Naive Bayes Classifier

- * Probabilistic classifier.
- * generative model.
- * calculates the joint distribution p (X, c), where X is the feature set, c is the class label.
- * the Naive Bayes conditional independence assumption, assume that the attribute values are independent of each other given the class.
- * probability values can be calculated quickly. Usually, very fast algorithm.
- * Learning : Learning parameters : class prior, likelihood.

The algorithm learns prior p(c) and likelihood p(xi/c) from the data.

* Prediction / inference: using the likelihood and prior (calculated in learning), the algorithm calculates posterior probability by applying Bayes rule.



* Learning: Conditional Probability tables

(A) Class Prior
$$P(c = Yes) = \frac{8}{10}; P(c = No) = \frac{2}{10}$$

$$Ves No$$

$$Ve$$

 $P(x_1 = Yes | c = Yes) = \frac{6}{8}; P(x_1 = No/c = Yes) = \frac{2}{8}$ $P(x_1 = Yes | c = No) = \frac{1}{2}; P(x_1 = No/c = No) = \frac{1}{2}$ $P(x_2 = Yes | c = Yes) = \frac{4}{8}; P(x_2 = No/c = Yes) = \frac{4}{8}$ $P(x_2 = Yes | c = No) = \frac{1}{2}; P(x_2 = No/c = No) = \frac{1}{2}$ $P(x_3 = Yes | c = Yes) = \frac{5}{8}; P(x_3 = No/c = No) = \frac{1}{2}$ $P(x_3 = Yes | c = Yes) = \frac{5}{8}; P(x_3 = No/c = Yes) = \frac{3}{8}$ $P(x_3 = Yes | c = No) = \frac{1}{2}; P(x_3 = No/c = No) = \frac{1}{2}$

XC	Yes	No				
Yes	6/8	1/2				
NO	2/8	1/2				
P(x1/c)						

* Inference: Calculate Posterior probability for new examples

Probability of infected given contact is 'Yes', symptoms is 'No' and test is 'Yes' $P(C = Yes \mid X_1 = Yes, X_2 = No, X_3 = Yes)$

=
$$P(x_1=Yes, X_2=No, X_3=Yes)C=Yes) \cdot P(c=Yes)$$

 $P(x_1=Yes, X_2=No, X_2=Yes)$

$$P(x_1 = Yes, X_2 = No, X_3 = Yes)$$

=
$$P(X_1 = Yes, X_2 = No, X_3 = Yes/c = No) \cdot P(c = No)$$

 $P(X_1 = Yes, X_2 = No, X_3 = Yes)$

$$\begin{array}{lll}
A &=& P(x_1 = Yes, x_2 = No, x_3 = Yes \mid C = Yes) \\
&=& P(x_1 = Yes \mid c = Yes) \cdot P(x_2 = No \mid c = Yes) \cdot P(x_3 = Yes \mid c = Yes) \\
&=& (Naive Assumption) \\
&=& (6/8) \cdot (4/8) \cdot (5/8) \\
&=& 15/64
\end{array}$$

$$= \frac{15}{64} + \frac{1}{8} = \frac{23}{64}$$

$$P(C = Yes | X_1 = Yes, X_2 = No, X_3 = Yes) = 0$$

$$= \frac{A \times B}{C}$$

$$= \frac{(15/64) \times (8/10)}{(23/64)}$$

$$= \frac{120}{230} = \frac{12}{23}$$

$$P(c=No/X,=Yes, X_2=No, X_3=Yes)$$
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$$=$$
 $\frac{D \times E}{C}$

$$= \frac{(1/8)(2/10)}{(23/64)}$$

$$= \left(\frac{1}{8}\right) \left(\frac{2}{10}\right) \left(\frac{64}{23}\right)$$

$$=\frac{16}{230}$$