

## 0.1 Plots of single attributes

### 0.1.1 residual sugar

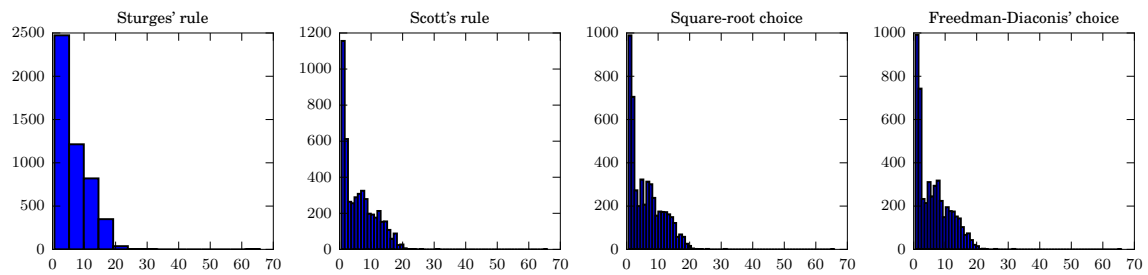


Figure 1: Histograms of attribute *residual sugar* using different binning methods

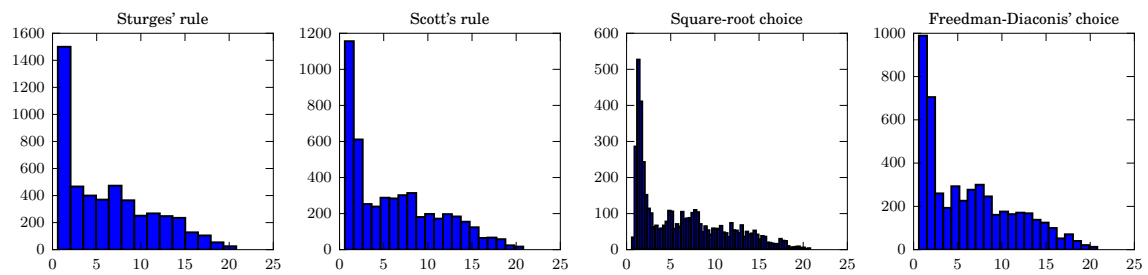


Figure 2: Histograms of attribute *residual sugar* with outliers further than 3 standard deviations from the mean filtered

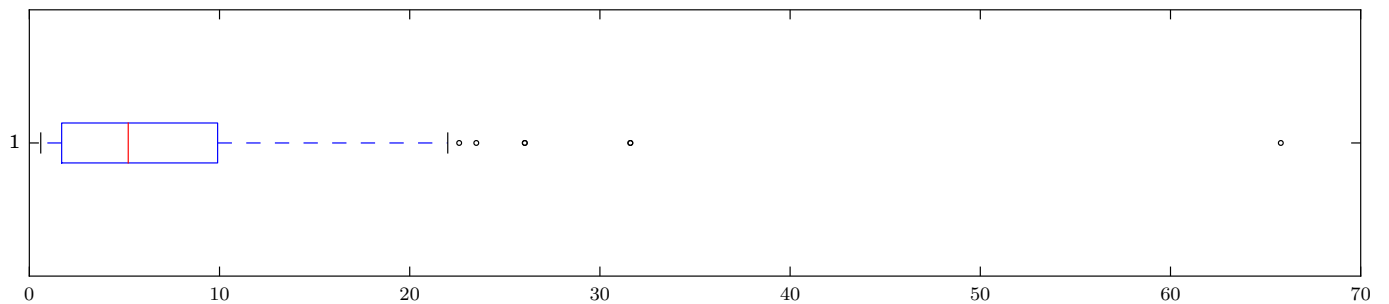


Figure 3: Boxplot of attribute *residual sugar*

## 0.1.2 fixed acidity

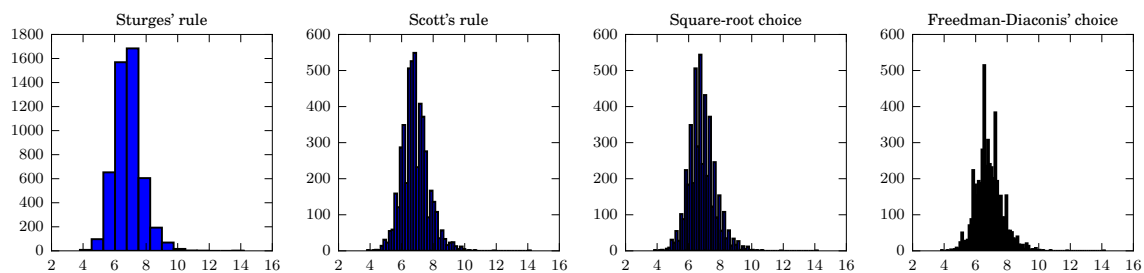


Figure 4: Histograms of attribute *fixed acidity* using different binning methods

