Due: 11:59 p.m., 22 March 2016

Problem. Add the function of computing *the length of a vector* and *scalar product of a vector* to the code of 2016-0316.

The length of a vector $\mathbf{u} = [\mathbf{x}, \mathbf{y}]$ is

$$||\mathbf{u}|| = \sqrt{x^2 + y^2}$$
 (definition 1)

or

$$||u|| = \sqrt{\mathbf{u} \cdot \mathbf{u}}$$
 (definition 2)

The scalar product of u = [x, y] and a is

$$a\mathbf{u} = [a\mathbf{x}, a\mathbf{y}]$$

Further, after you write up the function for calculating length of a vector, write a test to *verify* the following theorem of vector computation:

Let u, and v are vectors of the same dimensions. Then,

$$||u + v||^2 = ||u||^2 + 2u \cdot v + ||v||^2$$

Please complete the following list of tasks to solve the problem. Note that you must write unit tests in the test project.

- T1. (30%) Move your production code and test code in homework 2 to production project and the test project, respectively.
- T2. (20%) Write two unit tests for the length function based on the two definitions of length.
- T3. (10%) Compute length of a vector. Name the function like this:

double length (double * const u, int d);

T4. (20%) Write scalar product and one test for it. Name the function like this:

double * product_scalar (double * const u, int d, int a);

T5. (20%) Write a test to verify that $||u+v||^2 = ||u||^2 + 2u \cdot v + ||v||^2$, where u, and v are vectors of the same dimension.