

## Operational Amplifier Circuits Bias Circuits Suitable for IC Design

- Bias circuit used to bias discrete BJTs are not suitable. They require large numbers of resistors as well as large coupling and bypass capacitors.
- With present IC technology, impossible to fabricate large capacitors, uneconomical to manufacture large resistances.
- Basically, biasing in IC design is based on use of constant current sources.
- On an IC chip with number of amplifier stages, a constant DC current is generated at one location and is then reproduced at various other locations of biasing various amplifier stages.

## Diode-connected Transistor

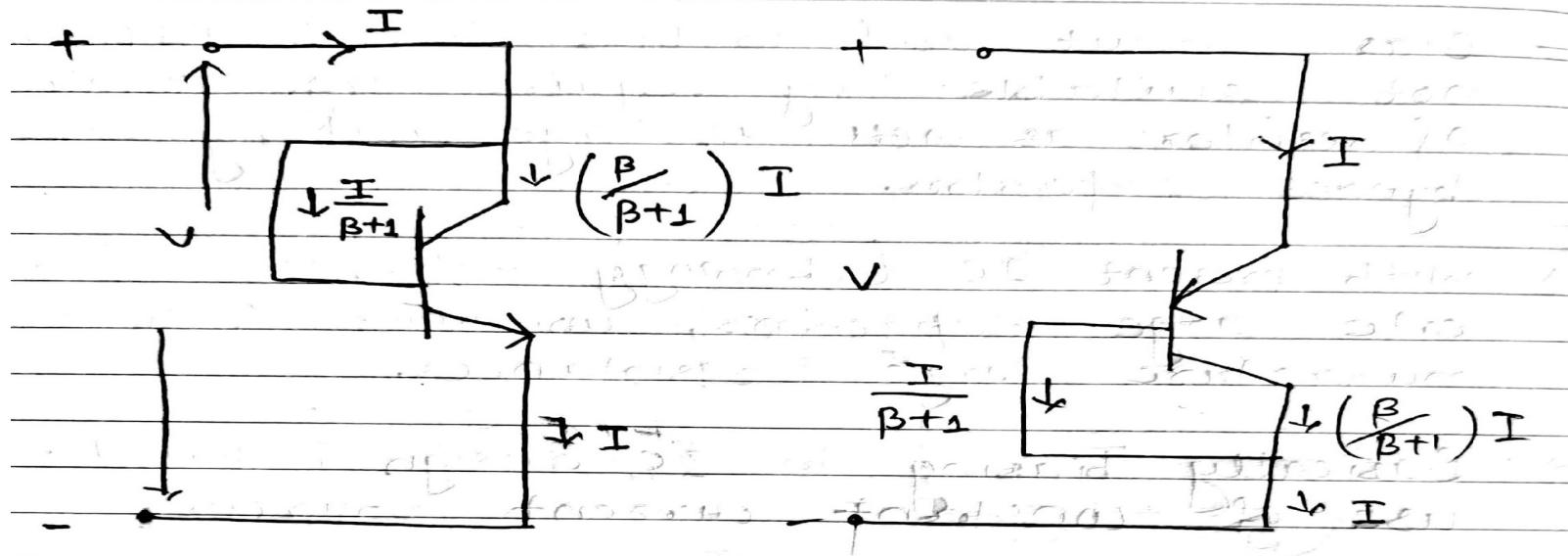
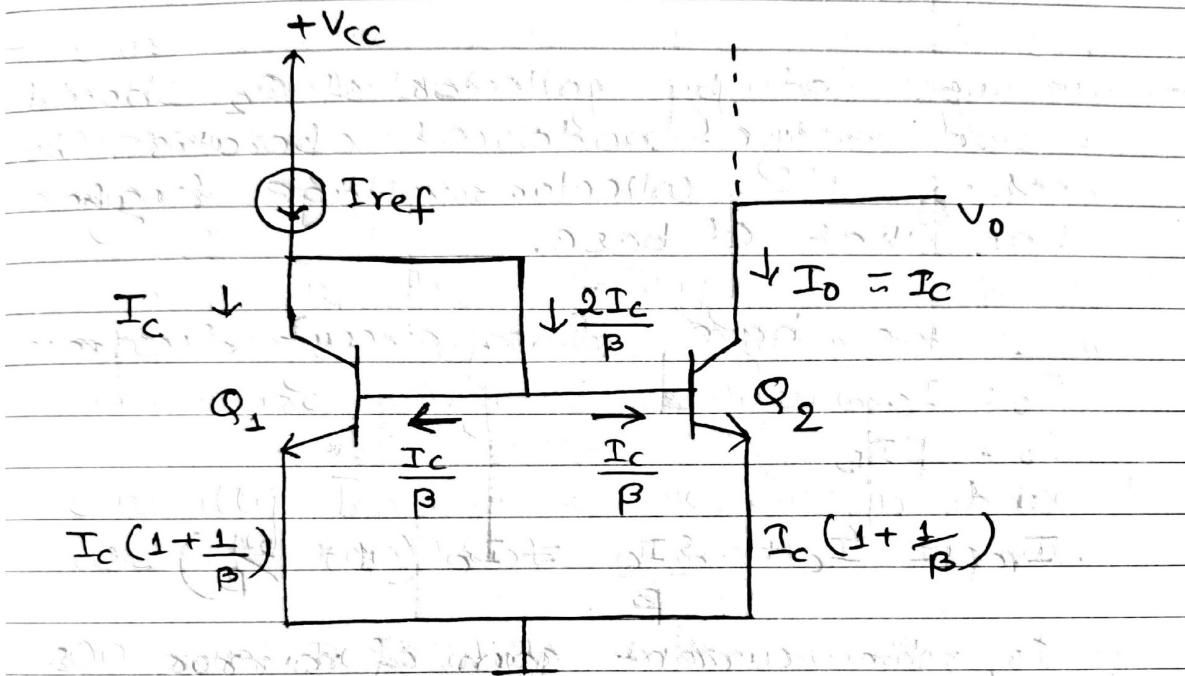


Fig. Diode connected BJT.

