## 11. Limits, Continuity and Differentiability

## EE24BTECH11047 - Niketh Prakash Achanta

I.	C: MCQs	WITH	ONE	CORRECT	ANSWER
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- 1)  $\lim_{x\to 0} \frac{\sin(\pi\cos^2 x)}{x^2}$  equals (2001S)a)  $-\pi$ 

  - b)  $\pi$
  - c)  $\pi/2$
  - d) 1
- 2) The left-hand derivative of  $f(x)=[x]\sin(\pi x)$  at x=k, k an integer, is (2001S)
  - a)  $(-1)^k (-1) \pi$
  - b)  $(-1)^{k-1} (k-1) \pi$
  - c)  $-1^k k\pi$
  - d)  $-1^{k-1}k\pi$
- 3) Let  $f: R \to R$  be a function defined by  $f(x)=\max\{x, x^3\}$ . The set of all points where f(x) is NOT differentiable is (2001S)
  - a)  $\{-1, 1\}$
  - b)  $\{-1,0\}$
  - c) {0, 1}
  - d)  $\{-1,0,1\}$
- 4) Which of the following functions is differentiable at x=0(2001S)
  - a)  $\cos(|x|) + |x|$
  - b)  $\cos(|x|) |x|$
  - c)  $\sin(|x|) + |x|$
  - d)  $\sin(|x|) |x|$
- 5) The domain of the derivative of the function  $f(x) = \begin{cases} \tan^{-1} x & \text{if } |x| \le 0 \\ \frac{1}{2}(|x| - 1) & \text{if } x > 1 \end{cases} \text{ is}$ (2002S)
  - a)  $R \{0\}$
  - b)  $R \{1\}$
  - c)  $R \{-1\}$
  - d)  $R \{-1, 1\}$
- 6) The integer n for which  $\lim_{x\to 0} \frac{(cosx-1)(cosx-e^x)}{x^n}$  is a finite non-zero number is (2002S)
  - a) 1
  - b) 2

- c) 3
- d) 4
- 7) Let  $f: R \to R$  be such that f(1) = 3 and f'(1) = 6. Then  $\lim_{x\to 0} \left( \frac{f(1+x)}{f(1)} \right)$ (2002S)equals

1

- a) 1
- b)  $e^{1/2}$
- c)  $e^2$
- d)  $e^3$
- 8) If  $\lim_{x\to 0} \frac{((a-n)nx-tanx)sinnx}{x^2} = 0$ , where n is nonzero real number, then a is equal (2003S)
  - a) 0
  - b)  $\frac{n+1}{n}$
  - c) n
  - d)  $n + \frac{1}{n}$
- 9)  $\lim_{h\to 0} \frac{f(2h+2+h^2)-f(2)}{f(h-h^2+1)-f(1)}$ given that f'(2)=6 and f'(1)=4(2003S)
  - a) Does not exist
  - b) is equal to -3/2
  - c) is equal to 3/2
  - d) is equal to 3
- 10) If f(x) is differentiable and strictly increasing function, then the value of  $\lim_{x\to 0} \frac{f(x^2)-f(x)}{f(x)-f(0)}$ 2004S)
  - a)  $(-1)^k (k-1) \pi$
  - b)  $(-1)^{k-1} (k-1) \pi$
  - c)  $(-1)^k k\pi$
  - d)  $(-1)^{k-1} k\pi$
- 11) The function given by y = ||x| 1| is differentiable for all real numbers except the points (2005S)
  - a)  $\{0, 1, -1\}$
  - $b) \pm 1$
  - c) 1
  - d) -1

- 12) If f(x) is a continuous and differentiable function and  $f(1/n) = 0 \ \forall \ n \ge 1 \ and \ n \in I$ , then (2005S)
  - a)  $f(x) = 0, x \in (0, 1]$
  - b) f(0) = 0, f'(0) = 0
  - c)  $f(0) = 0 = f'(0), x \in (0, 1]$
  - d) f(0) = 0 and f'(0) need not be zero
- 13) The value of  $\lim_{x\to 0} ((sin)^{1/x} + (1+x)^{sinx})$ , where x > 0 is (2006-3M,-1)
  - a) 0
  - b) -1
  - c) 1
  - d) 2
- 14) Let f(x) be differentiable on the interval  $(0, \infty)$  such that f(1) = 1, and  $\lim_{t \to x} \frac{t^2 f(x) x^2 f(t)}{t x} = 1$  for each x > 0. Then f(x) is (2007-3marks)
  - a)  $\frac{1}{3x} + \frac{2x^2}{3}$
  - b)  $\frac{-1}{3x} + \frac{4x^2}{3}$
  - c)  $\frac{-1}{x} + \frac{2}{x^2}$
  - d)  $\frac{1}{r}$
- 15)  $\lim_{x \to \frac{\pi}{4}} \frac{\int_{2}^{sec^{2}x} f(t)dt}{x^{2} \frac{\pi^{2}}{16}}$  equals (2007-3marks)
  - a)  $\frac{8}{\pi}f(2)$ b)  $\frac{2}{\pi}f(2)$ c)  $\frac{2}{\pi}f(\frac{1}{2})$

  - d) 4f(2)