

Attitude and Position Control of a Quadcopter in a Networked Distributed System



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Agenda



Introduction

Model

- Attitude Model
- Translational Model
- Linearization

Network

Control Solution

- Attitude Controller
- Translational Controller

Implementation

Results

Final Statements

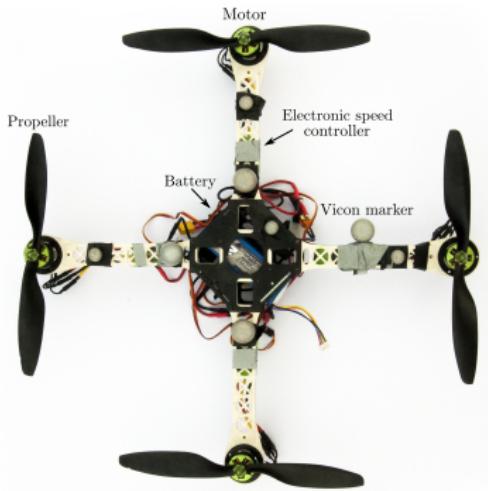
Introduction



- ▶ Surveillance and inspection
- ▶ Rescue
- ▶ Aerial photography
- ▶ ...

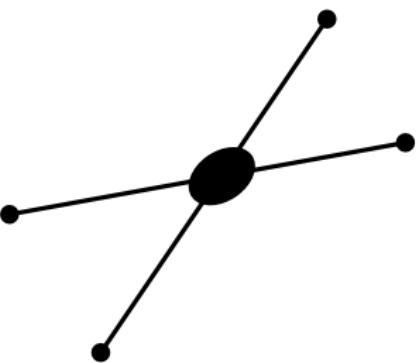
Introduction

Prototype



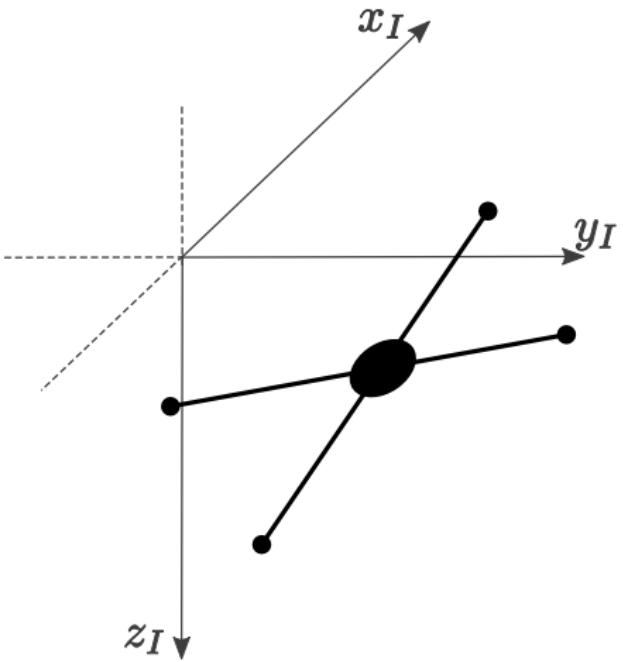
Model

Attitude Model



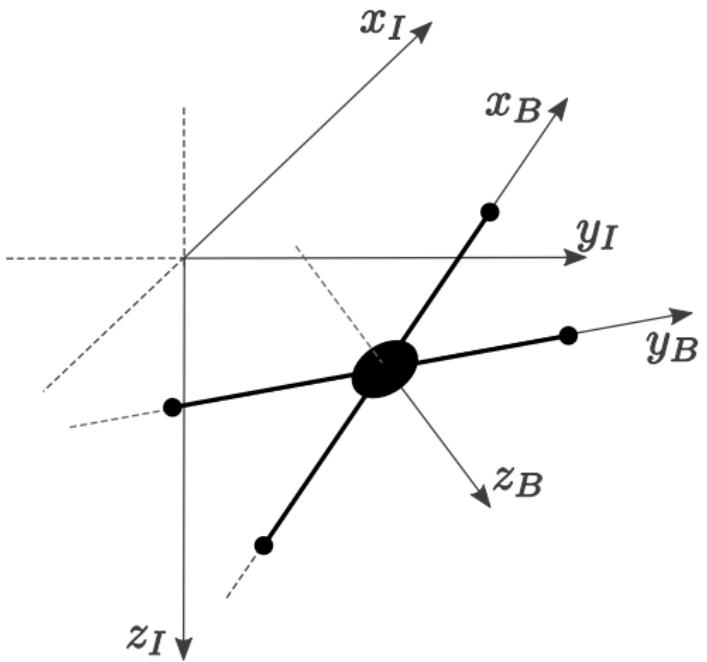
Model

Attitude Model



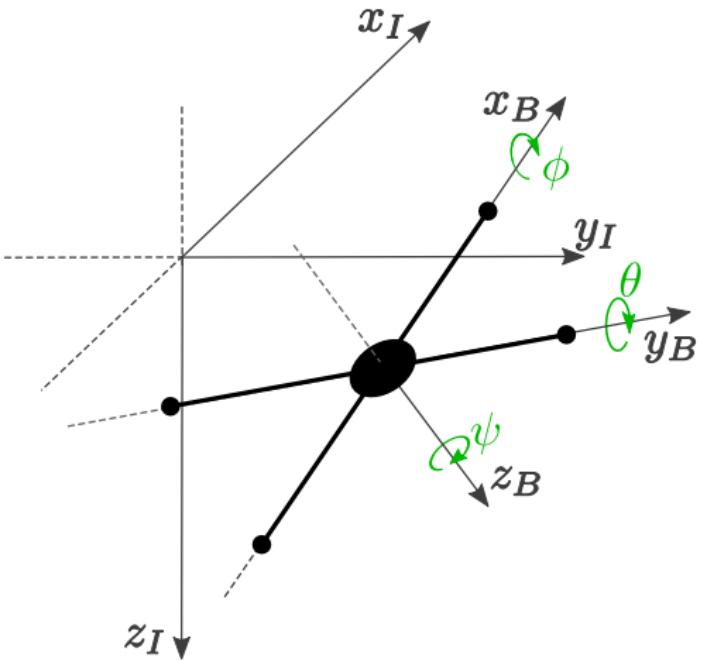
Model

Attitude Model



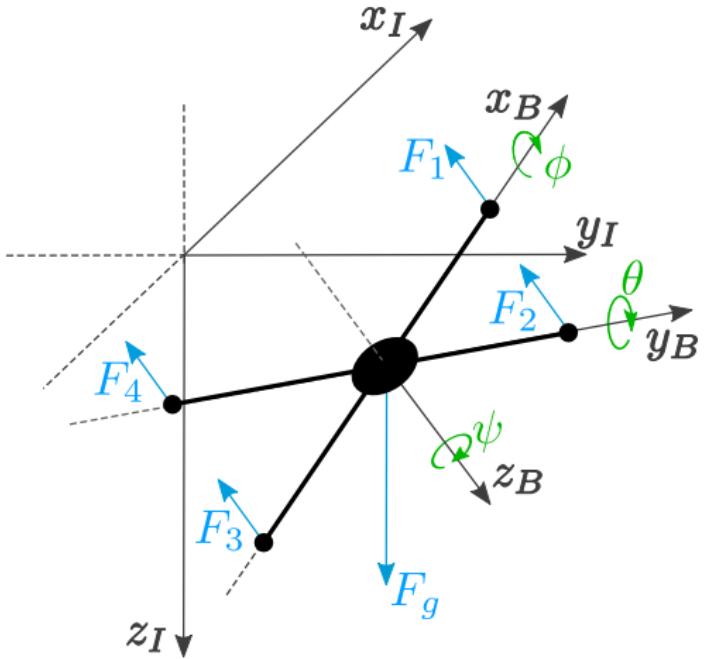
Model

Attitude Model



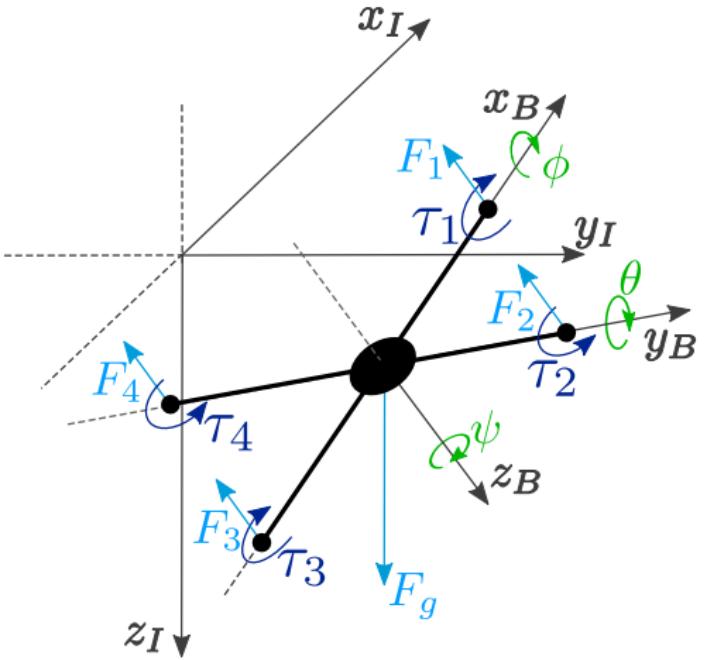
Model

Attitude Model



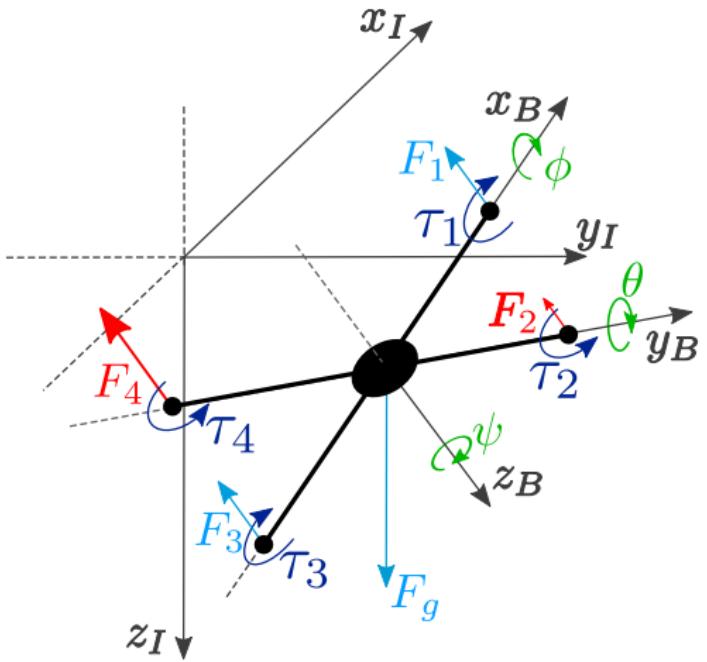
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Attitude Model



