

1. Draw the following DFA using table filling algorithm where A is start state. The states C, F and I are final states.

	0	1
A	B	E*
B	*C	*F
*C	D	H
D	E	H
E	*F	*I
*F	G	B
G	H	B
H	*I	*C
*I	A	E

Step 1:- Cross the combinations of final and non-final states in the table below.

B	X							
*C	X	X						
D	X	X	X					
E	X		X	X				
*F	X	X		X	X			
G		X	X		X	X		
H	X		X	X		X	X	
*I	X	X		X	X		X	X
	A	B	C*	D	E	F*	G	H

Step 2:- Check the \odot i/p and i/p combinations.

$$^X A \quad B \quad E \rightarrow (NF, NF)$$

$$B \quad C_* \quad F_* \rightarrow (F, F)$$

$$^X A \quad B \quad E \quad (NF, NF)$$

$$E \quad F_* \quad I_* \quad (F, F)$$

$$\checkmark A \quad B \quad E \quad (NF, NF)$$

$$D \quad E \quad H \quad (NF, NF)$$

$$\checkmark A \quad B \quad E \quad (NF, NF)$$

$$G \quad H \quad B \quad (NF, NF)$$

0 1

x A B E (NF, NF)

H I_x C_x (F, F)

x B C_x F_x

0 1

D E H

x D E H

✓ B C_x F_x

H I_x C_x

F F_x I_x

x E F_x I_x

x B C_x F_x

G H B

G H B

✓ E F_x I_x

✓ B C_x F_x

H I_x C_x

H I_x C_x

✓ I A E

✓ C_x D H

x P G B

x F G B

x G H B

✓ C_x D H

H I_x C_x

I_x A E

x D E H

E F_x I_x

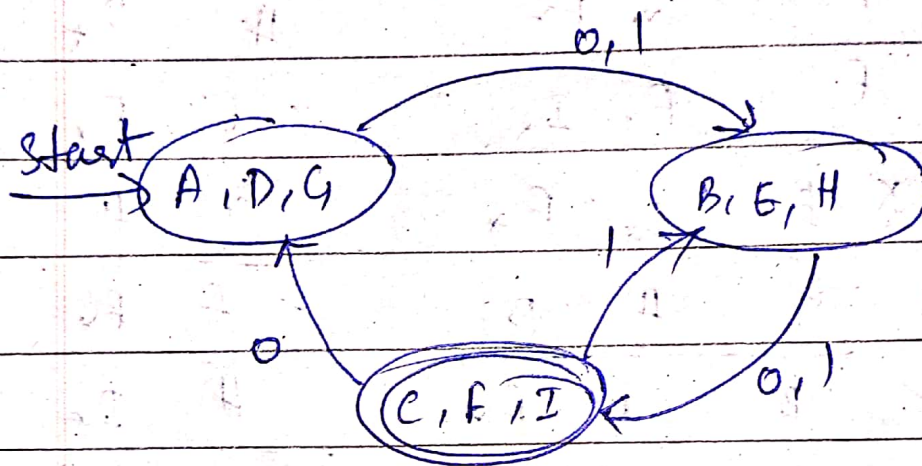
✓ D E H

G H B

Hence the remaining pairs are.

$(A, D), (A, G), (B, E), (B, H), (C, F), (C, I)$
 $(D, G), (E, H), (F, I)$

→ $(A, D, G), (B, E, H), (C, F, I)$



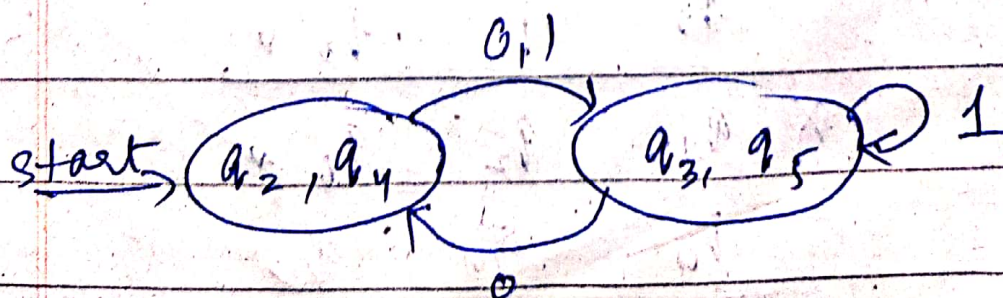
2:

	0	1
→ q_1	q_2	q_3^*
q_2	q_3^*	q_5^*
* q_3	q_4	q_3^*
q_4	q_3^*	q_5^*
* q_5	q_2	q_5^*

q_2	x			
q_3^*	x	x		
q_4	x		x	
q_5^*	x	x		x
	q_1	q_2	q_3^*	q_4


$\begin{array}{cccc} & 0 & 1 & \\ \hline x & q_1 & q_2 & q_3^* \\ & q_2 & q_3^* & q_5^* \\ \hline x & q_1 & q_2 & q_3^* \\ & q_4 & q_3^* & q_5^* \\ \hline \checkmark & q_2 & q_3^* & q_5^* \\ & q_4 & q_3^* & q_5^* \\ \hline \checkmark & *q_3 & q_4 & q_3^* \\ & *q_5 & q_2 & q_5^* \end{array}$

Hence the remaining pairs are
 (q_2, q_4) (q_3, q_5)



3.

	0	1
→ q_1	q_2	$q_6 +$
q_2	q_1	$q_3 +$
* q_3	q_2	q_4
q_4	q_4	q_2
q_5	q_4	q_5
* q_6	q_5	q_4

q_2					
$*q_3$	X	X			
q_4	X	X	X		
q_5	X	X	X		
$*q_6$	X	X		X	X
	q_1	q_2	q_3	q_4	q_5

	0	1
✓ q_1	q_2	$q_6 +$
q_2	q_1	$q_3 +$
X q_3	q_2	$q_6 +$
q_4	q_4	q_2

$\begin{array}{ccc} & 0 & 1 \\ \hline X & a_1 & a_2 & a_6 \end{array}$
 $\begin{array}{ccc} & a_5 & a_4 & a_5 \end{array}$
 $\begin{array}{ccc} X & a_2 & a_1 & a_3 \end{array}$
 $\begin{array}{ccc} & a_4 & a_4 & a_2 \end{array}$
 $\begin{array}{ccc} X & a_2 & a_1 & a_3 \end{array}$
 $\begin{array}{ccc} & a_5 & a_4 & a_5 \end{array}$
 $\begin{array}{ccc} \checkmark & a_3 & a_2 & a_4 \end{array}$
 $\begin{array}{ccc} & a_6 & a_5 & a_4 \end{array}$
 $\begin{array}{ccc} \checkmark & a_4 & a_4 & a_2 \end{array}$
 $\begin{array}{ccc} & a_5 & a_4 & a_5 \end{array}$

Remaining pairs are.

(a_1, a_2) (a_4, a_5) (a_3, a_6)

