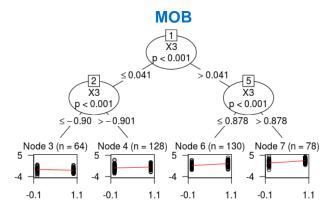


Subgroup Benchmarking Framework

Sophie Sun, AEA/AMDS Björn Bornkamp, SMC/AMDS Yao Chen, SMC/AMDS Jiarui Lu, SMC/AMDS Kostas Sechidis, AEA/AMDS

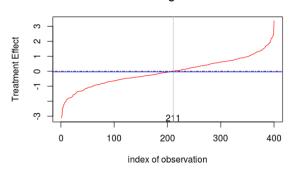


Motivation

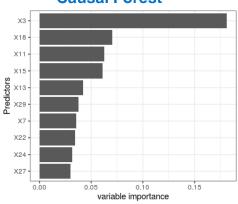


FindIt

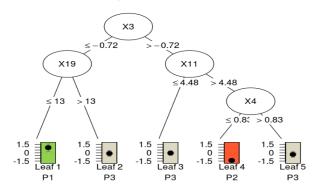
Causal Moderation: Heterogeneous Treatment Effect



Causal Forest



Quint



Challenge

- There has been review work to compare subgroup methods (Lipkovich et al. 2017, Huber et al. 2019, Zhang et al. 2018, Loh et al. 2019)
- Data: simulation data is not a good representation of the real clinical data
 - Mostly use variables generated from parametric distribution with simple dependent/ independent covariates distributions (Lipkovich et al. 2017, Huber et al. 2019, Zhang et al. 2018)
 - Large subgroup effects (Loh et al.2019)
- Methodology:
 - Only consider certain type of response (Loh et al. 2019, Huber et al. 2019)
 - Might tend to consider cases and metrics favoring the proposed methods
- Objective: Build objective & realistic benchmarking framework and considers metrics of practical importance, provide guidelines for subgroup analysis

Data generation: Prognostic and predictive structure

Generate data from: $f(X) = f_{prog}(X) + Trt * (\beta_0 + \beta_1 * f_{pred}(X))$

- Benchtm (go/benchtm) provides two covariate distributions:
 - 1. Synthetic data generated from a real clinical trials
 - Generated from real clinical trial data using "synthpop"
 - To ensure anonymization
 - Continuous covariates scaled to (0, 1)
 - Covariates relabeled to $X_1, X_2, ..., X_p$
 - 2. Generated from parametric distribution with dependence/ independent covariates distributions
- User can provide the structure of $f_{prog}(X)$ and $f_{pred}(X)$ to account for different type of problems (e.g. linear/non-linear, step)

Data generation: different sets of parameters

Generate data from: $f(X) = f_{prog}(X) + Trt * (\beta_0 + \beta_1 * f_{pred}(X))$

Parameter	Setting
Sample size	100, 500, 1000
Number of predictors	30,100
Overall Effect size (determined by power)	Large (power = 0.9) Medium (power = 0.5) Small (power = 0.05)
Standard deviation of treatment effect	Small, medium, large (multiple)
Treatment effect structure	Step, linear
Number of variables defining subgroup	0 (no subgroup), 1, 2
Clinical endpoints	Continuous, binary, count, survival



List of methods for simulation

Non-ensembling methods

- Tree-based methods: (suggest subgroup)
 - Virtual Twins (Foster, Taylor, and Ruberg 2011)
 - SIDES (Lipkovich et al. 2011)
 - GUIDE (Loh and Zhou 2020)
 - Interaction Tree (Su et al. 2008)
 - MOB (Zeileis and Hothorn 2015)
 - QUINT (Dusseldorp and Van Mechelen 2014)
 - STIMA (Dusseldorp, Conversano, and Van Os 2010)
- Linear- Regression-based methods:
 - (estimate interaction effect)
 - Lasso & Ridge, Glmnet (Hastie and Qian 2014)
 - FindIT (Imai, Ratkovic, and others 2013)
 - STIMA (Dusseldorp, Conversano, and Van Os 2010)
 - OWL (Fu, Zhou and Faries 2016, Yu et al. 2015)

Ensembling methods:

(provide variable importance)

- Casual forest (Athey et al. 2019)
- GUIDE (Loh and Zhou 2020)
- MOBFOREST (Garge et al. 2019)
- Virtual Twins (Foster, Taylor, and Ruberg 2011)
- BART (Chipman et al. 2010)
- TSDT (Battioui et al. 2018)
- subtee (Bornkamp et al. 2017)



Performance Metrics

Ability to reliably determine subgroups with higher or lower (relative to overall) treatment effect (reproducible in new studies)

- Test for existence of differential treatment effects
 - Right/wrong decision
- Variable selection bias based on variable importance rankings (for differential treatment effect)
 - "True treatment effect modifying variates" are most important variables
 - Prognostic variables falsely identified among most important variables
- Estimation of individual treatment effects
 - Bias & MSE overall (and maybe in top 50%, top 20%, top 10% of predicted effects)

Performance Metrics: Treatment effect heterogeneity?

