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Self Tuning Buck Converter

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Bachelor of Engineering with Honours.

Abstract

Switch-mode power supplies are commonly used in a wide variety of consumer and professional appliances to transform DC voltages with high efficiency. One such switch-mode supply is the buck converter, which steps down a DC voltage. The current buck converter design process requires that a specific output filter be designed around the switching frequency of the converter, the required output voltage, and the desired inductor ripple. This filter design process often results in the selection of non-standards components that are difficult to purchase or manufacture, increasing costs and leading to design compromises. This project will implement a control system to actively control the inductor current ripple by modulating the switching frequency of the converter. This will allow engineers to design buck converters directly for the inductor current ripple they wish to tolerate, eliminating the issues of designing this output filter.

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Chapter 1: Introduction

Historically power distribution has been primarily in the form of AC (Alternating current). This is credited to the fact that AC power is more efficient to transmit over long distances and made it easy to step up and down the voltages efficiently with transformers [1]. However, with the invention of solid-state electronics such as the metal–oxide–semiconductor field-effect transistor or MOSFET for short, it has become possible to efficiently step up and step down direct current (DC) voltages. This has been achieved by the invention of the switch-mode power supply, which has facilitated the continued reduction of size and increase in efficiency of electronics [2].

Today, switch-mode power supplies can be found in a wide variety of consumer and professional electronics, with some examples being laptops, phones, and any form of DC charger. Their widespread usage when compared to other DC-DC converters such as linear regulators can be attributed to their far greater efficiency. One such switch-mode power supply is the buck converter, which will step down a DC input voltage to a lower DC output voltage.

1.1 Project Motivation

Although buck converters are a widespread technology, they are not without their limitations and drawbacks. The current buck converter design process requires that a specific output filter be designed around the switching frequency of the converter, and the desired inductor ripple. This filter design process will often result in the converter requiring discrete passive components that are non-standard and hard to source. This will usually result in the designer having to make compromises in their design for either the cost or the performance of the converter.

Another drawback of this design process is the static nature of both the filter and the switching components once they have been selected. This results in the buck converters desired inductor current ripple only being achieved at a very specific designed output voltage or load. This means that with current buck converter designs varying the desired output voltage or varying the output load will cause the inductor current ripple to vary. This is an issue, as very few loads are static and will not change during their operation.

1.2 Project Goals

This project aims to eliminate the need to design the output stage of a buck converter. By implementing a control system that varies the switching frequency of the converter, we will be able to directly manipulate the inductor current ripple. This project aims to produce a proof of concept buck converter that is capable of operating at 12V, with an output range of 3-10V and precision of $\pm 5\%$. The converter will also be able vary its switching frequency between 1kHz and 100kHz, allowing for selection of inductor current ripple between 20% and 50% with precision of $\pm 5\%$. All of this must be implemented while maintaining the standard functionality of the converter. For full system requirements please refer to ??.

TODO Expand on the project goals, possibly convert the previous section into a bulleted list of project goals and requirements.

This will be referenced in the implementation and design sections many times, so it needs to clearly outline what we are looking to achieve in this project.

Chapter 2: Background

A literature research was performed to inform design decision made in this project, and to evaluate any existing research. It will discuss buck converter design factors and topologies, as well as the various different methods of PWM generation. In performing this literature research, we searched Google Scholar, Engineering Village, and Te Waharoa to find designs that utilised variable frequency PWM.

These searches returned no research relevant to the designs of this project, with the only related work focusing on the electromagnetic noise reduction using randomised frequency modulation [3, 4]. Because of this, research was instead performed to inform the design of the buck converter and the generation of PWM signals.

2.1 Pulse Width Modulated Signal Generation

Pulse width modulation (PWM) is a digital signal generation technique shown in Figure 2.1a, in which the Period T of the signal is held constant, while the ratio of its logic high period T_{on} to logic low period T_{off} is modulated. This ratio of high period to the low period is referred to as the duty cycle of the PWM signal and is often expressed as a percentage, this can be seen in Figure 2.1b.

PWM signals are used in a wide variety of applications for both digital and analogue electronics. PWM is often used to generate analogue signals from digital components by varying the average voltage of the digital PWM signal over time [5]. PWM is also used to control the switching elements contained within switch mode power supplies using this same principle, as discussed in Section 2.2. With regard to this project, we will be looking to generate a PWM signal that can be modulated in both duty cycle and frequency.

