

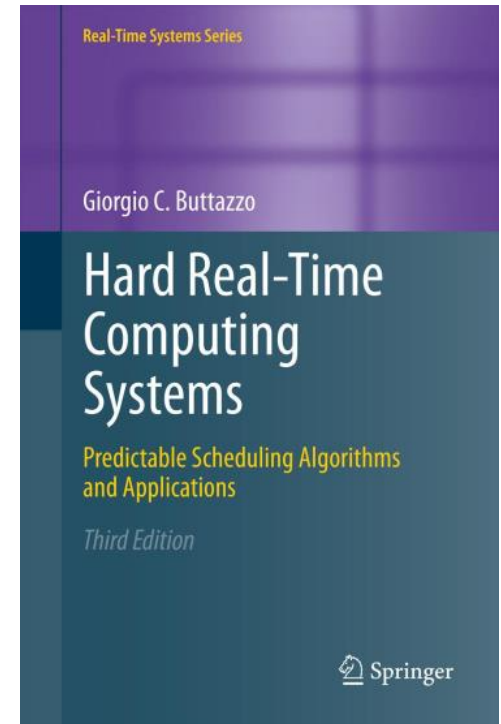
2IMN20 - Real-Time Systems

Schedulability analysis of EDF

Geoffrey Nelissen

Reference book

Chapter 4



Disclaimer:

Many slides were provided by Dr. Mitra Nasri and Prof. [Giorgio Buttazzo](#)



Assumptions

- For this lecture, we assume
 - A1.** All jobs of τ_i execute for no more than C_i
 - A2.** Tasks are periodic or sporadic with no release jitter
 - A3.** Tasks are fully preemptive
 - A4.** Context switch, preemption, and scheduling overheads are zero
 - A5.** Tasks are independent:
 - no precedence relations
 - no resource constraints
 - no blocking on I/O operations
 - A6.** No self-suspensions
 - A7.** Single core

EDF

Schedulability test

- Liu and Layland 1973

A task set τ is schedulable by EDF **if and only if**:

$$\sum_{i=1}^n \frac{C_i}{T_i} \leq 1$$

Why is this not enough?

EDF

Schedulability test

- Liu and Layland 1973

A task set τ is schedulable by EDF **if and only if**:

$$\sum_{i=1}^n \frac{C_i}{T_i} \leq 1$$

Assumption:

$$\forall i, D_i = T_i$$

What if $D_i \neq T_i$?

EDF schedulability analysis for $D_i < T_i$

Processor Demand Criterion [Baruah '90]

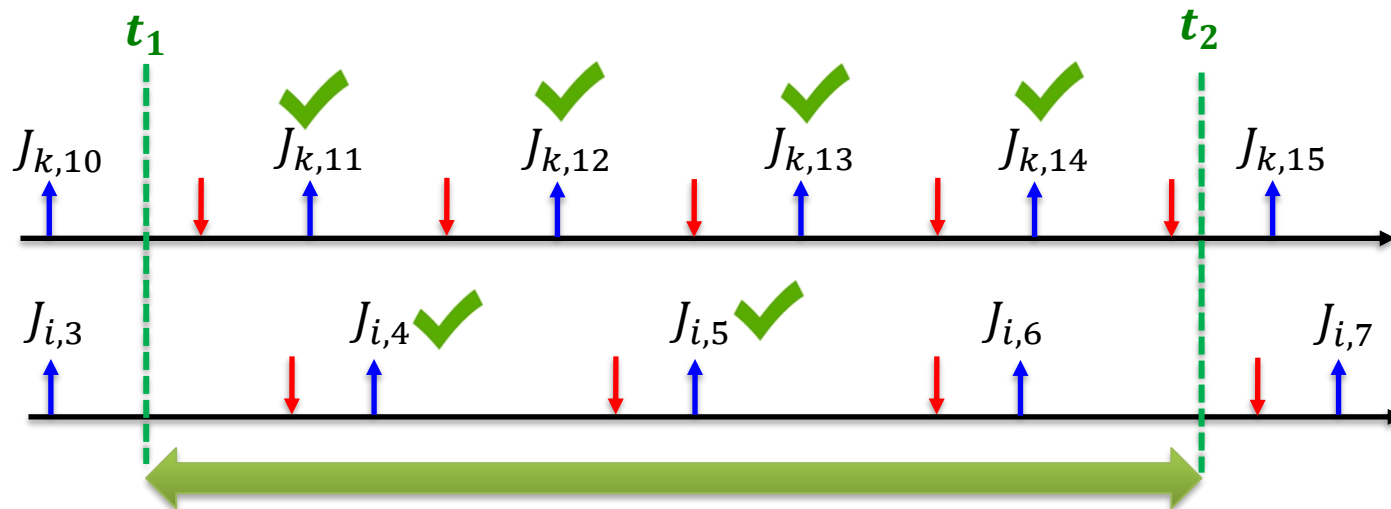
In **any interval** of length L , the computational demand $g(t, t + L)$ of the task set must be **no greater** than L .

