Yacc

Partha Pratin Das

Simple Calculator

Programmable Calculator

Ambiguous Grammar

CS31003: Compilers: Yacc

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A Simple Calculator Grammar

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Simple Calculator

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Ambiguous Grammar

```
1: S \rightarrow E
```

2: $E \rightarrow E + T$

3: $E \rightarrow E - T$

4: $E \rightarrow T$

5: $T \rightarrow T * F$

6: $T \rightarrow T/F$

7: $T \rightarrow F$

8: $F \rightarrow (E)$

9: $F \rightarrow -E$

10: $F \rightarrow \mathbf{num}$

Yacc Specs (calc.y) for Calculator Grammar

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```
%f /* C Declarations and Definitions */
#include <string.h>
#include <iostream>
extern int yylex();
void vverror(char *s):
%union {
    int intval:
%token <intval> NIMBER
%type <intval> expression
%type <intval> term
%type <intval> factor
%%
statement: expression
               { printf("= %d\n", $1); }
expression: expression '+' term
                \{ \$\$ = \$1 + \$3; \}
          | expression '-' term
                \{ \$\$ = \$1 - \$3 : \}
           | term
```

```
term: term '*' factor
           \{ \$\$ = \$1 * \$3 : \}
    | term '/' factor
           \{ if (\$3 == 0) \}
               vverror("divide by zero"):
             else $$ = $1 / $3:
    I factor
factor: '(' expression ')'
            \{ \$\$ = \$2 : \}
      l'-' factor
            \{ \$\$ = -\$2: \}
       I NUMBER
%%
void vverror(char *s) {
    std::cout << s << std::endl:
int main() {
    yyparse();
```

Note on Yacc Specs (calc.y)

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Terminal Symbols

- Symbolized terminals (like NUMBER) are identified by %token. Usually, but not necessarily, these are multi-character.
- Single character tokens (like '+') may be specified in the rules simply with quotes.
- Non-Terminal Symbols
 - Non-Terminal symbols (like expression) are identified by %type.
 - Any symbol on the left-hand side of a rule is a non-terminal.
- Production Rules
 - Production rules are written with left-hand side non-terminal separated by a colon (:) from the right-hand side symbols.
 - Multiple rules are separated by alternate (1).
 - ullet productions are marked by empty right-hand side.
 - Set of rules from a non-terminal is terminated by semicolon (;).
- Start Symbol
 - Non-terminal on the left-hand side of the first production rule is taken as the start symbol by default.
 - Start symbol may be explicitly defined by %start: %start statement.



Note on Yacc Specs (calc.y)

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Attributes

- Every terminal and non-terminal has an (optional) attribute.
- Multiple types of attributes are possible. They are bundled in a C union by %union.
- An attribute is associated with a terminal by the %token: %token
 <intval> NUMBER
- An attribute is associated with a non-terminal by the %type: %type
 <intval> term

Actions

- Every production rule has an action (C code snippet) at the end of the rule that fires when a reduction by the rule takes place.
- In an action the attribute of the left-hand side non-terminal is identified as \$\$ and the attributes of the symbols on the right-hand side are identified as \$1, \$2, \$3, ... counting from left to right.
- Missing actions for productions with single right-hand side symbol (like factor → NUMBER) imply a default action of copying the attribute (should be of compatible types) from the right to left: { \$\$ = \$1 }.

Header (y.tab.h) for Calculator

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```
/* A Bison parser, made by GNU Bison 2.5. */
/* Tokens. */
#ifndef YYTOKENTYPE
# define YYTOKENTYPE
  /* Put the tokens into the symbol table, so that GDB and other debuggers
     know about them */
  enum vytokentype {
    NUMBER = 258
  1:
#endif
/* Tokens. */
#define NUMBER 258
#if ! defined YYSTYPE && ! defined YYSTYPE_IS_DECLARED
typedef union YYSTYPE
/* Line 2068 of vacc.c */
#line 8 "calc.v"
int intval;
/* Line 2068 of vacc.c */
#line 62 "v.tab.h"
} YYSTYPE;
# define YYSTYPE IS TRIVIAL 1
# define vystype YYSTYPE /* obsolescent; will be withdrawn */
# define YYSTYPE_IS_DECLARED 1
#endif
extern YYSTYPE vylval;
```

Note on Header (y.tab.h)

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- y.tab.h is generated by Yacc from calc.y to specify the token constants and attribute type.
- y.tab.h is automatically included in y.tab.c and must be included in calc.l so that it can feature in lex.yy.c.
- Symbolized tokens are enumerated beyond 256 to avoid clash with ASCII codes returned for single character tokens.
- %union has generated a C union YYSTYPE.
- Line directives are used for cross references to source files. These help debug messaging. For example:

```
#line 8 "calc.y"
```

yylval is a pre-defined global variable of YYSTYPE type.
 extern YYSTYPE vylval;

This is used by lex.yy.c.