→ Shorting the base and collector of BJT together result in a two-terminal device having  $I-V$  characteristics identical to  $I_E - V_{BE}$  characteristics of BJT.

→ Since, BJT is operated in active-mode, the current I divides between base and collector according to the value of  $\beta$  of the BJT.

## Simple Current mirror:



- Fig. simple current mirror circuits in which the output current is forced to be equal to the input current is called current mirror circuit
- it consists of two matched transistors  $Q_1$  and  $Q_2$  and connected as shown in figure.  $Q_1$  is connected as diode.
- current mirror is fed with a constant current source  $I_{ref}$  and output is

taken from collector of  $Q_2$  as shown in figure.

- Circuit fed by collector of  $Q_2$  should ensure active mode of operation by keeping its collector-voltage higher than that of base.

we have from circuit diagram

$$I_o = I_c$$

$$I_o = \beta I_B$$

and,

$$I_{ref} = I_c + \frac{\alpha I_c}{\beta} = I_c \left(1 + \frac{\alpha}{\beta}\right)$$

So, the current gain of mirror is

$$\frac{I_o}{I_{ref}} = \frac{I_c}{I_c \left(1 + \frac{\alpha}{\beta}\right)} = \frac{1}{1 + \frac{\alpha}{\beta}}$$

If  $\beta \gg 1$ , then  $(1 + \frac{\alpha}{\beta}) \approx 1$

$$\frac{I_o}{I_{ref}} = 1$$

$$\therefore I_o = I_{ref}$$

Assumptions:

→  $Q_1$  and  $Q_2$  conduct equal collector currents.

Widlar current source: [678]

- Differ from basic current mirror in an important way i.e. resistor  $R_E$  is included in emitter load of  $Q_2$ .
- Assumption:  $Q_1$  and  $Q_2$  are perfectly matched.
- Neglecting base currents, we have

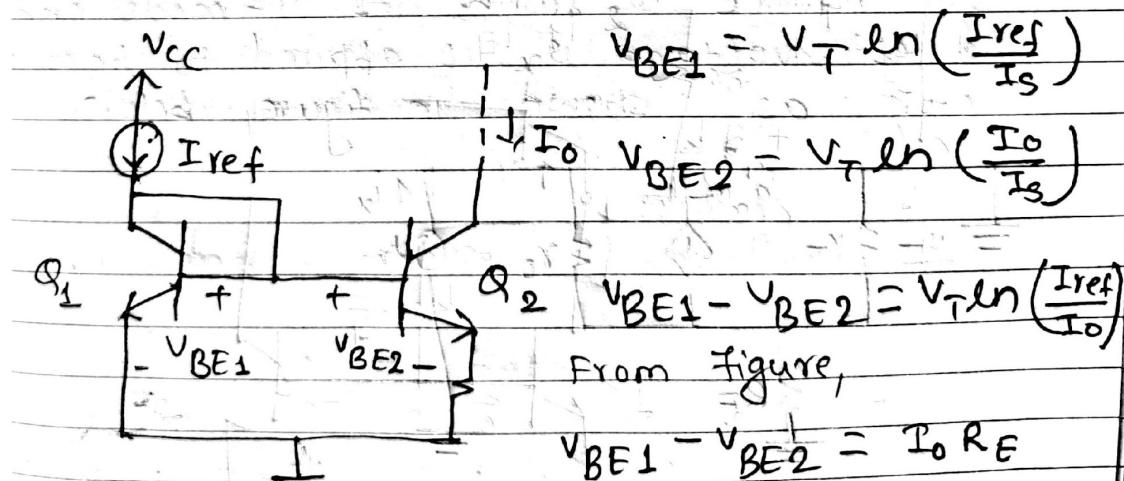


Fig. Widlar circuit

$$\therefore I_O R_E = V_T \ln\left(\frac{I_{ref}}{I_O}\right)$$

→ Widlar circuit allows generation of small constant currents using relatively small resistors. This is an important advantage that results in considerable saving in chip area.

→ Output resistance is high.

→ Increase in output resistance is due to emitter degeneration resistance  $R_E$ .

Calculation of output resistance ( $R_{out}$ ):

→ To determine the output resistance of  $\text{Q}_2$  we replace  $\text{Q}_2$  with its  $\pi$ -model and a test voltage  $v_x$  is applied to the collector as shown in figure below

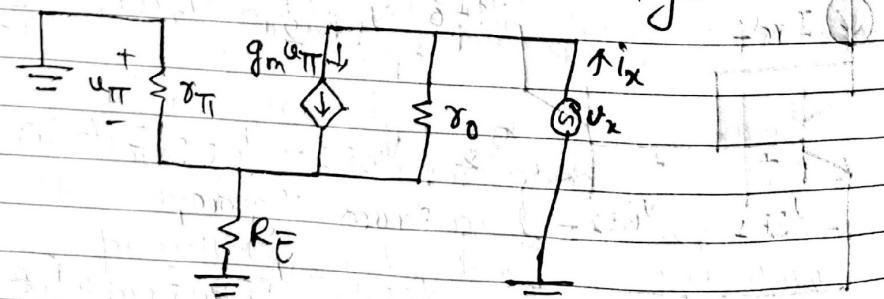
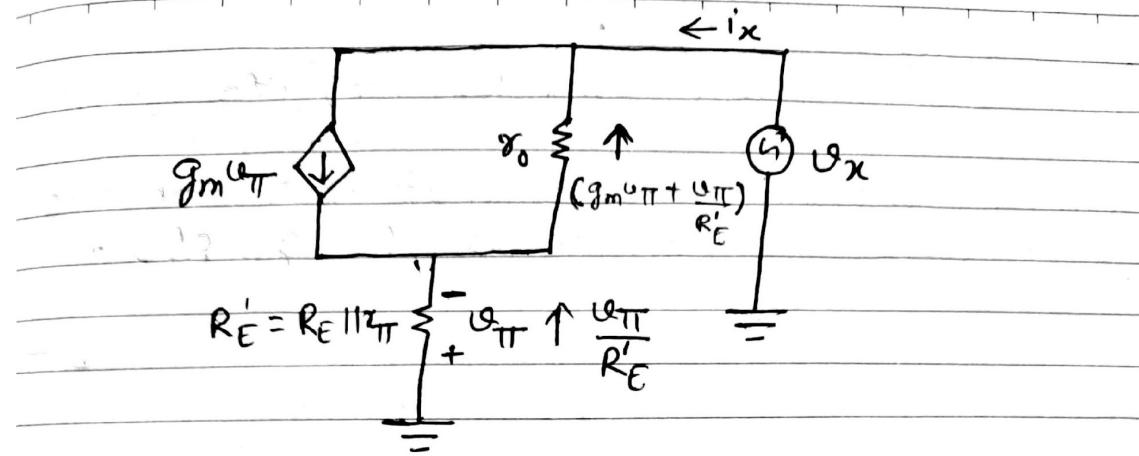