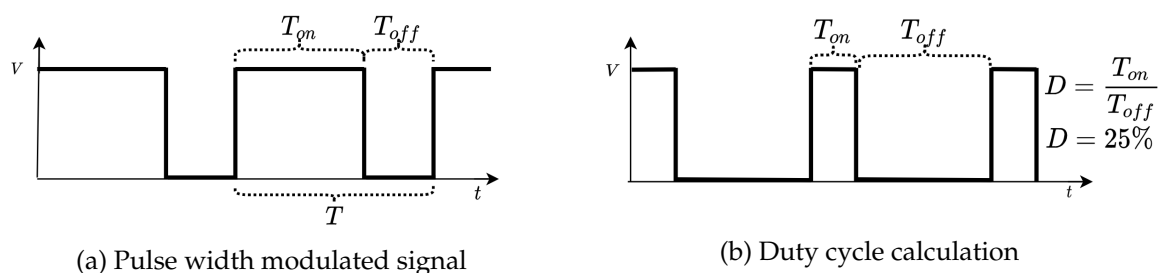


Figure 2.1: Pulse width modulated signal characteristics

2.1.1 Analogue PWM Signal Generation

Designing a PWM signal generator using analogue components has three distinct stages required to generate the signal. These stages can be seen in Figure 2.2, and include clock

generation, triangle wave generation, and signal comparator stages [6].

The clock generation stage generates a square wave clock signal at a set frequency. This is usually done using a quartz crystal oscillator, or another form of resonating oscillator circuit. The triangle wave generating state must take the clock signal from the previous stage, and produce a triangle wave of the same frequency. This stage is most often done using a standard op-amp integrating circuit with unity gain at the resonating frequency of the clock source. The final signal comparator stage will convert this triangle wave into a PWM signal. Using a comparator, a reference voltage can be applied to the non-inverting input, and then the triangle wave can be applied to the inverting input. This will produce a pulse train with the same frequency as the clock source, where the period of T_{on} and T_{off} is set by the reference voltage.

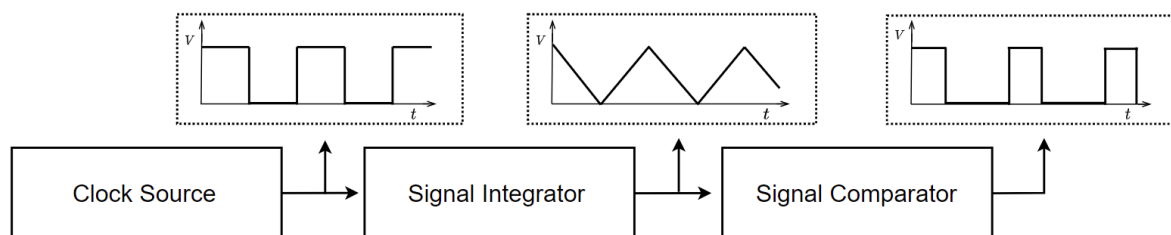


Figure 2.2: Stages of analogue PWM generation

2.1.2 Digital PWM Signal Generation

Designing a PWM signal generator with digital components is far simpler than the method described in Section 2.1.1, and can be done using either a microcontroller or a Field Programmable Gate Array (FPGA). By using an internal timer that is continually incrementing at a known period we can set a period for our PWM. Then by toggling a digital I/O when a compare variable is equal to the value of the timer, we are able to generate a PWM signal with a variable duty cycle [7]. This can be achieved on most microcontrollers, however the maximum frequency and duty cycle accuracy will be dependant on individual clock speed and internal register sizes.

2.2 Buck Converters

The buck converters is a variant of a switch mode power supply that steps down a DC input voltage to a DC output voltage. They are commonly used in a wide variety of consumer and professional appliances such as laptops, phones, and chargers due to their high efficiency compared to other DC-to-DC step down converters such as linear regulators [8].

The basic operational components of a buck converter can be seen below in Figure 2.3. From this we see that a buck converter has three main elements, the input voltage source, two switching components, and an output filter across the load. In the case of Figure 2.3, the first switching component is an actively controlled switch such as a MOSFET or transistor, and the second a passive switching diode. This configuration of an active and a passive switch is known as the non-synchronous buck converter topology, if the passive diode were to be replaced with a second active switch the topology would be considered synchronous. Although both topologies function under the same fundamental principles, the non-synchronous topology is easier to implement with the drawback of higher losses and

therefore lower efficiency.

It can also be seen from Figure 2.3 that a buck converter has two operating states that are controlled through the activation of these switching components. By toggling these switching components at high speed through the use of PWM, we can control the current flowing through the inductor of the output filter. By controlling this current we are also able to directly control the current through, and voltage across the output load of the converter. Using this, buck converters will often have a feedback control system in their design to be able to actively control and regulate the output voltage during usage. This controller will vary the duty cycle of the the switching PWM signal, thereby varying the output voltage of the buck converter as shown in Equation (2.1).