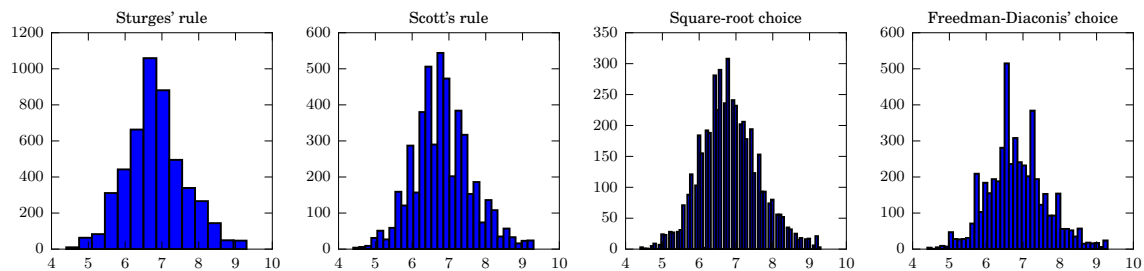


Figure 5: Histograms of attribute *fixed acidity* with outliers further than 3 standard deviations from the mean filtered

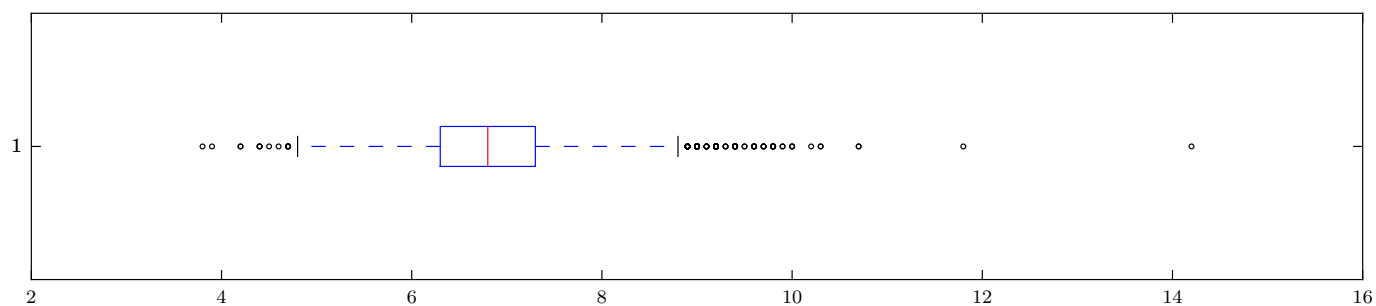


Figure 6: Boxplot of attribute *fixed acidity*

### 0.1.3 density

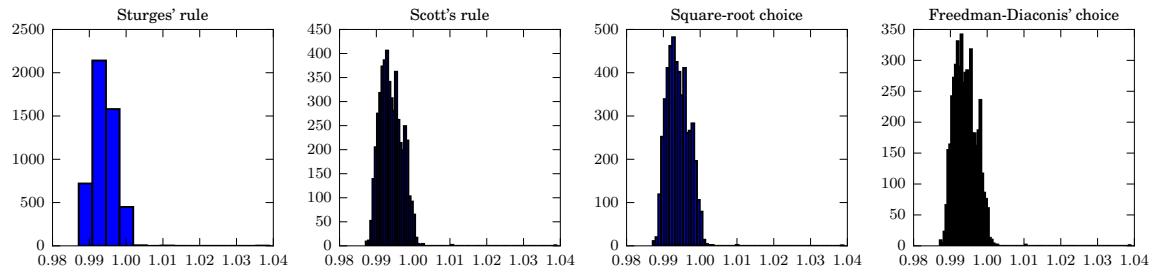


Figure 7: Histograms of attribute *density* using different binning methods

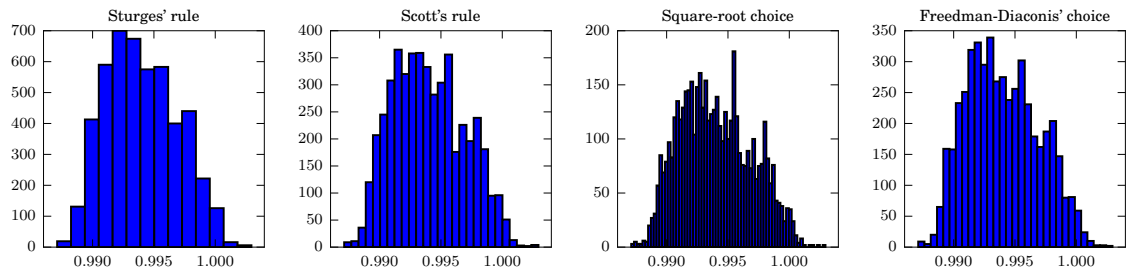


