expand(map(f,sol));
```

$$\begin{split} \left[x^3 + x^2 - x + 8 &= 4.440892098500626 \\ &\times 10^{-16} \, i + 1.77635683940025 \times 10^{-15}, \\ x^3 + x^2 - x + 8 &= 1.77635683940025 \times 10^{-15} \\ &- 4.440892098500626 \times 10^{-16} \, i, x^3 + x^2 - x + 8 = 0.0 \right] \end{split}$$



```
— Maxima
```

```
load(newton);
newton(x^7-5*x^6+4*x^4-
5*x^2+x+2,0);
```

#### – Maxima ·

$$-5.763042928902195_B \times 10^{-1}$$

$$8.194213634964119_B \times 10^{-1}$$

# **Commands Summary**



```
apropos apropos search
```

linsolve solve linear systems

solve solve algebraic equations

subst substitute values to expressions

allroots numerically estimate all roots of a polynomial

kill "kill(a,b,c);" lets you delete unwanted variables

map map the solutions to a function

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Symbolic Manipulations

#### Vectors



```
Maxima
```

```
load(vector);
functions;
```

```
[dimension (), type (arg), coordsystem (sys), cross(a,
 (b), grad (s), div (v), curl (a), laplacian (a), dotdel (v)
 b), christoffel (), curlgrad (s), graddiv (v), divcurl (v)]
```

## **Vectors**



Maxima

Maxima

$$\begin{aligned} & [y1\,z2 - y2\,z1, \\ & x2\,z1 - x1\,z2, x1\,y2 - x2\,y1] \end{aligned}$$

$$z1 z2 + y1 y2 + x1 x2$$



```
load(diag);
A:matrix([a,b,c],[d,e,f],[g,h,i]);
col(A,1);
row(A,2);
invert(A);
transpose(A);
determinant(A);
list_matrix_entries(A);
```

#### Row major!

Maxima

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#### **Matrix Products**

```
load(diag);
A:matrix([a,b,c],[d,e,f],[g,h,i]);
B:transpose(matrix([c,d,e]));
A.B;
A*A;
A^2;
A^2;
rank(A);
```



#### Matrix properties

Maxima

```
A: matrix([1,2],[4,5]);
eigenvectors(A);
```

$$\left[\left[\left[3-2\sqrt{3},2\sqrt{3}+3\right],\left[1,1\right]\right],\left[\left[\left[1,1-\sqrt{3}\right]\right],\left[\left[1,\sqrt{3}+1\right]\right]\right]\right]$$

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#### Other functionality

```
load(eigen);
load(linearalgebra);
```

# **Command Summary**



matrix create a matrix col access column of a matrix row access row of a matrix transpose transpose of a matrix determinant obtain the determinant of a matrix rank obtain the rank of a matrix invert invert a matrix list\_matrix\_entries list out the matrix in row major eigenvectors obtain the eigen vectors

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## Independant variable specified

— Maxim

$$diff(x^n,x,2);$$

$$(n-1) n x^{n-2}$$

# Unspecified independant variable

— Maxima

$$n x^{n-1} dx + x^n \log x dn$$



$$\frac{\partial}{\partial \mathbf{y}} \frac{\partial^2}{\partial \mathbf{x}^2} \left( \sin(x) \cos(y - x) \right)$$

Maxima

$$diff(sin(x)*cos(y-x),x,2,y,1);$$

$$2\sin x \sin (y-x) + 2\cos x \cos (y-x)$$

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— Maxima