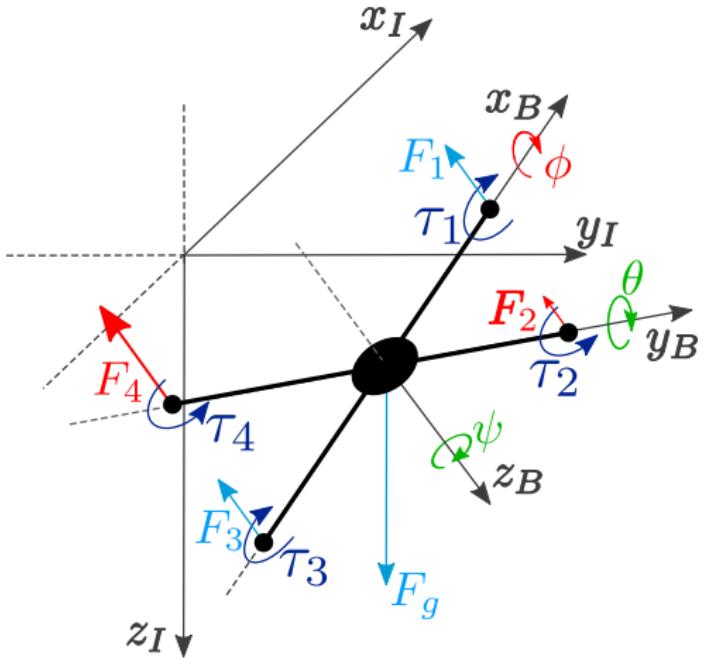
Model

Attitude Model



Model

Attitude Model



Model

Attitude Model



- ▶ Dynamic Equations

Model

Attitude Model



- ▶ Dynamic Equations

$$J\alpha = \sum \tau$$

Model

Attitude Model



► Dynamic Equations

$$J\alpha = \sum \tau$$

$$J_x \ddot{\phi} = (F_4 - F_2)L$$

$$J_y \ddot{\theta} = (F_1 - F_3)L$$

$$J_z \ddot{\psi} = \tau_1 - \tau_2 + \tau_3 - \tau_4$$

Model

Attitude Model



► Dynamic Equations

$$J\alpha = \sum \tau$$

$$J_x \ddot{\phi} = (F_4 - F_2)L$$

$$J_y \ddot{\theta} = (F_1 - F_3)L$$

$$J_z \ddot{\psi} = \tau_1 - \tau_2 + \tau_3 - \tau_4$$

$$J_x \ddot{\phi} = k_{\text{th}}(\omega_4^2 - \omega_2^2)L$$

$$J_y \ddot{\theta} = k_{\text{th}}(\omega_1^2 - \omega_3^2)L$$

$$J_z \ddot{\psi} = k_d(\omega_1^2 - \omega_2^2 + \omega_3^2 - \omega_4^2)$$

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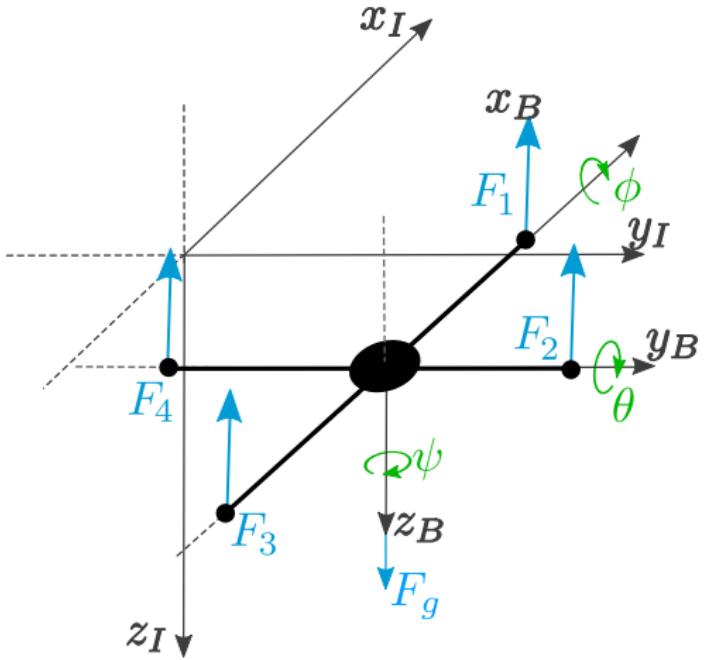
Implementation