Figure 8: Histograms of attribute *density* with outliers further than 3 standard deviations from the mean filtered

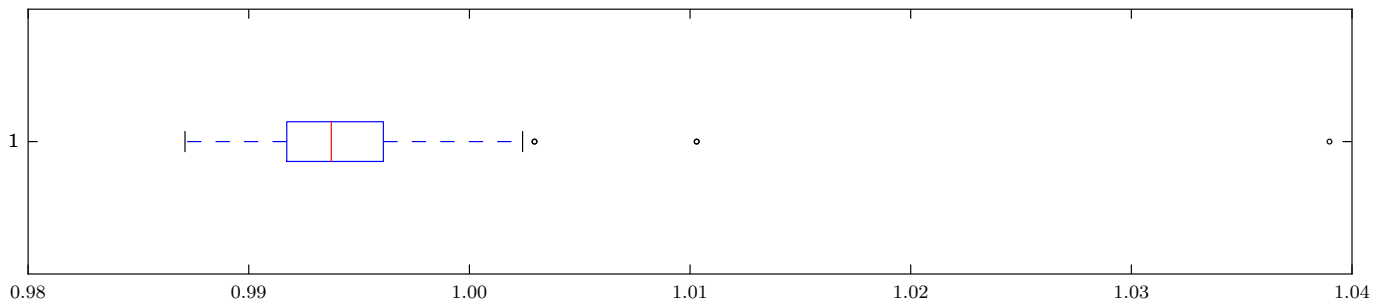


Figure 9: Boxplot of attribute *density*

### 0.1.4 volatile acidity

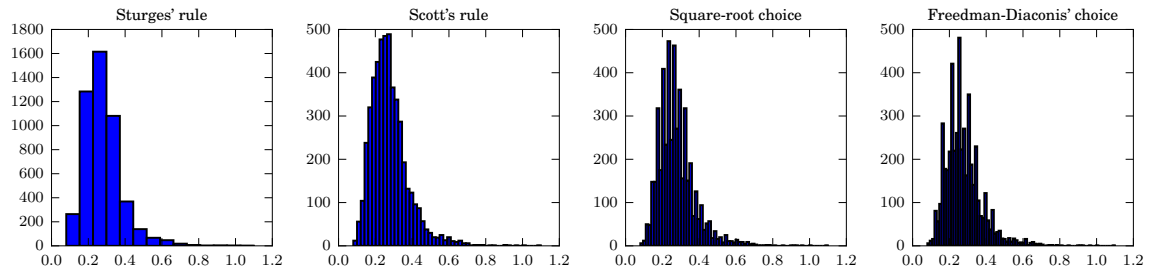


Figure 10: Histograms of attribute *volatile acidity* using different binning methods

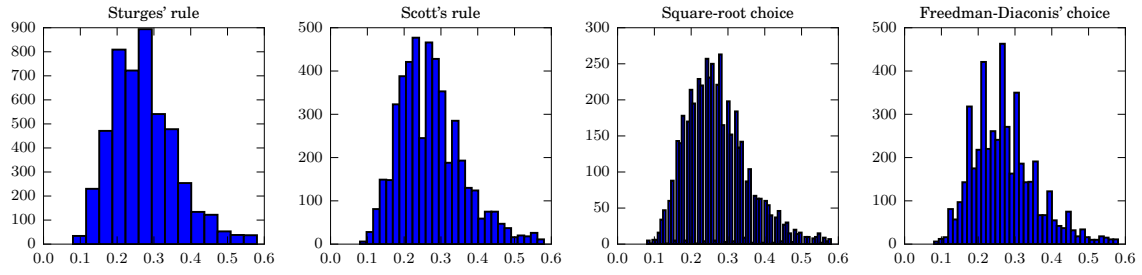


Figure 11: Histograms of attribute *volatile acidity* with outliers further than 3 standard deviations from the mean filtered