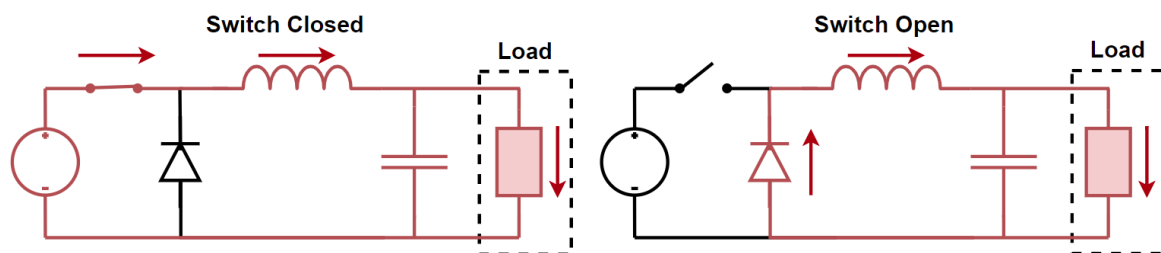


Figure 2.3: Operating states of a buck converter

2.2.1 Buck Converter Design

The design of a common buck converter has two primary considerations, the output voltage of the converter V_o , and the inductor current ripple of the converter Δi_L . These considerations can be specified by designing the buck converter using Equation (2.1) & Equation (2.2) [9, 10].

When designing a buck converter the first design specification that must be met is the output voltage. In Equation (2.1) the output voltage can be directly related to the input voltage V_{in} and the switching duty cycle D . Using this equation it is possible to directly set the output voltage of the buck converter by varying this duty cycle.

$$V_o = D \cdot V_{in} \quad (2.1)$$

Once the output voltage has been specified, the inductor current ripple can be calculated and specified with Equation (2.2). This equation allows for the inductor current ripple to be directly related to the inductor size L , and the PWM switching frequency f_s . This allows the the specification of the inductor current ripple through the varying of these two values.

$$\Delta i_L = \frac{V_o \cdot (1 - D)}{L \cdot f_s} \quad (2.2)$$

These two equations will be used to inform the designs and specifications of this project, and will be discussed in detail in Section 3.1.

2.3 Current Sensing

Discuss the varying methods of current sensing that are available, and what each of their advantages and disadvantages are.

2.3.1 Hall Effect Sensors

brief overview of hall effect sensors. They function by measuring the magnetic flux density, meaning that they are commonly used to sense the presence of a magnet. However since a current flowing through a wire will produce a magnetic flux, they can also be used to measure current flow.

Because of this operation, they are able to sense a current without contacting or altering the circuit. This means that they are commonly used in the measurement of high voltage or high current circuits, as they will remain completely isolated from the circuit being sensed, and will also not dissipate power from the sensed circuit. This provides large safety advantages, and can often decrease the complexity of the sensing circuit.

Hall effect sensors do however suffer from a lack of precision. Due to their operation, their measurements will constantly be offset by any ambient magnetic flux. This means that they are not commonly used for the sensing of small signal currents, as the noise floor of the Earth's own magnetic field can often be larger than the signal being sensed.

2.3.2 Current Sense Amplification

Current sense amplification works on the basic principle of Ohm's law $I = \frac{V}{R}$. By sensing the voltage dropped across a known value resistive element (Often called the current shunt), it is possible to calculate the current that is flowing through the element. This form of current sensing is very simple to implement in theory, however it has the effect of altering the system being sensed by adding a resistive load, and thereby increasing the losses of the system.

To mitigate the effects of this sensing on a circuit, a smaller resistive load can be used. However, this will also decrease the measurable voltage across the load, and therefore decrease the precision of a taken measurement. Because of this, shunt based current sensors are often paired with an operational amplifier known gain. This combination allows for accurate amplification of the shunt voltage drop, increasing the precision of the measurement, and allowing for drastically smaller shunt resistors.

2.4 Control Systems

Discuss the basics of control theory, and how a controller can be implemented on a digital system within discrete time.

- Discuss in very general terms what a control system is what it seeks to do in a system.
- Discuss what the control system will be doing in the case of this project. Talk about how a controller will be used to control both the output voltage of the converter, and the inductor ripple of the converter.
- Discuss the design, use, and implementation of a PID controller within a system.