Fig: Equivalent  $\pi$ -model of BJT ( $\text{Q}_2$ )



From figure, we have

$$u_x = -u_{\pi} - \left( g_m + \frac{1}{R'_E} \right) u_{\pi} \gamma_0$$

and,

$$i_x = g_m u_{\pi} - \left( g_m + \frac{1}{R'_E} \right) u_{\pi}$$

∴ The output resistance is

$$\begin{aligned} R_o &= \frac{u_x}{i_x} = \frac{-u_{\pi} - \left( g_m + \frac{1}{R'_E} \right) u_{\pi} \gamma_0}{g_m u_{\pi} - \left( g_m + \frac{1}{R'_E} \right) u_{\pi}} \\ &= \frac{-1 - \left( g_m + \frac{1}{R'_E} \right) \gamma_0}{g_m - g_m - \frac{1}{R'_E}} \\ R_o &= R'_E + (1 + g_m R'_E) \gamma_0 \end{aligned}$$

$$R_o = (1 + g_m R'_E) r_0 \\ = [1 + g_m (R_E / (2\pi))] r_0$$

which shows that output resistance is increased by factor of  $(1 + g_m R'_E)$ .

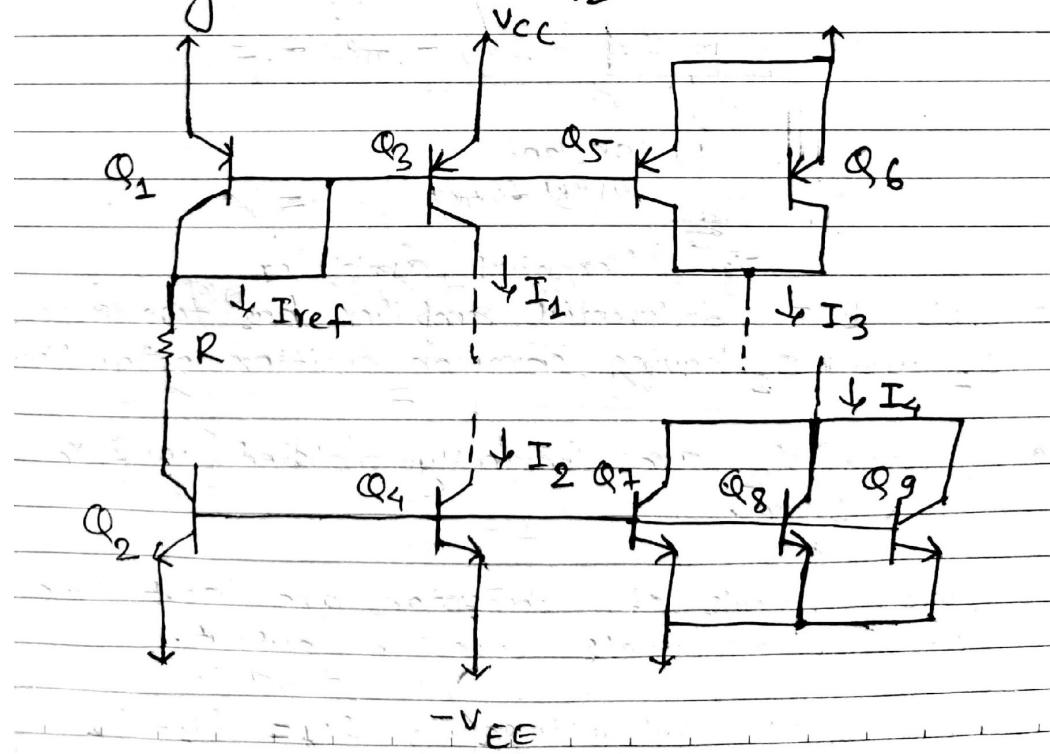
Q. Figure 8

### Current Steering Circuits [595]

- ↗ Utilizes two power supplies  $V_{CC}$  and  $-V_{EE}$
- ↗ Assuming high  $\beta$ ,  $I_{ref} = I_1$
- ↗ Transistor  $Q_3$  supplies current to any load as long as voltage at collector doesn't exceeds that at the base ( $V_{CC} - V_{BE3}$ )
- ↗ To generate dc current twice the value of  $I_{ref}$ , two transistors  $Q_5$  and  $Q_6$ , each of which is matched to  $Q_1$  are connected in parallel and the combination forms a mirror with  $Q_1$ . Thus  $I_3 = 2I_{ref}$

→ Parallel combination of  $Q_5$  and  $Q_6$  is equivalent to transistor with EBJ area double that of  $Q_1$ .

→ Similarly, to generate current three times  $I_{ref}$ , three transistors:  $Q_7$ ,  $Q_8$  and  $Q_9$ , each of which is matched to  $Q_2$ , are connected in parallel and the combination is placed in a mirror configuration with  $Q_2$ .