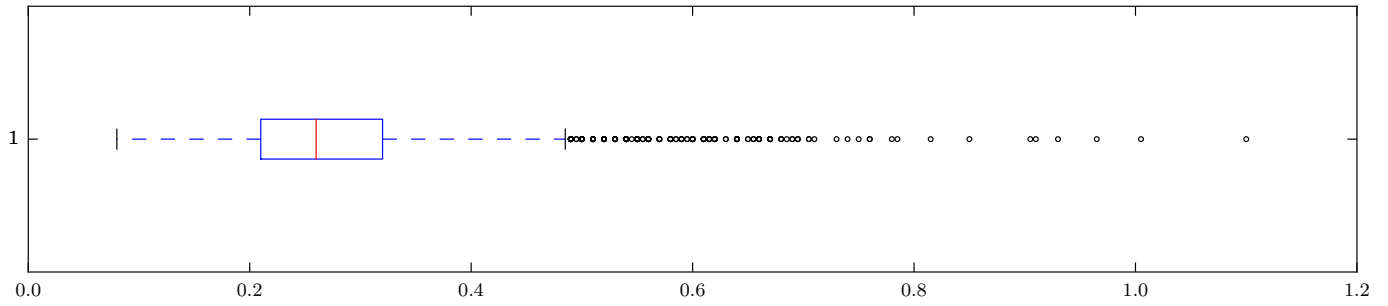


Figure 12: Boxplot of attribute *volatile acidity*

### 0.1.5 total sulfur dioxide

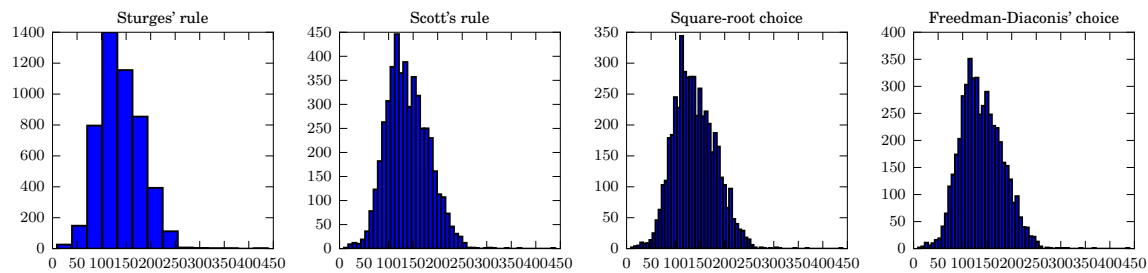


Figure 13: Histograms of attribute *total sulfur dioxide* using different binning methods

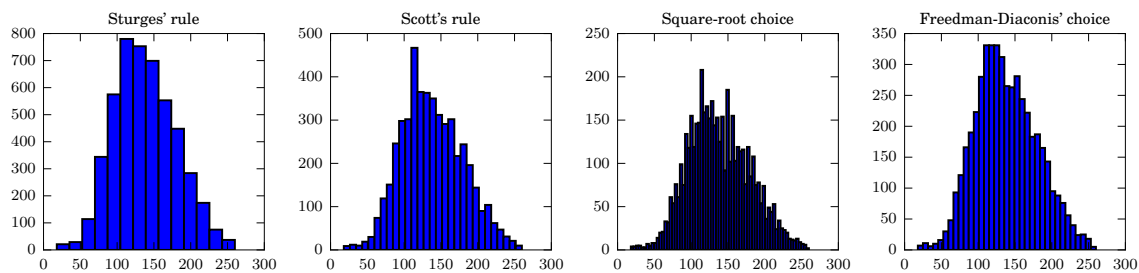


Figure 14: Histograms of attribute *total sulfur dioxide* with outliers further than 3 standard deviations from the mean filtered

