

# 2IMN20 - Real-Time Systems

## Server-based scheduling



**Lecturer: Dr. Mitra Nasri**

Assistant professor

IRIS Cluster

[m.nasri@tue.nl](mailto:m.nasri@tue.nl)

# A bit about me

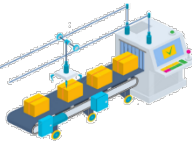
If you are looking for a **Master Thesis topic**, send me an email (to plan a meeting)

## Designing scheduling solutions with predictable performance

Since 2009



embedded systems



Product-lines and manufacturing systems (Canon, Bosch)



Real-time systems on cloud (Philips)



## Response-time analysis using formal methods

Since 2014

## Dependable Robotics on ROS 2 (Robot Operating System)

Since 2020



## Real-time systems security

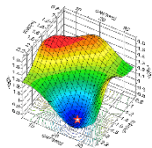
Attacks that can cause deadline misses, attacks that are harmful only if they are done at certain moments, vulnerabilities that come from predictability, ...

Since 2019

## Design-space exploration for timing parameters

How to set parameters of the tasks, how to partition the system, how to set priorities, ...

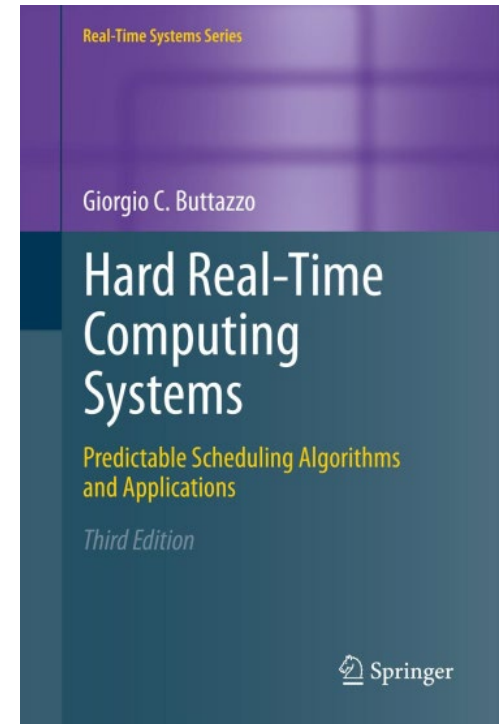
Since 2014



I collaborate with Canon, DAF, Philips, ...

# Sources

## Giorgio Buttazzo's book, chapter 9



Some slides have been taken from [Giorgio Buttazzo's](http://retis.sssup.it/~giorgio/rtS-MECS.html) website:

<http://retis.sssup.it/~giorgio/rtS-MECS.html>

Thank you Giorgio :)

# Why should we tame the beasts? And what to do with goblins?



Tasks that  
may overrun

Aperiodic  
events

Background  
tasks

Image: bing.com image creator

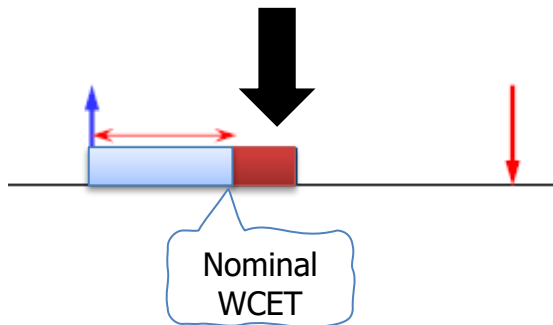
# Agenda

- **Server-based scheduling:** a remedy for aperiodic events, background work, and misbehaving real-time tasks
- **Types of servers**
  - Periodic servers
  - Polling servers
  - Deferrable servers
  - Constant-bandwidth servers (CBS)

# The beasts:

## What to do with tasks that may overrun their expected execution-time (or nominal WCET)?

**Overrun:** happens when a task exceeds its “expected execution time”.

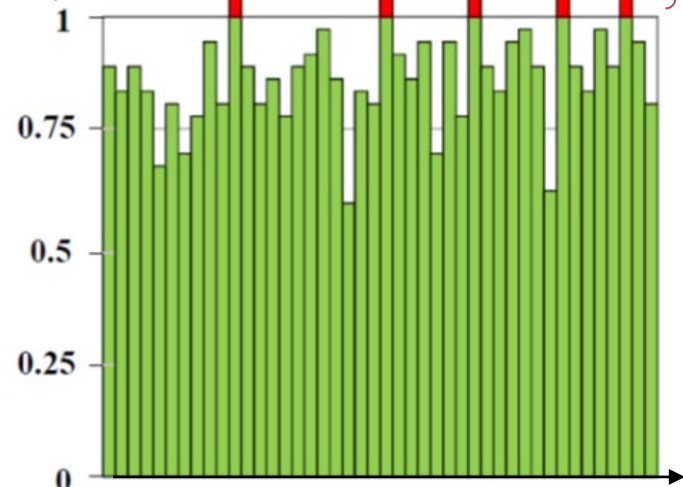


Actual execution time = WCET

Actual execution time > WCET

overruns

Actual execution time as a proportion of the WCET



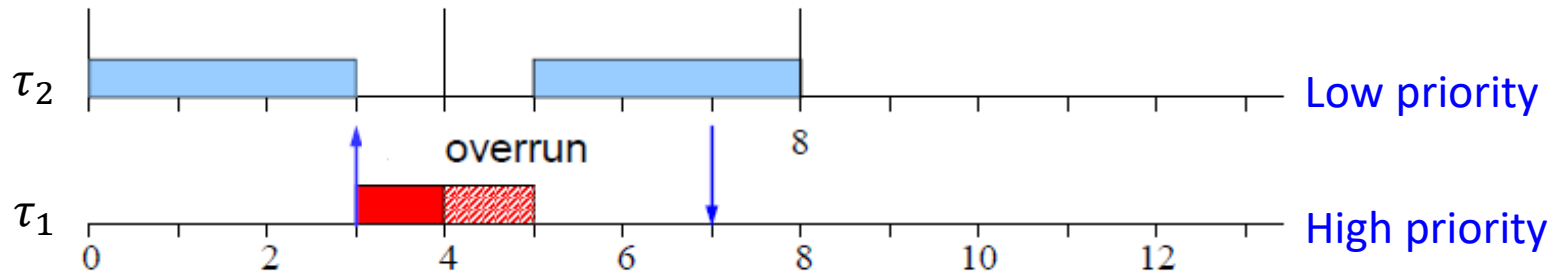
How is this possible?

For example, it happens if the WCET has been obtained by measurement (and therefore is inaccurate)

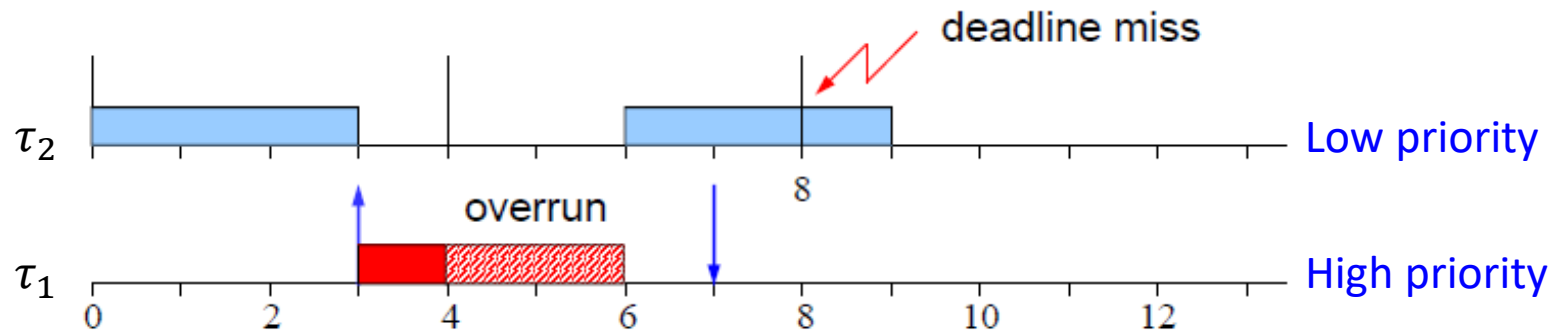


# Consequences of overruns

A task's overrun may not cause a deadline miss:



But in general, it may delay the execution of other tasks, causing a deadline miss for them:



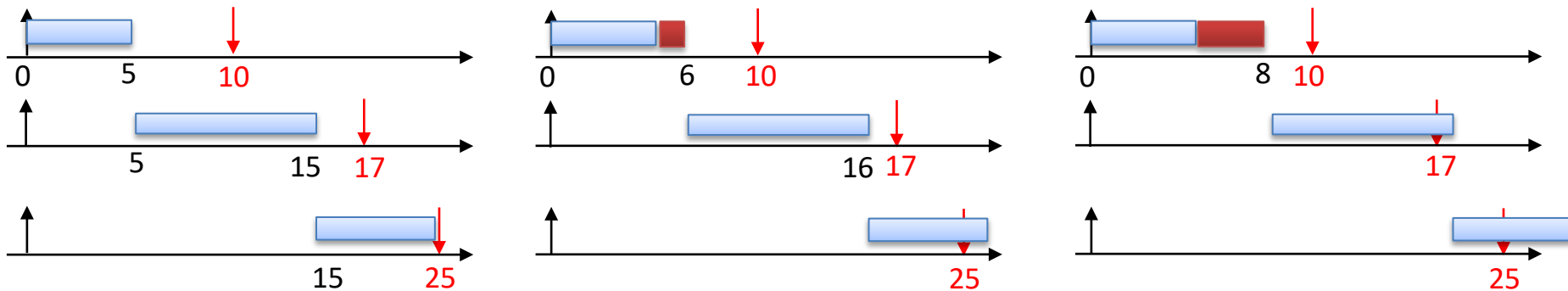
# What can go wrong if overruns are not controlled?

**EDF** may have **domino effect**:

Namely, one (or more) overrun(s) may result in a series of deadline misses

Example: Consider the following task set scheduled by EDF.

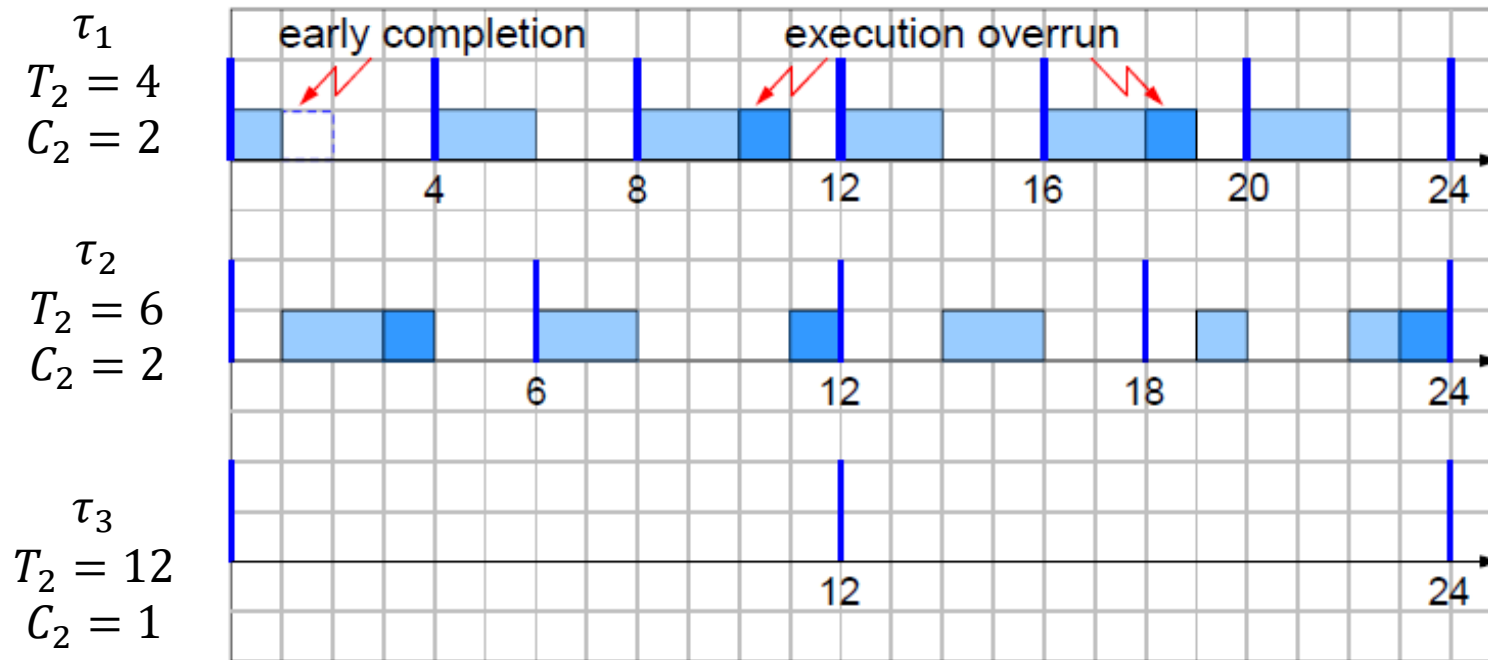
1. How much overrun in  $\tau_1$  will cause one deadline miss for any of these three tasks? 1 unit
2. How much overrun in  $\tau_1$  will cause two deadline misses for any of these three tasks? 3 units





# What can go wrong if overruns are not controlled?

In **FP**, low-priority tasks may **starve** due to an overrun in high-priority tasks



Assume a rate monotonic priority assignment.

# Server-based scheduling

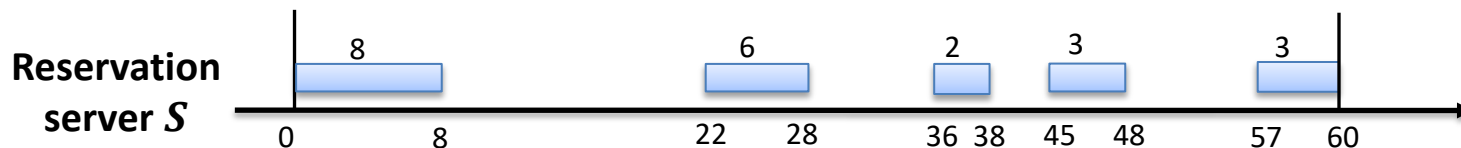
allows scheduling real-time and non-real-time tasks despite potential overruns

A **reservation server** determines when the processor could become available to the task(s) assigned to it

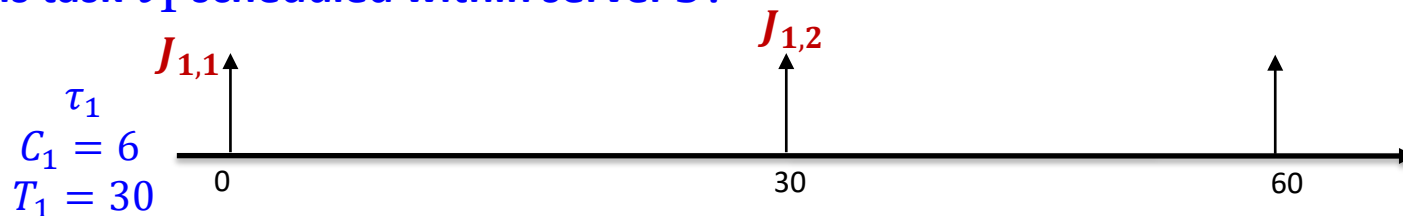
Therefore, it bound the resource consumption of tasks and limit their interference on each other

# Example: server-based scheduling

Assume this is the pattern of available budget from a reservation server:



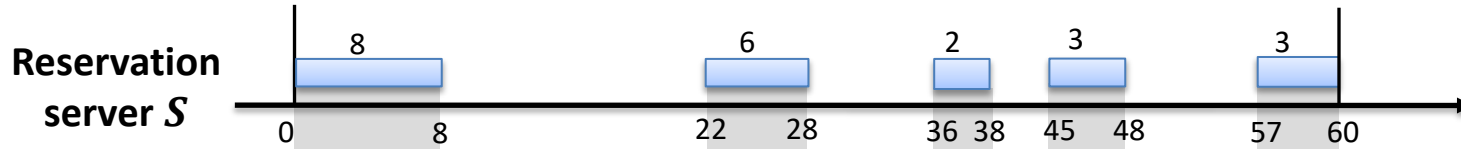
How is task  $\tau_1$  scheduled within server  $S$ ?



A reservation shows when the processor can be assigned to a task

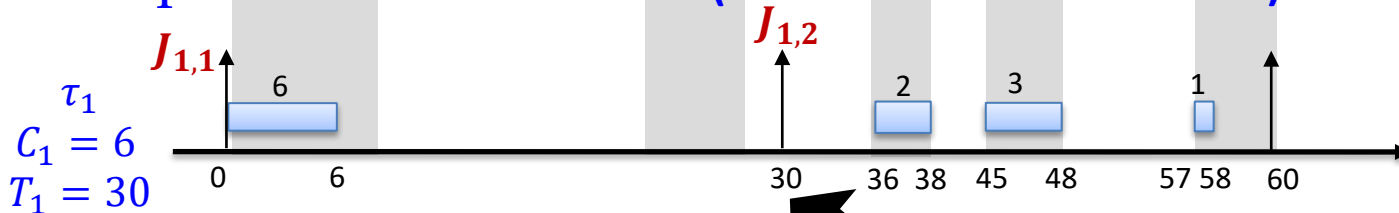
# Example: server-based scheduling

Assume this is the pattern of available budget from a reservation server:



More reservation is available than needed

How is task  $\tau_1$  scheduled within server  $S$  (assume there is no overrun)?