$$\forall t, \forall L > 0, \quad g(t, t + L) \leq L$$

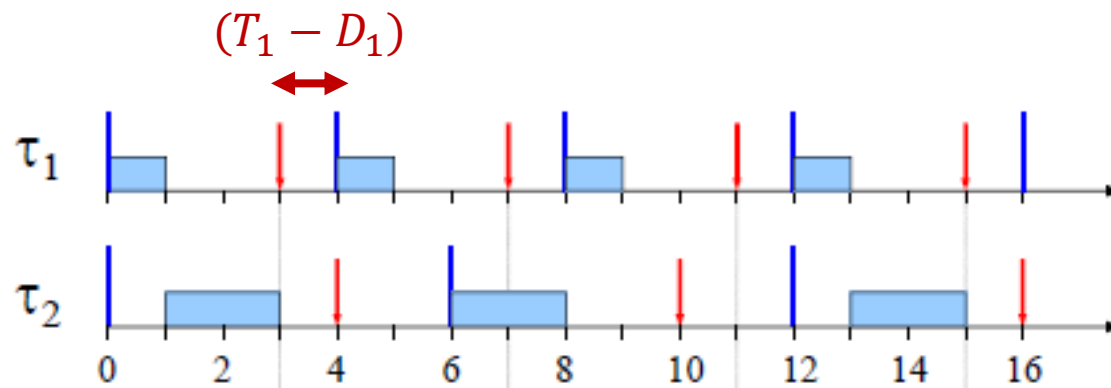
Understanding the processor demand (g function)

- The demand in $[t_1, t_2]$ is the computation time of those tasks arrived at or after t_1 with deadline less than or equal to t_2 :

$$g(t_1, t_2) = \sum_{a_{k,j} \geq t_1}^{d_{k,j} \leq t_2} C_k$$



Demand of a **periodic/sporadic** task set



Computational demand of τ_i

$$g_i(t, t + L) \leq g_i(0, L) = \left\lfloor \frac{L + (T_i - D_i)}{T_i} \right\rfloor \cdot C_i$$

$$= \left\lfloor \frac{L - D_i}{T_i} + 1 \right\rfloor \cdot C_i$$

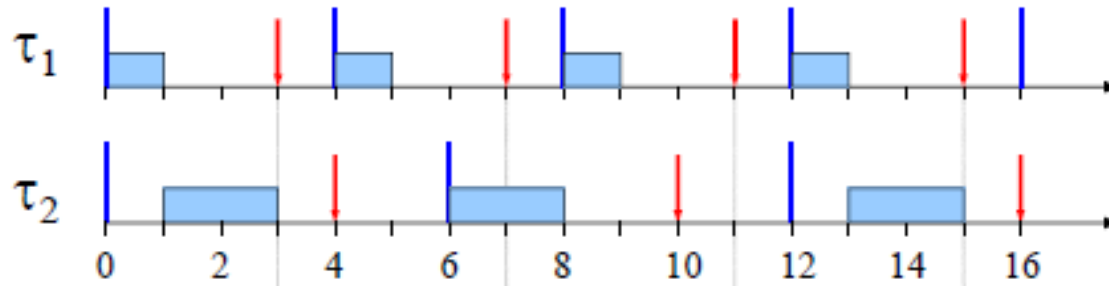
Total computational demand

$$g(0, L) = \sum_{i=1}^n g_i(0, L)$$

Applicable to sporadic tasks or periodic tasks without release jitter, i.e., $\forall i, \phi_i = 0$

Examples

$$g_i(0, L) = \left\lfloor \frac{L + (T_i - D_i)}{T_i} \right\rfloor \cdot C_i$$



- What is $g_2(0, 4)$?

$$g_2(0, 4) = \left\lfloor \frac{4 + 2}{6} \right\rfloor \cdot 2 = 2$$

- What is $g_2(0, 8)$?