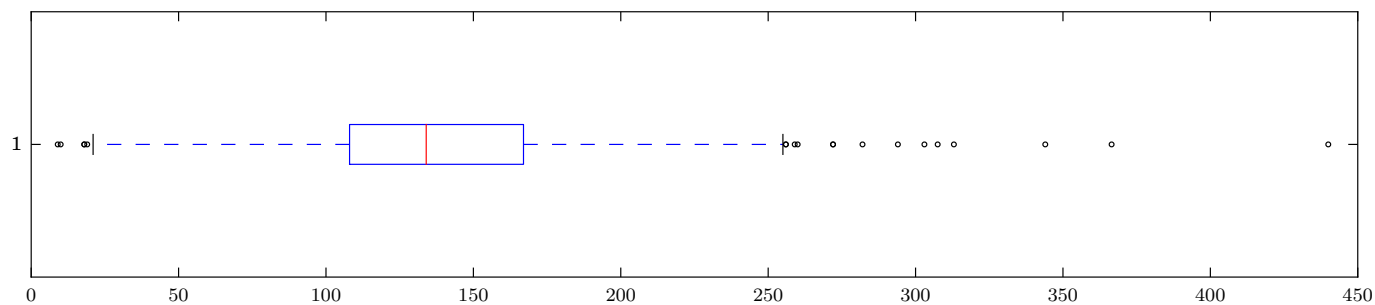


Figure 15: Boxplot of attribute *total sulfur dioxide*

## 0.1.6 alcohol

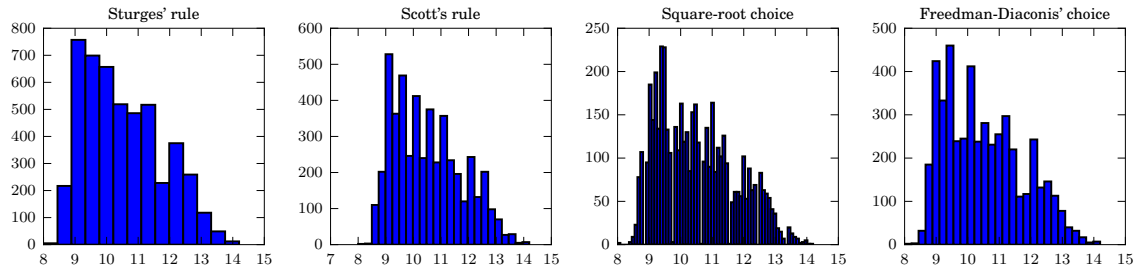


Figure 16: Histograms of attribute *alcohol* using different binning methods

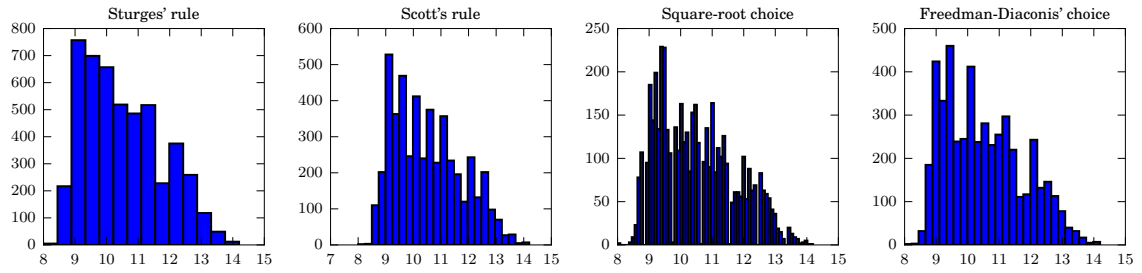


Figure 17: Histograms of attribute *alcohol* with outliers further than 3 standard deviations from the mean filtered