The task is released but there is no budget to start its execution

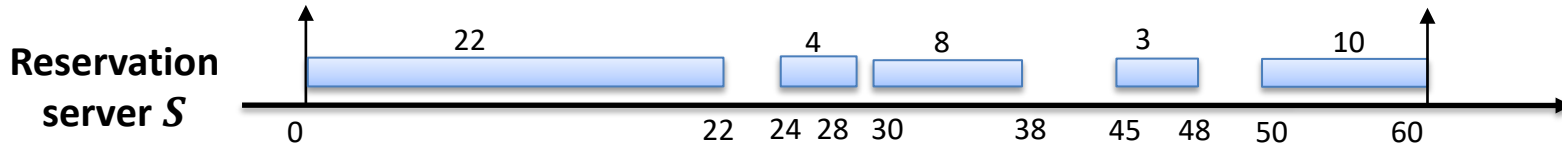
What is the response time of  $J_{1,1}$ ? 6

What is the WCRT of  $\tau_1$ ? 28

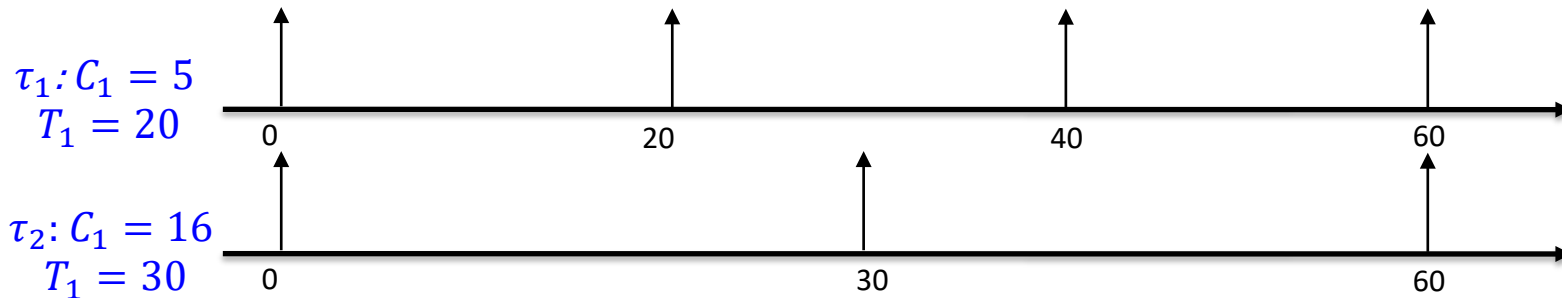
A reservation shows when the processor can be assigned to a task

# Example: server-based scheduling

Assume this is the pattern of available budget from a reservation server:



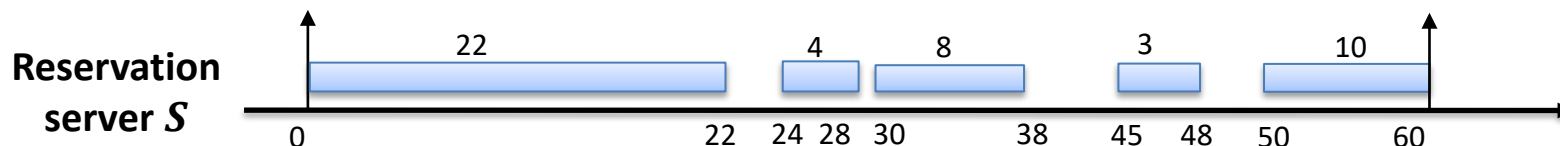
How are tasks  $\tau_1$  and  $\tau_2$  scheduled via server  $S$ ? Assume that within the server, these tasks are scheduled by the **Rate Monotonic** policy.



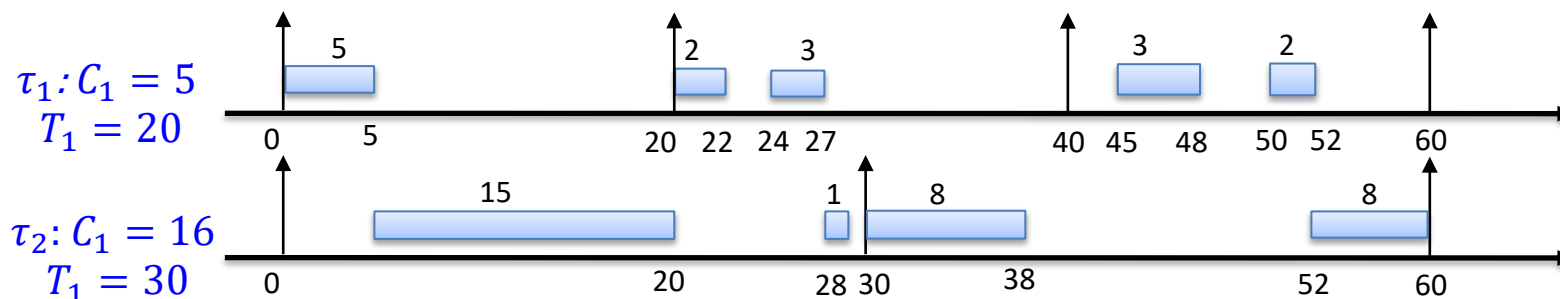
A reservation shows when the processor can be assigned to a task

# Example: server-based scheduling

Assume this is the pattern of available budget from a reservation server:



How are tasks  $\tau_1$  and  $\tau_2$  scheduled via server  $S$ ? Assume that within the server, these tasks are scheduled by the **Rate Monotonic** policy.



What is the WCRT of  $\tau_1$ ?

12

What is the WCRT of  $\tau_2$ ?

30

A reservation shows when the processor can be assigned to a task

# Agenda

- Handling overruns via server-based scheduling
- **Handling aperiodic events and background tasks via server-based scheduling**
- Types of servers

# The goblins!

## What to do with aperiodic events and background tasks?

### Event-driven tasks with deadline

They handle I/O events, garbage collection, etc. and typically have soft deadlines.

**Aperiodic tasks are important for the responsiveness of the system for non-critical events.**



### Background tasks

They perform non-critical functionalities like logging, etc.

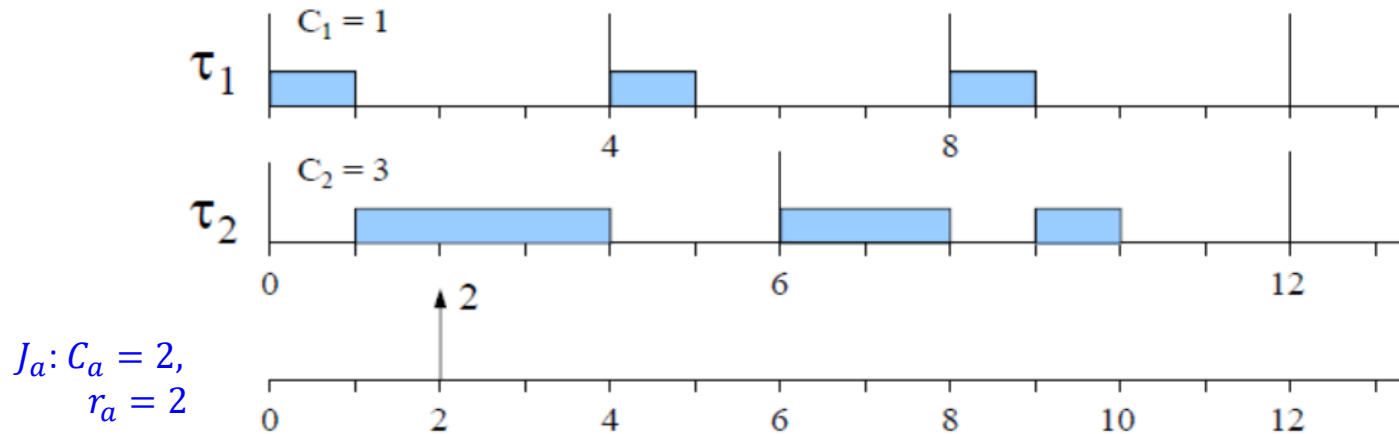
**Background tasks are important for the health of the system, but they do not have deadline.**

Image: bing.com image creator.



# Aperiodic task scheduling

**Example:** Two periodic tasks scheduled by RM and a single aperiodic job  $J_a$  (arrives at  $r_a = 2$  and its WCET is  $C_a = 2$ ):



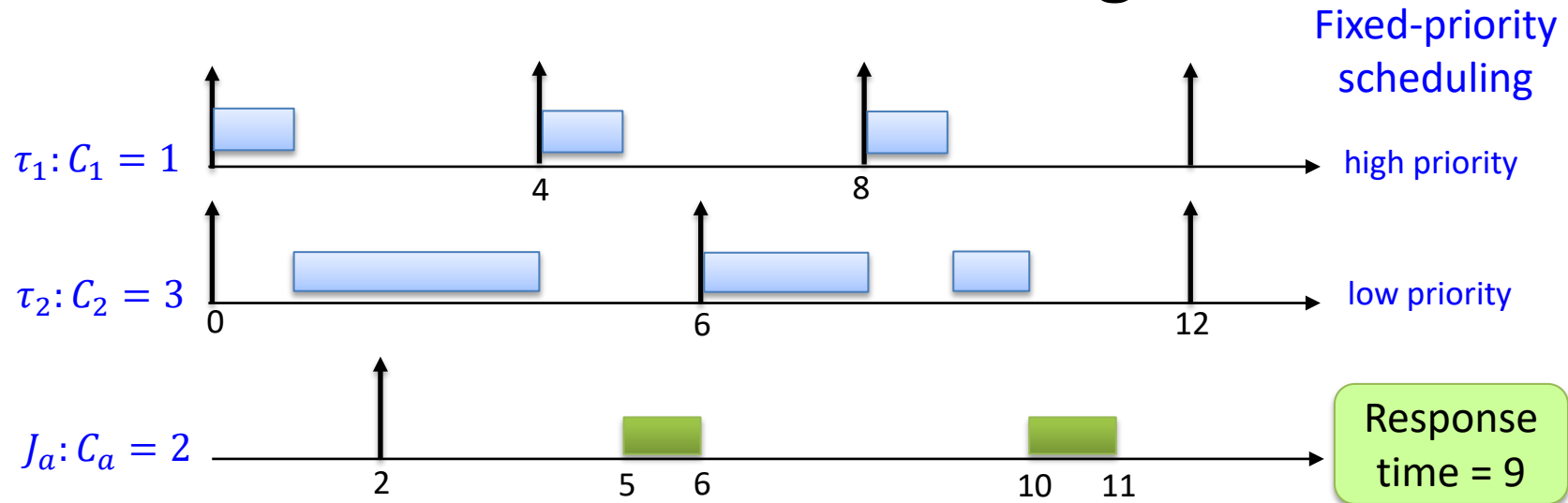
When should we schedule  $J_a$ ?

**Solution 1:**  
whenever nothing else is  
running (as a background  
task with the lowest priority)

**Solution 2:**  
immediately

**Solution 3:**  
Inside a reservation server

# Solution 1: schedule them as a background task



## Advantages?

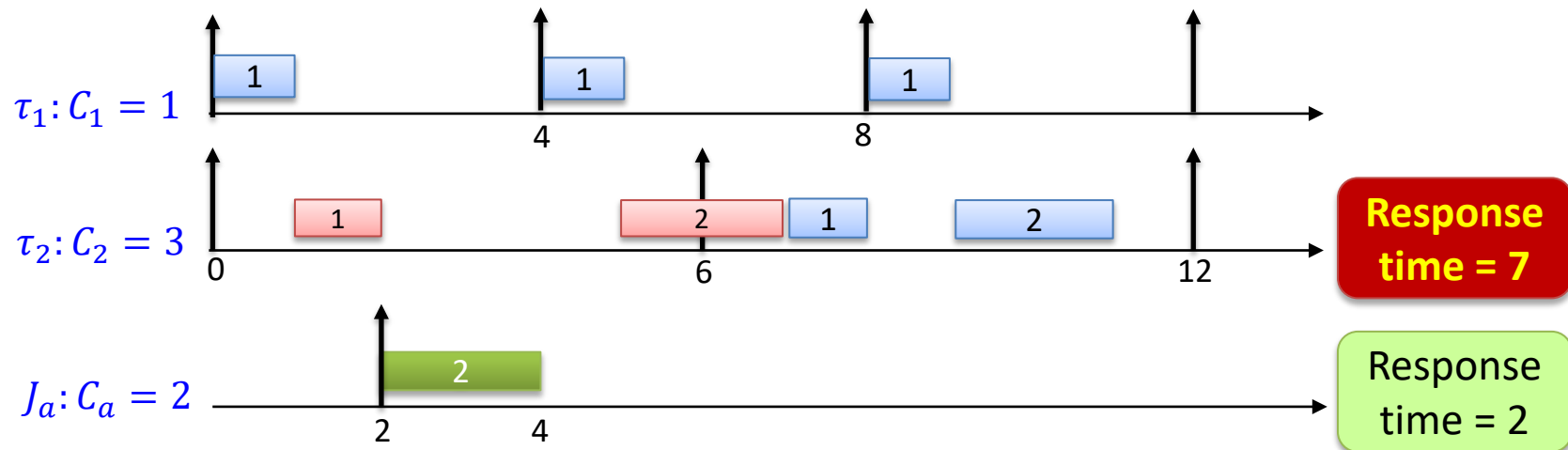
The aperiodic workload will never cause a deadline miss for the periodic tasks

## Disadvantages?

Long response time for the aperiodic task!

Fixed-priority scheduling (rate monotonic)

# Solution 2: schedule them immediately



## Advantages?

- The aperiodic workload will have a smaller response time.
- The system becomes more responsive to the aperiodic events (e.g., interrupts).

## Disadvantages?

Long response time and possibly deadline miss for the periodic tasks!

Fixed-priority scheduling (rate monotonic)

# Solution 3: use server-based scheduling

## Our goal:

Reduce the response time of  
aperiodic tasks (interrupt latency)



Keep the system **schedulable**



For this, we will need to  
learn about types of  
reservation servers and  
their properties

Image: bing.com image creator.

# Type of servers

- **Fixed-priority Servers**

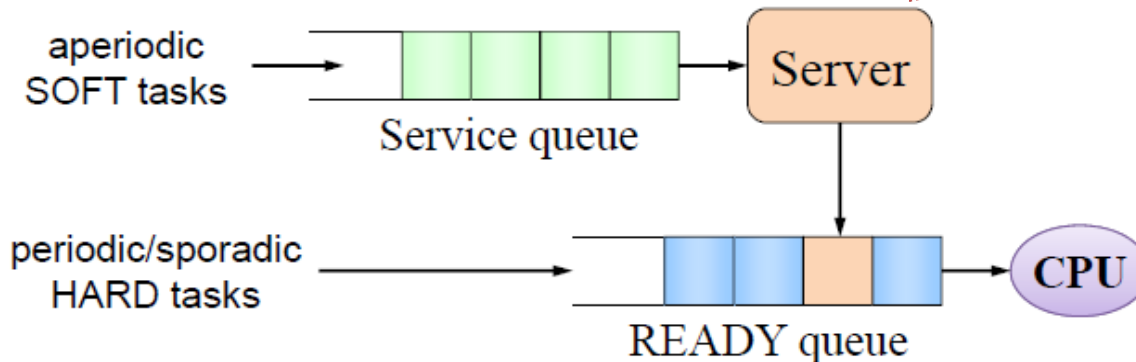
- ➡ • Periodic server
- ➡ • Polling server (PS)
- ➡ • Deferrable server (DS)
  - Sporadic server
  - Slack stealer

- **Dynamic-priority Servers (to be used with EDF scheduler)**

- Dynamic Polling Server
- Dynamic Sporadic Server
- Total Bandwidth Server
- Tunable Bandwidth Server
- ➡ • **Constant Bandwidth Server (CBS)** ← **Implemented in Linux**  
(this is the most interesting one)

# Periodic servers

In this lecture, we assume that there is **only one server** that services the aperiodic tasks



The server is **scheduled as any periodic task** (it can have any priority).

- maximum budget  $C_s$ ,
- period  $T_s$  and
- priority  $P_s$

**Aperiodic tasks** assigned to the server can execute **only when** the server has access to the CPU.

**Aperiodic tasks** can be selected using any queueing discipline (e.g., FIFO).

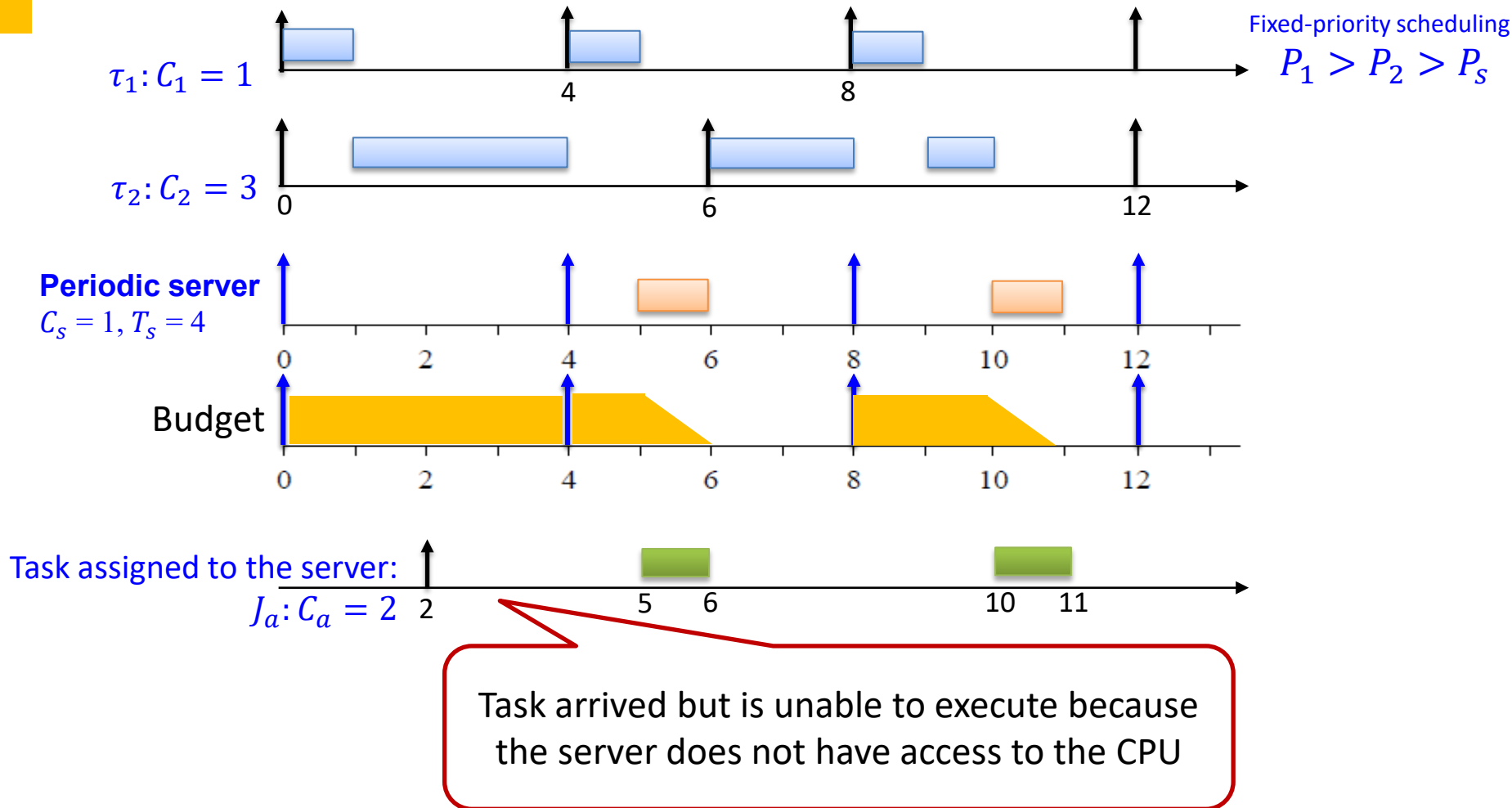
The server **releases a job** with period  $T_s$