Results

Final Statements

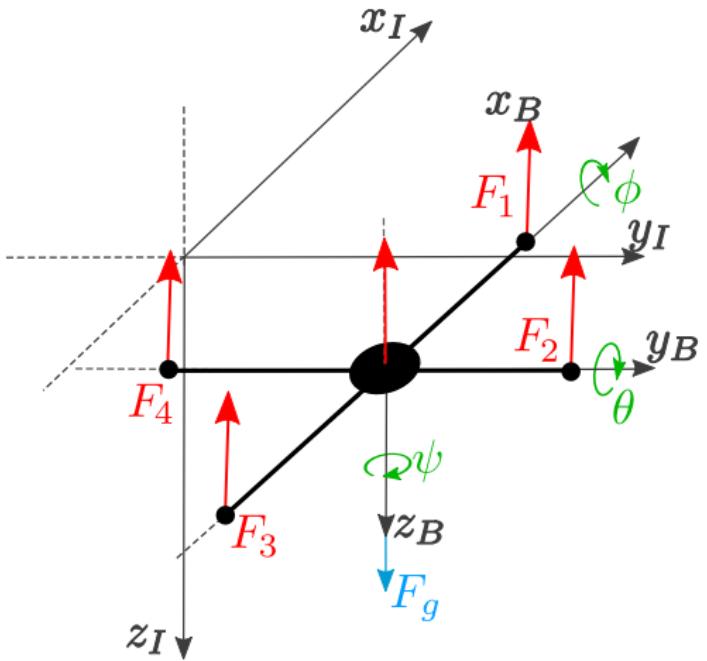
Model

Translational Model



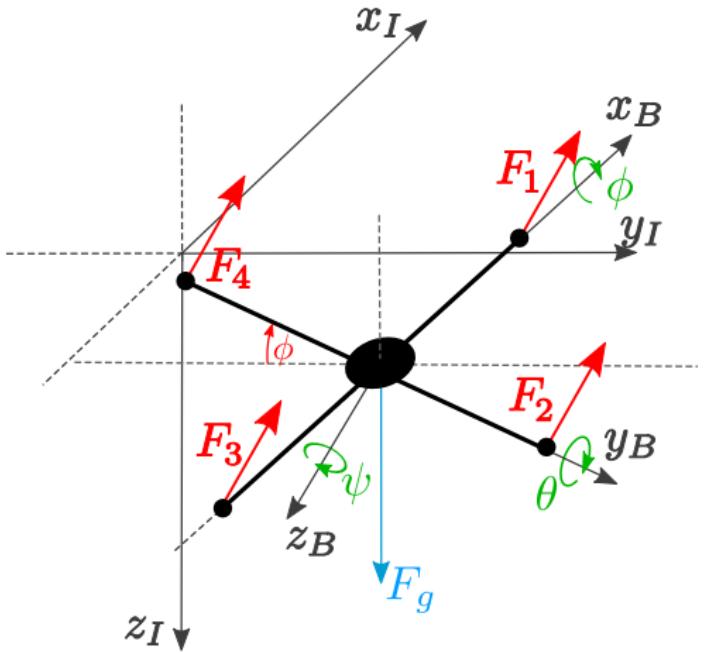
Model

Translational Model



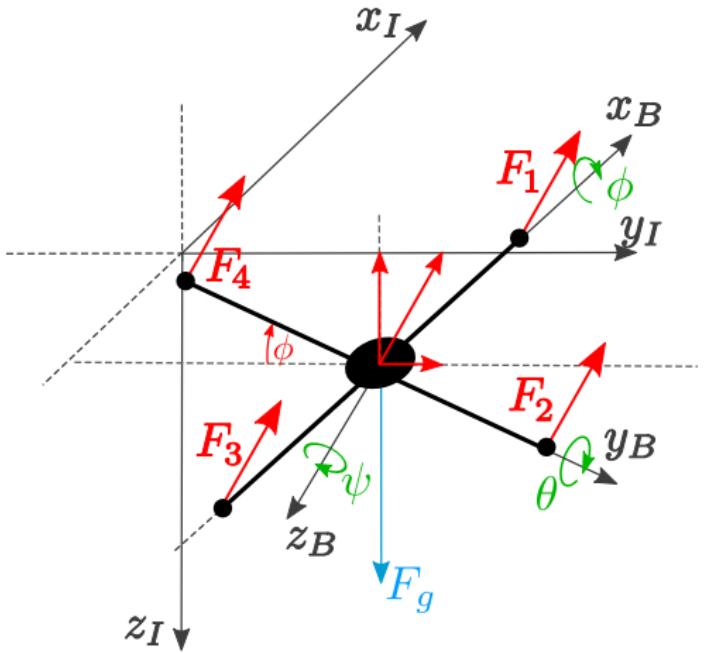
Model

Translational Model



Model

Translational Model



Translational Model



► Rotation Matrix

$$R_X = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c\phi & -s\phi \\ 0 & s\phi & c\phi \end{bmatrix} \quad R_Y = \begin{bmatrix} c\theta & 0 & s\theta \\ 0 & 1 & 0 \\ -s\theta & 0 & c\theta \end{bmatrix} \quad R_Z = \begin{bmatrix} c\psi & -s\psi & 0 \\ s\psi & c\psi & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$R = R_Z R_Y R_X$$

$$v_I = R v_B$$

Model

Translational Model



- ▶ Dynamic Equations

Model

Translational Model



- ▶ Dynamic Equations

$$ma = \sum F$$

Model

Translational Model



► Dynamic Equations

$$ma = \sum F$$

$$m\ddot{x}_I = -(F_1 + F_2 + F_3 + F_4)(\cos \phi \sin \theta \cos \psi + \sin \phi \sin \psi)$$

$$m\ddot{y}_I = -(F_1 + F_2 + F_3 + F_4)(\cos \phi \sin \theta \sin \psi - \sin \phi \cos \psi)$$

$$m\ddot{z}_I = F_g - (F_1 + F_2 + F_3 + F_4) \cos \phi \cos \theta$$

Model

Translational Model



► Dynamic Equations

$$ma = \sum F$$

$$m\ddot{x}_I = -(F_1 + F_2 + F_3 + F_4)(\cos \phi \sin \theta \cos \psi + \sin \phi \sin \psi)$$

$$m\ddot{y}_I = -(F_1 + F_2 + F_3 + F_4)(\cos \phi \sin \theta \sin \psi - \sin \phi \cos \psi)$$

$$m\ddot{z}_I = F_g - (F_1 + F_2 + F_3 + F_4) \cos \phi \cos \theta$$

$$m\ddot{x}_I = -k_{th}(\omega_1^2 + \omega_2^2 + \omega_3^2 + \omega_4^2)(\cos \phi \sin \theta \cos \psi + \sin \phi \sin \psi)$$

$$m\ddot{y}_I = -k_{th}(\omega_1^2 + \omega_2^2 + \omega_3^2 + \omega_4^2)(\cos \phi \sin \theta \sin \psi - \sin \phi \cos \psi)$$

$$m\ddot{z}_I = F_g - k_{th}(\omega_1^2 + \omega_2^2 + \omega_3^2 + \omega_4^2) \cos \phi \cos \theta$$