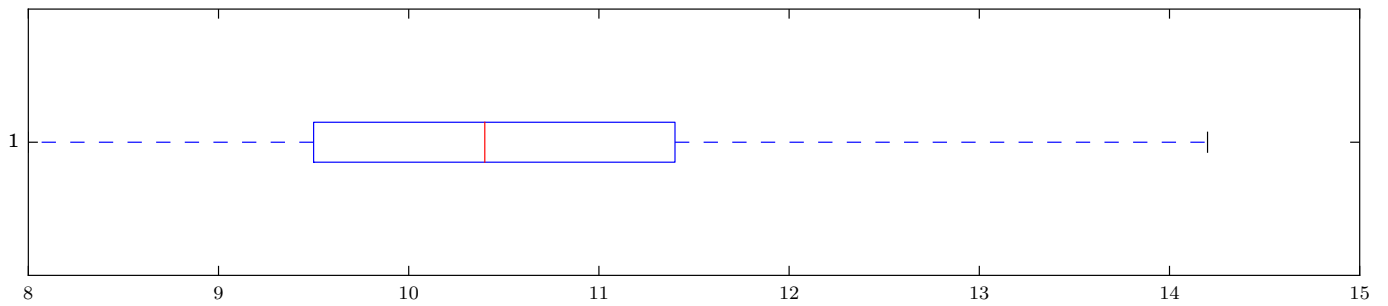


Figure 18: Boxplot of attribute *alcohol*

## 0.1.7 quality

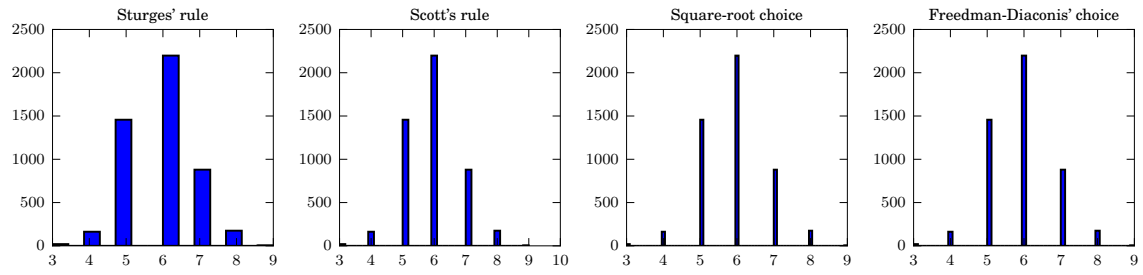


Figure 19: Histograms of attribute *quality* using different binning methods

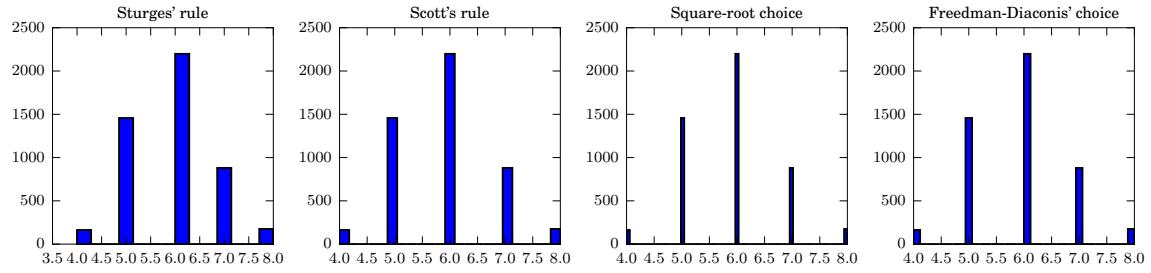


Figure 20: Histograms of attribute *quality* with outliers further than 3 standard deviations from the mean filtered