```
declare(a,constant);
depends([x,y],t);
diff(x^2+a*y^2,t);
```

$$2\,a\,y\,\left(\frac{d\,y}{d\,t}\right) + 2\,x\,\left(\frac{d\,x}{d\,t}\right)$$

Try out "properties(a);" & "propvars(constant);"



Maxima

$$gp:diff(x^(2/3),x);$$
  
 $limit(gp,x,0,plus);$ 

— Maxima

$$\frac{2}{3x^{\frac{1}{3}}}$$

$$\infty$$

 $-\infty$ 

infinity



– Maxima

$$\mathrm{dydx}\left(\mathrm{expr},x,y\right) \,:= \frac{\mathrm{diff}\left(\mathrm{expr},x\right)}{\mathrm{diff}\left(\mathrm{expr},y\right)}$$

$$-\frac{x}{y}$$



— Maxima

taylor(
$$f(x),x,0,3$$
);

$$f(0) + \left(\frac{df(x)}{dx}\Big|_{x=0}\right) x + \frac{\left(\frac{d^2f(x)}{dx^2}\Big|_{x=0}\right) x^2}{2} + \frac{\left(\frac{d^3f(x)}{dx^3}\Big|_{x=0}\right) x^3}{6} + \cdots$$



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— Maxima

$$1 - \frac{x^2}{2} + \frac{x^4}{24} - \frac{x^6}{720} + \frac{x^8}{40320} - \frac{x^{10}}{3628800} + \cdots$$
$$x - \frac{x^3}{6} + \frac{x^5}{120} - \frac{x^7}{5040} + \frac{x^9}{362880} + \cdots$$



— Maxima

taylor(cos(x+y),[x,y],[0,0],[2,4]); factor(ratsimp(
$$\$$
));

$$1 - \frac{y^2 + 2yx + x^2}{2} + \frac{y^4 + 4y^3x + 6y^2x^2 + 4yx^3 + x^4}{24} + \cdots$$

$$\frac{24 - 12\,{x}^{2} + {x}^{4} - 24\,x\,y + 4\,{x}^{3}\,y - 12\,{y}^{2} + 6\,{x}^{2}\,{y}^{2} + 4\,x\,{y}^{3} + {y}^{4}}{24}$$

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Maxima

$$taylor(sin(x+y),[x,0,4],[y,0,4]);$$

$$y - \frac{y^3}{6} + \dots + \left(\frac{y^4}{24} - \frac{y^2}{2} + 1 + \dots\right) x + \left(\frac{y^3}{12} - \frac{y}{2} + \dots\right) x^2 + \left(-\frac{y^4}{144} + \frac{y^2}{12} - \frac{1}{6} + \dots\right) x^3 + \left(-\frac{y^3}{144} + \frac{y}{24} + \dots\right) x^4 + \dots$$



– Maxima

 $\int f(x) dx$ 

Maxima

$$\frac{\cos(3x) - 9\cos x}{12}$$



Maxima

– Maxima

$$integrate(x^2*exp(-x^2),x);$$

$$\frac{\sqrt{\pi}\operatorname{erf}(x)}{4} - \frac{x\,e^{-x^2}}{2}$$

0.2332527106719843



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Maxima

– Maxima

$$2 \int x \left(1+x^2\right)^3 dx$$

$$\int u^3 du$$



Maxima

ev(exprc, nouns);

— Maxima

$$\frac{u^4}{4}$$

$$\frac{(1+x^2)^4}{4}$$

# **Command Summary**



diff differentiate expression
grind "non-pretty" output
display2d set to true for pretty output
declare declare a symbol as constant
depends establish dependency
integrate integrate expression
changevar apply a change of variable

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## Symbolic Manipulations



#### factoring and expanding polynomials

$$factor(x^2+2*x+1);$$

$$(1+x)^2$$

$$x^2 + 2x + 1$$



#### **Trigonometric expressions**

— Maxima —

Maxima

1

$$\cos x \, \cos (3 \, y) - \sin x \, \sin (3 \, y)$$



#### Rational expressions

— Maxima

ratsimp(
$$(x^2+2*x+1)/(x+1)+1/(4*x+3)$$
);

- Maxima

$$\frac{4+7\,x+4\,x^2}{4\,x+3}$$

$$\frac{4x^2}{4x+3} + \frac{7x}{4x+3} + \frac{4}{4x+3}$$



#### **Complex exponentials**

demoivre:true;
exp(a+b\*\%i);

Maxima

- Maxima -

demoivre:false;
exp(a+b\*\%i);

$$e^a (i \sin b + \cos b)$$

 $e^{a+ib}$ 



### expand(expr,p,n);

expand(
$$(x+1)^5+(x+1)^(-5)$$
,5,3);

$$\frac{1}{x^5 + 5x^4 + 10x^3 + 10x^2 + 5x + 1} + (1+x)^5$$

$$\frac{1}{(1+x)^5} + x^5 + 5x^4 + 10x^3 + 10x^2 + 5x + 1$$



#### **Partial fractions**

— Maxima

$$partfrac(1/(x^2+3*x+2),x);$$

$$\frac{1}{x+1} - \frac{1}{x+2}$$



#### Expressions with logs, exponentials and radicals

Maxima

$$(\log\left(1+x\right))^{\frac{a}{2}}$$

$$e^{\frac{x}{2}} - 1$$



- Maxima

### Simplification with rules

Maxima

expr:sin(x^2+y^2)-sin(3\*x); eq1:x^2+y^2-x=0;

$$\sin\left(x^2 + y^2\right) - \sin\left(3\,x\right)$$

$$\sin x = y$$

$$y^2 + x^2 - x = 0$$

$$y - \sin(3x)$$

## **Command Summary**



- ratsimp simplify rational expressions
- ratexpand expand rational expressions
  - trigsimp converts all trigonometric quantities in terms of  $\sin$  and  $\cos$  terms
- trigreduce Reduces powers of trigonometric quantities to terms with highest power one
- trigexpand expand trigonometric terms in terms of  $\sin$  and  $\cos$ 
  - radcan simplify expressions with logs, exponentials and radicals

### What has NOT been covered



- Numerical Integration
- ▶ FFT
- ODEs
- Advanced plotting
- Orthonormal series and transforms
- Inequalities

# Setting up imaxima on emacs I

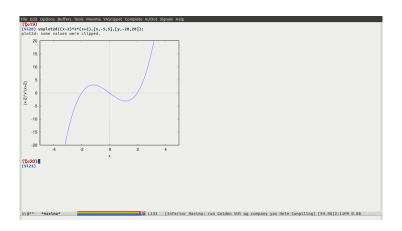