Flex Specs (calc.l) for Calculator Grammar

```
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```

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Note on Flex Specs (calc.l)

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- y.tab.h is automatically included in y.tab.c and must be included in calc.l so that it can feature in lex.yy.c.
- yylval is a pre-defined global variable of YYSTYPE type. So attributes of terminal symbols should be populated in it as appropriate. So for NUMBER we have:

```
yylval.intval = atoi(yytext);
Recall, in calc.y, we specified:
    %token <intval> NUMBER
binding intval to NUMBER.
```

- Note how
 - $\n \$ return yytext[0]; would return single character operators by their ASCII code.
- Newline is not treated as a white space but returned separately so that calc.y can generate error messages on line numbers if needed (not shown in the current example).

Flex-Bison Flow & Build Commands

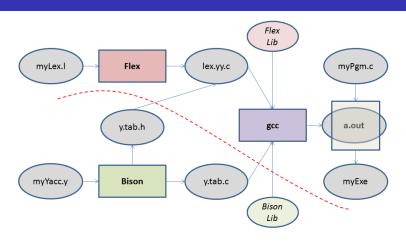
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Programmable Calculator

Ambiguous Grammar



```
$ flex calc.1
```

\$ g++ lex.yy.o y.tab.o -lfl



^{\$} yacc -dtv calc.y

^{\$} g++ -c lex.yy.c

Sample Run

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```
$ ./a.out
12+8 $
= 20
$ ./a.out
12+2*45/4-23*(7+1) $
= -150
```

Handling of 12+8 \$

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- In the next slide we show the working of the parser on the input:
 - 12 + 8 \$
- We use a pair of stacks one for the grammar symbols for parsing and the other for keeping the associated attributes.
- We show the snapshot on every reduction (skipping the shifts).

Handling of 12+8 \$

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Ambiguou: Grammar

Grammar

Reductions

 \rightarrow

 $\begin{array}{ccc} & \underbrace{\text{num}_{12} + \text{num}_{8} \$} \\ \Rightarrow & \underline{F} + \text{num}_{8} \$ \\ \Rightarrow & \underline{T} + \text{num}_{8} \$ \\ \Rightarrow & \underline{E} + \underline{\text{num}}_{8} \$ \\ \Rightarrow & \underline{E} + \underline{T} \$ \\ \Rightarrow & \underline{E} \$ \\ \Rightarrow & 5 \$ \end{array}$

Stack

10:



num





		num	8
		+	
Ε	12	Ε	12

Stack

F	8
+	
Ε	12







Output





A Programmable Calculator Grammar

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Programmable Calculator

Ambiguous Grammar

```
1: L \rightarrow LS \setminus n
 2: L \rightarrow S \setminus n
 3: S \rightarrow id = E
 4: S \rightarrow E
 5: E \rightarrow E + T
 6: E \rightarrow E - T
 7: E \rightarrow T
 8: T \rightarrow T * F
 9: T \rightarrow T/F
10: T \rightarrow F
11: F \rightarrow (E)
12: F \rightarrow -E
13: F \rightarrow \text{num}
```

