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Assignment 1

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Download all python codes from

https://github.com/Nik123-cpp/Assignment-1/blob/main/assignment1.py

and latex-tikz codes from

https://github.com/Nik123-cpp/Assignment-1/blob/main/Assignment1.tex

1 Problem 3.4

The probability that a bulb produced by a factory will fuse after 150 days is 0.05. Find the probability that out of 5 such bulbs

- (i) none
- (ii) not more than one
- (iii)more than one
- (iv) atleast one

will fuse after 150 days of use.

Solution

Let X be random variable which denoting number of bulbs fuses after 150 days of use, among the 5 bulbs. Then by Bionomial Distribution.

$$\Pr(X = k) = \binom{n}{k} p^k (1 - p)^{n - k}$$
 (1.0.1)

$$k = 0, \dots, n \tag{1.0.2}$$

For given question n = 5, p = 0.05,1-p = 0.95.

1) From (1.0.2)

$$\Pr(X = 0) = {5 \choose 0} (0.05)^0 (0.95)^5 = 0.77378094$$
(1.0.3)

i.e the probability of all 5 bulbs working after 150 days of use

2) simillarly

$$\Pr(X \le 1) = \sum_{k=0}^{1} \Pr(X = k)$$
 (1.0.4)

$$= \sum_{k=0}^{1} {5 \choose k} (0.050^k (0.95)^{5-k} \quad (1.0.5)^{5-k}$$

$$= 0.9774075025$$
 (1.0.6)

i.e the probabity of either none of the bulbs or exactly one bulb will fuse after 150 days of use of 5 such bulbs.

3)

4)

$$\Pr(X > 1) = \sum_{k=2}^{5} \Pr(X = k)$$
 (1.0.7)

Which is complement of second case i.e case(ii),So we can write

$$Pr(X > 1) = 1 - Pr(X \le 1)$$
 (1.0.8)

From (1.0.6)

$$Pr(X > 1) = 1 - 0.9774075025 \qquad (1.0.9)$$

$$= 0.0225924975$$
 (1.0.10)

$$\Pr(X \ge 1) = \sum_{k=1}^{5} \Pr(X = k)$$
 (1.0.11)

which is complement of first case i.e case(i),So we can write

$$Pr(X \ge 1) = 1 - Pr(X < 1)$$
 (1.0.12)

From (1.0.3)

$$Pr(X > 1) = 1 - 0.77378094 (1.0.13)$$

$$= 0.22621906$$
 (1.0.14)