$$g_2(0, 8) = \left\lfloor \frac{8 + 2}{6} \right\rfloor \cdot 2 = 2$$

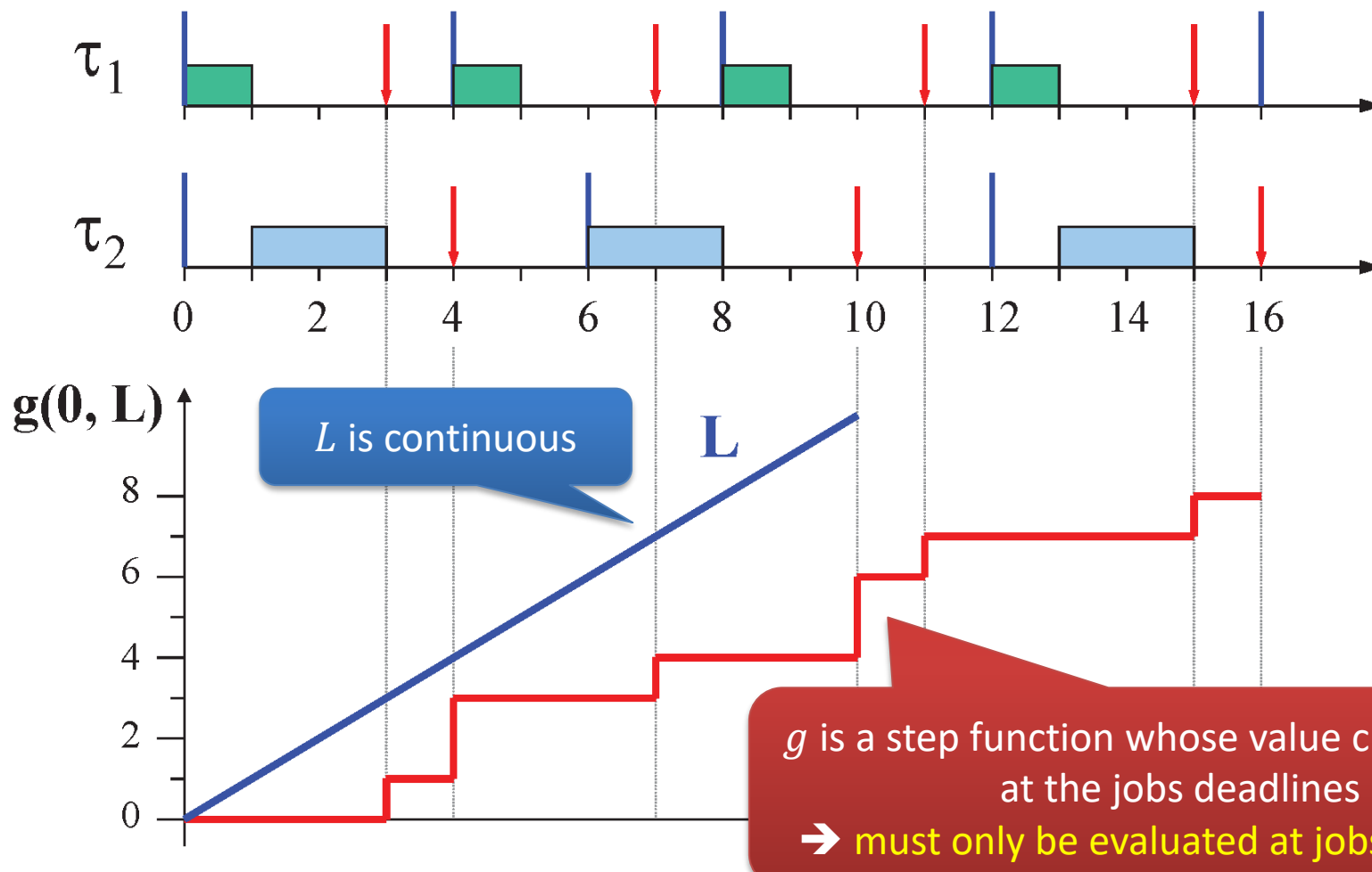
- What is $g_2(0, 16)$?

$$g_2(0, 16) = \left\lfloor \frac{16 + 2}{6} \right\rfloor \cdot 2 = 6$$

Simplifying the test

$$\forall L, \quad g_i(0, L) = \left\lfloor \frac{L + (T_i - D_i)}{T_i} \right\rfloor \cdot C_i \leq L$$