14: $F \rightarrow$

id

Yacc Specs (calc.y) for Programmable Calculator Grammar

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Programmable Calculator

Ambiguous Grammar

```
%.{
                                                 statement: NAME '=' expression
#include <string.h>
                                                                 { $1->value = $3: }
#include <iostream>
                                                           expression
                                                                 { printf("= %d\n", $1); }
#include "parser.h"
extern int vvlex():
                                                expression: expression '+' term
void vyerror(char *s);
                                                                  \{ \$\$ = \$1 + \$3; \}
                                                            | expression '-' term
#define NSYMS 20 /* max # of symbols */
                                                                  \{ \$\$ = \$1 - \$3 : \}
symboltable symtab[NSYMS];
                                                            I term
%}
                                                term: term '*' factor
%union {
                                                           \{ \$\$ = \$1 * \$3: \}
    int intval;
                                                     | term '/' factor
    struct symtab *symp;
                                                           \{ \text{ if } (\$3 == 0.0) \}
                                                                  vverror("divide by zero"):
                                                              else
%token <svmp> NAME
                                                                  $$ = $1 / $3;
%token <intval> NUMBER
                                                     I factor
%type <intval> expression
                                                factor: '(' expression ')'
%type <intval> term
                                                             \{ \$\$ = \$2; \}
%type <intval> factor
                                                       l '-' factor
%%
                                                              \{ \$\$ = -\$2; \}
stmt list: stmt list statement '\n'
                                                       I NUMBER
          | statement '\n'
                                                       I NAME.
                                                             { $$ = $1->value: }
```

4□ > 4同 > 4 = > 4 = > ■ 900

Yacc Specs (calc.y) for Programmable Calculator Grammar

```
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```

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Programmable Calculator

```
struct symtab *symlook(char *s) {
    char *p;
    struct symtab *sp;
    for(sp = symtab;
        sp < &symtab[NSYMS]; sp++) {
       /* is it already here? */
        if (sp->name &&
           !strcmp(sp->name, s))
            return sp;
        if (!sp->name) {
        /* is it free */
            sp->name = strdup(s);
            return sp;
        /* otherwise continue to next */
    yyerror("Too many symbols");
    exit(1); /* cannot continue */
} /* symlook */
```

```
void yyerror(char *s) {
    std::cout << s << std::endl;
}
int main() {
    yyparse();
}</pre>
```

Header (y.tab.h) for Programmable Calculator

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Simple Calculator

Programmable Calculator

```
/* A Bison parser, made by GNU Bison 2.5. */
/* Tokens. */
#ifndef YYTOKENTYPE
# define YYTOKENTYPE
  /* Put the tokens into the symbol table, so that GDB and other debuggers know about them. */
  enum vytokentype {
    NAME = 258.
     NIIMRER = 259
  };
#endif
/* Tokens. */
#define NAME 258
#define NUMBER 259
#if ! defined YYSTYPE && ! defined YYSTYPE_IS_DECLARED
typedef union YYSTYPE {
#line 11 "calc.v" /* Line 2068 of vacc.c */
    int intval;
    struct symtab *symp:
#line 65 "v.tab.h" /* Line 2068 of vacc.c */
} YYSTYPE:
# define YYSTYPE IS TRIVIAL 1
# define vystype YYSTYPE /* obsolescent; will be withdrawn */
# define YYSTYPE_IS_DECLARED 1
#endif
extern YYSTYPE vylval;
```

Header (parser.h) for Programmable Calculator

```
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```

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Programmable Calculator

```
#ifndef __PARSER_H
#define __PARSER_H

typedef struct symtab {
    char *name;
    int value;
} symboltable;

symboltable *symlook(char *);
#endif // __PARSER_H
```

Flex Specs (calc.l) for Programmable Calculator Grammar

```
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```

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Simple Calculator

Programmable Calculator

```
%{
#include <math h>
#include "v.tab.h"
#include "parser.h"
%}
TD
          [A-Za-z][A-Za-z0-9]*
%%
[0-9]+
            vylval.intval = atoi(vytext);
            return NUMBER:
[\t]
          ; /* ignore white space */
{ID}
          { /* return symbol pointer */
            yylval.symp = symlook(yytext);
            return NAME;
"$"
          { return 0; /* end of input */ }
\nl.
          return yytext[0];
%%
```

Note on Programmable Calculator

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Simple Calculato

Programmable Calculator

Ambiguou Grammar

Symbol Table

- We have introduced variables (id) in the grammar now to support programmability (to store intermediate results).
- id's are maintained in the (rudimentary) symbol table as a name-value doublet (refer: parser.h).

