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KNN

classmate

Date _____
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d

		[5, 5]		[1, 2]	$\sqrt{16+9}$ $= 5$
	0				
	0			[2, 3]	$\sqrt{9+4}$ $= \sqrt{13}$
				3-6	
	0			[3, 1]	$\sqrt{4+16}$ $= \sqrt{20}$
				4-4	
class	}	1	→	[6, 5]	$\sqrt{1}$ $= 1$
		1			
		1		[7, 7]	$\sqrt{4+4} = \sqrt{8}$
				2-828	
			→	[8, 6]	$= \sqrt{9+1} = \sqrt{10}$
			→	3-16	

KNN is a supervised learning algorithm used for classification and regression.

Steps:-

- Choose the value of K (number of neighbours)
- calculate the distance (euclidean) between the new-data and training samples
- Sort and pick the k-nearest neighbour.
- Take a majority vote (for classification)
- Assign the most frequent class as the predicted label.

import numpy as np
from collections import Counter

class KNN:

def __init__(self, k=3):

self.k = k

def fit(self, x, y):

self.x_train = np.array(x)

self.y_train = np.array(y)

def edistance(self, x1, x2):

return sqrt(np.sum((x1-x2)**2))

def predict(self, x):

predictions = [self.predict(x) for
x in x]

return np.array(predictions)

def predict(self, x)

d = [self.edistance(x, x_train) for
x_train in self.x_train]

k_i = np.argsort(d)[:self.k]

k_labels = [self.y_train[i] for i in
k_indices]

most_common = Counter(k_nearest_labels).
most_common(1)

return most_common[0][0]

x, y = load_iris_data()

train_size = int(0.8 * len(x))

x_train, x_test = x[:train_size], x[train_size:]

$x_{train}, y_{test} = x[\text{train_size}], y[\text{train_size}]$

$knn = KNN(k=3)$

$knn.fit(x_{train}, y_{train})$

$predicts = knn.predict(x_{test})$

* Support Vector Machine. (SVM)

Steps :-

1) Input the data

- Feature matrix X consisting of (samples \times features)
- Target labels y (multi-class - 0, 1, 2)
- Regularization constant c
- max_iteration

2) Split the Dataset into training set (70%) and testing set (30%)

3) Initialize the SVM classifier

set the following parameters.

c : regularization constant

max_iter: Number of training iterations

Kernel - linear defined $K(x, x') = x \cdot x'$

4) One vs Rest Training Strategy

For each class c in the set of unique classes: convert labels into Binary format

$$y_{binary} = \begin{cases} 1 & \text{if } y=c \\ -1 & \text{otherwise} \end{cases}$$

- Train a binary SVM classifier using the sequential minimal optimization

5) Binary SVM Training

Initialize

$$\alpha = 0$$

Lagrange multiplier

$$\beta = 0$$

Bias term

Repeat for max_iter iterations

For each training sample i :

- Randomly select another index j
- compute prediction errors ϵ_i and ϵ_j

- save old values α_i, α_j

- compute bounds L, H

if $L = H$ continue

- compute

$$\eta = 2K(x_i, x_j) - K(x_i, x_i) - K(x_j, x_j)$$

if $\eta \geq 0$ skip update

- update α_j

$$\alpha_j = \alpha_j + y_j \frac{(\epsilon_i - \epsilon_j)}{\eta}$$

- clip $\alpha_j \in [L, H]$

- update α_i

- compute β

e. Prediction Phase

For each test sample x

- For each trained binary classifier:
- compute decision score

$$f(x) = \sum_j \alpha_j y_j k(x_i, x_j) + b$$

- Store the score
- Predict the class with max decision score

f) Evaluation

- Compare predicted labels \hat{y}_{pred} with true labels y_{test}

- calculate accuracy

$$\text{Accuracy} = \frac{\text{No of correct predictions} \times 100}{\text{No of samples.}}$$

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