## The Differential Amplifier [808]

Ideal Differential Amplifier :

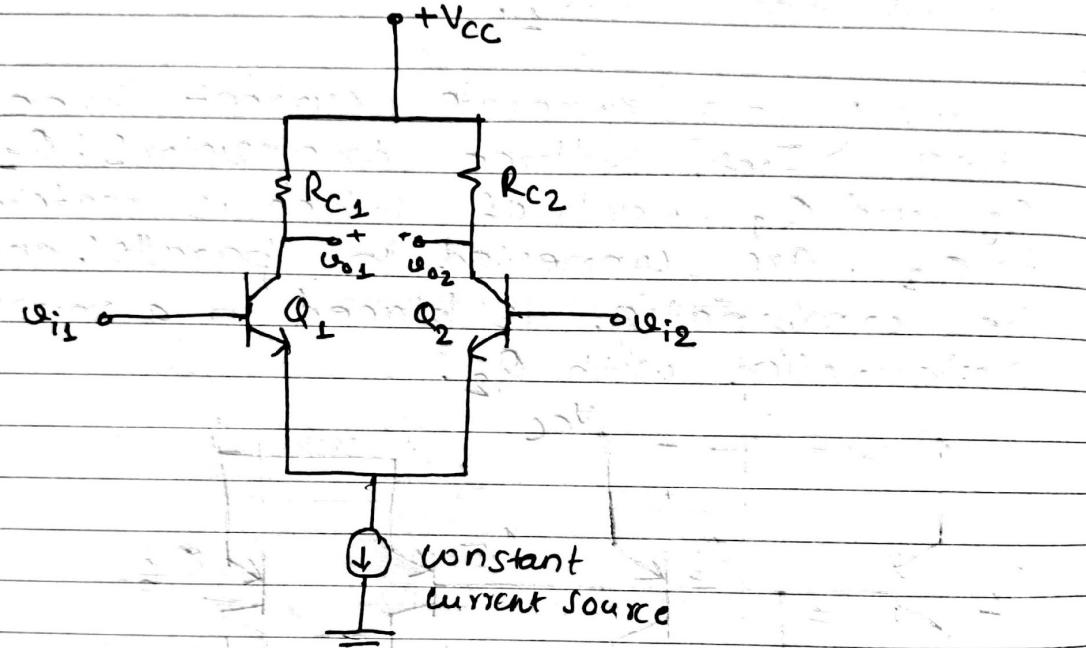


Fig. Differential amplifier

- Basic BJT differential amplifier has two transistors  $Q_1$  and  $Q_2$  having common emitter configuration.
- $Q_1$  and  $Q_2$  are perfectly matched i.e.  $\beta$ ,  $r_e$  are same.
- Base terminals of transistors are input while collector terminals are the output.
- Differential input voltage is,  $v_{id} = v_{i1} - v_{i2}$

- Differential output voltage is  $v_{od} = v_{o1} - v_{o2}$

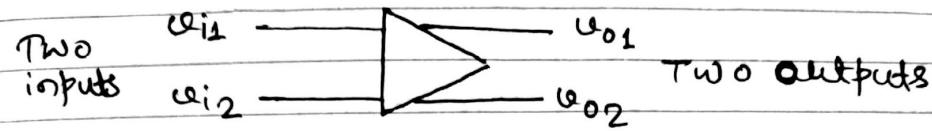


Fig. Schematic symbol for differential amplifier.

- Since there are two inputs and two outputs, amplifier is said to has double ended (double sided) input and double ended output.

Single ended Voltage gain

The voltage is applied at both the inputs whereas output is taken from one end only i.e.

$$A_v = \frac{v_{o1}}{u_{i1} - u_{i2}} \text{ or } A_v = \frac{v_{o2}}{u_{i1} - u_{i2}}$$

