

2020-09-11/MS

Signal Processing, lecture -2

Topics:

- Chebyshev filters
- Brief comparison of Butterworth and Chebyshev filters
- Other filter types
- Impact of group delay variations (examples)

Literature:

Kendall Su: "Analog Filters", Kluwer Academic Publishers, 2nd ed. 2002, ISBN 1-4020-7033-0
The book is available in electronic form at <http://www.en.aub.aau.dk>.

| Topic | Pages ({*} ⇔ supplementary lit.) |
|-----------------------------|-------------------------------------|
| Filter design | 7-20 (partly repetition) |
| Chebyshev characteristic | 30-36 |
| Chebyshev transfer function | 58-62 |
| Filter tables | {App. A} |

Supplementary: Lecture presentation "slides"

Exercises:

2.1

A Chebyshev prototype filter is (usually) normalized to a ripple bandwidth of 1 rad/s.

a. Show that the 3 dB bandwidth can be found as:

$$\omega_{3dB} = \cosh\left(\frac{1}{n} \cosh^{-1} \frac{1}{\varepsilon}\right)$$

Hints:

$$\varepsilon^2 C_n^2(\omega_{3dB}) = 1 \quad \text{and}$$

$$C_n(\omega) = \cosh(n \cdot \cosh^{-1} \omega) \quad \text{for } \omega > 1$$

b. Find the 3-dB bandwidth for a 4th order filter with a 0.5 dB ripple bandwidth of 1 rad/s.

2.2

The requirements for a Chebyshev low-pass filter are:

- Passband ripple: 0.5 dB
 - Ripple bandwidth: 20 kHz
 - The attenuation at 190 kHz shall be at least 30 dB
- a. Find the frequency scaling factor, k_f , and the necessary filter order.
 - b. Find (analytically) the actual attenuation at 190 kHz
 - c. Compare the results with Exercise 1.2
 - d. Find (analytically) the poles of the prototype filter.
 - e. Check the results of d. with Matlab

- f. Use Matlab to plot the transfer function (1 kHz - 1 MHz) and the group delay together with the filter from Exercise 1.2. Note that the frequency scaling factors, k_f , are different for the two filters. Hints: There are many ways to do this. A possible way is shown in Exerc2_2_template.m

where $H_{Scaled}(j2\pi f) = H_{Norm}(j\omega_{Norm})$ and $\omega_{Norm} = \frac{2\pi f}{k_f}$.

2.3

A low-pass prototype filter has the transfer function shown.

$$H_{LPP}(s) = \frac{0.423}{(s + 0.446)(s^2 + 0.446s + 0.949)}$$

- Find the location of the poles.
- Determine which types of filter it is (and explain your conclusion):
 - Butterworth?
 - Chebyshev?

Results:**2.1**

- a.
- b. 1.093 rad/s

2.2

-

- a. $125664, 2$
- b. 35.95 dB
- c.
- d. $-0.713 \pm j1.004$
- e.
- f.

2.3

- a. $-0.446 + j0; -0.223 \pm j0.948$
- b.