Model

Linearization



- ▶ First order Taylor approximation

Model

Linearization



- ▶ First order Taylor approximation

$$m\ddot{\bar{z}}_I = F_g - k_{th}(\bar{\omega}_1^2 + \bar{\omega}_2^2 + \bar{\omega}_3^2 + \bar{\omega}_4^2) \cos \bar{\phi} \cos \bar{\theta}$$

Model

Linearization



- ▶ First order Taylor approximation

$$m\ddot{\bar{z}}_I = F_g - k_{th}(\bar{\omega}_1^2 + \bar{\omega}_2^2 + \bar{\omega}_3^2 + \bar{\omega}_4^2) \cos \bar{\phi} \cos \bar{\theta}$$

$$\bar{\omega}_i = \sqrt{\frac{F_g}{4k_{th}}}$$

Model

Linearization

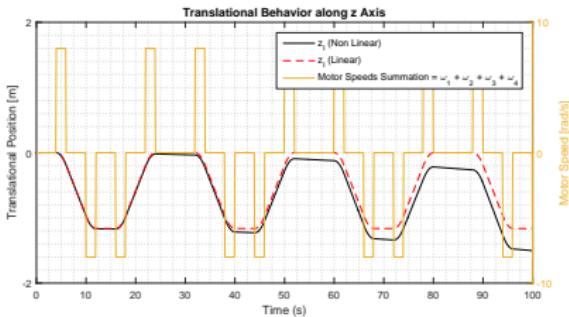
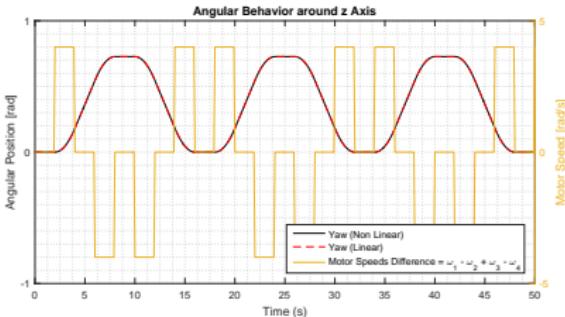


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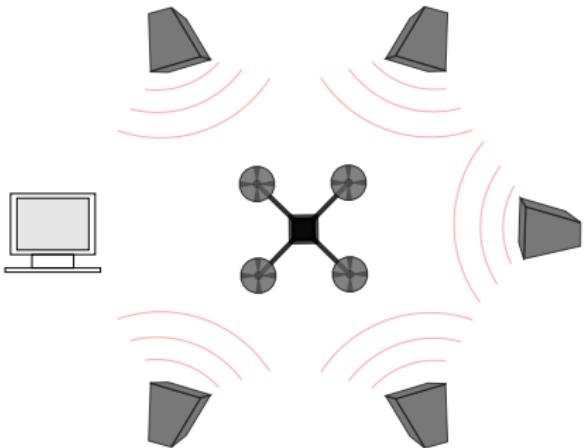
- ▶ First order Taylor approximation

$$m\ddot{z}_I = F_g - k_{th}(\bar{\omega}_1^2 + \bar{\omega}_2^2 + \bar{\omega}_3^2 + \bar{\omega}_4^2) \cos \bar{\phi} \cos \bar{\theta}$$

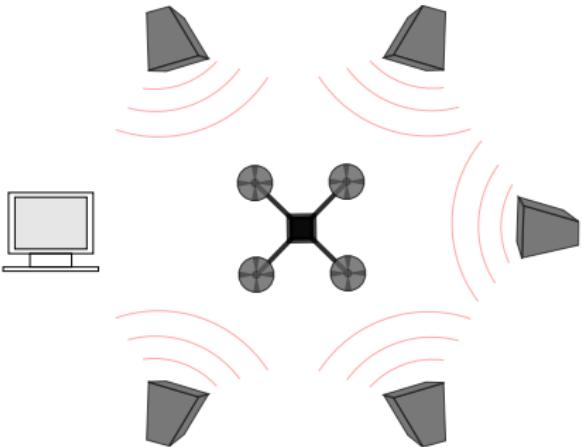
$$\bar{\omega}_i = \sqrt{\frac{F_g}{4k_{th}}}$$



Network



Network

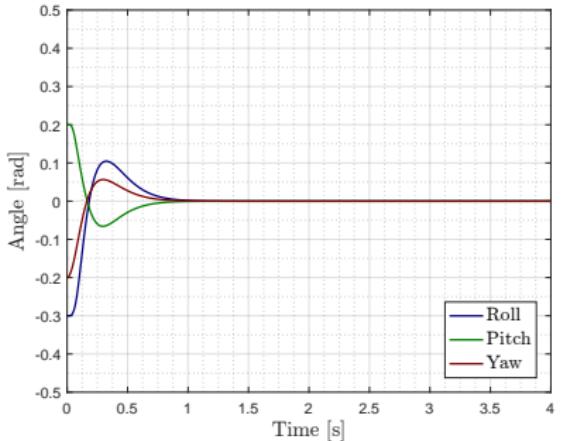


- ▶ Delay
- ▶ Missed packets

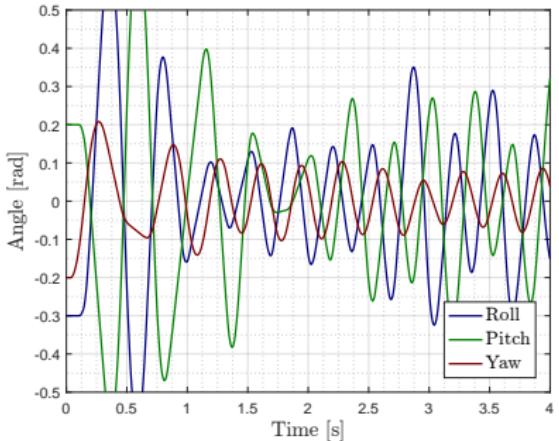
Network



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Control design only taking the model into account