Double ended Voltage gain

$$A_v = \frac{v_{o1} - v_{o2}}{u_{i1} - u_{i2}}$$

Q. Show that the output of differential amplifier is proportional to difference between two input voltages.

To show:  $V_o \propto u_{i1} - u_{i2}$

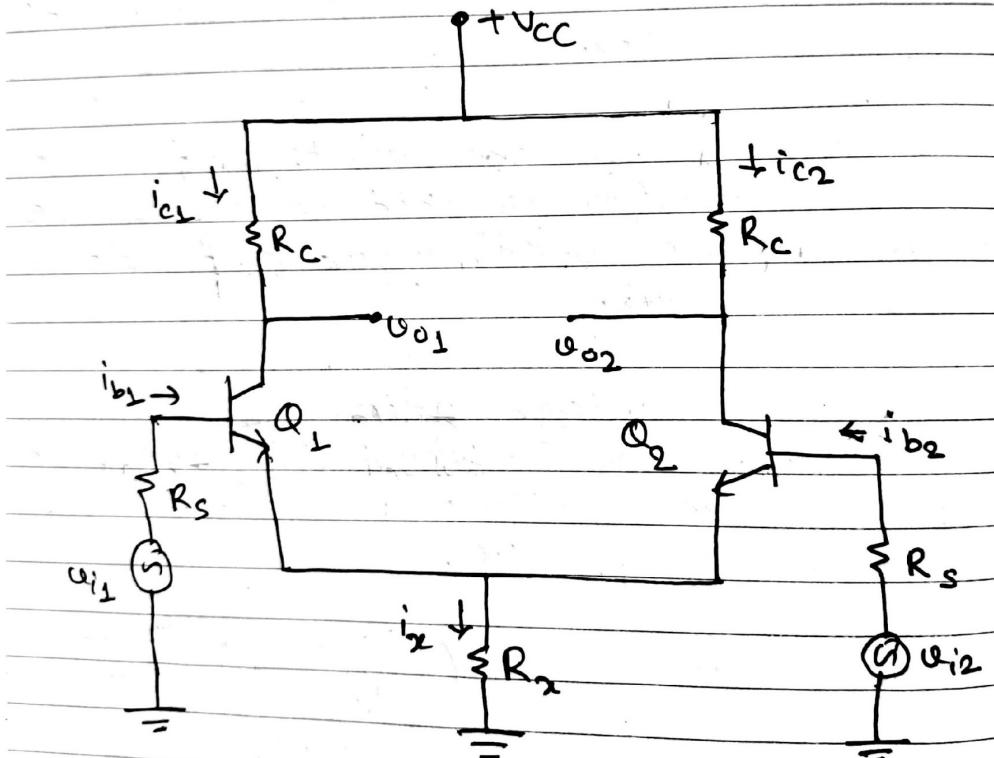


Fig. Differential amplifier

From, the circuit, we have

$$u_{i1} = i_{b1} R_s + i_{e1} r_e + i_x R_x \longrightarrow i>$$

$$u_{i2} = i_{b2} R_s + i_{e2} r_e + i_x R_x \longrightarrow ii>$$

Now,

$$u_{i1} - u_{i2} = (i_{b1} - i_{b2}) R_s + (i_{e1} - i_{e2}) r_e$$

we also have,

$$i_{e1} = (\beta + 1) i_{b1} \text{ and } i_{e2} = (\beta + 1) i_{b2}$$

$$\begin{aligned} \therefore u_{i1} - u_{i2} &= (i_{b1} - i_{b2}) R_s + (\beta + 1)(i_{b1} - i_{b2}) r_e \\ &= (i_{b1} - i_{b2}) [R_s + (\beta + 1) r_e] \end{aligned}$$

$$\therefore i_{b1} - i_{b2} = \frac{u_{i1} - u_{i2}}{R_s + (\beta + 1) r_e} \longrightarrow (iii)$$

$$\text{Again, } u_o = u_{o1} - u_{o2}$$

$$= i_{c1} R_C - i_{c2} R_C$$

$$= \beta i_{b1} R_C - \beta i_{b2} R_C$$

$$= \beta R_C (i_{b1} - i_{b2}) \longrightarrow iv>$$

From (iii) and (iv) we get

$$v_o = \beta R_c \left[ \frac{u_{i_2} - u_{i_1}}{R_s + (\beta + 1)r_e} \right]$$

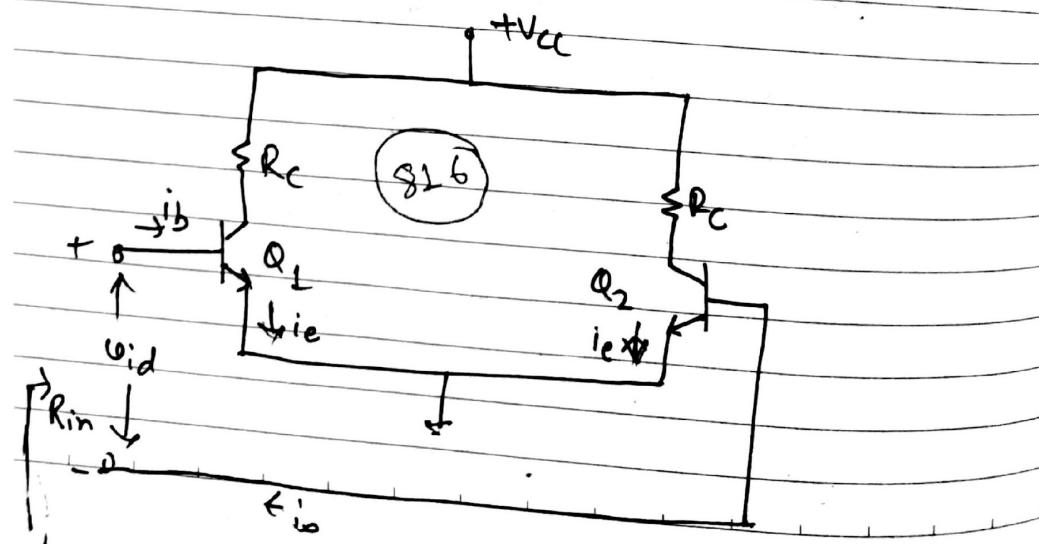
$$v_o = K (u_{i_2} - u_{i_1})$$

where,

$$K = \frac{\beta R_c}{R_s + (\beta + 1)r_e}$$

$$v_o \propto (u_{i_2} - u_{i_1}) \quad \text{Proved}$$

Differential input resistance in terms of circuit parameters :



$$i_e = \frac{u_{id}}{2r_e} \Rightarrow i_b = \frac{i_e}{\beta + 1}$$

$$R_{in} = \frac{u_{id}}{i_b} = 2(\beta + 1) r_e.$$

## DC Analysis of Differential Amplifier

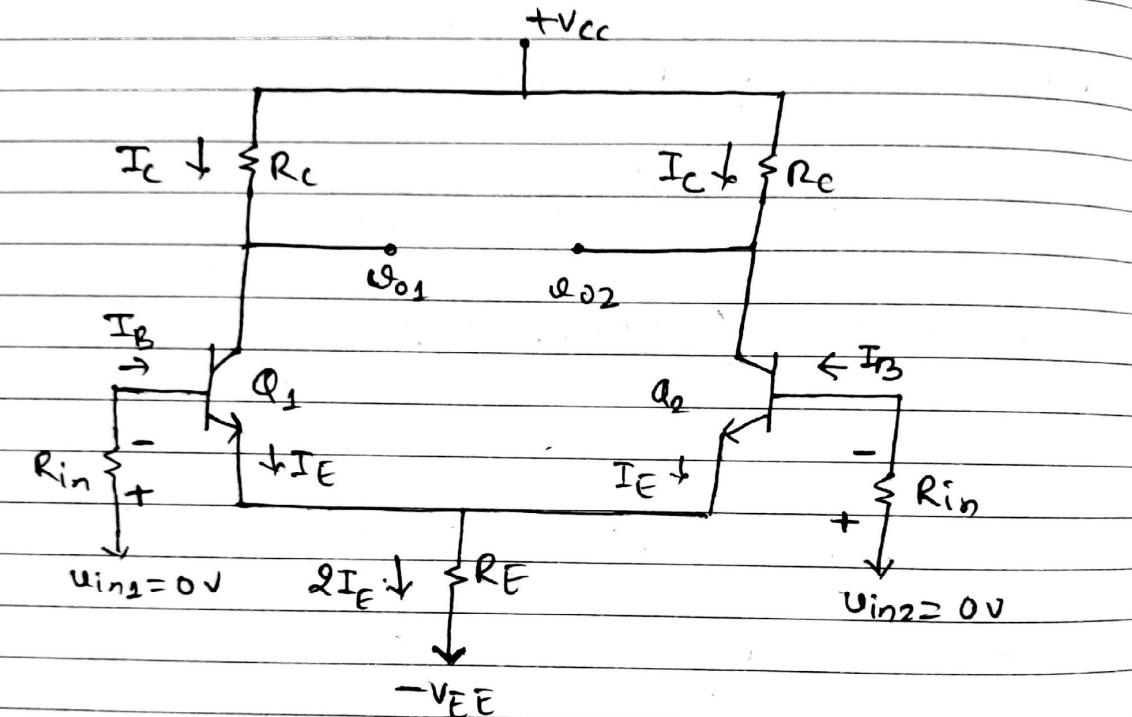


Fig: Dual input balanced output differential amplifier.