```
struct symtab { char *name; int value; };
```

- Every id, as soon as found in the lexer for the first time, is inserted in the symbol table. On every subsequent occurrence the same id is referred from the symbol table. The function struct symtab *symlook(char *); achieves this.
- union Wrapper
 - Tokens NAME and NUMBER have different attributes intval and symp respectively.
 - For defining a value-stack in C, these are wrapped in a single union:

```
typedef union YYSTYPE {
   int intval;
   struct symtab *symp;
} YYSTYPE;
```



Sample Run

Yacc

Programmable Calculator

Output

\$./a.out a = 8 + 9a + 4 = 21 \$

Grammar

S \n id = EΕ 5: \rightarrow E + T

LS\n

L\$

7:
$$E \rightarrow T$$

8: $T \rightarrow T*F$
9: $T \rightarrow T/F$

13:
$$F \rightarrow \mathbf{nu}$$

14: $F \rightarrow \mathbf{id}$

\rightarrow - É num

Derivation

$$\Rightarrow \overline{L} \, \underline{E} \setminus n \, \$$$

$$\Rightarrow L \, \underline{E} + \underline{T} \setminus n \, \$$$

$$\Rightarrow L \, \overline{E} + \underline{F} \setminus n \, \$$$

$$\Rightarrow L \, \underline{E} + \underline{\text{num}}_4 \setminus n \, \$$$

$$\Rightarrow L \, \underline{T} + \underline{\text{num}}_4 \setminus n \, \$$$

 $LS \n$ \$

$$\Rightarrow L \overline{F} + \text{num}_4 \setminus \text{n} \$$$

$$\Rightarrow L \underline{\text{id}}_a + \text{num}_4 \setminus \text{n} \$$$

$$\Rightarrow S \setminus \text{n} \underline{\text{id}}_a + \text{num}_4 \setminus \text{n} \$$$

$$\Rightarrow \frac{\overline{id_a} = E \setminus n id_a + num_4 \setminus n \$}{\overline{id_a} = E + T \setminus n id_a + num_4 \setminus n \$}$$
$$\Rightarrow id_a = E + F \setminus n id_a + num_4 \setminus n \$$$

$$\Rightarrow id_a = E + \underline{\text{num}}_9 \setminus n id_a + \underline{\text{num}}_4 \setminus n$$

$$\Rightarrow id_a = \underline{T} + \underline{\text{num}}_9 \setminus n id_a + \underline{\text{num}}_4 \setminus n$$

$$\Rightarrow id_a = \overline{F} + num_9 \setminus n id_a + num_4 \setminus n \$$$

$$\Rightarrow id_a = num_8 + num_9 \setminus n id_a + num_4 \setminus n \$$$

Handling of $a = 8 + 9 \setminus n \ a + 4 \setminus n \$

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Programmable Calculator

Grammar

L S \n

id = E

E + T

E - T

Т

S \n`

 \rightarrow

 \rightarrow

ы

Reductions

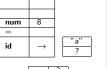
 $id_a = num_8 + num_9 \setminus n id_a + num_4 \setminus n$ \$ $id_a = F + num_9 \setminus n id_a + num_4 \setminus n$ \$ $id_a = T + num_0 \setminus n id_a + num_4 \setminus n$ \$

 $id_a = \overline{E} + num_9 \setminus n id_a + num_4 \setminus n$ \$ $id_a = E + \overline{F \setminus n} id_a + num_4 \setminus n$ \$

 $id_a = E + \overline{T} \setminus n id_a + num_4 \setminus n$ \$ $id_a = \overline{E \setminus n} id_a + num_4 \setminus n$ \$ $\overline{S \setminus n id_a} + num_4 \setminus n$ \$

 $\overline{L id_2} + num_4 \setminus n$ \$

Stack



num	9	
+		
Ε	8	
=		١.
id	\rightarrow	[

_ T	9
+	
E	8
-	
id	\rightarrow

Symtab

а	?	

Stack

_		l
=		
id	\rightarrow	"a"

| F | 17 |



17

j		
	L	

17

Symtab



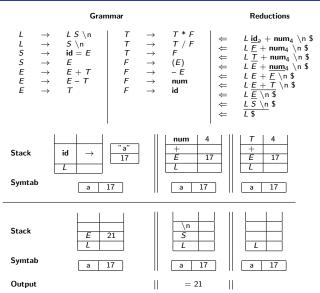
Handling of $a = 8 + 9 \mid n \mid a + 4 \mid n \mid s$

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A Programmable Calculator Grammar (with Ambiguous Grammar)

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Simple Calculato

Programmable Calculator

- 1: $L \rightarrow LS \setminus n$
- 2: $L \rightarrow S \setminus n$
- 3: $S \rightarrow id = E$
- 4: $S \rightarrow E$
- 5: $E \rightarrow E + E$
- 6: $E \rightarrow E E$
- 7: $E \rightarrow E * E$
- 8: $E \rightarrow E/E$
- 9: $E \rightarrow (E')$
- 10: $E \rightarrow -E$
- 11: $E \rightarrow num$
- 12: $E \rightarrow \text{id}$

Yacc Specs (calc.y) for Programmable Calculator Grammar

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Simple Calculator

Programmable Calculator