The server competes for the CPU with other tasks based on its **priority**  $P_s$

**Priority ties** are broken in **favor** of the server.

The budget is **replenished** to  $C_s$  at each **arrival** of a **new job** of the server

# Periodic servers: example

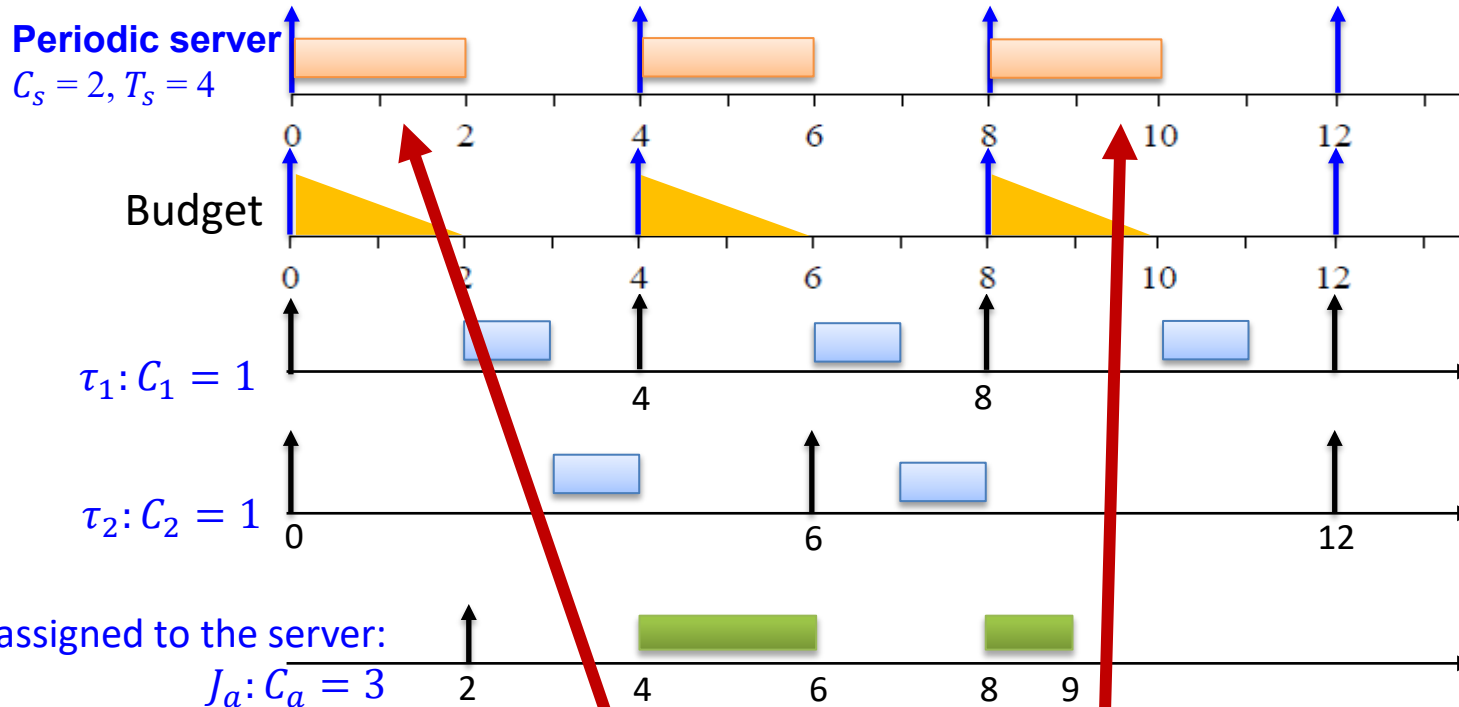


Note: the server in this example may miss its deadline (no schedulability test was done)

# Periodic servers: another example



Fixed-priority scheduling  
 $P_s > P_1 > P_2$



**Drawback:** The server reserves the processor even when there is no task to execute, thus wasting CPU cycles



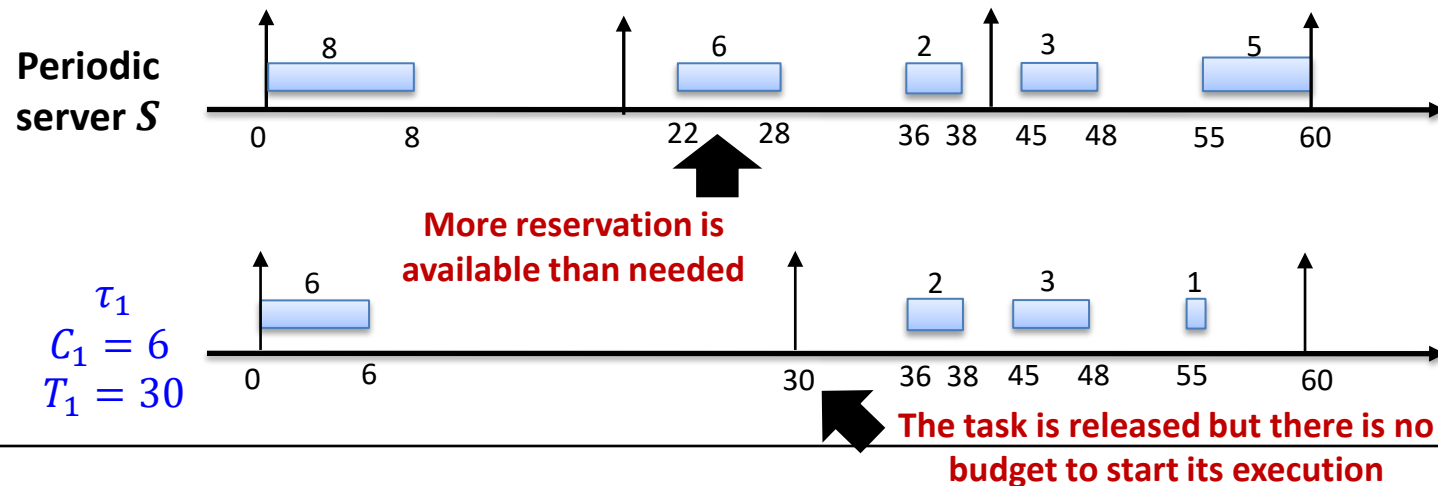
# What is bad about periodic servers?

It wastes the budget if there is nothing in the queue to execute

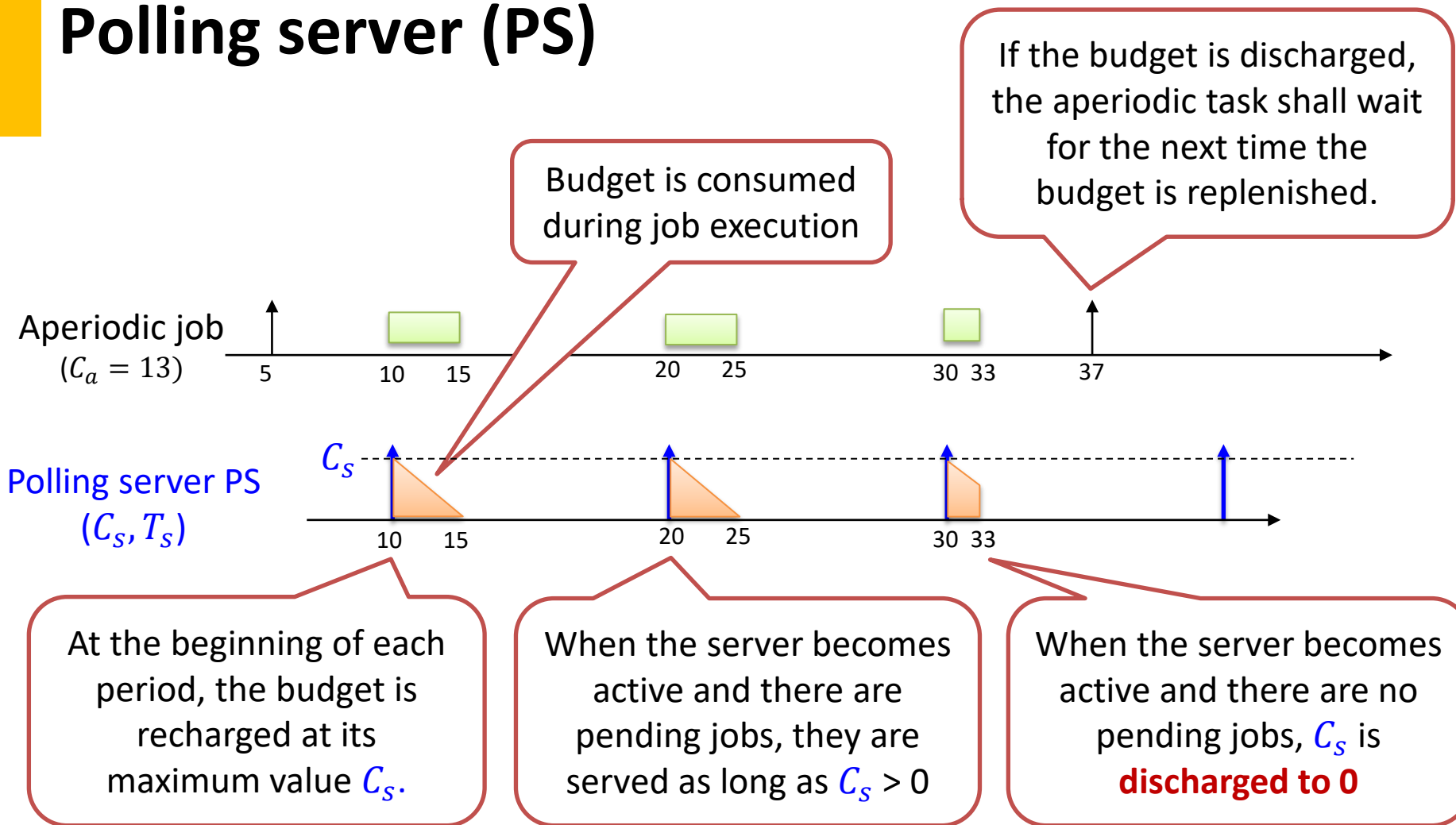
It increases the response time of the tasks running within the server

Solution: discharge the budget to zero if there is nothing in the queue!

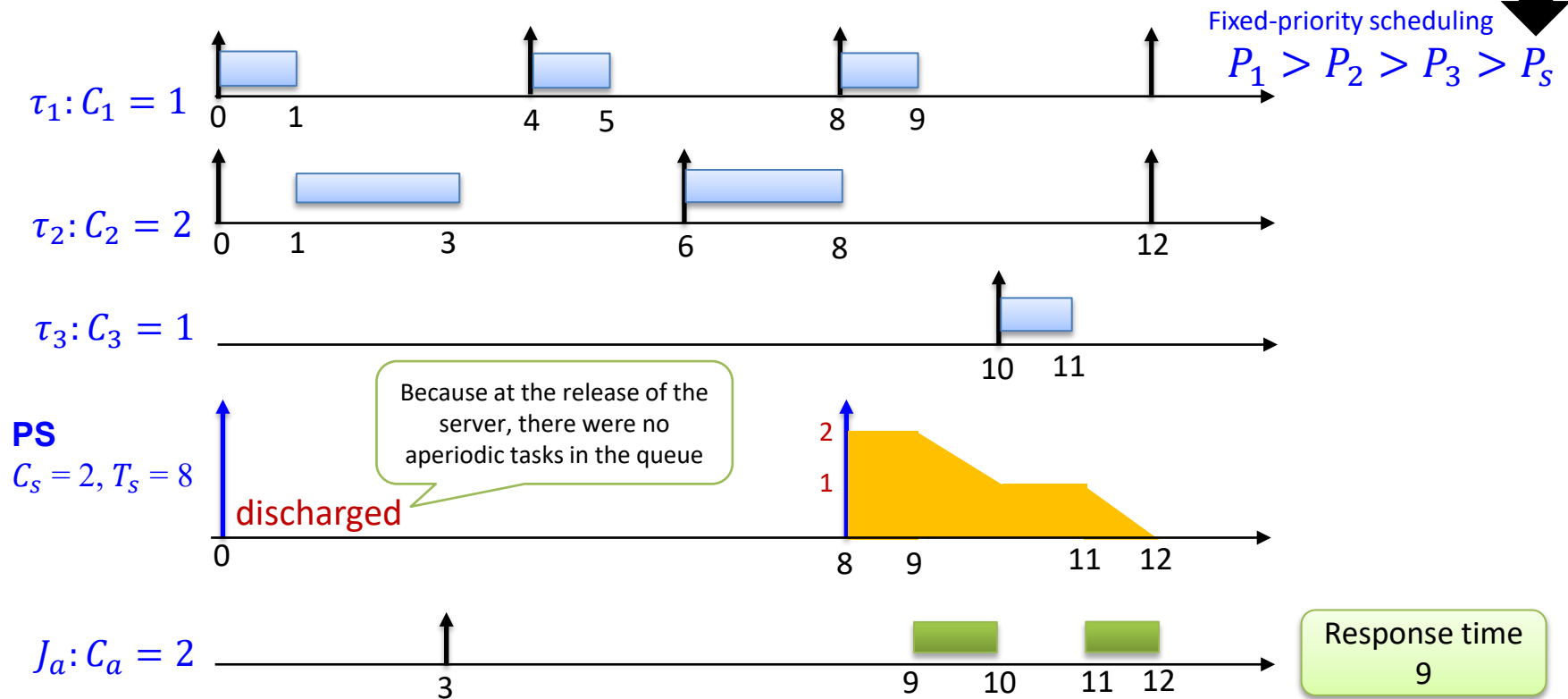
This is called **Polling Server (PS)**!  
(Invented in 1987)



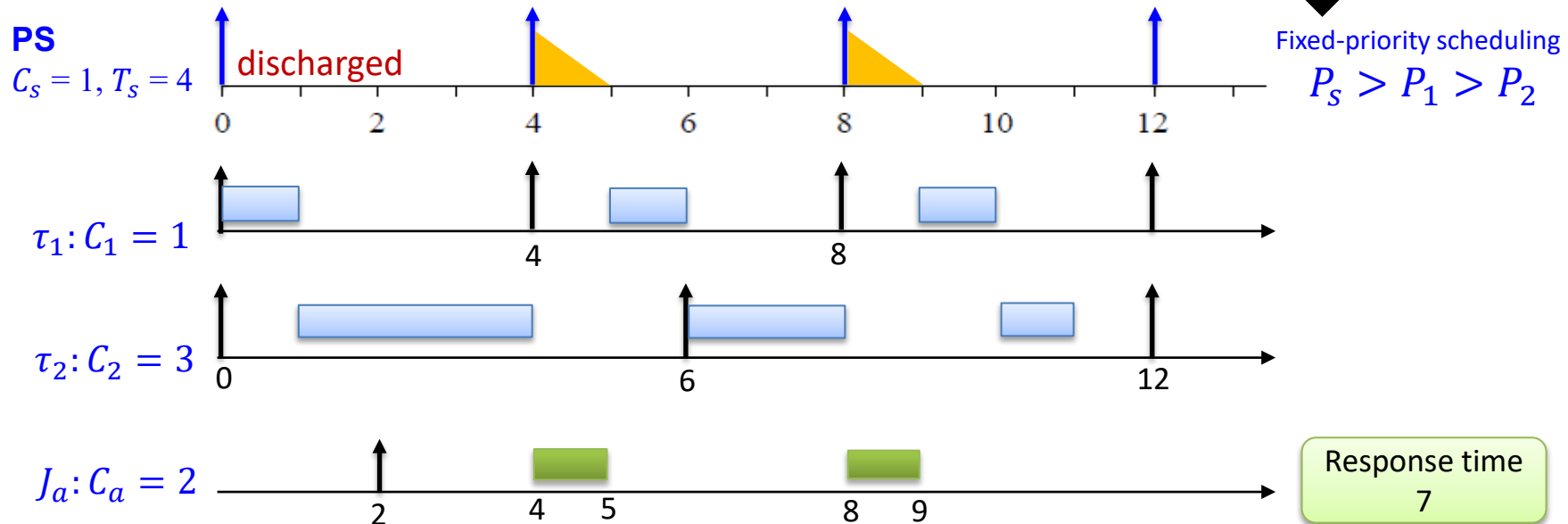
# Polling server (PS)