- DC Analysis of differential amplifier circuit is done for determination of operating points ( $I_{CQ}$  and  $V_{CEQ}$ ) when no signal is applied.
- For dc analysis, we set  $u_{in1} = u_{in2} = 0$  (i.e. ground).

. Since, both transistors  $Q_1$  and  $Q_2$  are identical we calculate Q-point for transistor  $Q_1$  only. The same Q-point can be used for transistor  $Q_2$  also.

Applying KVL to base-emitter loop of transistor  $Q_1$ , we get

$$-I_B R_{in} - V_{BE} - 2I_E R_E + V_{EE} = 0$$

since  $I_C \approx I_E$  and  $I_B = \frac{I_E}{\beta+1}$ , we have

$$-\frac{I_E}{\beta+1} R_{in} - V_{BE} - 2I_E R_E + V_{EE} = 0$$

$$I_E = \frac{V_{EE} - V_{BE}}{R_E + \frac{R_{in}}{\beta+1}}$$

since  $\frac{R_{in}}{\beta+1} \ll R_E$ , so

$$I_E = \frac{V_{EE} - V_{BE}}{R_E}$$

$I_C = \frac{V_{EE} - V_{BE}}{R_E}$
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The above expression shows that emitter current can be set by varying  $R_E$  only. Also, it is noticeable that emitted current in transistors  $Q_1$  and  $Q_2$  is independent of collector resistance  $R_C$ .

To find  $V_{CE}$ , we have

$$V_C = V_{CC} - I_C R_C$$

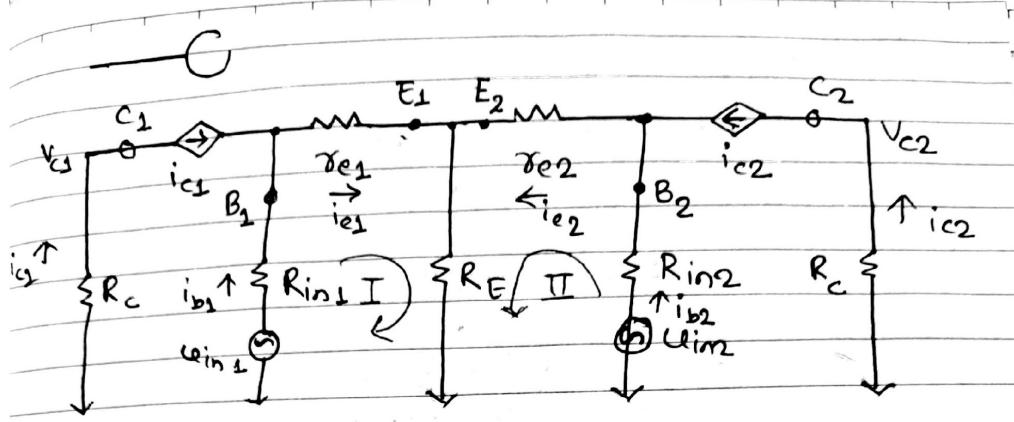
$$\text{and, } V_{CE} = V_C - V_E \\ = V_{CC} - I_C R_C - (-V_{BE})$$

$$V_{CE} = V_{CC} + V_{BE} - I_C R_C$$

Hence, for both transistors  $I_C$  and  $V_{CE}$  can be determined by using above expressions.

### AC Analysis

For ac analysis, the dc voltages  $+V_{CC}$  and  $-V_{EE}$  are set at zero and small signal T-equivalent models are substituted for transistors  $Q_1$  and  $Q_2$ .



Since the transistors  $Q_1$  and  $Q_2$  are matched so that  $\tau_{e1} = \tau_{e2} = \tau_e$  and  $R_{in1} = R_{in2} = R_{in}$

Now, applying KVL in loop I and loop II, we get

$$u_{in1} = i_{b1}R_{in1} + i_{e1}\tau_{e1} + (i_{e1} + i_{e2})R_E$$

$$u_{in2} = i_{b2}R_{in2} + i_{e2}\tau_{e2} + (i_{e1} + i_{e2})R_E$$

$$\text{So, } u_{in1} - u_{in2} = (i_{b1} - i_{b2})R_{in} + (i_{e1} - i_{e2})\tau_e$$

$$= (i_{b1} - i_{b2})R_{in} + (\beta + 1)(i_{b1} - i_{b2})\tau_e$$

$$= (i_{b1} - i_{b2}) [R_{in} + (\beta + 1)\tau_e]$$

$$i_{b1} - i_{b2} = \frac{u_{in1} - u_{in2}}{R_{in} + (\beta + 1)\tau_e}$$

NOW, we have,

$$\begin{aligned} v_o &= v_{c2} - v_{c1} \\ &= -i_{c2}R_c - (-i_{c1}R_c) \\ &= (i_{c1} - i_{c2})R_c \\ &= \beta(i_{b1} - i_{b2})R_c \end{aligned}$$

$$\Rightarrow v_o = \beta R_c \frac{(u_{in1} - u_{in2})}{R_{in} + (\beta + 1)\gamma_e}$$

$$\Rightarrow \frac{v_o}{u_{in1} - u_{in2}} = \frac{\beta R_c}{R_{in} + (\beta + 1)\gamma_e}$$