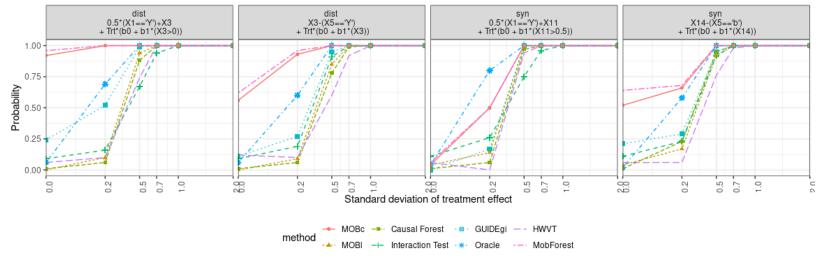
Setup:

- Continuous response
- Sample size n = 500
- power = 0.5
- Repeat on 1000

Methods to compare:

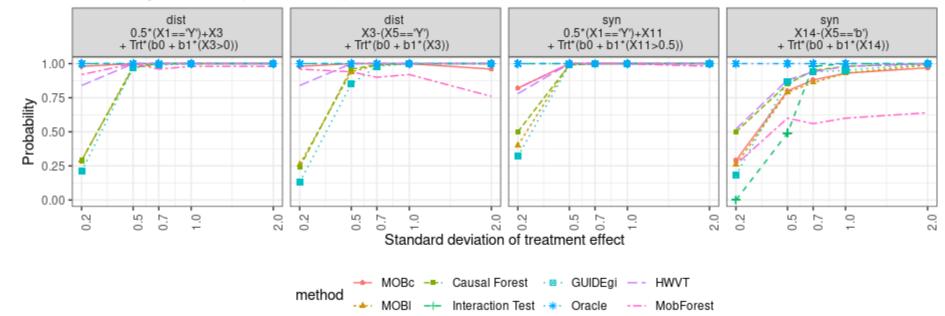
- CausalForest: Forest based
- MOB: MOBc with node fit Y = Trt, MOBl: $Y = \alpha Trt + \sum_i \beta_i X_i$, MobForest: ensemble MOBc
- GUIDE: tree-based
- Interaction test: Univariate interaction model
- HWVT: Holmes and Watson (2020) + virtual Twins implementation
- Oracle: true model

Probability of detecting heterogeneity



Performance Metrics: Variable selection bias

Probability that the top variable is predictive



Performance Metrics: estimation of treatment effect

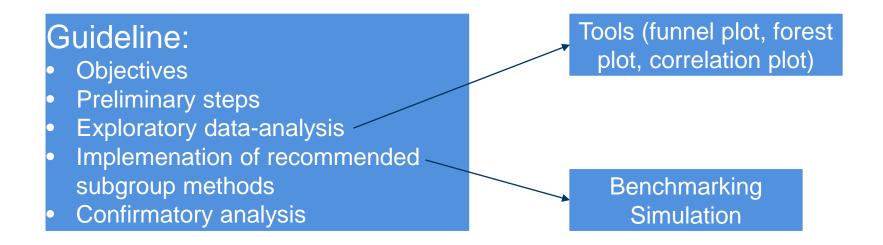
MSE of treatment effect dist X3-(X5=='Y') + Trt*(b0 + b1*(X3)) syn 0.5*(X1=='Y')+X11 + Trt*(b0 + b1*(X11>0.5)) dist syn X14-(X5=='b') + Trt*(b0 + b1*(X14)) 0.5*(X1=='Y')+X3 + Trt*(b0 + b1*(X3>0)) MSE 2 Ø 0 CA 0 0.2 0.5 0.2 0.5 0.5 0.2 0.5 Standard deviation of treatment effect Causal Forest Interaction Test Oracle MobForest



Subgroup identification method recommendation

- Benchmarking framework help us to better understand the performance of each methods for subgroup identification problems on:
 - Test for treatment effect heterogeneity
 - Variable selection bias (important variables are predictive)
 - Prediction bias (predicted treatment effect close to truth)
- Other than the performance part, whether a subgroup identification is recommended also depends on
 - Types of responses it can handle
 - o Interpretability of the result
 - Computation cost
 - How easy it is to use the method (whether there is a package, how easy it is to use it in different systems)

Future work (go/subgroup)





Thank you



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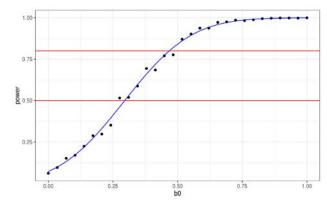
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How to choose β_0 and β_1 in benchtm?

Generate data from: $f(X) = f_{prog}(X) + Trt * (\beta_0 + \beta_1 * f_{pred}(X))$

- 1. Can specify β_0 and β_1 (difficult in practice)
- 2. Derive β_0 and β_1 based on the overall treatment effect power and the standard deviation of the treatment effect
 - Derive β_1 based on $\operatorname{sd}_{\operatorname{TE}} : \operatorname{sd}_{\operatorname{TE}} = \beta_1 \operatorname{sd}(f_{\operatorname{pred}}(X))$
 - Find β_0 for a pre-specified overall power (for the naive unadjusted test)



Depends on covariate distribution for X and structural form of $f_{pred}(X)$ as well as $f_{prog}(X)$

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