# Polling server (PS)



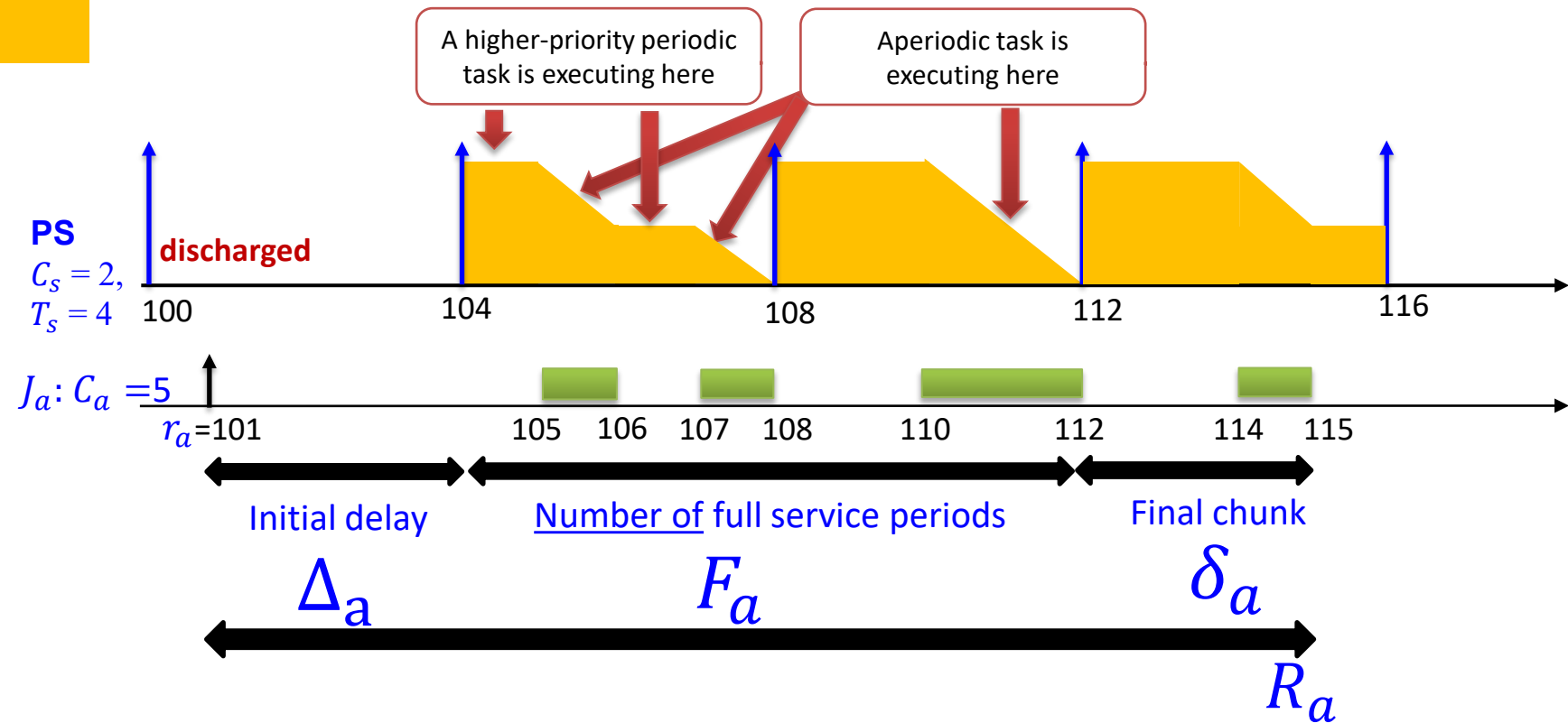
# Polling server (PS): another example



If the budget is discharged, the aperiodic task shall wait for the next time the budget is replenished.

Next, we try to formulate the WCRT of an aperiodic task that is released at time  $r_a$  and has execution time of  $C_a$  as a function of parameters of the PS (i.e.,  $C_s, T_s$ )

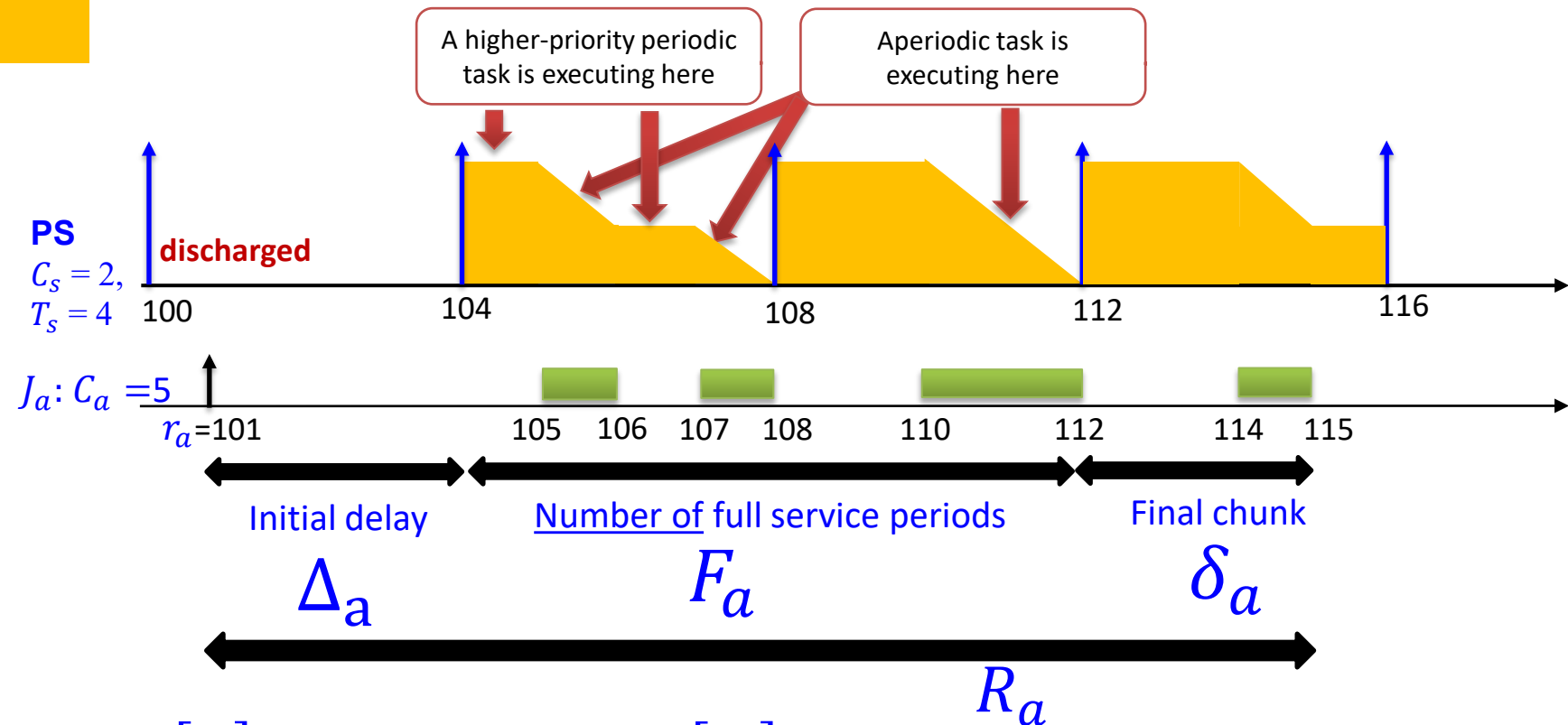
# WCRT of an aperiodic task under PS



Does the schedule of “full-service period” impact the worst-case response time of the aperiodic job?  
 (assume that the server meets its deadlines)

No, because in each release of the server, we can only execute up to  $C_s$  units of the execution time of  $J_a$ . The WCRT is affected by the “final chunk”!

# WCRT of an aperiodic task under PS



$$\Delta_a = \left\lceil \frac{r_a}{T_s} \right\rceil \cdot T_s - r_a$$

A bit pessimistic

$$F_a = \left\lfloor \frac{C_a}{C_s} \right\rfloor - 1$$

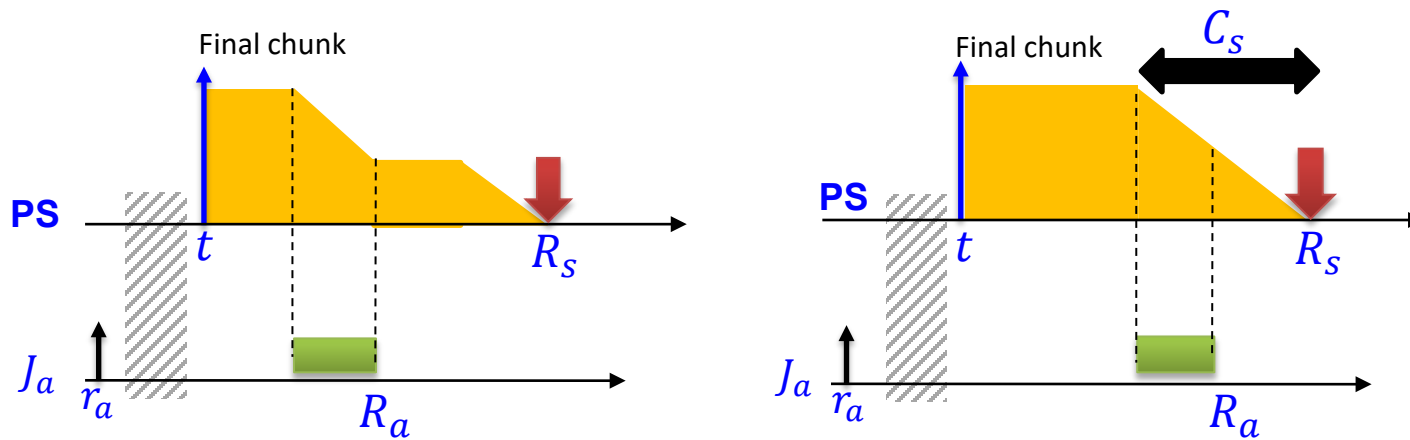
⇒ Duration of full service periods:  $F_a \cdot T_s$

$$R_a = \Delta_a + F_a \cdot T_s + \delta_a$$

# WCRT of an aperiodic task under PS

Finding  $\delta_a$

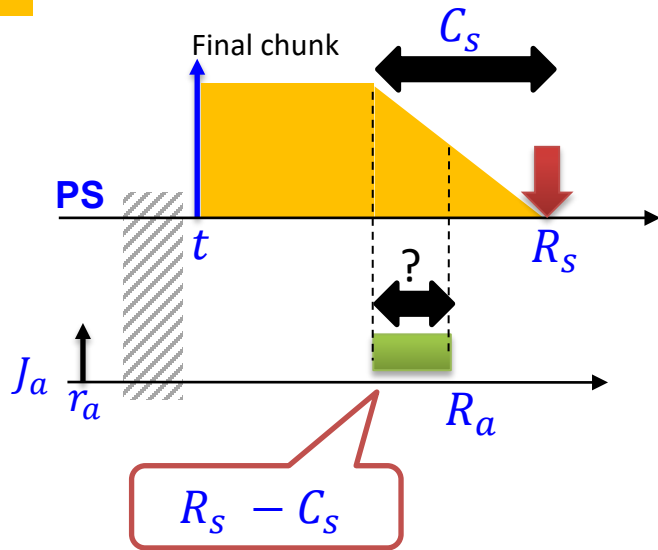
We can use the WCRT analysis (RTA) to obtain the **WCRT of the server**, denoted by  $R_s$ , (assuming that it consumes all its  $C_s$  units of budget) because a server is like a periodic task in the task set.



Now, given that we know the value of  $R_s$ ,  
which scenario creates a larger  $R_a$ ?

# WCRT of an aperiodic task under PS

Finding  $\delta_a$



The latest start time of the aperiodic job in the final chunk

$$\delta_a \leq (R_s - C_s) + (C_a - F_a C_s)$$

Remained execution time of the aperiodic task in the last chunk

$$R_a = \left\lfloor \frac{r_a}{T_s} \right\rfloor \cdot T_s - r_a + \left( \left\lfloor \frac{C_a}{C_s} \right\rfloor - 1 \right) \cdot T_s + (R_s - C_s) + C_a - F_a C_s$$

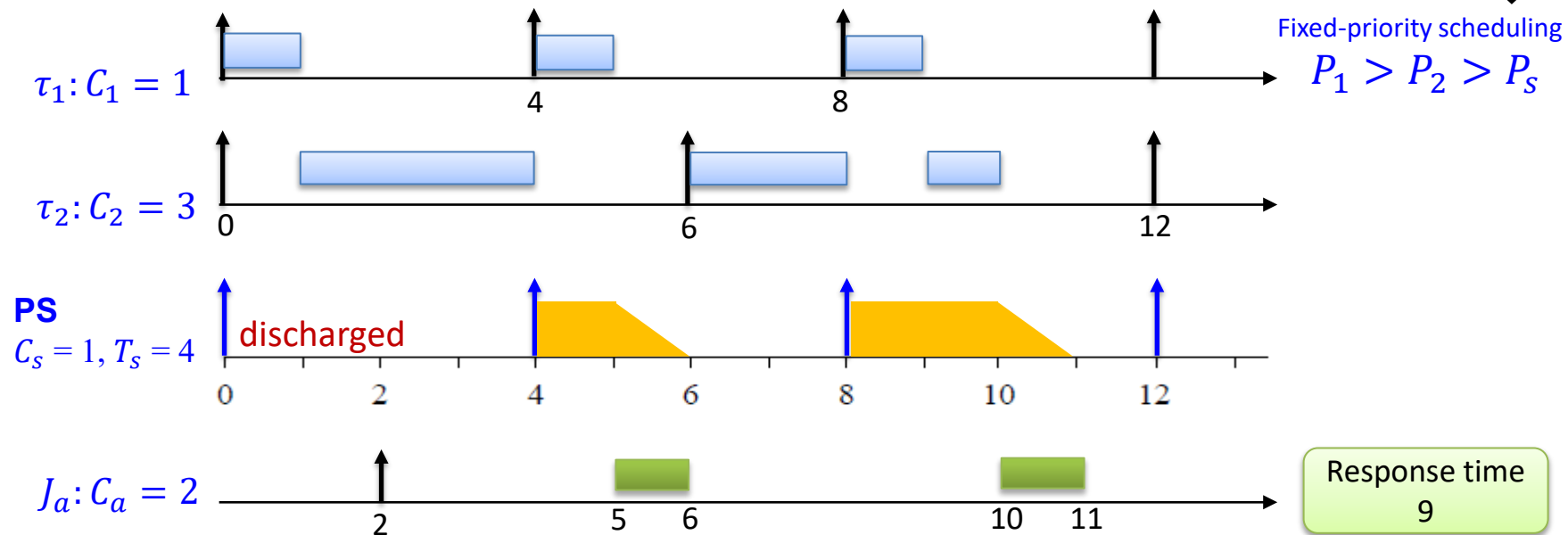




Executing aperiodic tasks with a ...

# **polling server v.s. a background service**

# Polling server v.s. background service



If the polling server has the lowest priority, can we say it is like if the aperiodic tasks are executed as a background service?

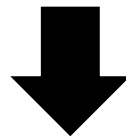
No (because the budget might be “discharged” just before the arrival of the aperiodic task)

# How to improve PS?

If aperiodic tasks come later than the release time of the server, they have to wait for the next release of the server!

How can we fix this?

Keep the budget even if there is no aperiodic task in the queue.



This is called **Deferrable Server (DS)**!

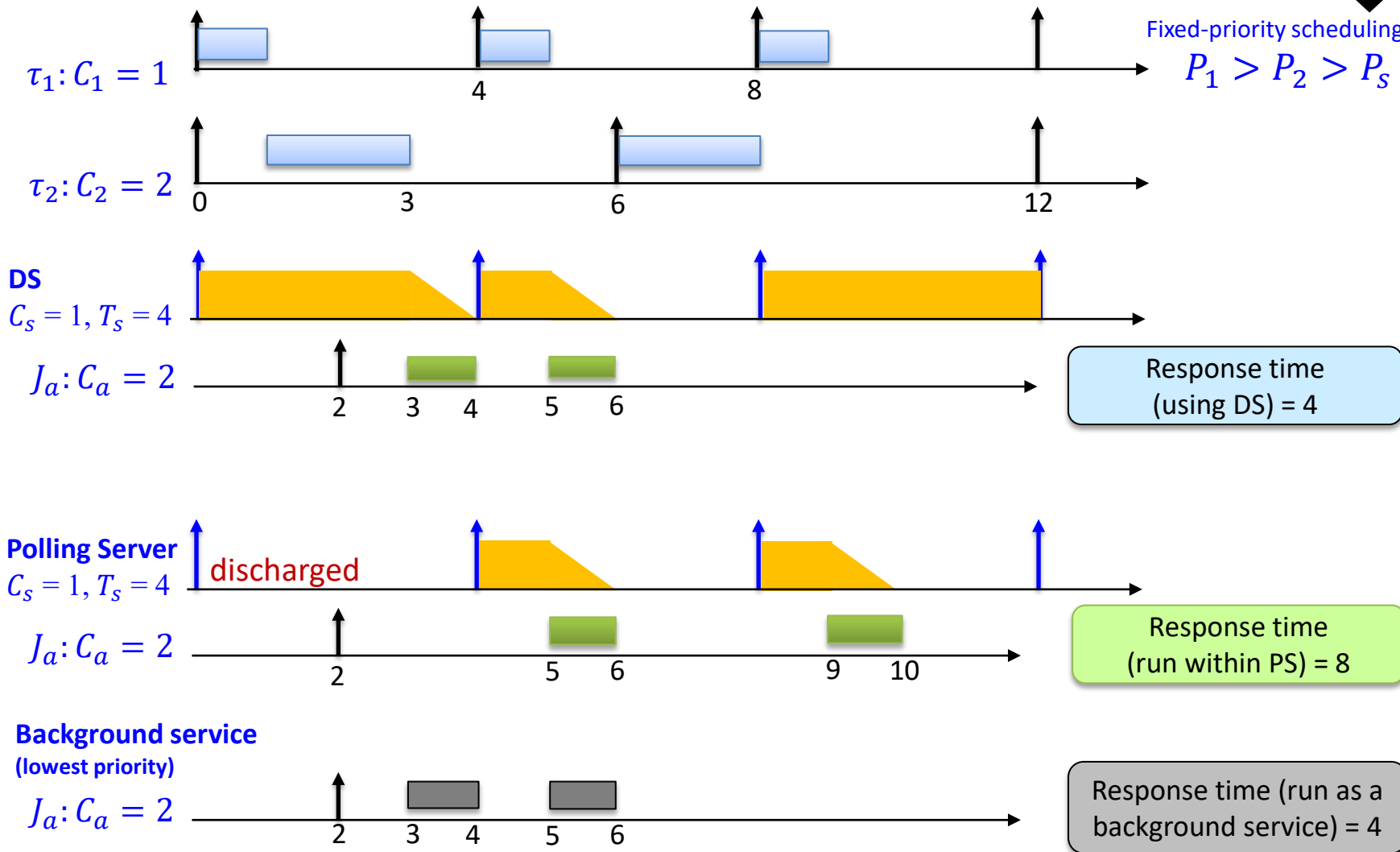
(Invented in 1987 and improved in 1995)

# Deferrable server (DS)

DS: Keep the budget even if there is no aperiodic task in the queue.