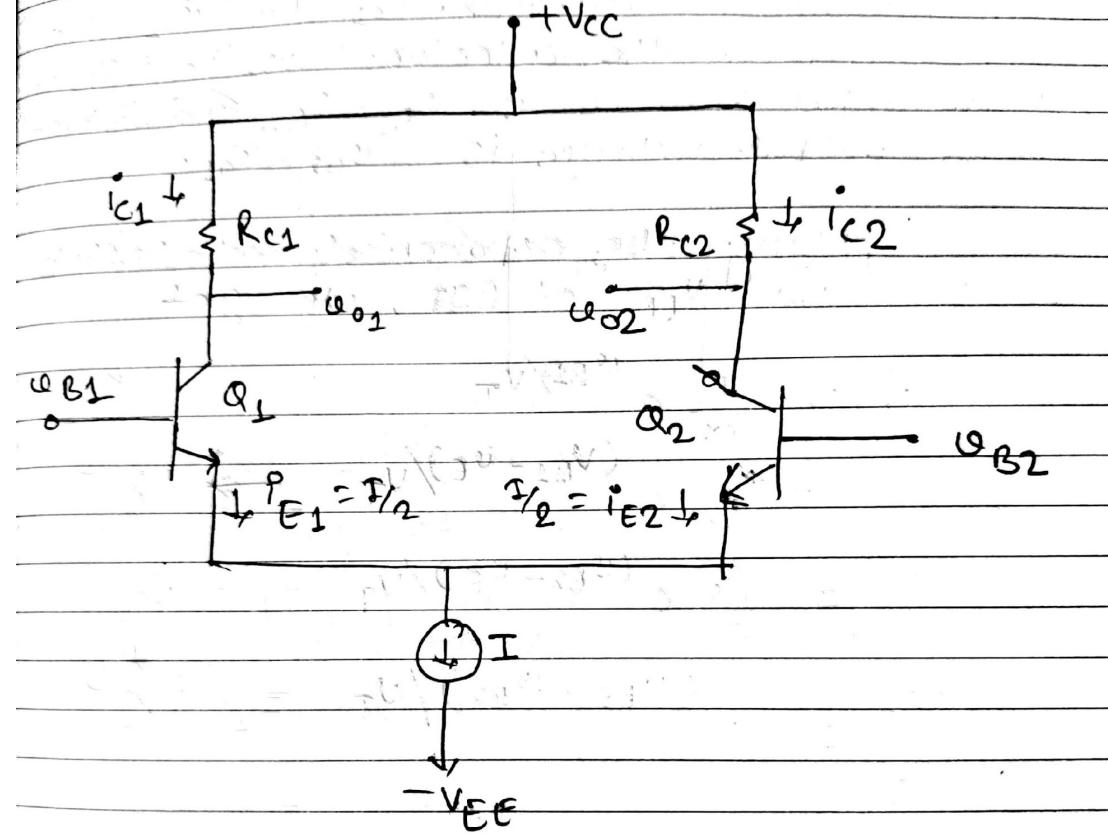
since  $(\beta + 1)\gamma_e \gg R_{in}$ , we have

$$\Rightarrow \frac{v_o}{u_{in1} - u_{in2}} = \frac{R_c}{\gamma_e}$$

$$\therefore A_d \text{ (differential gain)} = \frac{v_o}{u_{id}} = \frac{R_c}{\gamma_e}$$

The expression shows that  $A_d$  is directly proportional to the collector resistance  $R_c$  i.e. load.

# complete analysis of Differential Amplifier



Let  $v_{B_1}$  and  $v_{B_2}$  be two input signals to the differential amplifier.  $v_{o_1}$  and  $v_{o_2}$  be the outputs at the collector. Thus, the differential input voltage is  $v_{B_1} - v_{B_2}$  and differential output voltage is  $v_{o_2} - v_{o_1}$ .

NOW, applying the exponential relationship of  $i_E^o$  and  $v_{BE}$  of BJT, we get

$$\begin{aligned} i_{E1}^o &= \frac{I_s}{\alpha} e^{(v_{B1} - v_E)/V_T} \\ &= \frac{I_s}{\alpha} e^{(v_{B1} - v_E)/V_T} \rightarrow i) \end{aligned}$$

$$i_{E2}^o = \frac{I_s}{\alpha} e^{(v_{B2} - v_E)/V_T} \rightarrow ii)$$

$$\frac{i_{E1}^o}{i_{E2}^o} = e^{(v_{B1} - v_{B2})/V_T} \rightarrow iii)$$

Thus, we get

$$\frac{i_{E1}^o}{i_{E1}^o + i_{E2}^o} = \frac{1}{1 + e^{-(v_{B1} - v_{B2})/V_T}} \rightarrow iv)$$

$$\frac{i_{E2}^o}{i_{E1}^o + i_{E2}^o} = \frac{1}{1 + e^{(v_{B1} - v_{B2})/V_T}} \rightarrow v)$$

we have,

$$i_{E1}^{\circ} + i_{E2}^{\circ} = I$$

$$\therefore i_{E1}^{\circ} = \frac{I}{1 + e^{-\frac{V_{id}}{V_T}}} \quad [V_{fd} = V_{B1} - V_{B2}]$$

and,  $i_{E2}^{\circ} = \frac{I}{1 + e^{\frac{V_{id}}{V_T}}} \quad [V_{id} = V_{B1} - V_{B2}]$

so,  $i_{C1} = \frac{\alpha I}{1 + e^{-\frac{V_{id}}{V_T}}}$

$$i_{C2} = \frac{\alpha I}{1 + e^{\frac{V_{id}}{V_T}}}$$

Now, multiplying numerator and denominator by  $e^{\frac{V_{id}}{2V_T}}$ , we get

$$i_{C1} = \frac{\alpha I e^{\frac{V_{id}}{2V_T}}}{e^{\frac{V_{id}}{2V_T}} + e^{-\frac{V_{id}}{2V_T}}}$$

$$= \frac{\alpha I (1 + \frac{V_{id}}{2V_T} + \dots)}{(1 + \frac{V_{id}}{2V_T} + \dots) + (1 - \frac{V_{id}}{2V_T} + \dots)}$$

$$= \frac{\alpha I}{2} + \frac{\alpha I}{2V_T} \cdot \left( \frac{V_{id}}{2} \right)$$

$$= I_{C1} + \frac{i_{C1}}{(\alpha C)}$$

Similarly,

$$i_{C2} = \frac{\alpha I}{2} - \frac{\alpha I}{2V_T} \cdot \frac{U_{id}}{2}$$

So,

$$(ac) \quad i_{C1} = \frac{\alpha I}{2V_T} \cdot \frac{U_{id}}{2} = \frac{I_C}{V_T} \cdot \frac{U_{id}}{2} = \frac{g_m U_{id}}{2}$$

$$(ac) \quad i_{C2} = -\frac{\alpha I}{2V_T} \cdot \frac{U_{id}}{2} = -\frac{I_C}{V_T} \cdot \frac{U_{id}}{2} = -\frac{g_m U_{id}}{2}$$