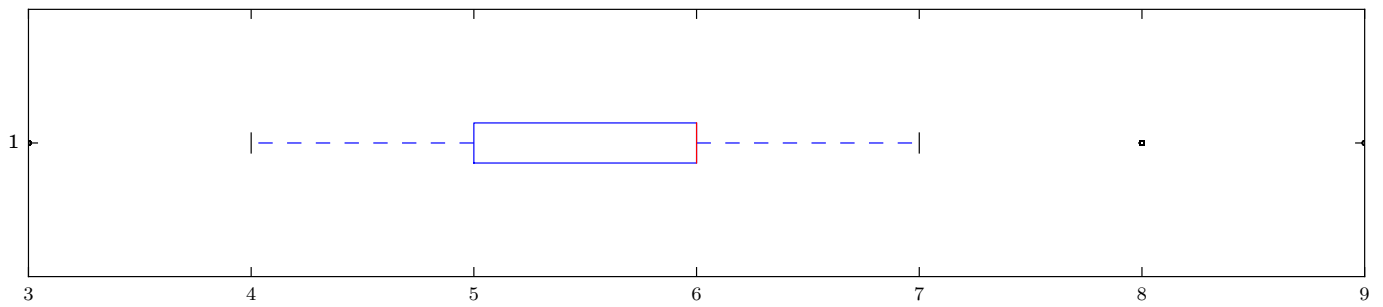


Figure 21: Boxplot of attribute *quality*

### 0.1.8 sulphates

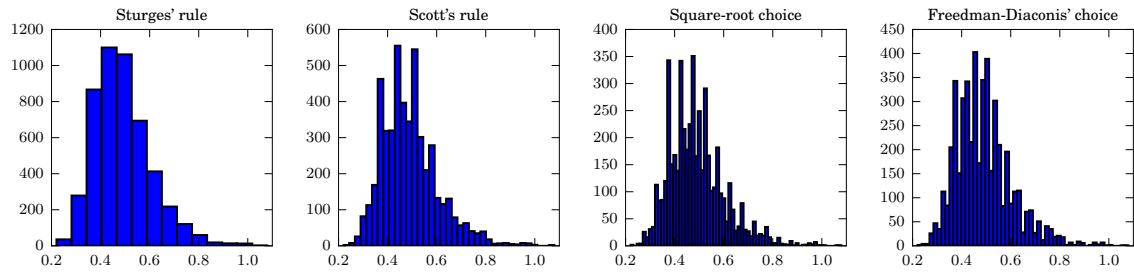


Figure 22: Histograms of attribute *sulphates* using different binning methods

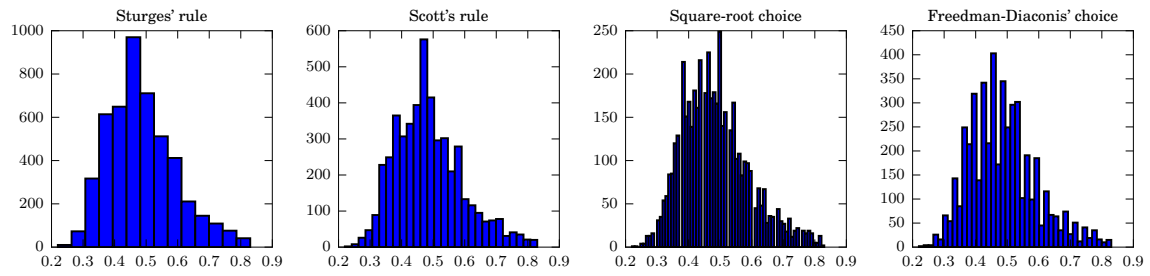


Figure 23: Histograms of attribute *sulphates* with outliers further than 3 standard deviations from the mean filtered

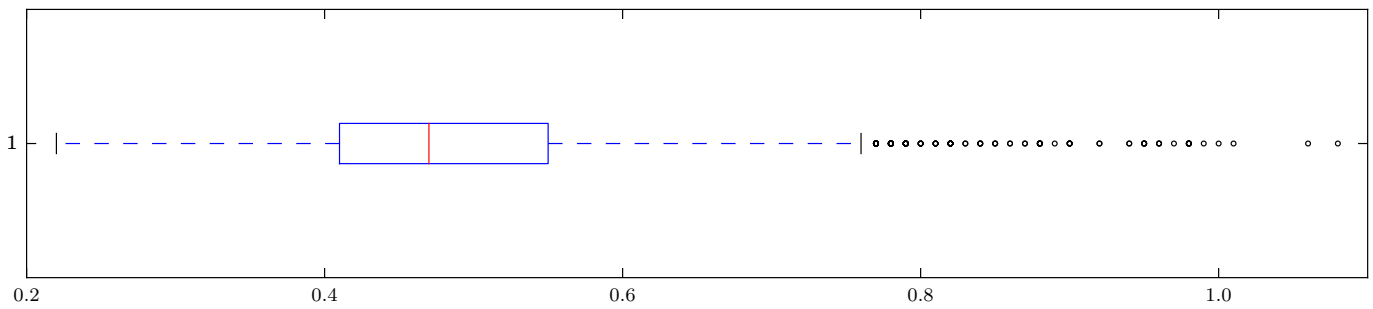


Figure 24: Boxplot of attribute *sulphates*



### 0.1.9 free sulfur dioxide

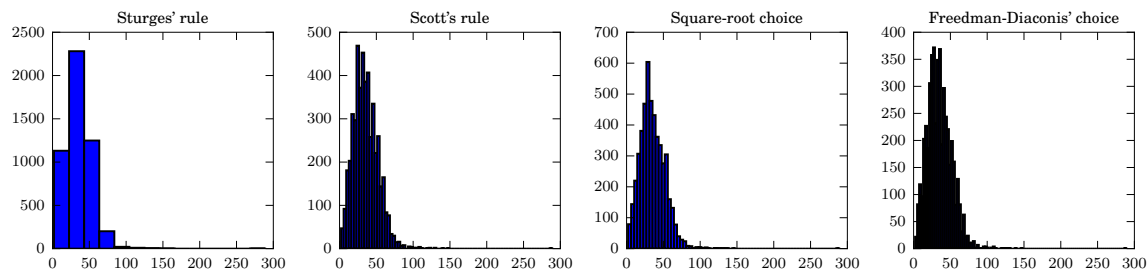


Figure 25: Histograms of attribute *free sulfur dioxide* using different binning methods