Testing all possible values of L is impractical



Processor Demand Test

$$\forall L \in \mathcal{D}, \quad g(\mathbf{0}, L) \leq L$$

Where \mathcal{D} is the set of deadline points for which $g(\mathbf{0}, L)$ must be calculated:

$$\mathcal{D} = \{d_{i,j} \mid d_{i,j} \leq \min\{H, L^*\}\}$$

Deadlines are the only points where the value of $g(\mathbf{0}, L)$ changes

$$H = \text{lcm}(T_1, \dots, T_n)$$

$$L^* = \frac{\sum_{i=1}^n (T_i - D_i) \cdot U_i}{1 - U}$$

Two bounds on the maximum value of L that must be checked

Summary

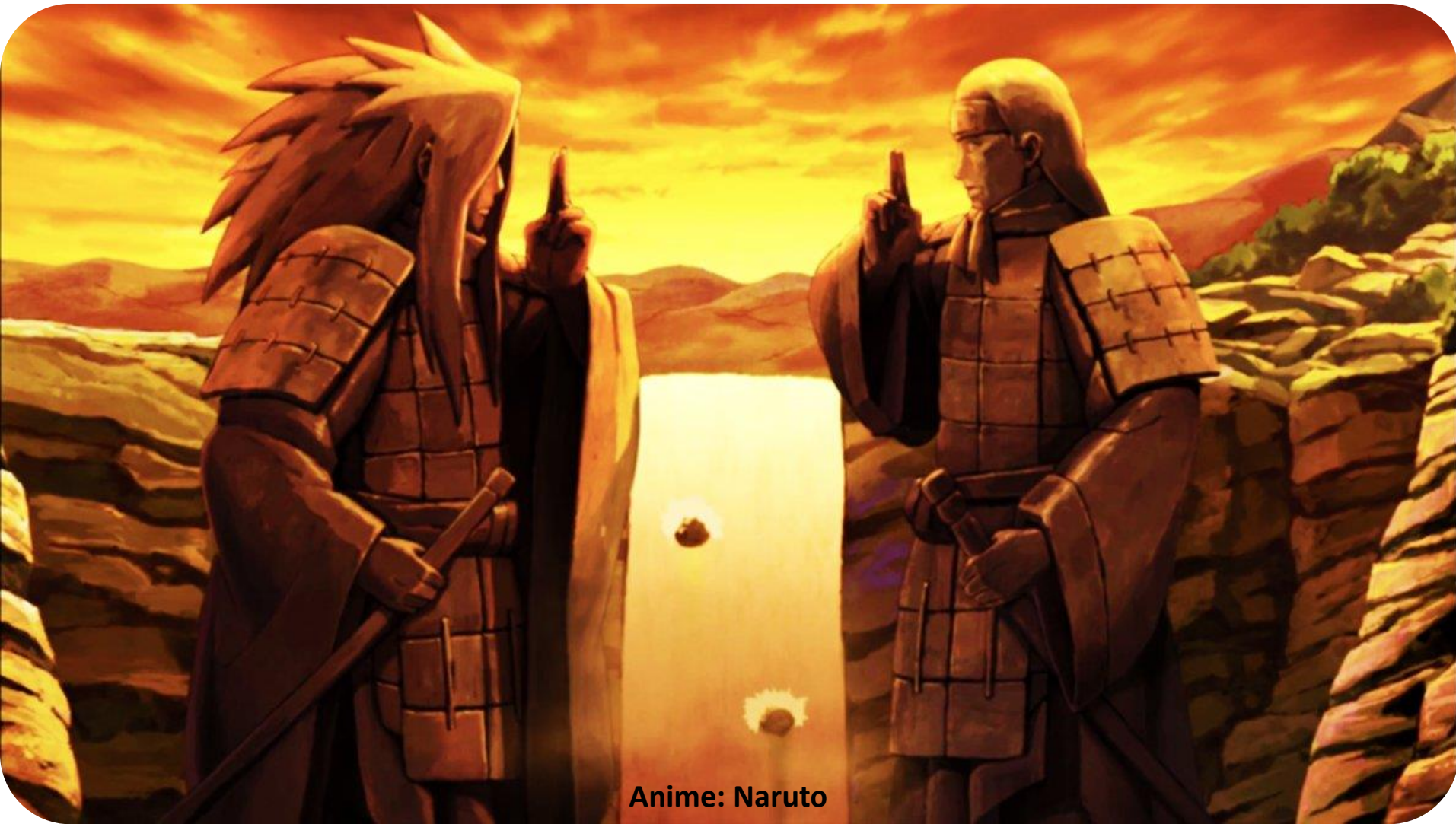
Three analysis techniques:

- Processor **utilization** bound $U \leq U_{lb}$
- **Response** time analysis $\forall i, \quad R_i \leq D_i$
- Processor **demand** criterion $\forall L > 0, \quad g(0, L) \leq L$

RM

v.s.

