

ENGR222 Assignment 1

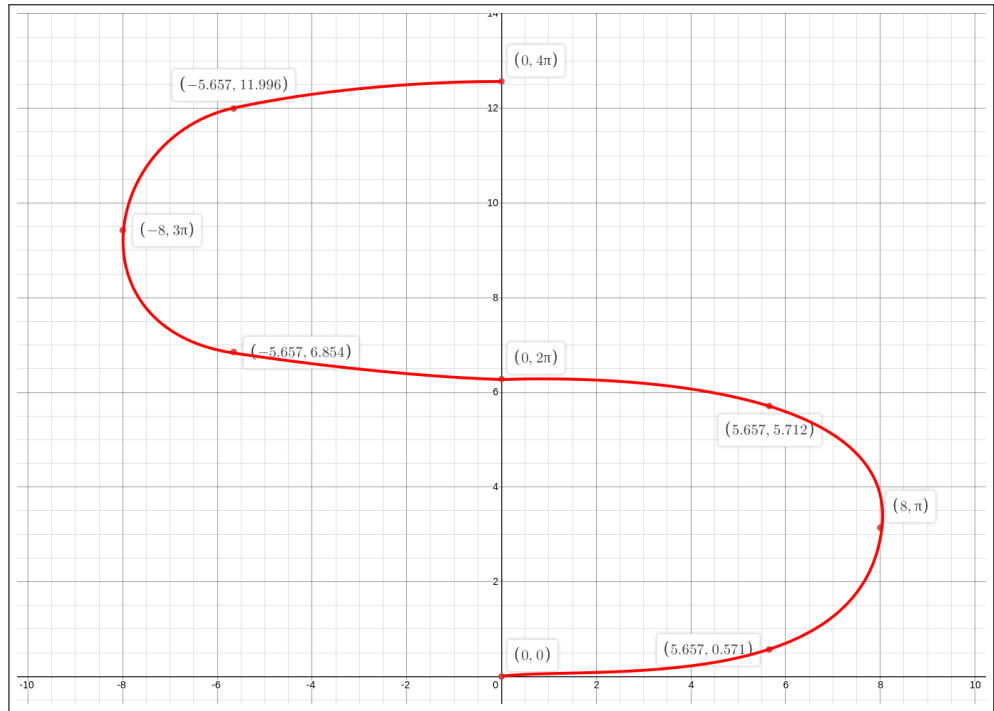
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1. Consider the parametric equation:

$$(x, y) = (8\sin(t), 2t - \sin(2t))$$

over the interval $0 \leq t \leq 2\pi$

- (a) Determine the location at $t = 0, \frac{\pi}{4}, \frac{\pi}{2}, \frac{3\pi}{4}, \pi, \frac{5\pi}{4}, \frac{3\pi}{2}, \frac{7\pi}{4}, 2\pi$ and use this to draw a rough sketch of the curve.



- (b) Find the unit tangent vector to the curve when $t = \frac{\pi}{6}$

$$(f'(t), g'(t)) = (8\cos(t), 2 - 2\cos(2t))$$

$$t = \frac{\pi}{6} : (f'(t), g'(t)) = (6.928203, 1)$$

Calculate the unit tangent vector:

$$\frac{(f'(t), g'(t))}{\|(f'(t), g'(t))\|} = \frac{(6.928203, 1)}{\sqrt{6.928203^2 + 1}} = \left(\frac{6.928203}{7}, \frac{1}{7} \right)$$

- (c) Determine an equation describing the tangent line at $t = \frac{\pi}{6}$

$$= (f(t), g(t)) + t \frac{(f'(t), g'(t))}{\|(f'(t), g'(t))\|}$$

$$= (4, 0.181) + t \cdot \left(\frac{6.928203}{7}, \frac{1}{7} \right)$$

$$= \left(\frac{6.928203 \cdot t}{7} + 4, \frac{t}{7} + 0.181 \right)$$

- (d) Determine an equation describing the normal line at $t = \frac{\pi}{6}$

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