Same controller with the effect of the network

Agenda



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Control Solution

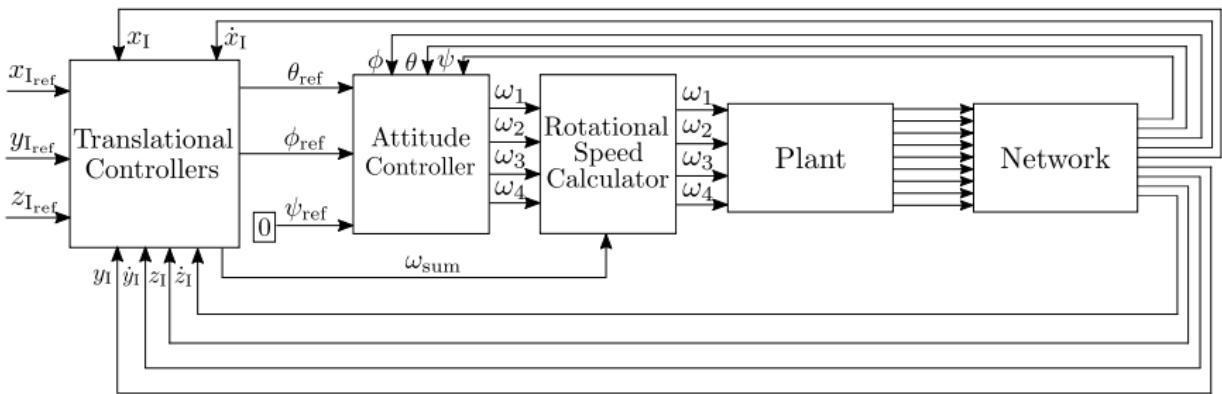
- Attitude Controller
- Translational Controller

Implementation

Results

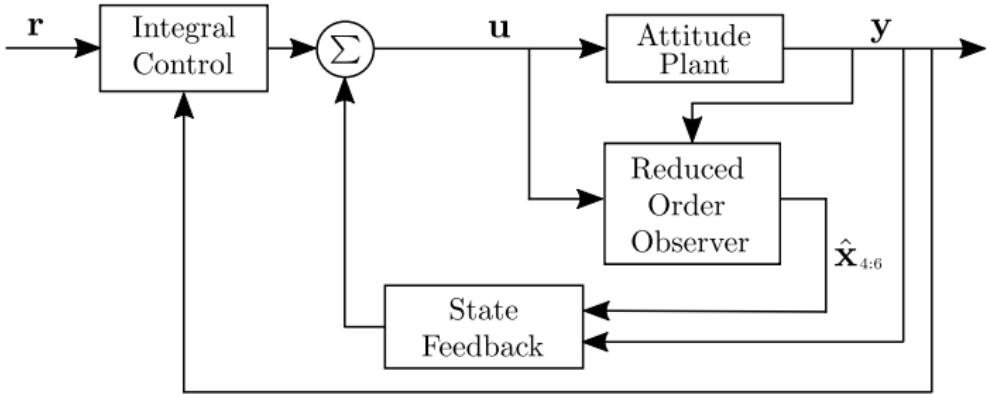
Final Statements

Control Solution



Control Solution

Attitude Controller



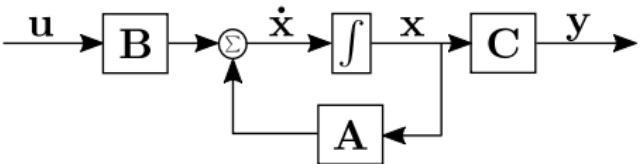
Control Solution

Attitude Controller



► System Representation

$$\begin{aligned}\dot{\mathbf{x}}(t) &= \mathbf{A}\mathbf{x}(t) + \mathbf{B}\mathbf{u}(t) \\ \mathbf{y}(t) &= \mathbf{C}\mathbf{x}(t)\end{aligned}$$



$$\mathbf{x} = \begin{bmatrix} \phi \\ \theta \\ \psi \\ \dot{\phi} \\ \dot{\theta} \\ \dot{\psi} \end{bmatrix}$$

$$\mathbf{u} = \begin{bmatrix} \omega_1 \\ \omega_2 \\ \omega_3 \\ \omega_4 \end{bmatrix}$$

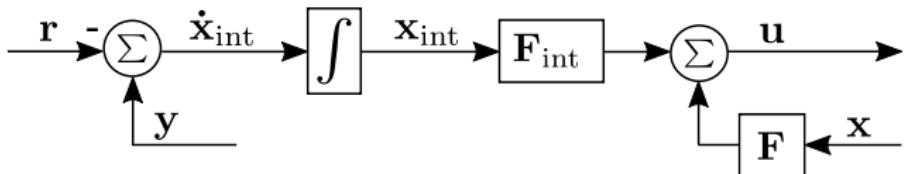
$$\mathbf{y} = \begin{bmatrix} \phi \\ \theta \\ \psi \end{bmatrix}$$

Control Solution

Attitude Controller



- ▶ State Feedback with Integral Control



$$\dot{\mathbf{x}}_{\text{Int}}(t) = \mathbf{y}(t) - \mathbf{r}(t)$$

$$\mathbf{u}(t) = \mathbf{F}\mathbf{x}(t) + \mathbf{F}_{\text{Int}}\mathbf{x}_{\text{Int}}(t)$$