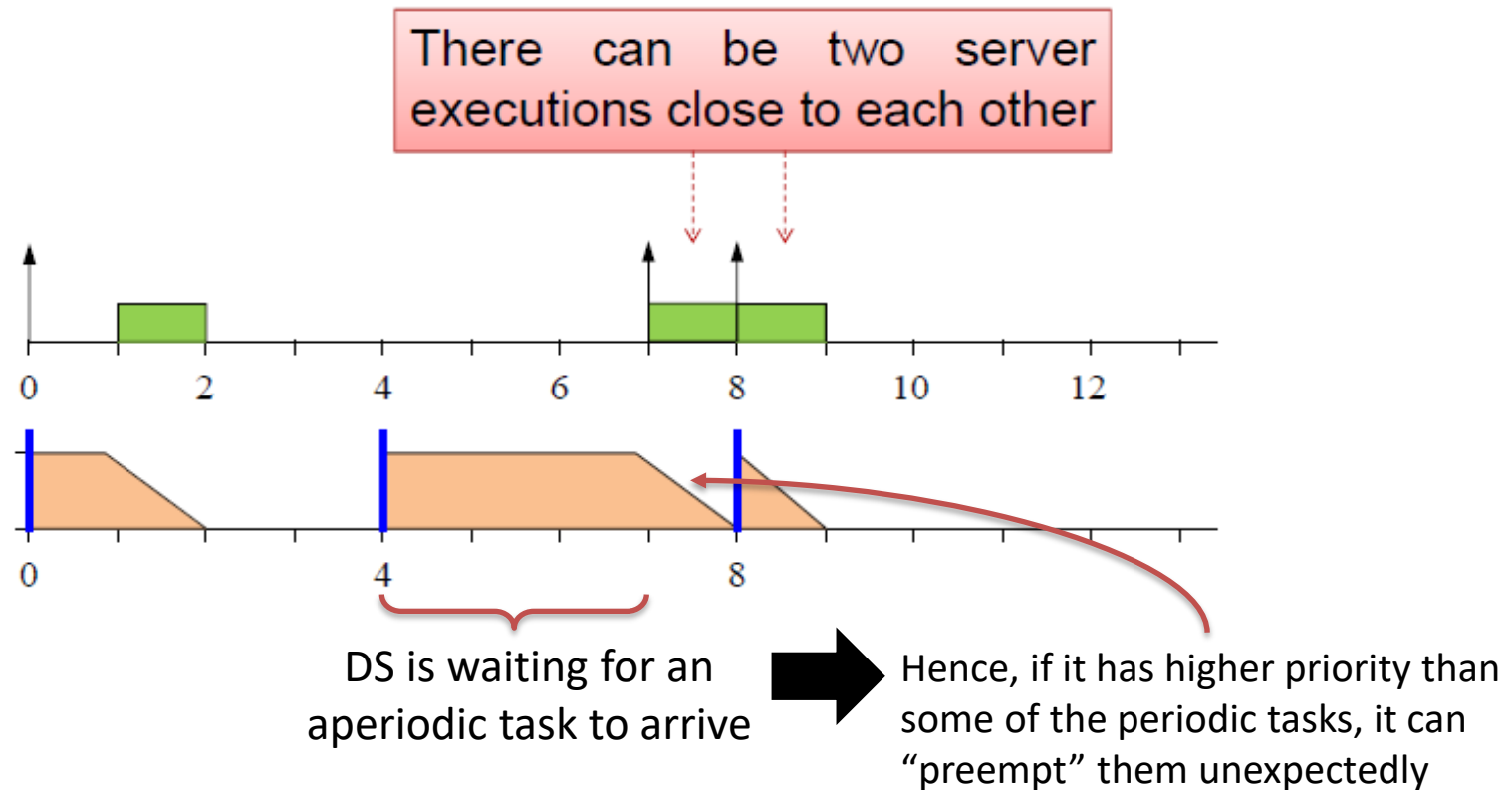


Fixed-priority scheduling  
 $P_1 > P_2 > P_s$



# Issue with DS

- DS does not behave like a periodic task. It is more invasive than PS.
- Keeping the budget decreases the schedulable utilization bound of fixed-priority scheduling.



# WCRT of periodic tasks in the presence of a DS



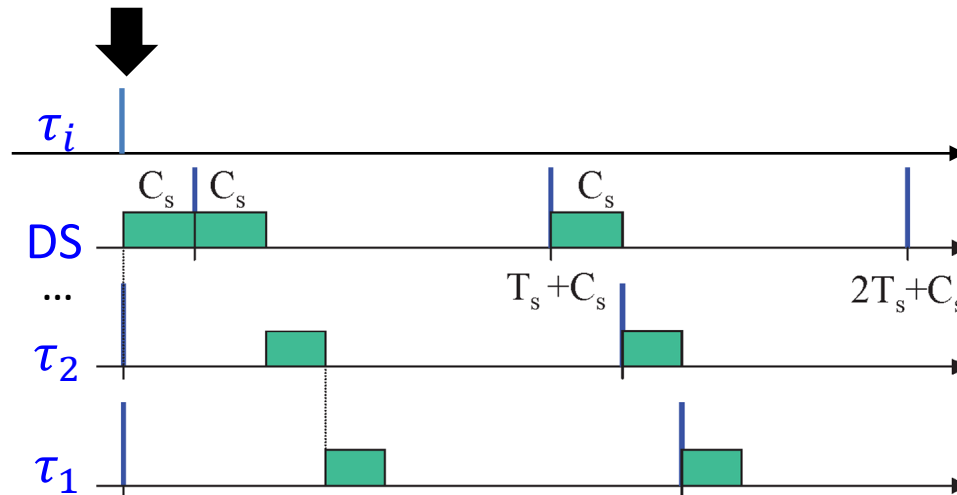
Assume we use FP with the following priorities:  $P_1 > P_2 > \dots > P_{i-1} > P_s > P_i > \dots > P_n$

Can DS impact the schedule of ANY higher-priority task?

No! DS never preempts a task with a higher priority

Can DS impact the schedule of any low-priority task?

Yes!

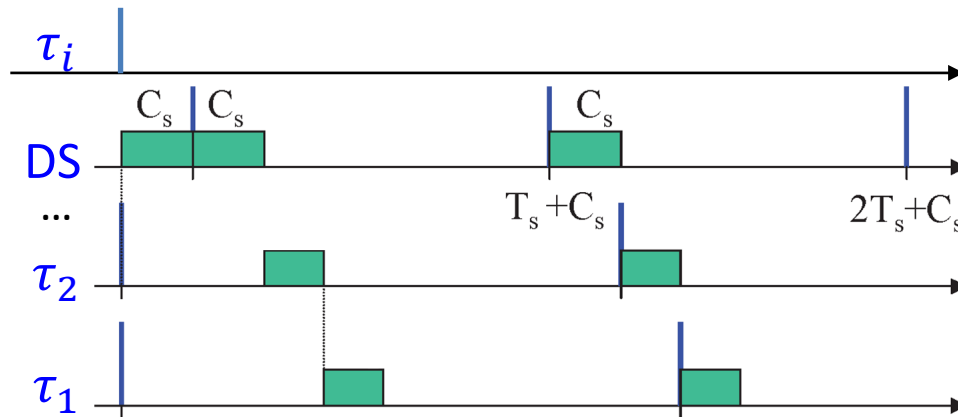


How is it different from a normal fixed-priority schedule?

# WCRT of periodic tasks in the presence of a DS



Assume we use FP with the following priorities:  $P_1 > P_2 > \dots P_{i-1} > P_s > P_i > \dots > P_n$



- The critical instance in FP is when **all higher-priority tasks are released together**.
- However, here we need to account for the previous job of DS that has not been scheduled until just before the release of  $\tau_i$

# Type of servers

- **Fixed-priority Servers**

- Periodic server (previous lecture)
- Polling server
- Deferrable server
- Sporadic server
- Slack stealer

- **Dynamic-priority Servers (to be used with EDF scheduler)**

- Dynamic Polling Server
- Dynamic Sporadic Server
- Total Bandwidth Server
- Tunable Bandwidth Server

 • **Constant Bandwidth Server**



**Implemented in Linux  
(this is the most interesting one)**



# Constant bandwidth server (CBS)

- It is a server designed to work with the EDF scheduling policy
- It keeps the “bandwidth = utilization” constant.

## CBS parameters

|                   |                          |                            |
|-------------------|--------------------------|----------------------------|
| Maximum budget:   | $Q_s$                    | } assigned by the user     |
| Server period:    | $T_s$                    |                            |
| Server bandwidth: | $U_s = Q_s/T_s$          |                            |
| Current budget:   | $q_s$ (initialized to 0) | } maintained by the server |
| Server deadline:  | $d_s$ (initialized to 0) |                            |

Constant (provided at design time)

Dynamic (varying at runtime)

# CBS idea

Replenish the budget as soon as it is finished!

↳ Allows using the resource more efficiently

However, each time you do so, increase the current deadline by the value of  $T_s$

↳ Why do we do this?

It **smoothly reduces the priority** of the current job of the server among other jobs in the system **while keeping the utilization of the server constant!**

Note: in EDF, the priority comes from the absolute deadline.

Always make sure that the server does not have a utilization larger than  $U_s$

Recall: the absolute deadline determines a job's priority in EDF

# CBS idea

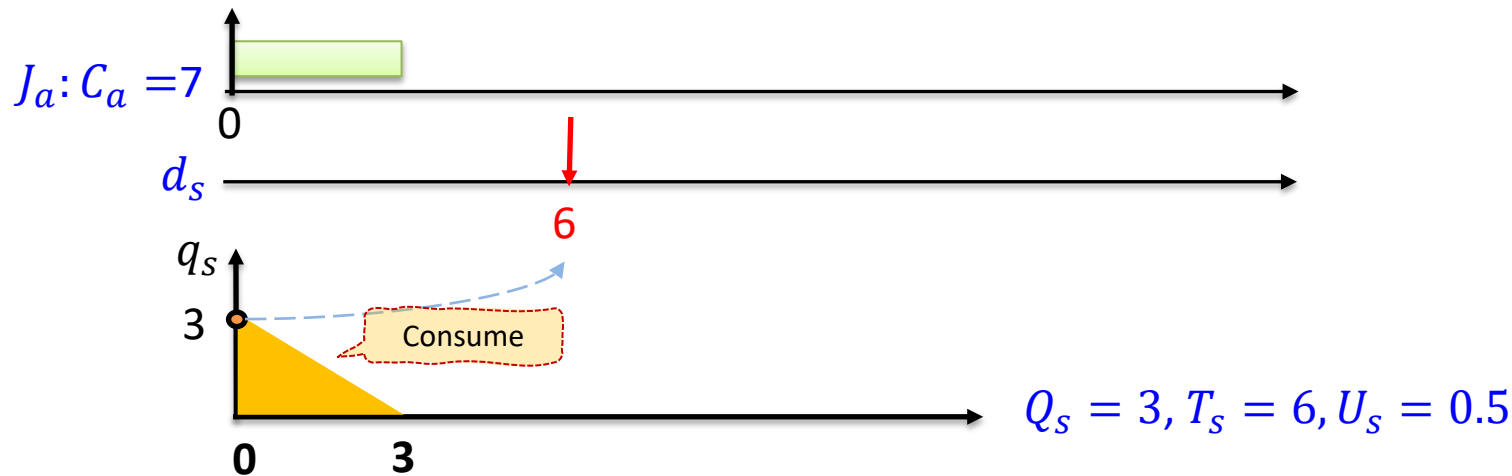
Replenish the budget as soon as it is finished!

However, each time you do so, increase the current deadline by the value of  $T_s$

Always make sure that the server does not have a utilization larger than  $U_s$

What is the benefit?

It **smoothly reduces the priority** of the current job of the server among other jobs in the system **while keeping the utilization of the server constant!**



Recall: the absolute deadline determines a job's priority in EDF

# CBS idea

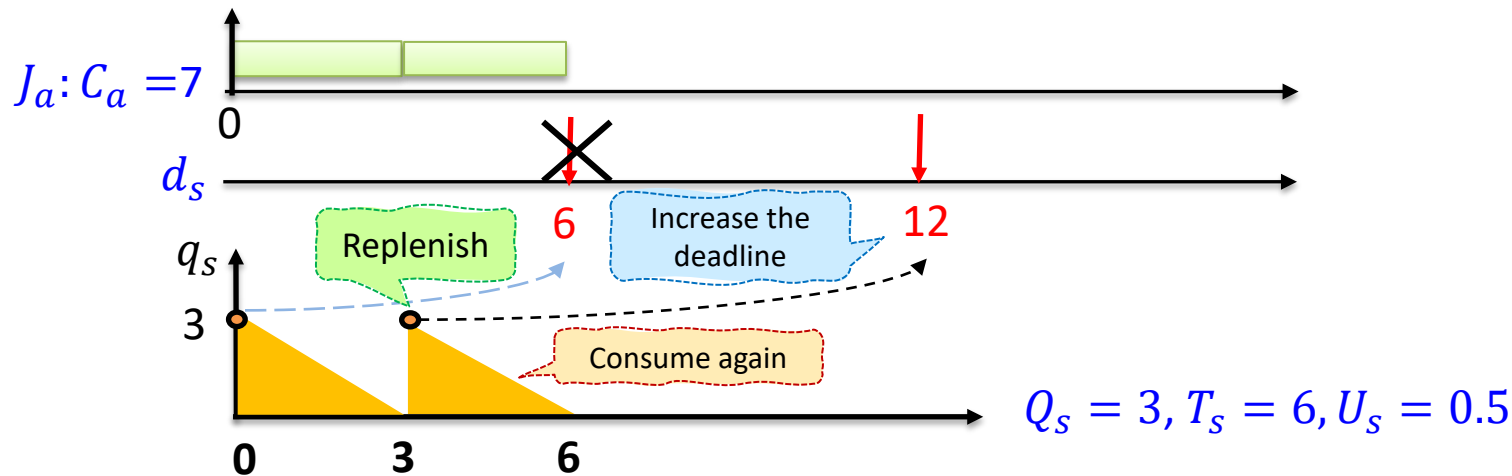
Replenish the budget as soon as it is finished!

However, each time you do so, increase the current deadline by the value of  $T_s$

Always make sure that the server does not have a utilization larger than  $U_s$

What is the benefit?

It **smoothly reduces the priority** of the current job of the server among other jobs in the system **while keeping the utilization of the server constant!**



Recall: the absolute deadline determines a job's priority in EDF

# CBS idea

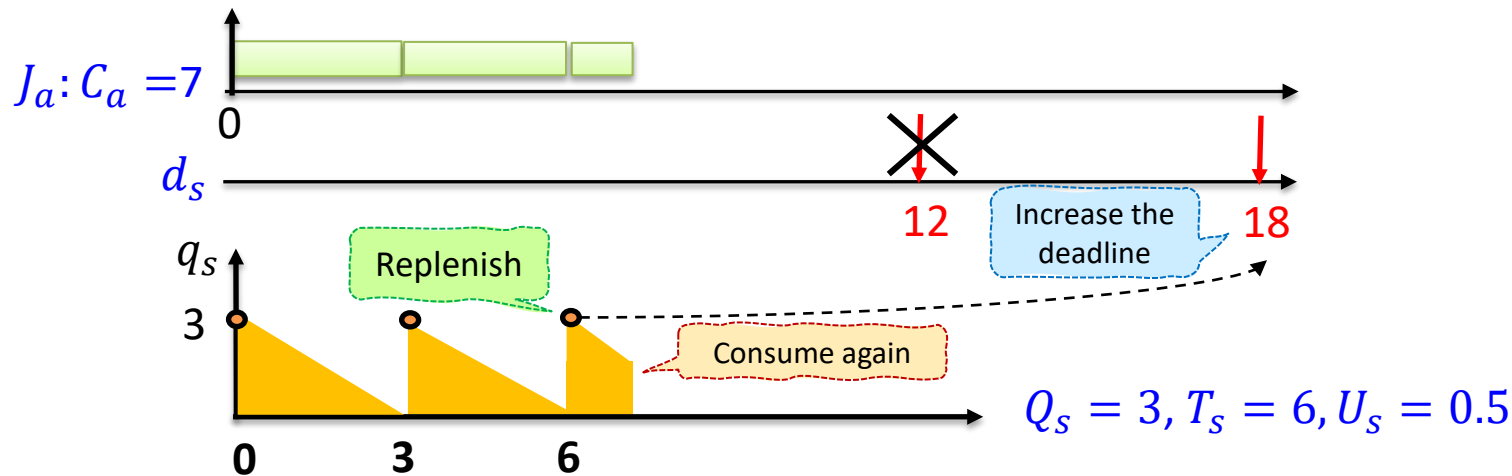
Replenish the budget as soon as it is finished!

However, each time you do so, increase the current deadline by the value of  $T_s$

Always make sure that the server does not have a utilization larger than  $U_s$

What is the benefit?

It **smoothly reduces the priority** of the current job of the server among other jobs in the system!  
**While keeping the utilization of the server constant!**



Recall: the absolute deadline determines a job's priority in EDF

# Basic CBS rules

Arrival of job  $J_k$  at time  $r_k \Rightarrow$  assign a new  $d_s$

If ( $\exists$  a pending aperiodic job) then <enqueue  $J_k$ >

else if ( $U_s < \frac{q_s}{d_s - r_k}$ ) then {

$$q_s \leftarrow Q_s$$

$$d_s \leftarrow r_k + T_s$$

} else {use the current  $q_s$  and  $d_s$ }

**Case 1:** Some jobs already waiting? Just put the new job in the queue (do nothing else)

**Case 2:** Nothing in the queue but with the current budget, we won't respect the **constant-bandwidth rule** in the interval  $[r_k, d_s]$  (namely, the remaining budget divided by the length of the interval results in a larger utilization than  $U_s$ )?