2.4.1 PID Controllers

Chapter 3: Design

The design processes outlined within this report will draw heavily on the background research discussed in Chapter 2. These designs aim to effectively implement the outlined system requirements in a robust and repeatable manner.

3.1 Defining & Justifying System Specifications

Based on the system requirements that have been outlined in Chapter 1, a set of system specifications can be created to inform our design decisions.

It has been specified that the final system design will be able to select for both the output load voltage, and the inductor current ripple of the buck converter. From this requirement we can identify that two separate control systems should be designed, one to regulate the output voltage of the converter, and one to regulate the inductor current ripple.

Next we can identify that to control the output load voltage and the inductor current ripple, we must be able to actively effect their current state. Based on Equation (2.1) we can see that by varying the duty cycle of the converters PWM signal, we are able to directly control the output voltage. Similarly, from Equation (2.2) we can see that by varying the converters PWM switching frequency we are able to directly control the inductor current ripple. From this we can specify that our designs of the PWM generation must be capable of varying both the duty cycle and the switching frequency of the output PWM signal independently and simultaneously.

The outlined requirements also specify the level of precision that will be required from the output load voltage and the inductor current ripple. This allows us to specify the tolerable error for the system design, and calculate the minimum required system specifications. Based on the buck converter design equations from Section 2.2.1, The following specifications have been identified:

- Maximum allowable duty cycle step size

$$V_{error} = V_{min} \cdot error = 0.15V \quad (3.1)$$

$$D_{step} = \frac{V_{error}}{V_{in}} = 0.0125 \quad (3.2)$$

$$N_{step} = \frac{1}{D_{step}} = 80 \quad (3.3)$$

- Maximum & minimum inductor sizes

$$L_{max} = \frac{V_{max} \cdot (1 - D_{max})}{f_{min} \cdot I_{min}} = 27.7mH \quad (3.4)$$

$$L_{min} = \frac{\frac{V_{in}}{2} \cdot (1 - 0.5)}{f_{max} \cdot I_{min}} = 0.5mH \quad (3.5)$$

- Maximum allowable frequency step size

$$f_{step} = \frac{V_{max} \cdot (1 - D_{max})}{(I_{min} - I_{Error}) \cdot L_{max}} - f_{min} = 52Hz \quad (3.6)$$

$$N_{steps} = \frac{(f_{max} - f_{min})}{f_{step}} = 1881 \quad (3.7)$$

The derivation of these values can be found in Appendix A.

TODO Refactor this to be a list of specifications

From these equations we can build a list of final specifications to inform the design of our PWM generator and buck converter. The PWM generator must provide a minimum voltage step size of 0.0125V, for a resolution of 80 voltage steps between 3V and 10V. The PWM generator must also be able to provide a minimum frequency step size of 52Hz, for a resolution of 1881 frequency steps between 1kHz & 100kHz. Finally we can also specify that the buck converter must be capable of functioning with inductor values between 0.5mH & 27.7mH.

By designing the PWM generator and the buck converter to these specifications, we are able to guarantee that we can always achieve the requirements outlined in Chapter 1.

TODO Discuss the minimum and maximum sense current, along with the bandwidth requirement of the sensors

Design the system specifications around the current sensing and voltage sensing. What is the required bandwidth of the sensor? What is the required precision?

3.2 System Architecture & Design

To achieve the specifications that have been outlined in Section 3.1, it is important to design the system architecture around them. In Figure 3.1 an overview of the system architecture can be seen, with three main design sections outlined. These sections each represent a significant segment of work that must be completed for the final artefact of this project to be achieved.

The first section of work that must be completed is the design of the PWM generation, denoted 1 in Figure 3.1. This PWM generator will be used to control both the output voltage and the inductor current ripple, and as such must be able to modulate both the duty cycle and the frequency of the PWM to the precisions required.

The second section of work is the design of the sensing elements required by the system, denoted 2 in Figure 3.1. These elements will be used to measure both the output voltage and the inductor current ripple, and therefore must be able to achieve the required precisions and sampling rates.

Finally the third section of work is the design and implementation of the two control systems, denoted 3 in Figure 3.1. These control systems will be responsible for maintaining the desired output voltage and inductor current ripple of the buck converter. This system will therefore be responsible for facilitating the final functionality of the project, combining sections 1 & 2.