Control Solution

Attitude Controller



- ▶ LQR

$$\mathcal{J} = \int_0^{\infty} \mathbf{x}^T \mathbf{Q} \mathbf{x} + \mathbf{u}^T \mathbf{R} \mathbf{u} \, dt$$

- ▶ Bryson's Rule

$$Q_{ii} = \frac{1}{\text{maximum acceptable value of } [x_i^2]}$$

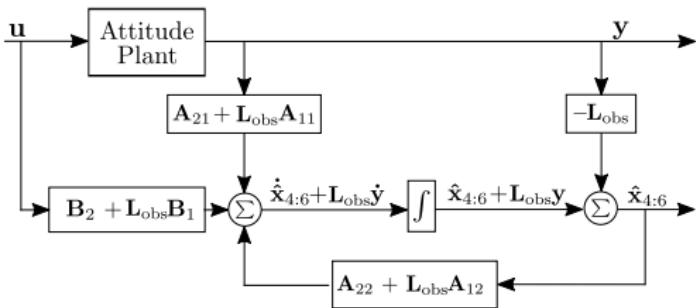
$$R_{ii} = \frac{1}{\text{maximum acceptable value of } [u_i^2]}$$

Control Solution

Attitude Controller



► Reduced Order Observer



$$\dot{\mathbf{x}}_{4:6} = \begin{bmatrix} \dot{\phi} \\ \dot{\theta} \\ \dot{\psi} \end{bmatrix}$$

$$A_{22} + L_{obs}A_{12}$$

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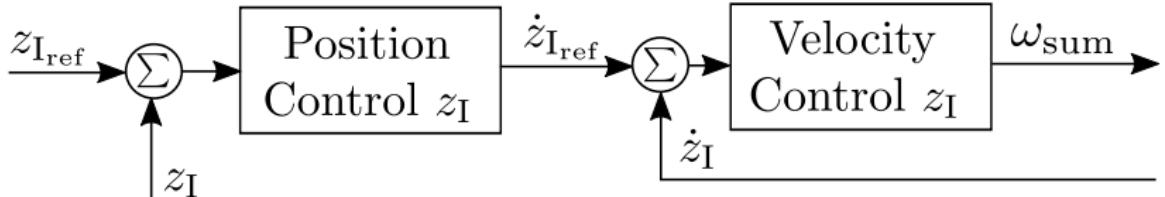
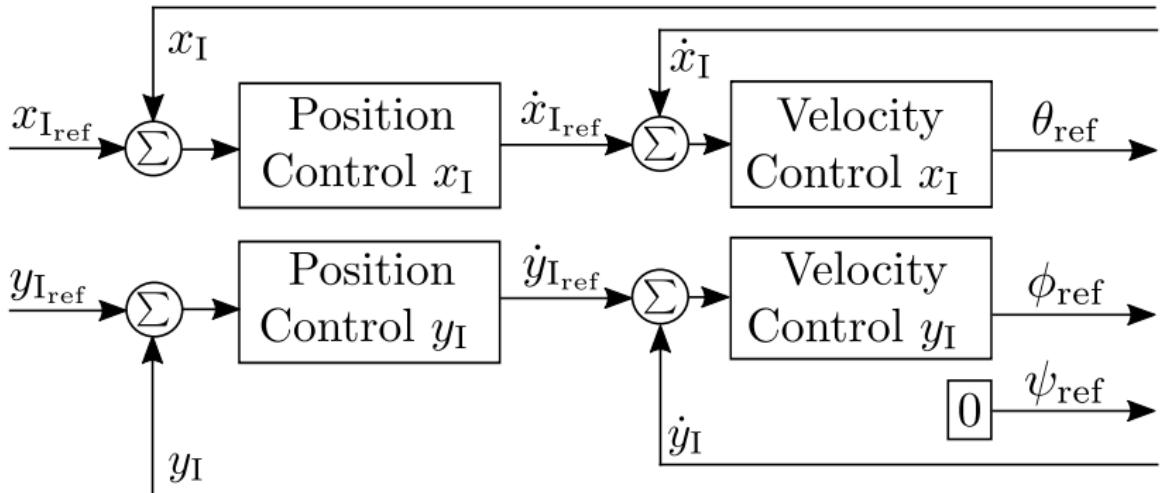
Final Statements

Control Solution

Translational Controller



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Control Solution

Translational Controller



transfer functions with block diagram

Control Solution

Translational Controller



put three root locus

Control Solution

Translational Controller



consideration of bandwidth equations for velocity controllers
equations for position controllers

Implementation



FreeRTOS, tasks

Implementation Schedule



old 35ms

Implementation Schedule



new, 25ms, less sampling freq.