EDF



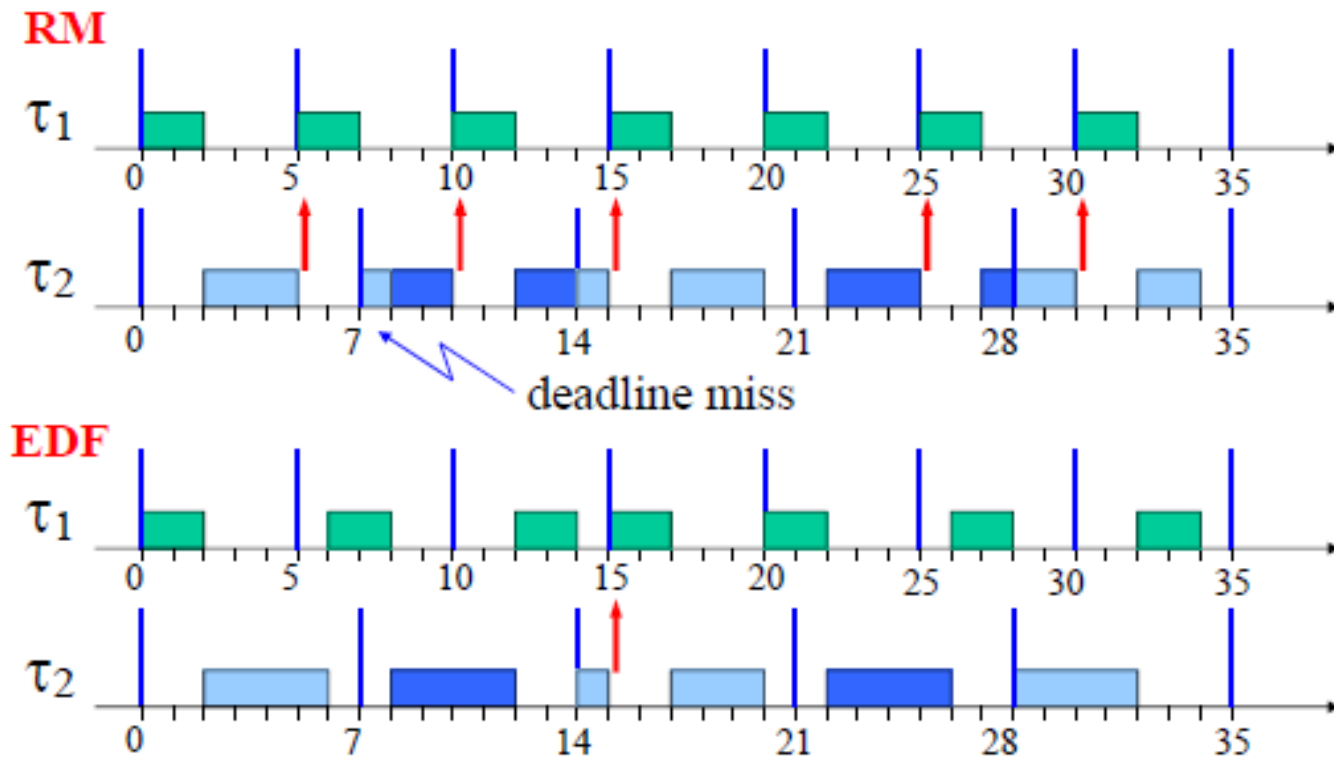
Anime: Naruto

EDF vs FP

- **EDF is optimal** for independent tasks on single core, FP is not
- **FP is supported in almost all OS**, EDF is supported in a handful of them
- **FP is easier to implement** (lower runtime complexity)
- Runtime behavior may be simpler to explain with FP for non-experts