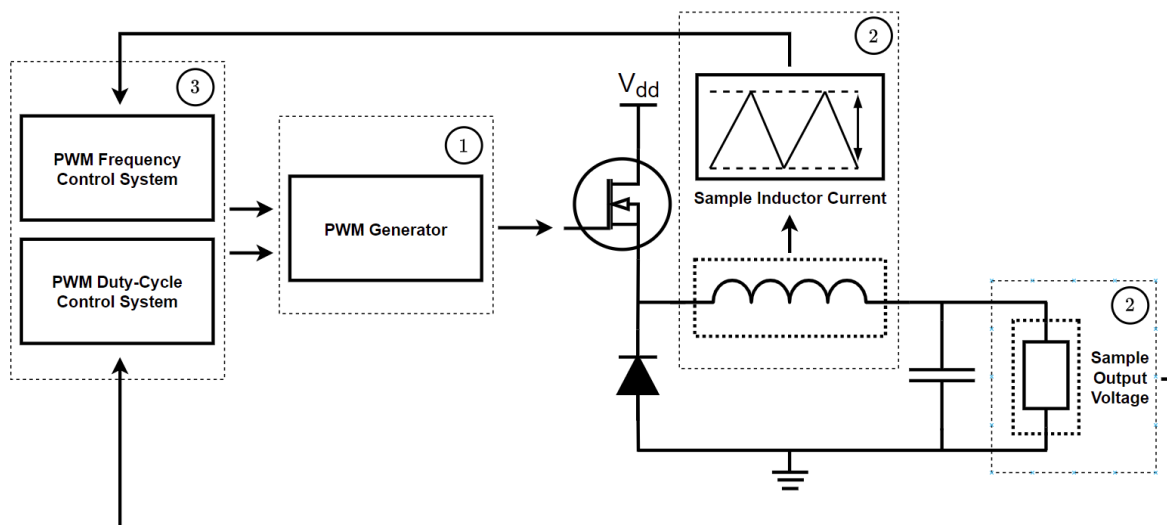


Figure 3.1: High level system overview

3.3 PWM Generation

In the design of the PWM generator, both the analogue and digital designs discussed in Section 2.1 were considered, designed, and tested for. Each of these designs presented pros and cons that would affect the overall design of the system architecture. This section will discuss these designs and finalise the design of the PWM generator for this system.

3.3.1 Analogue PWM Generator Design

As discussed in Section 2.1.1, the design of the analogue PWM signal generator requires three stages, each of which will have its own design requirements based on the specifications outlined in Section 3.1.

The clock generation stage will be responsible for setting the frequency of the final PWM signal. This specifies that the clock source have a variable frequency output range between 1kHz and 100kHz , with a minimum step size of 52Hz . Research was done on a variety of clock sources, looking at voltage-controlled oscillators (VCO's), signal generator IC's, and even the basic 555 timer. From this VCO's were identified to operate at much higher frequencies than those used in this project. It was also identified that signal generator IC's

often require selections of passive components to operate effectively, increasing their complexity. For this reason the variable frequency 555 timer circuit was selected, as it provided the required specifications.

The next section designed was the signal integrator stage. This stage consisted of a basic op-amp integrator circuit, with a design requirement that it be able to integrate the clock signal across the frequency range required. This circuit was designed and implemented in an LTSpice simulation to evaluate its performance, and can be seen in Appendix B. From this simulation it was noted that the integrator's frequency response was similar to that of a first order low pass filter, and greatly attenuated the integrated signal. For this reason it was decided that analogue PWM generation would not be implemented in this system, as it presented many issues.

TODO insert images of the designed integrator circuit, and its frequency response (bode plot)

3.3.2 Digital PWM Generator Design

As discussed in Section 2.1.2, The design of the digital PWM generator is far simpler than that of the analogue, and can be implemented in a wide variety of methods. In this project microcontrollers and FPGA's have been considered.

Based solely on the capabilities of the platform, the PWM generator would be best designed and implemented on an FPGA as it would allow for superior speed and precision. However FGPA design brings a lot of difficulties, primarily in the prototyping and testing stages. Because of this, due to the limited time from of this project, we have decided to implement this PWM design using a microcontroller.

The selection of the microcontroller is highly dependant on the clock frequency and design of the PWM peripherals, as it must be capable of achieving the specifications outlined in Section 3.1. A large selection of microcontroller data-sheets were reviewed to identify their specifications, including AVR, STM8, Espressif, and teensy based microcontrollers. From this review it was decided that the ESP32 microcontroller would be best suited to this project [11]. This microcontroller is capable of outputting a maximum PWM frequency $125kHz$ with a duty cycle resolution of 9 bits (512 voltage steps). From here a short C program was written to test the PWM functionality of the ESP32, and it was confirmed that it met the required specifications. The source code and images of this PWM signal can be found in Appendix C.