```
%{
                                                statement: NAME '=' expression
#include <string.h>
                                                                 { $1->value = $3: }
#include <iostream>
                                                          expression
#include "parser.h"
                                                                 { printf("= %d\n", $1); }
extern int yylex();
void vyerror(char *s);
#define NSYMS 20 /* max # of symbols */
                                                expression: expression '+' expression
symboltable symtab[NSYMS]:
                                                                  \{ \$\$ = \$1 + \$3 : \}
%}
                                                           | expression '-' expression
                                                                 \{ \$\$ = \$1 - \$3; \}
%union {
                                                           | expression '*' expression
                                                                 \{ \$\$ = \$1 * \$3 : \}
    int intval;
                                                           | expression '/' expression
    struct symtab *symp;
                                                                 \{ \text{ if } (\$3 == 0) \}
                                                                        vverror("divide by zero"):
%token <symp> NAME
                                                                    else
%token <intval> NUMBER
                                                                        $$ = $1 / $3:
%left '+' '-'
                                                           | '(' expression ')'
%left '*' '/'
                                                                 \{ \$\$ = \$2; \}
                                                           / '-' expression %prec UMINUS
%nonassoc UMINUS
                                                                  \{ \$\$ = -\$2; \}
%type <intval> expression
                                                           I NUMBER
%%
                                                             NAME.
                                                                 { $$ = $1->value: }
stmt_list: statement '\n'
         | stmt list statement '\n'
                                                %%
```

Yacc Specs (calc.y) for Programmable Calculator Grammar

```
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```

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Simple Calculator

Programmable Calculator

```
struct symtab *symlook(char *s) {
    char *p;
    struct symtab *sp;
    for(sp = symtab;
        sp < &symtab[NSYMS]; sp++) {
       /* is it already here? */
       if (sp->name &&
           !strcmp(sp->name, s))
            return sp;
        if (!sp->name) {
        /* is it free */
            sp->name = strdup(s);
            return sp;
        /* otherwise continue to next */
    yyerror("Too many symbols");
    exit(1); /* cannot continue */
} /* symlook */
```

```
void yyerror(char *s) {
    std::cout << s << std::endl;
}
int main() {
    yyparse();
}</pre>
```

Note on Yacc Specs (calc.y) for Ambiguous Grammar

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Simple Calculator

Programmable Calculator

Ambiguous Grammar

Ambiguous Grammars

- Ease specification of languages particularly the operator expressions.
- Offer shorter and more compact representation.
- Lead to less reduction steps during parsing.
- Introduce shift / reduce conflicts in the LR parser.
- Conflict are resolved by precedences and associativities of operators.

Associativity

- %left is used to specify left-associative operators.
- %right is used to specify right-associative operators.
- %nonassoc is used to specify non-associative operators.

Precedence

- Precedence is specified by the order of %left, %right, or %nonassoc definitions. Later in the order, higher the precedence. However, all operators in the same definition have the same precedence.
- All operators having the same precedence must have the same associativity.

Note on Yacc Specs (calc.y) for Ambiguous Grammar

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Ambiguous Grammar

Overloaded Operators

 Operators like '-' are overloaded in unary and binary forms and have different precedences. We use a symbolic name UMINUS for (say) the unary operator while the binary one is marked as '-'.

```
%left '-'
%nonassoc UMINUS
```

 The rule with the unary minus is bound to this symbolic name using %prec marker.

```
expression: '-' expression %prec UMINUS | expression '-' expression
```

Note that the lexer (calc.l) would continue to return the same '-'
token for unary as well as binary instances of the operators. However,
Yacc can use the precedence information to resolve between the two.