Thus,  $V_{O1} = V_{CC} - i_{C1} R_C$

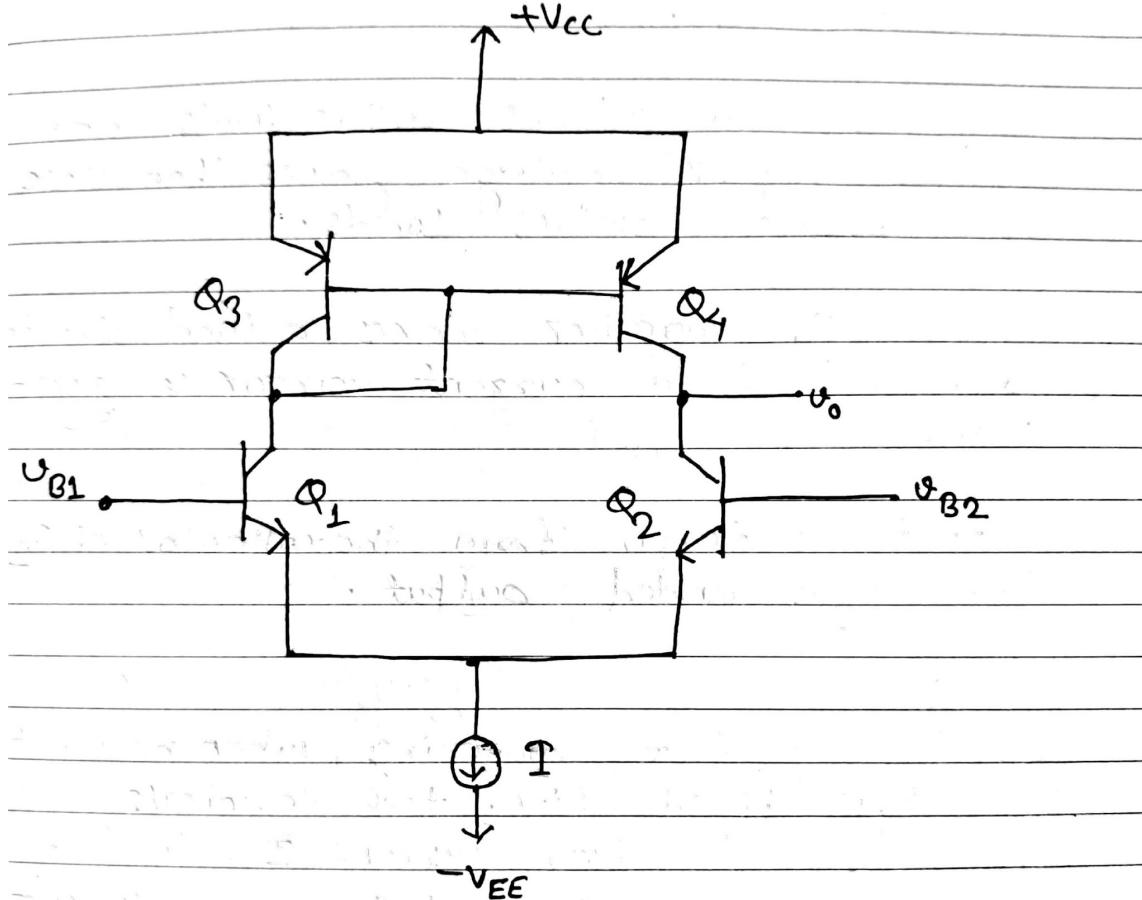
$$V_{O2} = V_{CC} - i_{C2} R_C$$

∴ Output voltage is given by

$$\begin{aligned} V_O &= V_{O2} - V_{O1} \\ &= -\frac{g_m U_{id}}{2} R_C - \frac{g_m U_{id}}{2} R_C \end{aligned}$$

$$V_O = g_m U_{id} R_C$$

## BJT Amplifier with active load



→ Active devices (transistors) occupy much less silicon area than medium and large sized resistors.

→ BJT load transistor is usually connected as a current source.

- The output resistance of current source is very high.
- Amplifiers that utilizes active loads can achieve higher voltage gains than those with passive (resistive) loads.
- $Q_3$  and  $Q_4$  together makes a load circuit connected in a current mirror configuration.
- Output is taken from the collector of  $Q_2$  i.e. single ended output.

#### Case I:

Assuming perfect matching, when no input signal is applied (i.e. two terminals are grounded), the bias current  $I$  divided equally between  $Q_1$  and  $Q_2$ . The current of  $Q_1$  is fed to the input transistor of the mirror  $Q_3$ . Thus, the replica of this current is provided by the output transistor of mirror  $Q_4$ . The output node of the two current  $I/2$  balance each other out leaving a zero current to the load.

Case II:

consider, differential signal  $v_{rid} = (v_{B1} - v_{B2})$  is applied at the input. Then the current signals  $g_m v_{rid}$  will result in the collector of  $Q_1$  and  $\frac{1}{2} Q_2$  with polarities indicated.

Also, due to current mirror configuration, the current signal  $g_m \frac{(v_{rid})}{2}$  flows through collector of  $Q_1$ . Now, if resistance between output terminal and ground is  $R_o$ , then

$$v_o = g_m v_{rid} R_o$$