**Then** set a new budget (replenish) and set a new deadline (reset the server)

**Case 3:** Nothing is in the queue, and we respect the constant-bandwidth rule?

**Then** continue with the current budget and deadline.

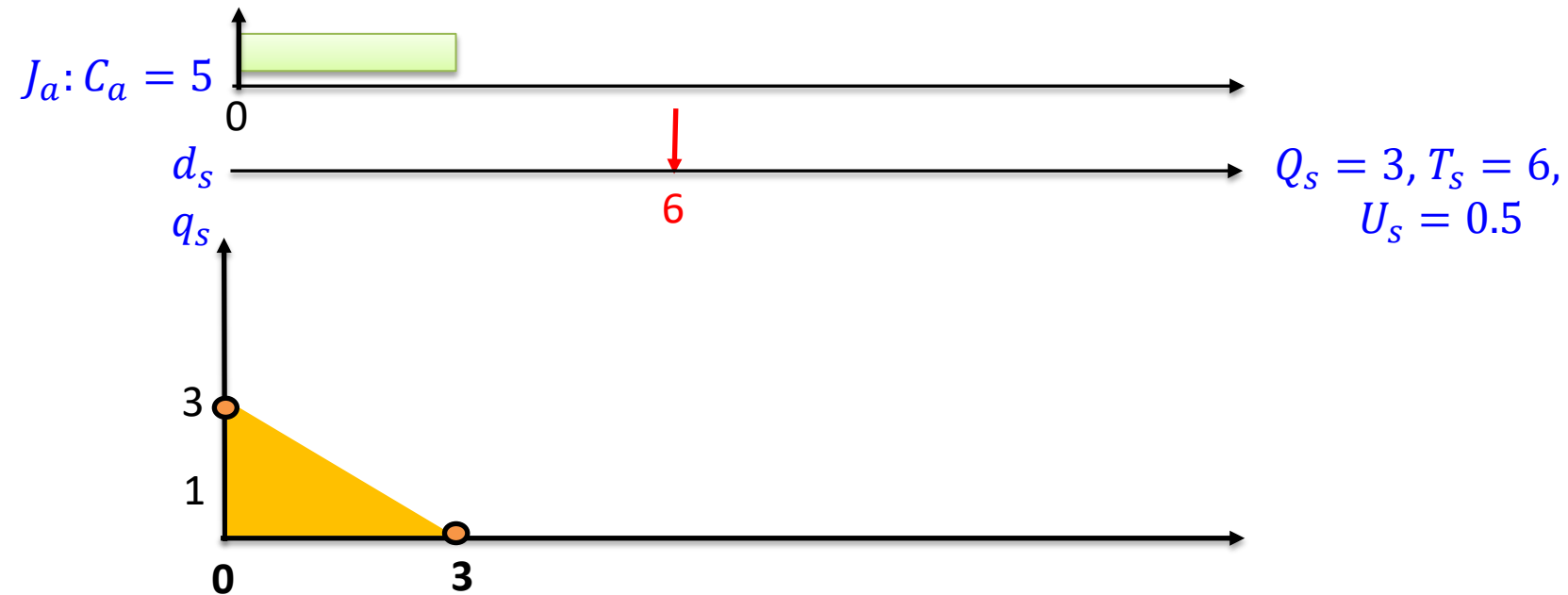
**Budget exhausted  $\Rightarrow$**   
replenish and set a new deadline

$$q_s \leftarrow Q_s$$

$$d_s \leftarrow d_s + T_s$$

# CBS budget exhaustion

$$\begin{aligned} q_s &\leftarrow Q_s \\ d_s &\leftarrow d_s + T_s \end{aligned}$$



At time 0:

What is  $d_s$ ? 6

What is  $q_s$ ? 3

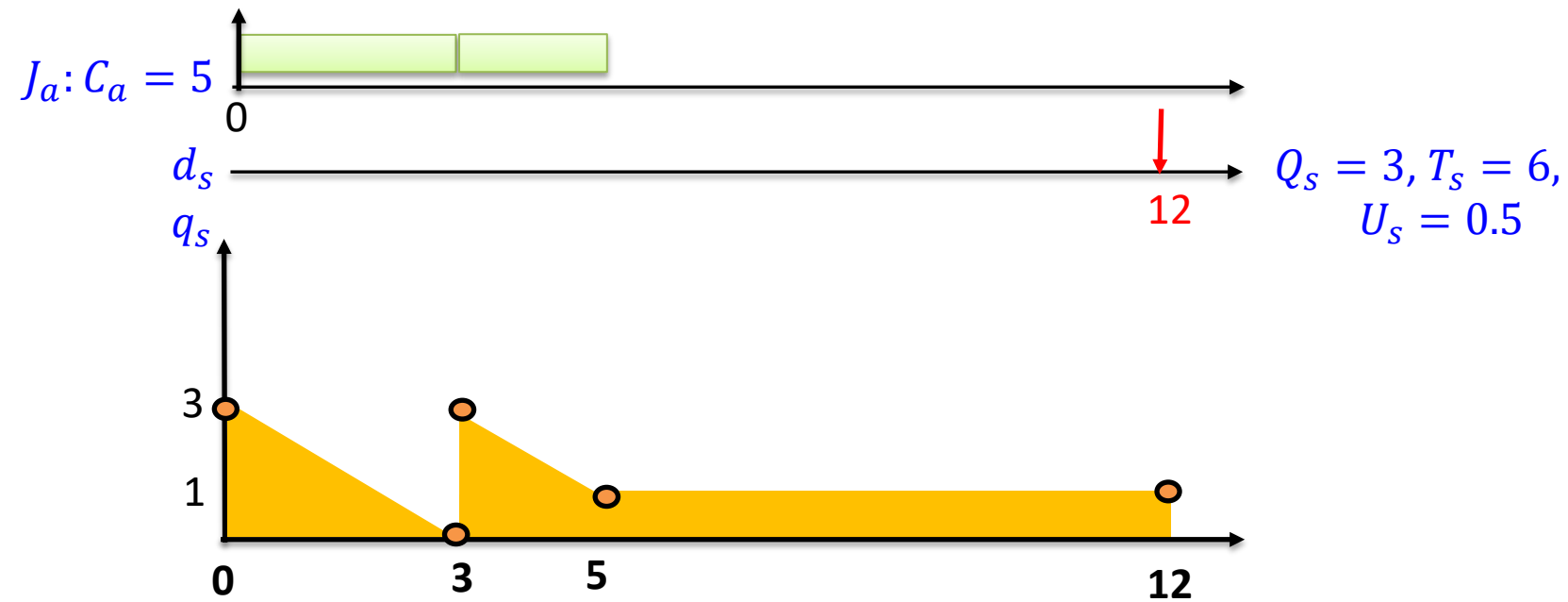
At time 3 after the budget exhausts:

What is  $d_s$ ? 12

What is  $q_s$ ? 3

# CBS budget exhaustion

$$\begin{aligned} q_s &\leftarrow Q_s \\ d_s &\leftarrow d_s + T_s \end{aligned}$$



At time 3 after the budget exhausts:

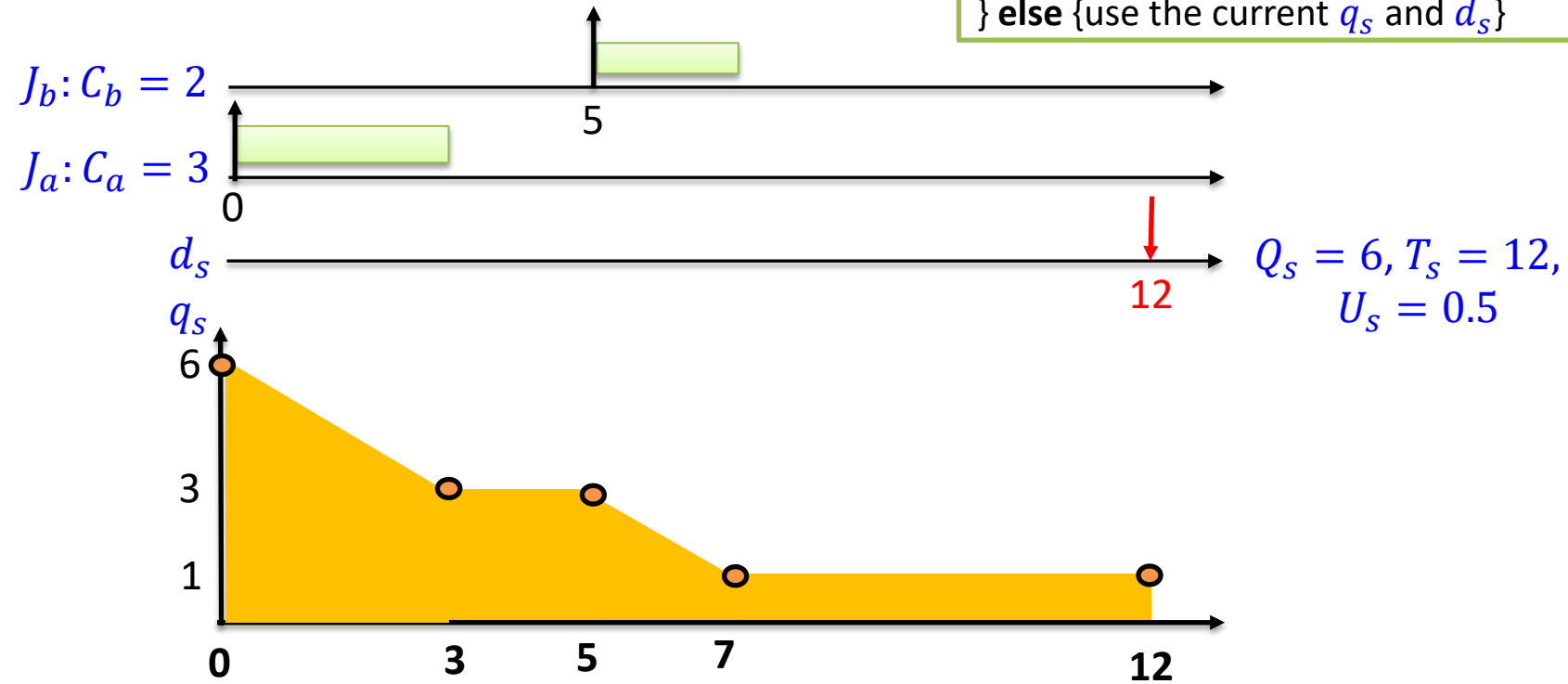
What is  $d_s$ ? 12

What is  $q_s$ ? 3



# CBS deadline assignment on job arrival

If ( $\exists$  a pending aperiodic job) then  $\langle \text{enqueue } J_k \rangle$   
 else if ( $U_s < \frac{q_s}{d_s - r_k}$ ) then {  
 $q_s \leftarrow Q_s$   
 $d_s \leftarrow r_k + T_s$   
 } else {use the current  $q_s$  and  $d_s$ }



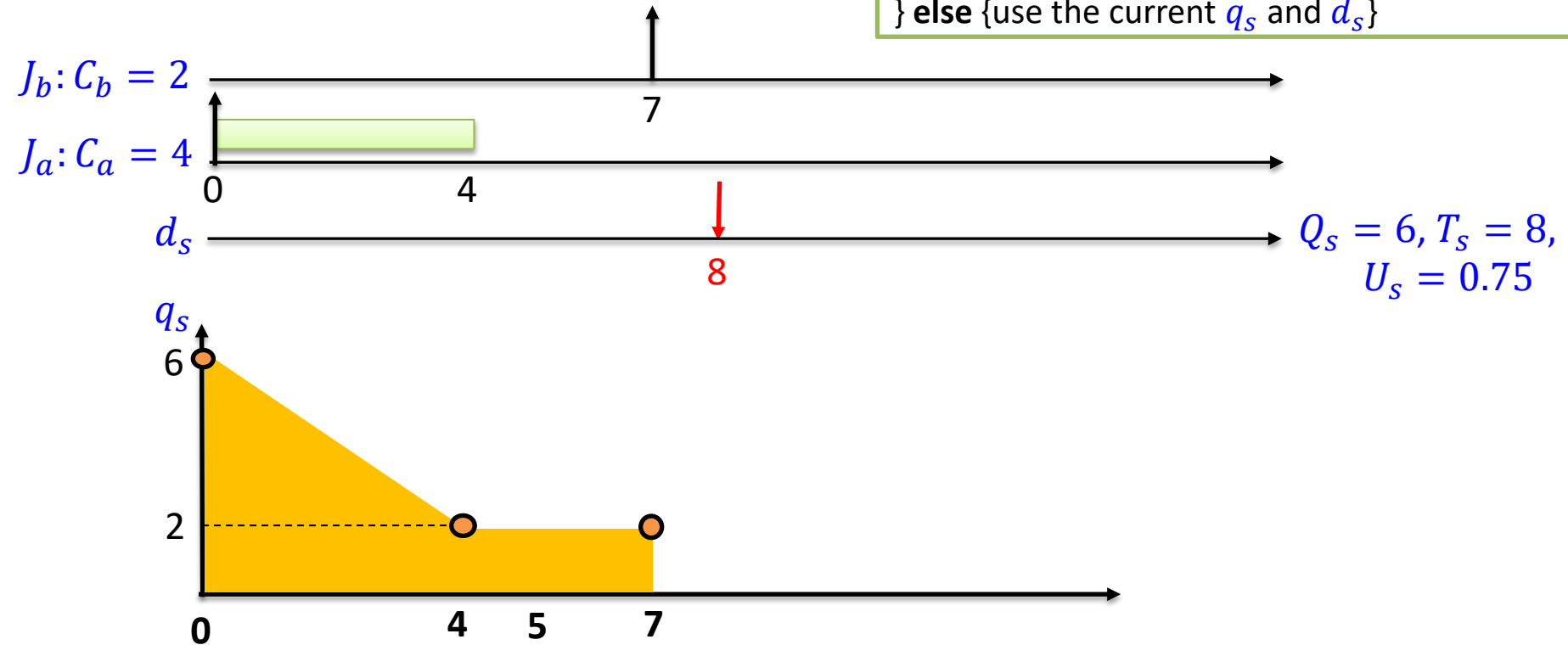
At time 0:  
 What is  $d_s$ ? 12  
 What is  $q_s$ ? 6

At time 5 after  $J_2$  arrives:  
 What is  $d_s$ ? 12  
 What is  $q_s$ ? 3

$$0.5 > 3/(12-5) = 0.375$$

# CBS deadline assignment on job arrival

If ( $\exists$  a pending aperiodic job) then  $\langle \text{enqueue } J_k \rangle$   
 else if ( $U_s < \frac{q_s}{d_s - r_k}$ ) then {  
 $q_s \leftarrow Q_s$   
 $d_s \leftarrow r_k + T_s$   
 } else {use the current  $q_s$  and  $d_s$ }



At time 0:

What is  $d_s$ ? 8

What is  $q_s$ ? 6

At time 7 after  $J_2$  arrives:

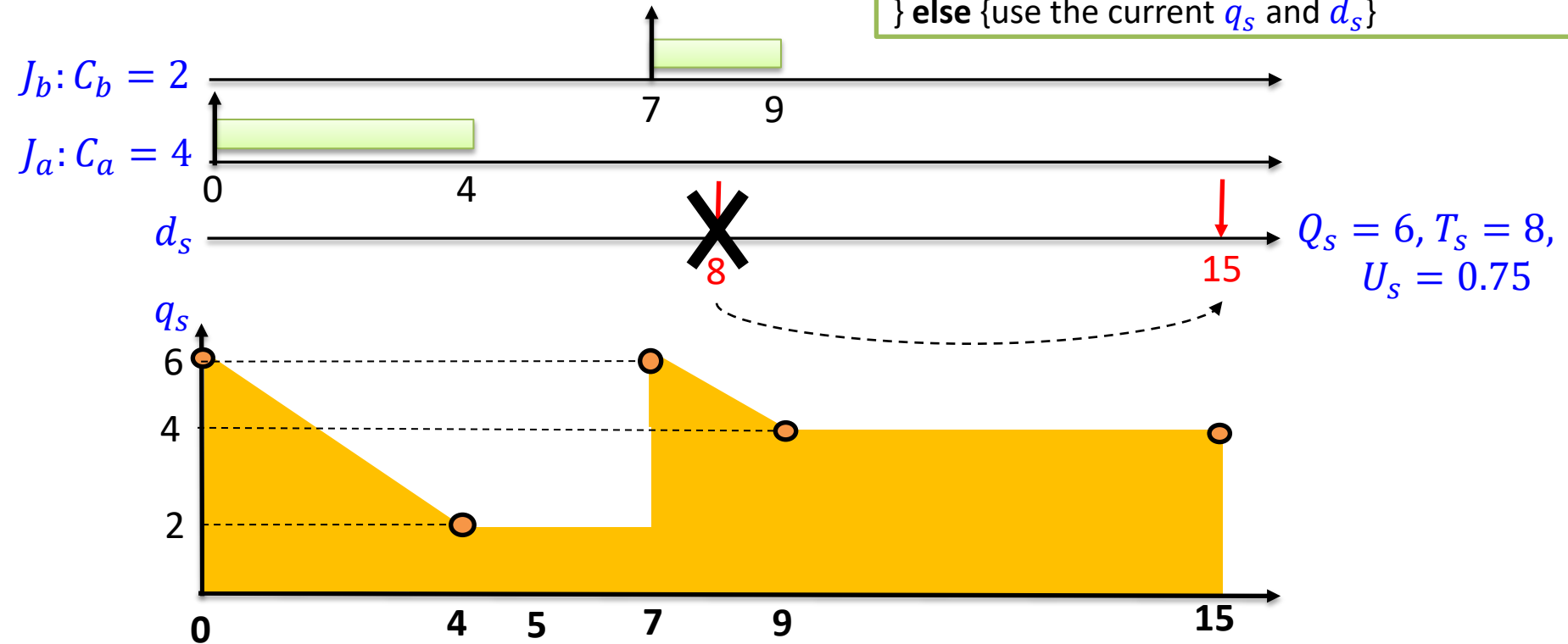
What is  $d_s$ ?  $15 = 7 + 8$

What is  $q_s$ ? 6

$0.75 < 2/(8-7)$ ? Yes. So we need to replenish the budget

# CBS deadline assignment on job arrival

If ( $\exists$  a pending aperiodic job) then  $\langle \text{enqueue } J_k \rangle$   
 else if ( $U_s < \frac{q_s}{d_s - r_k}$ ) then {  
 $q_s \leftarrow Q_s$   
 $d_s \leftarrow r_k + T_s$   
 } else {use the current  $q_s$  and  $d_s$ }