```
(add to list 'load path "/usr/share/maxima/5.37.2/emacs")
(autoload 'maxima mode "maxima" "Maxima⊔mode" t)
(autoload 'imaxima "imaxima"
        "Frontend, for maxima, with Image, support" t)
(autoload 'maxima "maxima" "Maxima; interaction "t)
(autoload 'imath mode "imath"
        "Imath, mode, for, math, formula, input" t)
(setq imaxima use maxima mode flag t)
(add to list 'auto mode alist '("\\.ma[cx]".
        maxima mode))
(setq imaximafntsize "Large")
(autoload 'emaximamode "emaxima" "Emaxima" t)
(add hook 'emaxima mode hook 'emaxima mark file as emaxima)
(setq emaximaabbreviationsallowed t)
```

# Setting up imaxima on emacs II



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# A quick example I



$$F_r = -\mu R L \left(\frac{L}{c}\right)^2 \left[ (\omega - 2\dot{\phi}) \frac{\epsilon^2}{(1 - \epsilon^2)^2} + \frac{\pi}{2} \frac{(1 + 2\epsilon^2)\dot{\epsilon}}{(1 - \epsilon^2)^{5/2}} \right]$$
$$F_t = \mu R L \left(\frac{L}{c}\right)^2 \left[ (\omega - 2\dot{\phi}) \frac{\pi}{4} \frac{\epsilon}{(1 - \epsilon^2)^{3/2}} + \frac{2\epsilon\dot{\epsilon}}{(1 - \epsilon^2)^2} \right]$$

```
depends ([e],t)$ ex:0.3*50.8e 6* cos(%pi/4)$ ey:0.3*50.8e 6* cos(%pi/4)$ exd:0.1* ex*omega$ eyd:0.1* ey*omega$ vals:[mu=0.00689,h[0]=50.8
```

vals:  $[mu=0.00689, h[0]=50.8e\ 6, L=12.7e\ 3, R=25.4e\ 3, diff(e[x],t)=exd, diff(e[y],t)=eyd, e[x]=ex, e[y]=ey, omega=10000*2*%pi/60]$$ 





```
epsilon: sqrt (e[x]**2+e[y]**2)/h[0]$
phi:atan2(e[x],e[y])$
Fr: mu*R*L*(L/h[0])**2*((omega 2* diff(phi,t))*
epsilon **2/(1 \text{ epsilon} **2) **2 + \%pi*(1+2*epsilon **2)*
diff(epsilon,t)/(2*(1 epsilon**2)**(5/2)))$
Ft:mu*R*L*(L/h[0])**2*((omega 2* diff(phi,t))*
\% pi*epsilon / (4*(1 \text{ epsilon} **2)**(3/2)) +
2*epsilon*diff(epsilon,t)/(1epsilon**2)**2)$
Fx:radcan(Fr*cos(phi) Ft*sin(phi))$
Fy:radcan(Fr*sin(phi)+Ft*cos(phi))$
FxFy: transpose (matrix ([Fx,Fy]))$
```

# A quick example III



```
float(subst(vals, FxFy));
float(subst(vals, diff(FxFy, e[x])));
float(subst(vals, diff(FxFy, e[y])));
float(subst(vals, diff(FxFy, diff(e[x], t))));
float(subst(vals, diff(FxFy, diff(e[y], t))));
```

## Thank You!



Questions?

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