3.4 Inductor Current Ripple Sensing

Discuss the purpose of this sensors, and the requirements of the sensing system in regards to its range, precision, and bandwidth. Also discuss the required outputs of the sensor (we need to detects the current peak value, and the mean current).

3.4.1 Current Sensor Selection

Talk about how hall effect sensors were identified to not be suitable for this design due to the reasons outlined in Section 2.3.1. From here the discuss the selection of a current sense amplifier (its gain, bandwidth, and precision), and then the selection and design of the shunt resistor. Then discuss the expected voltage output of this current and the expected waveform.

Based on the specifications outlined in Section 3.1, it can be identified that directly sampling the output waveform from this sensors is not feasible due to its large possible bandwidth.

From there then discuss the design of varying analog circuits to attempt to identify the peak current and mean current.

I want to show circuit designs, and simulations for both the precision rectifier peak detection design, and the capture and hold peak detection design.

3.4.2 Precision Rectifier Peak Voltage Detection

Design, and simulations of the Precision Rectifier Peak Voltage Detection.

3.4.3 Sample and Hold Peak Voltage Detection

Design, and simulations of the Sample and Hold Peak Voltage Detection.

3.4.4 Current sensing digitisation

Discuss the selection of the ADC for measuring the peak ripple and mean ripple currents. Talk about the minimum required ADC precision, and bandwidth requirements.

3.5 Control System

The control system designs will inform the selection of the sensors used within the system design. This section will cover the selection of the controller topology (PI & PID), some basic modelling of the system, and then the selection of the sensors required to generate the correct feedback signals.

3.5.1 Output Load Voltage Controller

3.5.2 Inductor Current Ripple Controller

Chapter 4: Implementation

4.1 PWM Generation

TODO Gate driving and Bootstrapping

Discuss how the micro will be unable to directly drive the gate of the switching MOSFET, as it's $V_{GS_{on}}$ will be too large. Because of this a gate driver will need to be selected. The driver will need to be driven using the 3.3V logic from the ESP32, and will need timings fast enough to function correctly at 100kHz. I can also discuss how during the lock-down I was unable to purchase a gate driver, and so I built a bootstrapping circuit from components I located around the house.

4.2 Inductor Current Ripple Sensor

4.3 Control System

Chapter 5: Evaluation

The evaluation of the system will be conducted using a range of load resistances, evaluating its performance with 10Ω , 15Ω , and 20Ω output loads, using a constant supply voltage of 12V DC. S

- The buck converter will be able to take input voltages up to 12V DC
- The buck converter must maintain the basic functionality outlined in eq. (2.1)
- The buck converter will have an output voltage range between 3V and 10V DC
- The output voltage accuracy will be within $\pm 5\%$ of the target output voltage
- The user will be able to define the inductor ripple between 20% and 50%
- The inductor ripple accuracy will be within $\pm 5\%$ of the defined inductor ripple
- The buck converter will have a switching frequency range of 1kHz to 100kHz
- The control system will have no steady state error

5.1 PWM Generation

5.2 Inductor Current Ripple Sensor

5.3 Control System

Chapter 6: Conclusions

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Acknowledgments

Thank you Danny B for being great :-)

Thank you ECS Techs for putting up with my questions

And thank you to my wonderful girlfriend for not kicking me out when I was working on this stupid fucking project really late

Appendix A: System Specification Derivation Equations

The system specification derivation equations have been input into the graphing platform Desmos.com. This has allowed me to visually inspect these equations and form conclusions. The full working and step by step derivation is also available on Desmos.com using the following links.

Duty cycle equation derivation:

<https://www.desmos.com/calculator/8c7wmbyzw4>

Inductor sizing equation derivation:

<https://www.desmos.com/calculator/v7ntrescw5>

PWM frequency equation derivation:

<https://www.desmos.com/calculator/ekjhcrt9zg>

Appendix B: Analogue PWM Generation

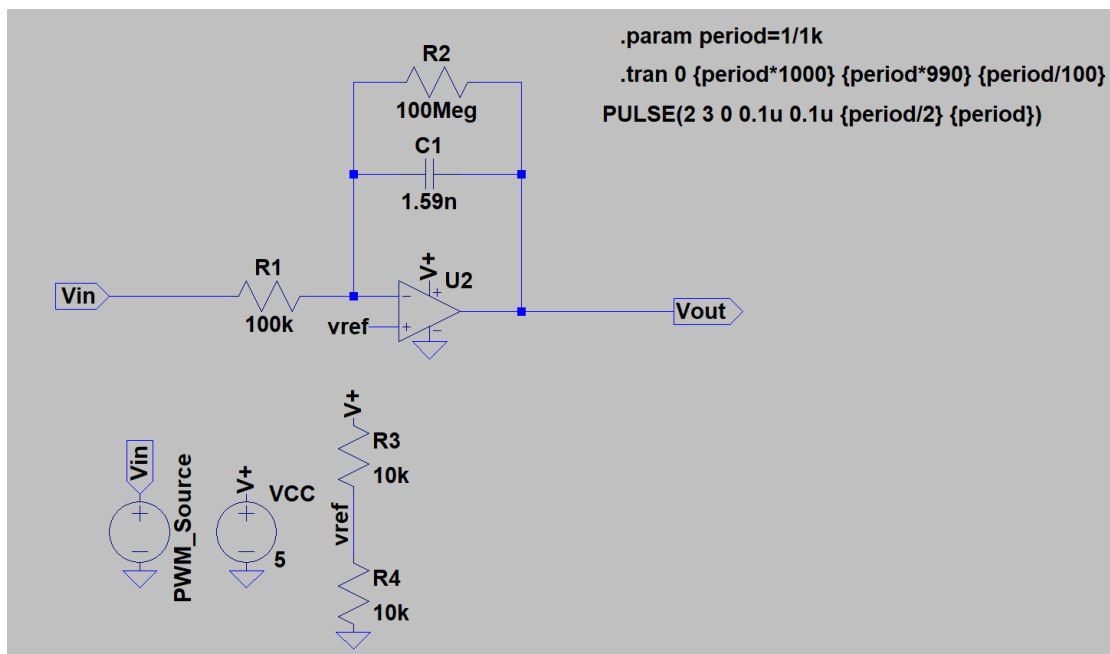


Figure B.1: Analogue PWM LTSpice circuit

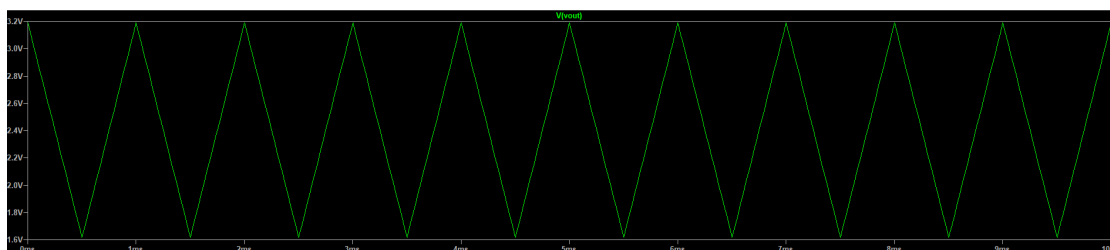


Figure B.2: Analogue PWM LTSpice simulation 1kHz

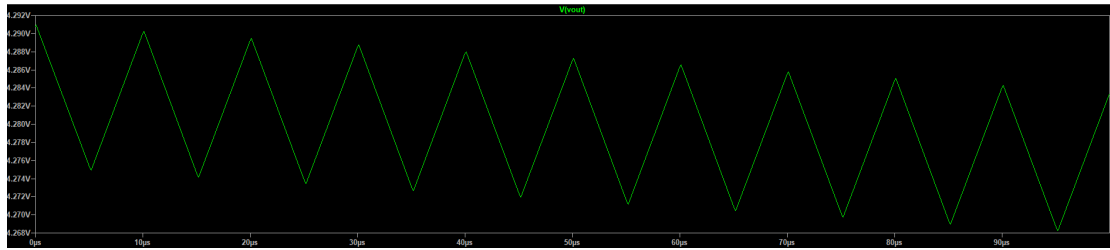
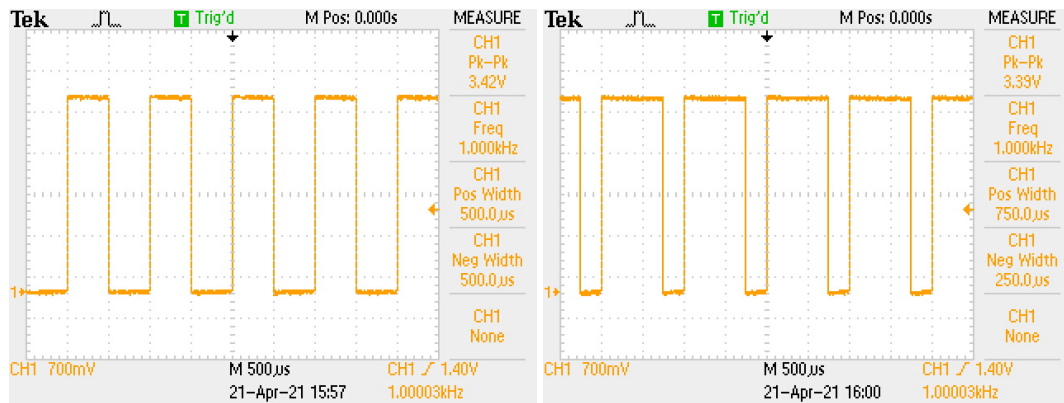