At time 0:

What is  $d_s$ ? 8

What is  $q_s$ ? 6

At time 7 after  $J_2$  arrives:

What is  $d_s$ ?  $15 = 7 + 8$

What is  $q_s$ ? 6

# Example: CBS

Aperiodic jobs:

$J_a: (r_a = 2, C_a = 3), J_b: (r_b = 12, C_b = 3)$

Server:

$Q_s = 2$  and  $T_s = 6$

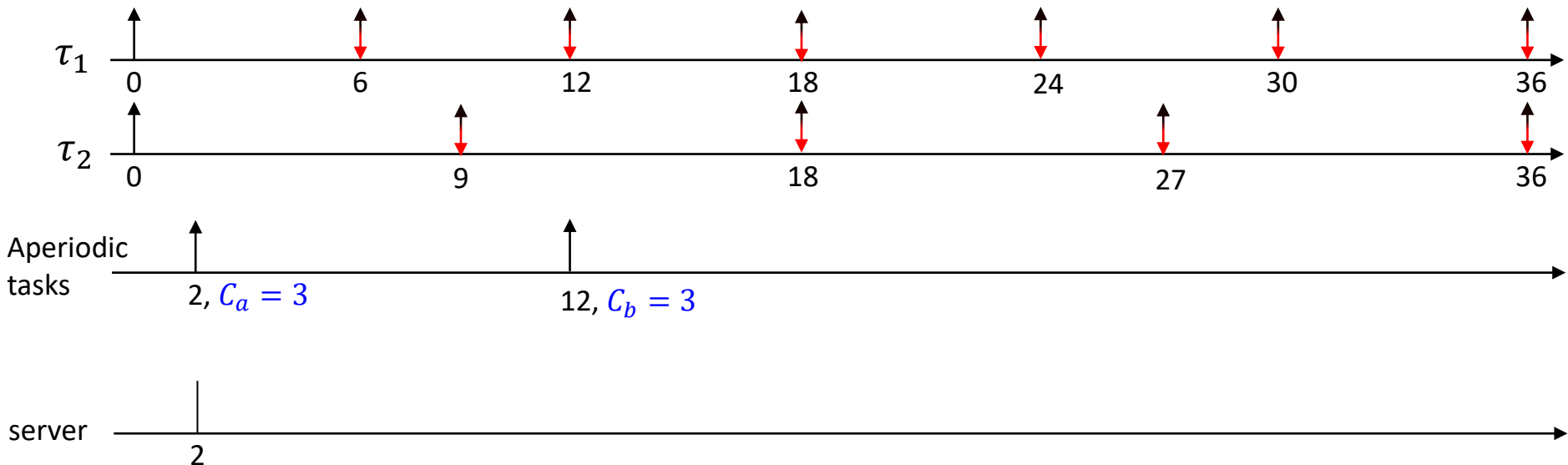
Periodic tasks:

$\tau_1: (C_1 = 2, T_1 = 6)$  and  $\tau_2: (C_2 = 3, T_2 = 9)$

If ( $\exists$  a pending aperiodic job) then  $\langle \text{enqueue } J_k \rangle$   
 else if ( $U_s < \frac{q_s}{d_s - r_k}$ ) then {  
 $q_s \leftarrow Q_s$   
 $d_s \leftarrow r_k + T_s$   
 } else {use the current  $q_s$  and  $d_s$ }

**Exhaustion:**

$q_s \leftarrow Q_s$   
 $d_s \leftarrow d_s + T_s$



# Example: CBS

**Aperiodic jobs:**

$J_a: (r_a = 2, C_a = 3), J_b: (r_b = 12, C_b = 3)$

**Server:**

$Q_s = 2$  and  $T_s = 6$

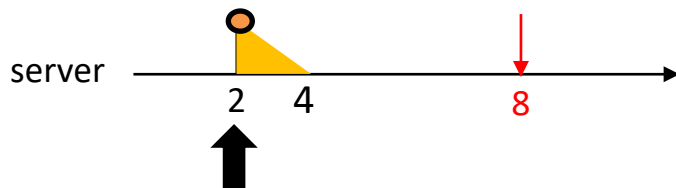
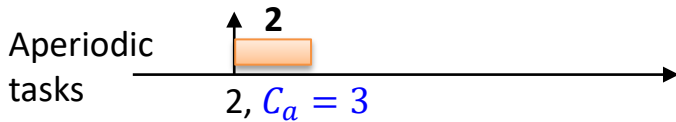
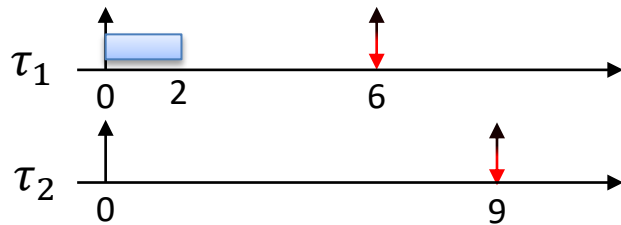
**Periodic tasks:**

$\tau_1: (C_1 = 2, T_1 = 6)$  and  $\tau_2: (C_2 = 3, T_2 = 9)$

If ( $\exists$  a pending aperiodic job) then  $\langle \text{enqueue } J_k \rangle$   
 else if ( $U_s < \frac{q_s}{d_s - r_k}$ ) then {  
      $q_s \leftarrow Q_s$   
      $d_s \leftarrow r_k + T_s$   
 } else {use the current  $q_s$  and  $d_s$ }

**Exhaustion:**

$q_s \leftarrow Q_s$   
 $d_s \leftarrow d_s + T_s$



**What are  $d_s$  and  $q_s$  at time 2 right after the arrival of  $J_a$ ?**

$d_s = 2 + 6 = 8$

$q_s = 2$

**Which task will be scheduled at time 2?**

$J_a$  because its deadline is smaller than  $\tau_2$ 's deadline.

**What happens at time 4?**

The budget has exhausted. Server must be updated.

# Example: CBS

Aperiodic jobs:

$J_a: (r_a = 2, C_a = 3), J_b: (r_b = 12, C_b = 3)$

Server:

$Q_s = 2$  and  $T_s = 6$

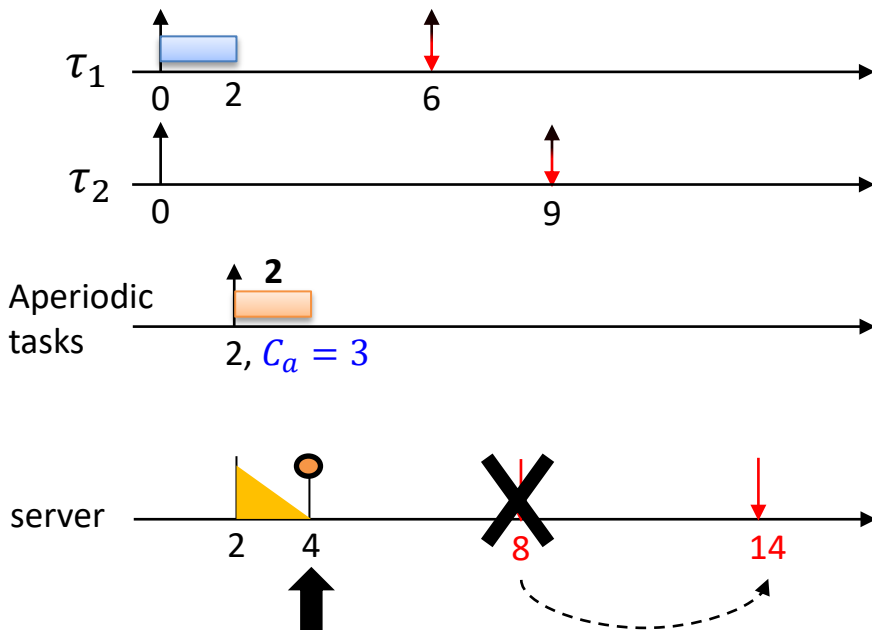
Periodic tasks:

$\tau_1: (C_1 = 2, T_1 = 6)$  and  $\tau_2: (C_2 = 3, T_2 = 9)$

If ( $\exists$  a pending aperiodic job) then  $\langle \text{enqueue } J_k \rangle$   
 else if ( $U_s < \frac{q_s}{d_s - r_k}$ ) then {  
 $q_s \leftarrow Q_s$   
 $d_s \leftarrow r_k + T_s$   
 } else {use the current  $q_s$  and  $d_s$ }

**Exhaustion:**

$q_s \leftarrow Q_s$   
 $d_s \leftarrow d_s + T_s$



**Which task will be scheduled at time 4?**

$\tau_2$  because it has an earlier deadline than the server (i.e.,  $d_s > d_{2,1}$ ).

# Example: CBS

Aperiodic jobs:

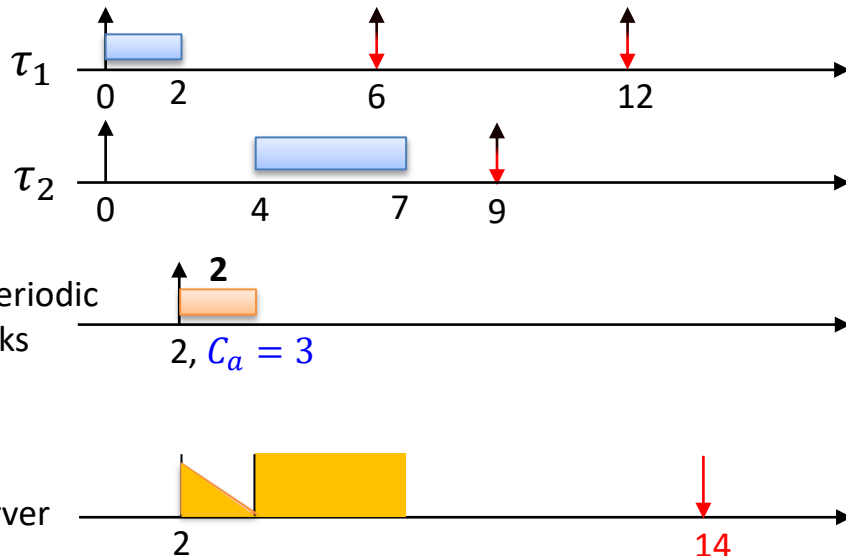
$$J_a: (r_a = 2, C_a = 3), J_b: (r_b = 12, C_b = 3)$$

Server:

$$Q_s = 2 \text{ and } T_s = 6$$

Periodic tasks:

$$\tau_1: (C_1 = 2, T_1 = 6) \text{ and } \tau_2: (C_2 = 3, T_2 = 9)$$



**Which task will be scheduled at time 7?**

$\tau_1$  because it has an earlier deadline than the server (i.e.,  $d_s > d_{1,2}$ ).

If ( $\exists$  a pending aperiodic job) then  $\langle \text{enqueue } J_k \rangle$   
 else if ( $U_s < \frac{q_s}{d_s - r_k}$ ) then {  
 $q_s \leftarrow Q_s$   
 $d_s \leftarrow r_k + T_s$   
 } else {use the current  $q_s$  and  $d_s$ }

**Exhaustion:**

$$q_s \leftarrow Q_s$$

$$d_s \leftarrow d_s + T_s$$

# Example: CBS

Aperiodic jobs:

$J_a: (r_a = 2, C_a = 3), J_b: (r_b = 12, C_b = 3)$

Server:

$Q_s = 2$  and  $T_s = 6$

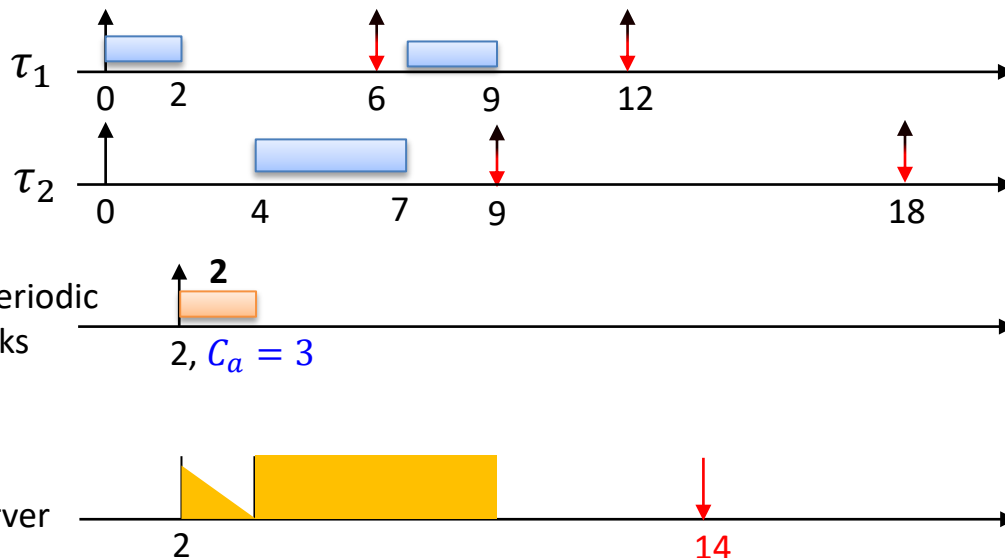
Periodic tasks:

$\tau_1: (C_1 = 2, T_1 = 6)$  and  $\tau_2: (C_2 = 3, T_2 = 9)$

If ( $\exists$  a pending aperiodic job) then  $\langle \text{enqueue } J_k \rangle$   
 else if ( $U_s < \frac{q_s}{d_s - r_k}$ ) then {  
 $q_s \leftarrow Q_s$   
 $d_s \leftarrow r_k + T_s$   
 } else {use the current  $q_s$  and  $d_s$ }

**Exhaustion:**

$q_s \leftarrow Q_s$   
 $d_s \leftarrow d_s + T_s$



**Which task will be scheduled at time 9?**

$J_a$  because it has an earlier deadline than  $\tau_2$  (i.e.,  $d_s < d_{2,2}$ ).

**Until when  $J_a$  will be scheduled using the current server parameters?**

Until time 10 because it has only 1 units of remained execution time.



# Example: CBS

**Aperiodic jobs:**

$J_a: (r_a = 2, C_a = 3), J_b: (r_b = 12, C_b = 3)$

**Server:**

$Q_s = 2$  and  $T_s = 6$

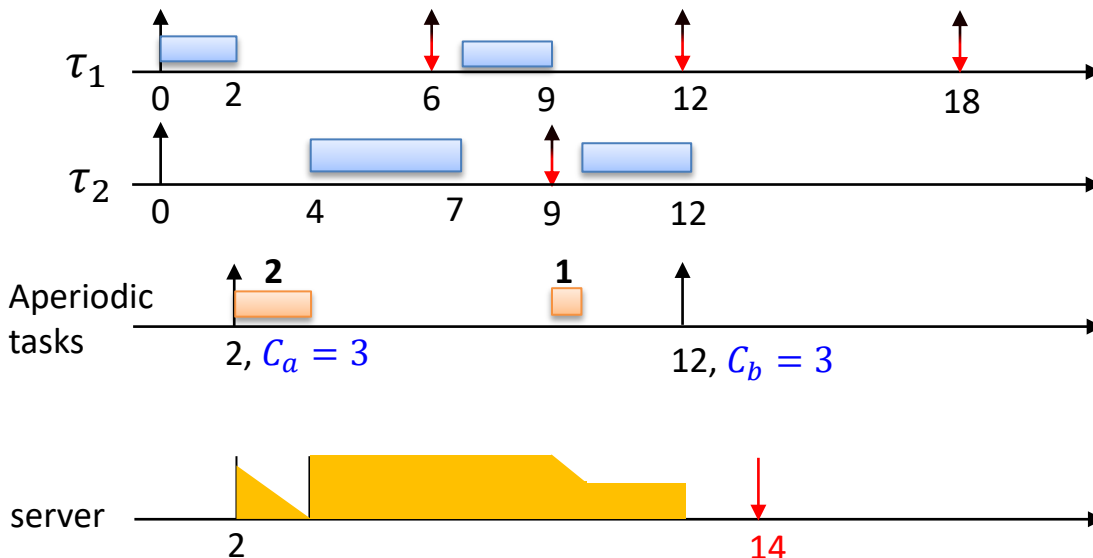
**Periodic tasks:**

$\tau_1: (C_1 = 2, T_1 = 6)$  and  $\tau_2: (C_2 = 3, T_2 = 9)$

If ( $\exists$  a pending aperiodic job) then  $\langle \text{enqueue } J_k \rangle$   
 else if ( $U_s < \frac{q_s}{d_s - r_k}$ ) then {  
 $q_s \leftarrow Q_s$   
 $d_s \leftarrow r_k + T_s$   
 } else {use the current  $q_s$  and  $d_s$ }

**Exhaustion:**

$q_s \leftarrow Q_s$   
 $d_s \leftarrow d_s + T_s$



# Example: CBS

Aperiodic jobs:

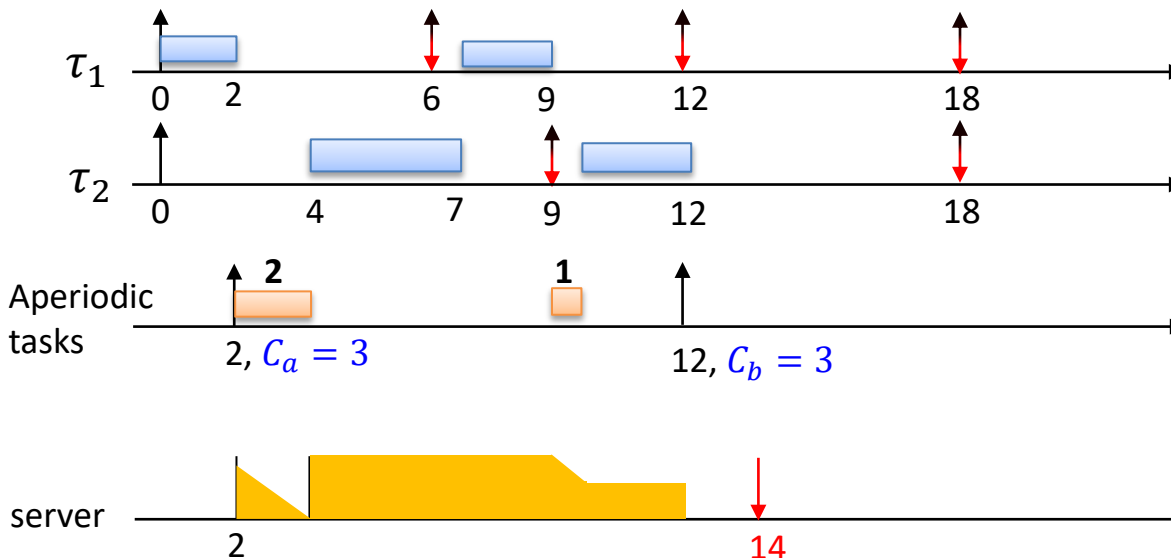
$$J_a: (r_a = 2, C_a = 3), J_b: (r_b = 12, C_b = 3)$$

Server:

$$Q_s = 2 \text{ and } T_s = 6$$

Periodic tasks:

$$\tau_1: (C_1 = 2, T_1 = 6) \text{ and } \tau_2: (C_2 = 3, T_2 = 9)$$



If ( $\exists$  a pending aperiodic job) then  $\langle \text{enqueue } J_k \rangle$   
 else if ( $U_s < \frac{q_s}{d_s - r_k}$ ) then {  
 $q_s \leftarrow Q_s$   
 $d_s \leftarrow r_k + T_s$   
 } else {use the current  $q_s$  and  $d_s$ }

**Exhaustion:**

$$q_s \leftarrow Q_s$$

$$d_s \leftarrow d_s + T_s$$

**What are the parameters of the server after the arrival of  $J_b$ ?**

$$d_s = 12 + 6 = 18$$

$$q_s = 2$$

Because at time 12, we have  $1/(14-12) = 0.5 > 0.33$

Hence, we need to replenish the server.