EDF vs RM

Context switches



In average, RM has more context switches

EDF vs RM

Schedulability analysis

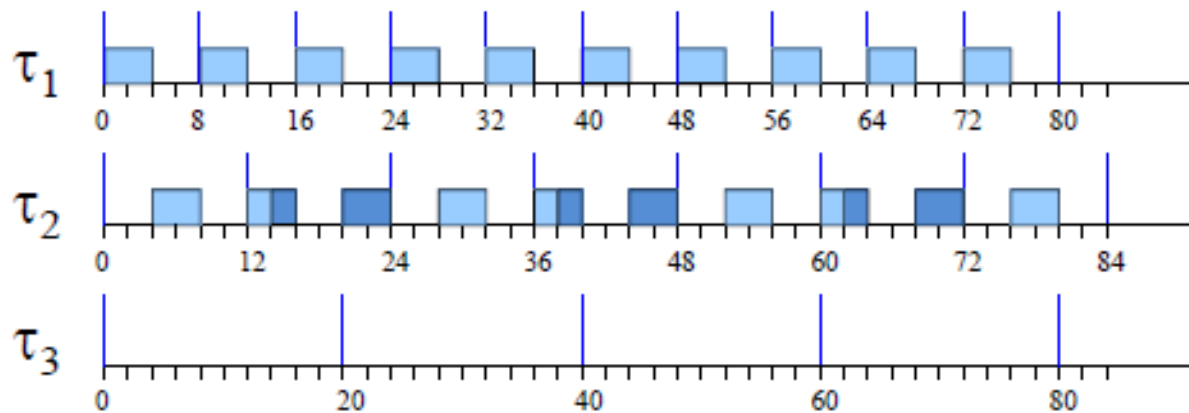
	$D_i = T_i$	$D_i \leq T_i$
RM	<p><i>Suff.:</i> polynomial $O(n)$</p> <p>LL: $\sum U_i \leq n(2^{1/n} - 1)$</p> <p>HB: $\prod(U_i + 1) \leq 2$</p> <p><i>Exact</i> pseudo-polynomial RTA</p>	<p><i>pseudo-polynomial</i> Response Time Analysis</p> <p>$\forall i \quad R_i \leq D_i$</p> $R_i = C_i + \sum_{k=1}^{i-1} \left\lceil \frac{R_i}{T_k} \right\rceil C_k$
EDF	<p><i>polynomial:</i> $O(n)$</p> <p>$\sum U_i \leq 1$</p>	<p><i>pseudo-polynomial</i> Processor Demand Analysis</p> <p>$\forall L > 0, \quad g(0, L) \leq L$</p>

Not seen in the course but RM response-time analysis is faster than EDF

EDF vs RM

RM under permanent overload: **starvation for low priority tasks**

$$U = \frac{4}{8} + \frac{6}{12} + \frac{5}{20} = 1.25$$

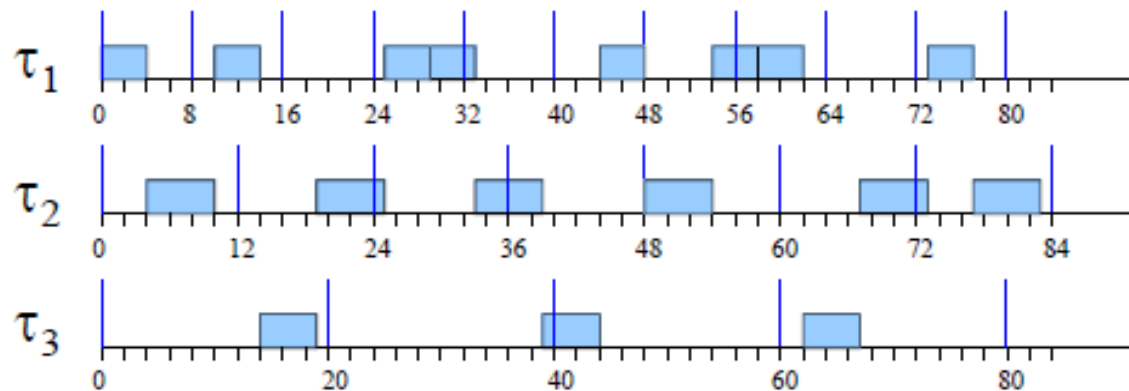


- High priority tasks execute at the proper rate
- Low priority tasks are completely blocked

EDF vs RM

EDF under permanent overload

$$U = \frac{4}{8} + \frac{6}{12} + \frac{5}{20} = 1.25$$



- All tasks execute at a slower rate
- No task is blocked