

VICTORIA

UNIVERSITY OF WELLINGTON

TE WHARE WĀNANGA
O TE ŪPOKO O TE IKA A MĀUI



ENGR142 2018, 2nd Trimester

Lecturers: B. Ruck, F. Natali, and C. Hollitt

Assignment 3 Due date: 11:59 PM, Thursday 9th August, 2018

Problem 1: Cyclotron resonance

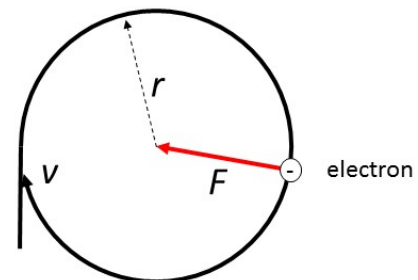
(5 Marks)

An electron moving at velocity $v = 10^6 \text{ ms}^{-1}$ enters a magnetic field of strength 2 Tesla which is directed perpendicular to the velocity. The magnetic field exerts a force on the electron which is perpendicular to the velocity, and also perpendicular to the field. This causes the electron to move in a circle, as shown below, where the magnetic field is directed into the page.

- (a) The strength of the magnetic force is given by $F = qvB$, where q is the electric charge, v the velocity, and B the magnetic field strength. Show that the orbit has radius given by

$$r = \frac{mv}{qB}, \quad (1)$$

and calculate the radius (use $q = -1.6 \times 10^{-19} \text{ C}$, $m = 9.1 \times 10^{-31} \text{ kg}$ and $B = -2 \text{ T}$ since the field is directed into the page).



- (b) The electron moves while the magnetic force is acting. Does the force do any work on the electron? Explain your answer, using only one short sentence.

Problem 2: Terminal velocity: numerical solution

(15 Marks)

Write some code (e.g., using Python) to calculate the position and velocity as a function of time for a hailstone falling under the force of gravity while experiencing a drag force $F_D = -\eta v^2$. Assume the initial velocity is zero, take the mass to be $5 \times 10^{-4} \text{ kg}$ and use $\eta = 2 \times 10^{-5} \text{ kg/m}$. Refer to the lecture notes for an example of how to construct your code (especially lectures 7 and 8).

Append your code to your submitted assignment, and provide plots of height versus time and velocity versus time. From your results answer the following questions.

- (a) How long does it take for the hailstone to come within 10% of its terminal velocity? Assume that the hailstone does not hit the ground first. **Note:** The value of the terminal velocity was calculated in assignment 2.
- (b) How far has the hailstone fallen when it comes within 10% of its terminal velocity?