Figure B.3: Analogue PWM LTSpice simulation 100kHz

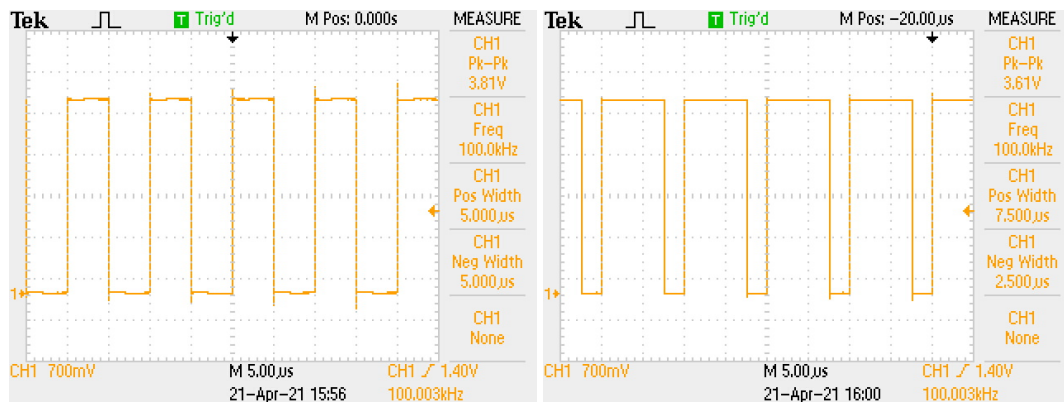
Appendix C: Digital PWM Generation

C.1 Digital PWM Generation Figures



(a) Digital PWM Generation at 1kHz and a 50% duty cycle (b) Digital PWM Generation at 1kHz and a 75% duty cycle

Figure C.1: Digital PWM Generation at 1kHz



(a) Digital PWM Generation at 100kHz and a 50% duty cycle (b) Digital PWM Generation at 100kHz and a 75% duty cycle

Figure C.2: Digital PWM Generation at 100kHz

C.2 Digital PWM Generation Code

```
1 #include "buck_converter.h"
2
3 void app_main()
4 {
5
6     init_buck();
7
8     // Declare task handles
9     TaskHandle_t VO_controller = NULL;
10
11     QueueHandle_t target_voltage_queue;
12
13     // initialise the queues
14     target_voltage_queue = xQueueCreate(5, sizeof(float));
15
16     // Create the output voltage control task
17     xTaskCreatePinnedToCore(control_loop, //
18         Voltage control loop function
19         "Vout_controller", // Task
20         2048, // Task
21         stack size
22         (void *)&target_voltage_queue, //
23         Function parameters
24         2, //
25         Priority of the task (app_main has
26         priority 1)
27         &VO_controller, // Task
28         handle
29         tskNO_AFFINITY); // Core
30     // the task has been pinned to (No
31     // core selected)
32
33     float input_voltage;
34     char input_buffer[20] = {0};
35     uint8_t buf_index = 0;
36
37     while (true)
38     {
39         char input = fgetc(stdin);
40
41         if (input != 0xFF)
42         {
43             input_buffer[buf_index++] = input; // read in the
44             // character, and increment the index
45             fputc(input, stdout); //echo the
46             // character back
47         }
48     }
49 }
```

```

38         if ((input_buffer[buf_index - 1] == '\n'))
39         {
40
41             input_voltage = strtod(input_buffer, NULL);
42
43             xQueueSend(target_voltage_queue, (void
44                 *)&input_voltage, (TickType_t)1);
45
46             printf("\nInput Target Voltage: %f\n",
47                 strtod(input_buffer, NULL));
48             buf_index = 0;
49         }
50     }
51     vTaskDelay(1);
52
53     // printf("task stack unused: %d\n\n",
54         uxTaskGetStackHighWaterMark(VO_controller));
55     // vTaskDelay(100);
56 }
57 }

```

code/main.c