# Example: CBS

Aperiodic jobs:

$J_a: (r_a = 2, C_a = 3), J_b: (r_b = 12, C_b = 3)$

Server:

$Q_s = 2$  and  $T_s = 6$

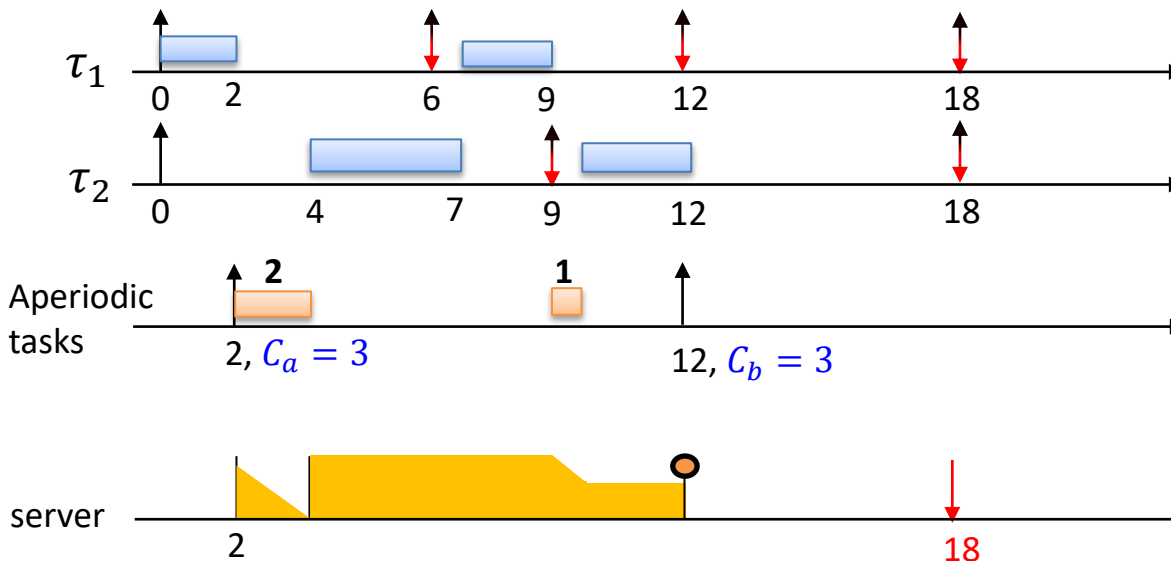
Periodic tasks:

$\tau_1: (C_1 = 2, T_1 = 6)$  and  $\tau_2: (C_2 = 3, T_2 = 9)$

If ( $\exists$  a pending aperiodic job) then  $\langle \text{enqueue } J_k \rangle$   
 else if ( $U_s < \frac{q_s}{d_s - r_k}$ ) then {  
 $q_s \leftarrow Q_s$   
 $d_s \leftarrow r_k + T_s$   
 } else {use the current  $q_s$  and  $d_s$ }

**Exhaustion:**

$q_s \leftarrow Q_s$   
 $d_s \leftarrow d_s + T_s$



**Which job will be scheduled at time 12?**

$J_b$  because the server wins all ties on deadlines

# Example: CBS

Aperiodic jobs:

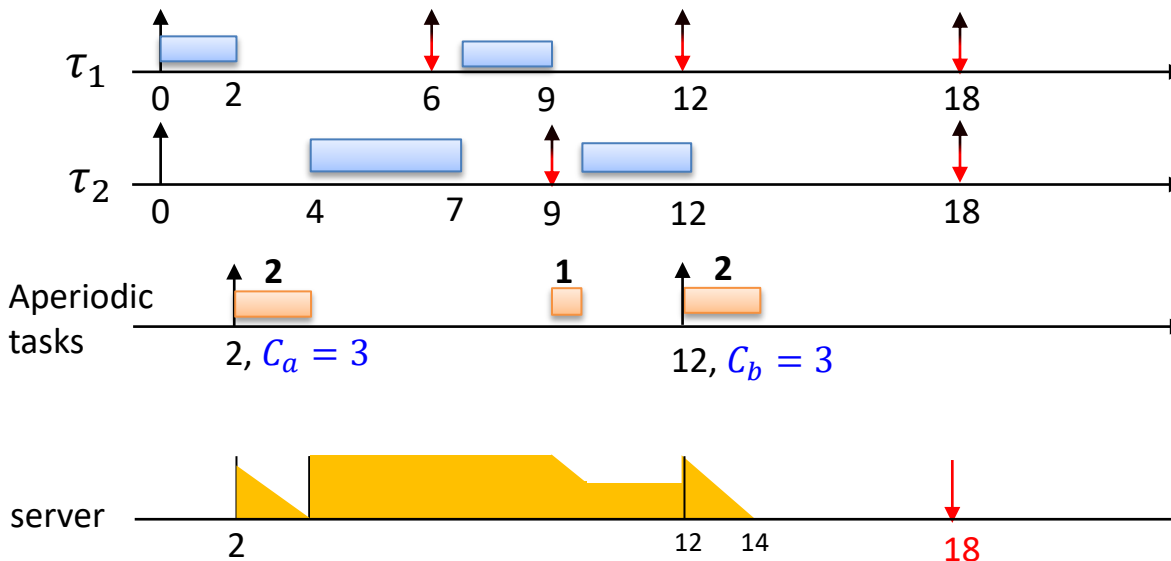
$$J_a: (r_a = 2, C_a = 3), J_b: (r_b = 12, C_b = 3)$$

Server:

$$Q_s = 2 \text{ and } T_s = 6$$

Periodic tasks:

$$\tau_1: (C_1 = 2, T_1 = 6) \text{ and } \tau_2: (C_2 = 3, T_2 = 9)$$



If ( $\exists$  a pending aperiodic job) then  $\langle \text{enqueue } J_k \rangle$   
 else if ( $U_s < \frac{q_s}{d_s - r_k}$ ) then {  
 $q_s \leftarrow Q_s$   
 $d_s \leftarrow r_k + T_s$   
 } else {use the current  $q_s$  and  $d_s$ }

**Exhaustion:**

$$q_s \leftarrow Q_s$$

$$d_s \leftarrow d_s + T_s$$

**What are the parameters of the server after being exhausted at time 14?**

$$d_s = 18 + 6 = 24$$

$$q_s = 2$$

# Example: CBS

Aperiodic jobs:

$J_a: (r_a = 2, C_a = 3), J_b: (r_b = 12, C_b = 3)$

Server:

$Q_s = 2$  and  $T_s = 6$

Periodic tasks:

$\tau_1: (C_1 = 2, T_1 = 6)$  and  $\tau_2: (C_2 = 3, T_2 = 9)$

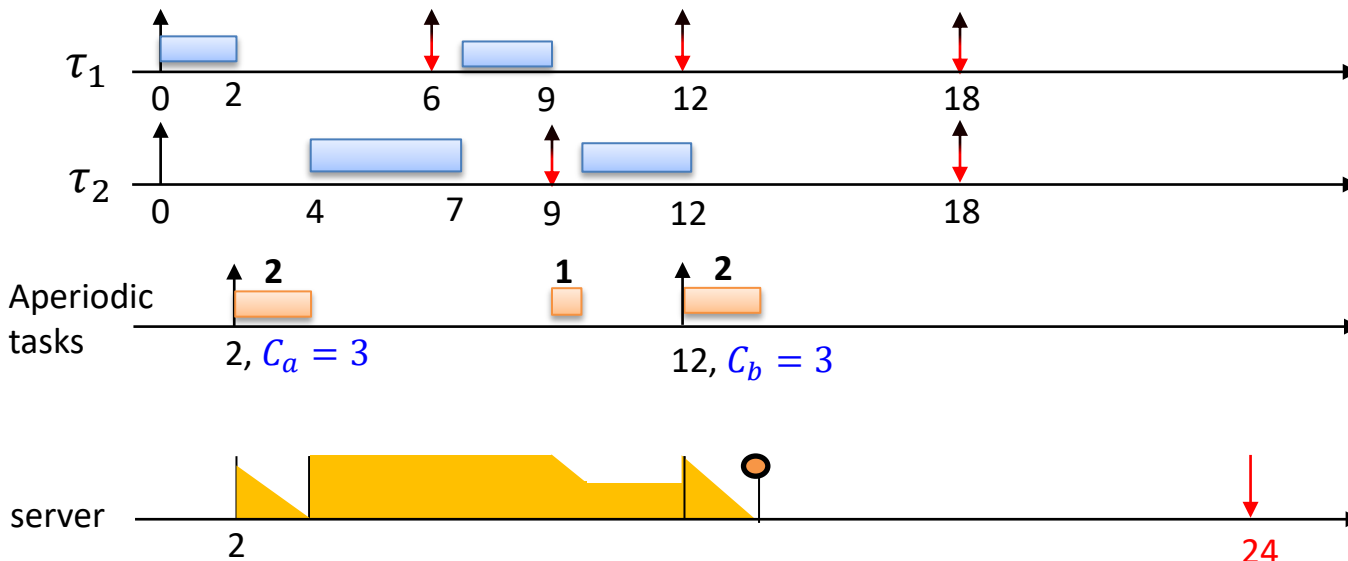
If ( $\exists$  a pending aperiodic job) then  $\langle \text{enqueue } J_k \rangle$   
 else if ( $U_s < \frac{q_s}{d_s - r_k}$ ) then {  
 $q_s \leftarrow Q_s$   
 $d_s \leftarrow r_k + T_s$   
 } else {use the current  $q_s$  and  $d_s$ }

**Exhaustion:**

$q_s \leftarrow Q_s$   
 $d_s \leftarrow d_s + T_s$

**Which job will be scheduled at time 14?**

$J_{1,3}$  because it has an earlier deadline  
 and then  $J_{2,2}$



# Example: CBS

Aperiodic jobs:

$$J_a: (r_a = 2, C_a = 3), J_b: (r_b = 12, C_b = 3)$$

Server:

$$Q_s = 2 \text{ and } T_s = 6$$

Periodic tasks:

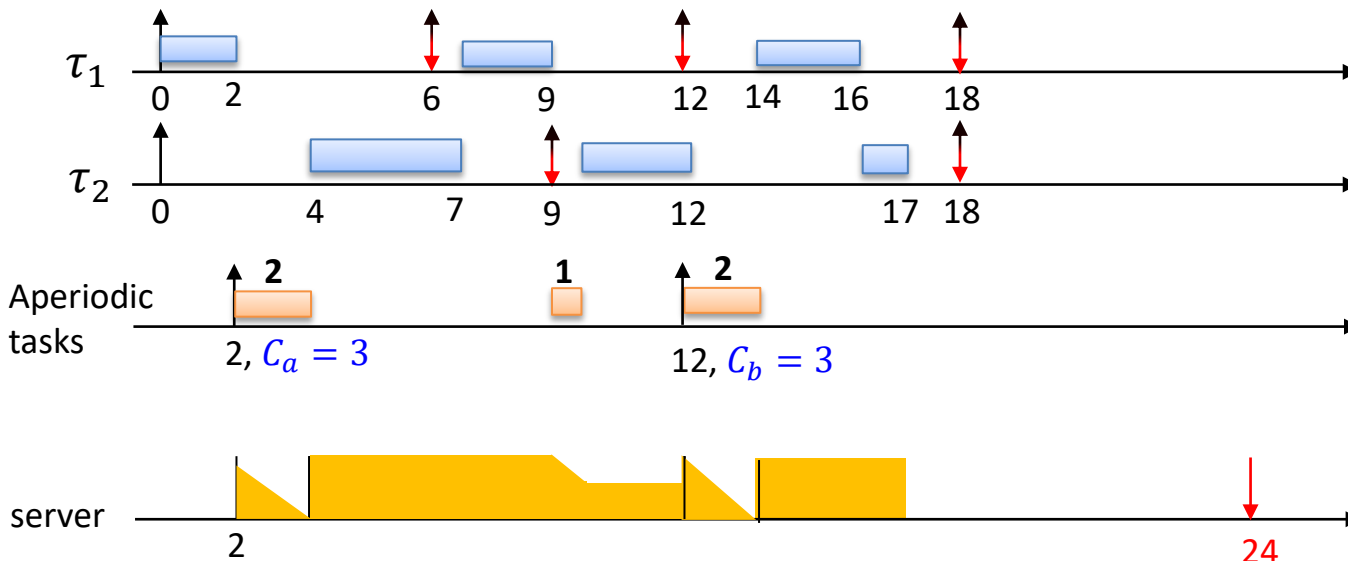
$$\tau_1: (C_1 = 2, T_1 = 6) \text{ and } \tau_2: (C_2 = 3, T_2 = 9)$$

If ( $\exists$  a pending aperiodic job) then  $\langle \text{enqueue } J_k \rangle$   
 else if ( $U_s < \frac{q_s}{d_s - r_k}$ ) then {  
 $q_s \leftarrow Q_s$   
 $d_s \leftarrow r_k + T_s$   
 } else {use the current  $q_s$  and  $d_s$ }

**Exhaustion:**

$$q_s \leftarrow Q_s$$

$$d_s \leftarrow d_s + T_s$$



# Example: CBS

Aperiodic jobs:

$$J_a: (r_a = 2, C_a = 3), J_b: (r_b = 12, C_b = 3)$$

Server:

$$Q_s = 2 \text{ and } T_s = 6$$

Periodic tasks:

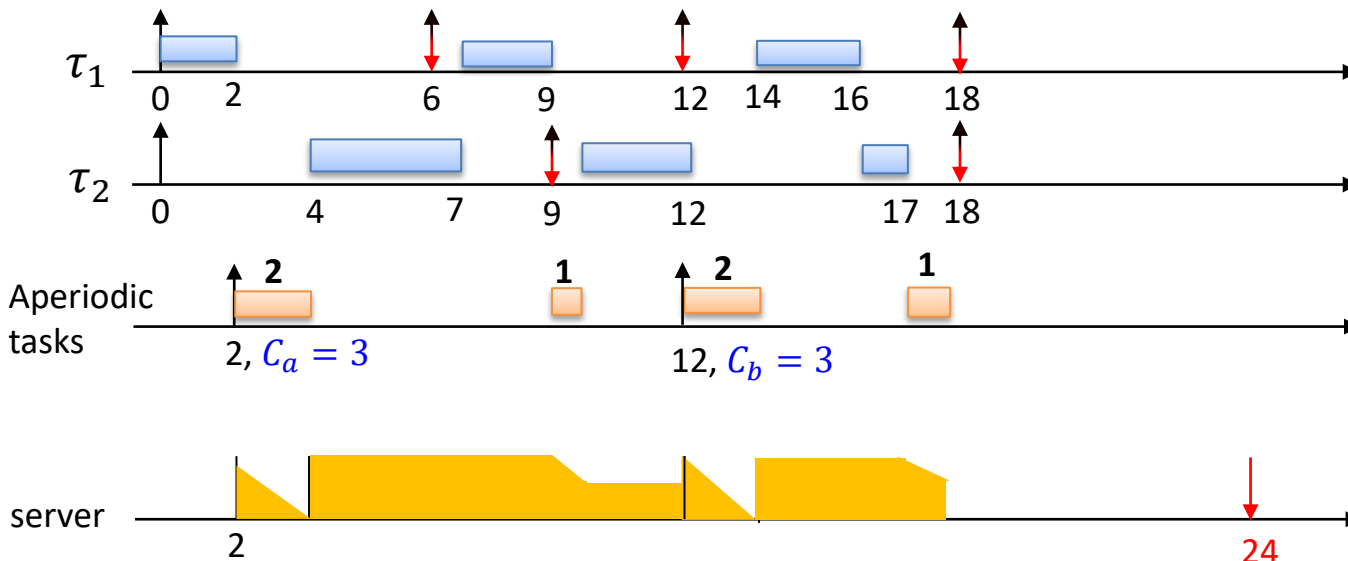
$$\tau_1: (C_1 = 2, T_1 = 6) \text{ and } \tau_2: (C_2 = 3, T_2 = 9)$$

If ( $\exists$  a pending aperiodic job) then  $\langle \text{enqueue } J_k \rangle$   
 else if ( $U_s < \frac{q_s}{d_s - r_k}$ ) then {  
 $q_s \leftarrow Q_s$   
 $d_s \leftarrow r_k + T_s$   
 } else {use the current  $q_s$  and  $d_s$ }

**Exhaustion:**

$$q_s \leftarrow Q_s$$

$$d_s \leftarrow d_s + T_s$$



# Summary

- **Server-based scheduling:** a remedy for aperiodic events, background work, and misbehaving real-time tasks
- **Types of servers**
  - Periodic servers
  - Polling servers
  - Deferrable servers
  - Constant-bandwidth servers (CBS)

