1

Assignment 4

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Download latex-tikz codes from

https://github.com/Nik123-cpp/Assignment-4/blob/main/main.tex

1 Problem UGC—MATH 2019,Q.58

A sample of size n=2 is drawn from a population of size N=4 using probability proportional to size without replacement scheme, Where the probabilities proportional to size are

| i: | 1 | 2 | 3 | 4 | |
|-------|-----|-----|-----|-----|--|
| p_i | 0.4 | 0.2 | 0.2 | 0.2 | |

Table: Probability vs Size

The probability of inclusion of unit (1) in the sample is

- (1)0.4 (2)0.6
- (3)0.7 (4)0.75

2 Solution

Let $P_i(j)$ represent the probability for selecting unit (j) as second unit after selecting unit (i)

$$P_i(j) = \frac{p_j}{1 - p_i} \tag{2.0.1}$$

Let Pr(i, j) be probability of selecting sample $\{i,j\}$, using (2.0.1) is

$$Pr(i, j) = P_i(j) + P_j(i)$$

$$= (p_i \times \frac{p_j}{1 - p_i}) + (p_j \times \frac{p_i}{1 - p_i})$$
(2.0.2)

Total samples(Size n = 2)are

| Case | 1 | 2 | 3 | 4 | 5 | 6 |
|-----------------------|-----------|-------|-------|-------|-------|-------|
| Sample(size $n = 2$) | $\{1,2\}$ | {1,3} | {1,4} | {2,3} | {2,4} | {3,4} |

TABLE 0: list of samples

Let P_i be the probability of inclusion of unit (i) in the sample(size n = 2), Now i will calculate P_1

, Favourable cases for inclusion of unit(1) are case (1,2,3), So

$$P_1 = \Pr(1,2) + \Pr(1,3) + \Pr(1,4)$$
 (2.0.4)

using (2.0.3) and p_i from question,

$$P_1 = \frac{7}{30} + \frac{7}{30} + \frac{7}{30}$$
 (2.0.5)
= 0.7 (2.0.6)

Therefore Option (3)is correct.