Header (y.tab.h) for Programmable Calculator

Yacc

```
/* A Bison parser, made by GNU Bison 2.5. */
/* Tokens. */
#ifndef YYTOKENTYPE
# define YYTOKENTYPE
  /* Put the tokens into the symbol table, so that GDB and other debuggers know about them. */
  enum vvtokentvpe {
   NAME = 258,
   NUMBER = 259.
    IIMINIIS = 260
  };
#endif
/* Tokens. */
#define NAME 258
#define NUMBER 259
#define IMINUS 260
#if ! defined YYSTYPE && ! defined YYSTYPE_IS_DECLARED
typedef union YYSTYPE {
#line 11 "calc.v" /* Line 2068 of vacc.c */
   int intval:
    struct symtab *symp;
#line 67 "v.tab.h" /* Line 2068 of vacc.c */
} YYSTYPE:
# define YYSTYPE_IS_TRIVIAL 1
# define yystype YYSTYPE /* obsolescent; will be withdrawn */
# define YYSTYPE IS DECLARED 1
#endif
extern YYSTYPE vvlval:
```

Header (parser.h) for Programmable Calculator

```
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```

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Programmabl Calculator

```
#ifndef __PARSER_H
#define __PARSER_H

typedef struct symtab {
    char *name;
    int value;
} symboltable;

symboltable *symlook(char *);
#endif // __PARSER_H
```

Flex Specs (calc.l) for Programmable Calculator Grammar

```
Yacc
```

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Simple Calculator

Programmable Calculator

```
%{
#include <math h>
#include "v.tab.h"
#include "parser.h"
%}
TD
          [A-Za-z][A-Za-z0-9]*
%%
[0-9]+
            vylval.intval = atoi(vytext);
            return NUMBER:
[\t]
          ; /* ignore white space */
{ID}
          { /* return symbol pointer */
            yylval.symp = symlook(yytext);
            return NAME;
"$"
          { return 0; /* end of input */ }
\nl.
          return yytext[0];
%%
```

Sample Run

Yacc

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Simple Calculator

Programmable Calculator

Ambiguous Grammar

Output

\$./a.out a = 8 + 9 a + 4 = 21 \$

Grammar

Derivation

1:	L	\rightarrow	<i>L S</i> \n	,	\$ =	_	L S \n \$
2:	L	\rightarrow	<i>S</i> \n`	L		~	
3:	5	\rightarrow	id = E		=	\Rightarrow	<i>L</i> <u>E</u> \n \$
					=	\Rightarrow	<i>L E</i> + <i>E</i> \n \$
4:	S	\rightarrow	E _		-	\Rightarrow	$L \overline{E + E} \setminus n $ \$
5:	Ε	\rightarrow	E + E			⇒	L E + num ₄ \n \$
6:	Е	\rightarrow	E – E				
7:	E	\rightarrow	E * E			\Rightarrow	$L_{\underline{id}_a} + num_4 \setminus n $
8:	Ē	\rightarrow	E / E		=	\Rightarrow	$S \setminus n id_a + num_4 \setminus n $
					-	\Rightarrow	$\overline{id_a} = E \setminus n \ id_a + num_4 \setminus n \$
9:	E	\rightarrow	(E)			⇒	$\overline{id_a = E} + E \setminus n id_a + num_4 \setminus n $ \$
10:	Ε	\rightarrow	– E				
11:	Е	\rightarrow	num		=	\Rightarrow	$id_a = E + \underline{num}_9 \setminus n id_a + num_4 \setminus n $ \$
12:	E	\rightarrow	id		=	\Rightarrow	$id_a = \underline{num}_8 + num_9 \setminus n id_a + num_4 \setminus n $

Handling of $a = 8 + 9 \setminus n \ a + 4 \setminus n \$

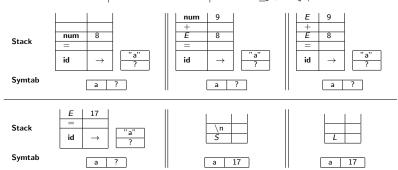
Yacc

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Simple Calculator

Programmable Calculator

Ambiguous Grammar



Handling of $a = 8 + 9 \setminus n \ a + 4 \setminus n \$

Yacc

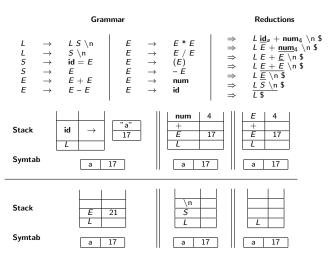
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Output

Ambiguous Grammar



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= 21