Implementation Schedule



comparison oscilloscope

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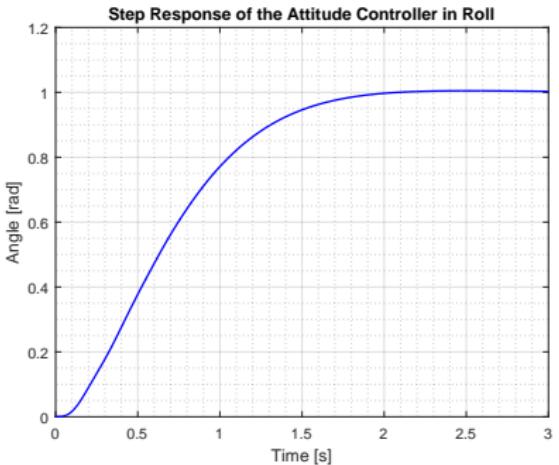
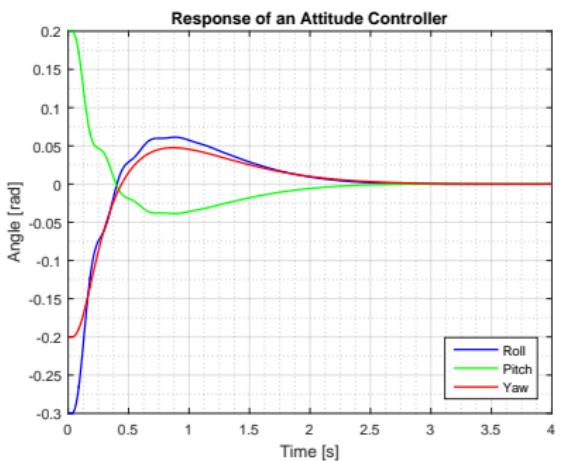
Implementation

Results

Final Statements

Results

Attitude Controller Simulations

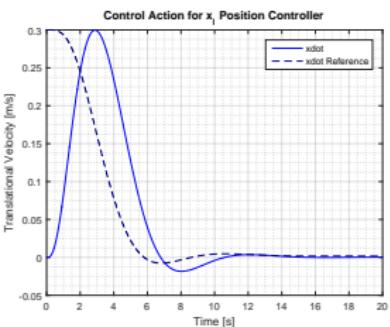
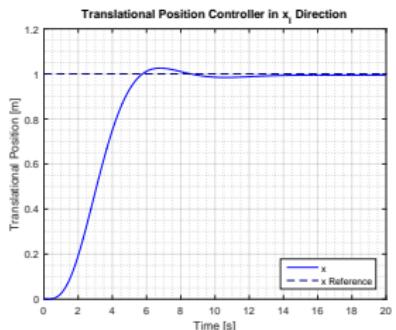
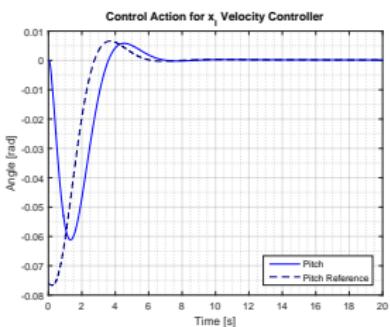
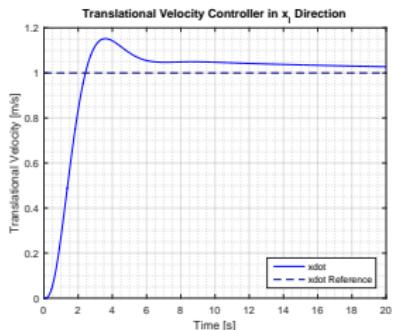


Results

Translational Controllers Simulations



- x_I (and y_I) controllers for velocity and position

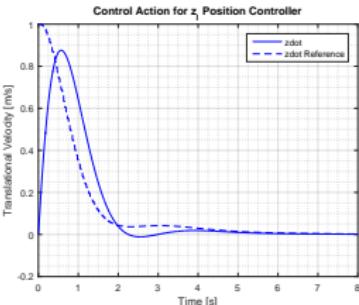
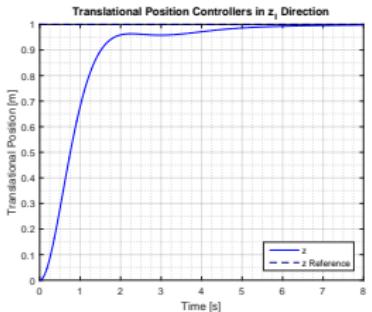
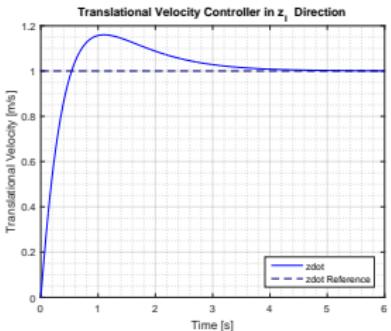


Results

Translational Controllers Simulations

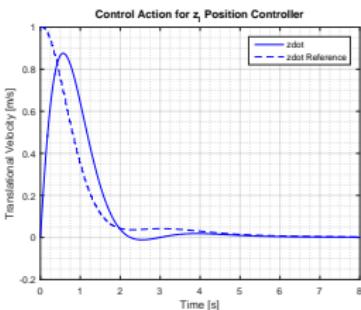
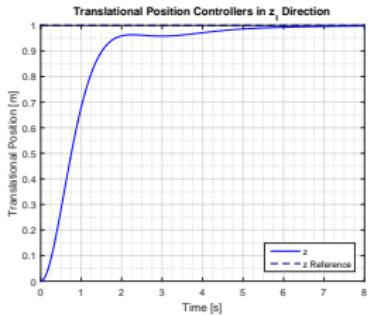
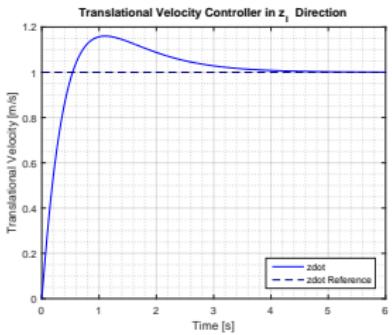


- z_I controllers for velocity and position



Results

Attitude Controller Functional Tests



Final Statements



- Limited bandwidth of controllers due to sampling.
- Control design working in simulation for attitude and translational controller.
- Implementation/Hardware issue when testing the translational controllers.
- Attitude controller tests carried out successfully.

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