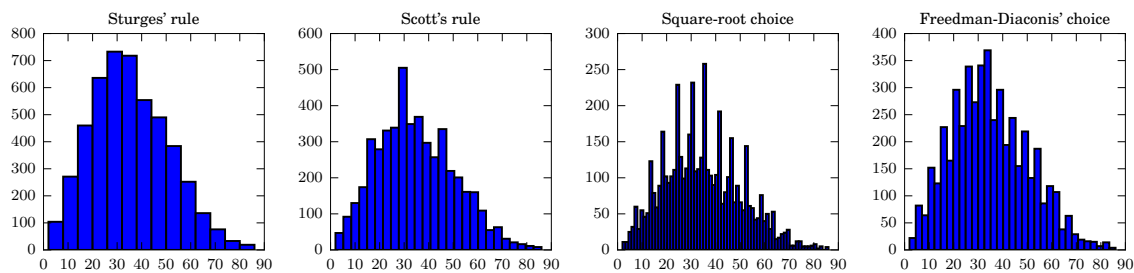


Figure 26: Histograms of attribute *free sulfur dioxide* with outliers further than 3 standard deviations from the mean filtered

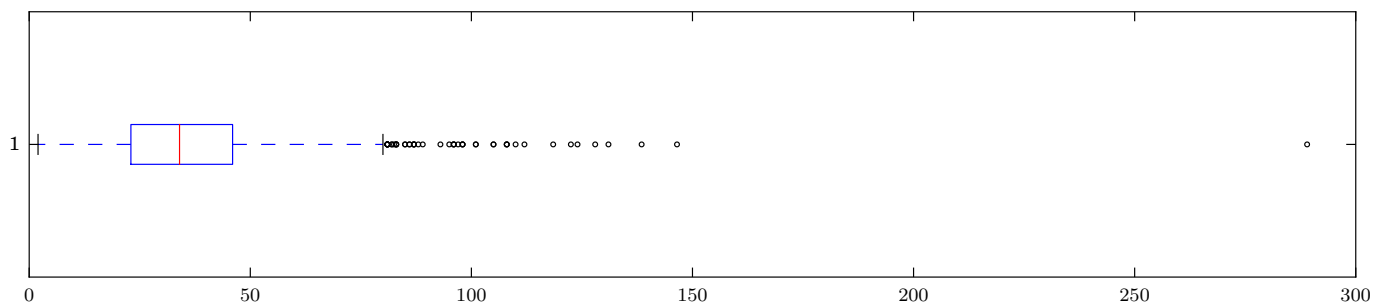


Figure 27: Boxplot of attribute *free sulfur dioxide*

### 0.1.10 chlorides

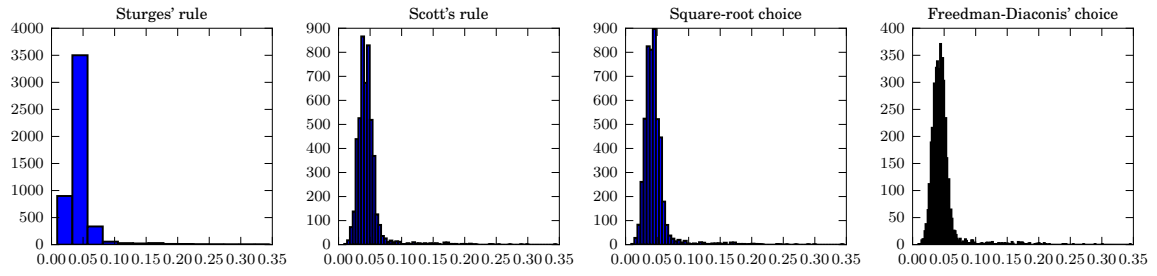


Figure 28: Histograms of attribute *chlorides* using different binning methods

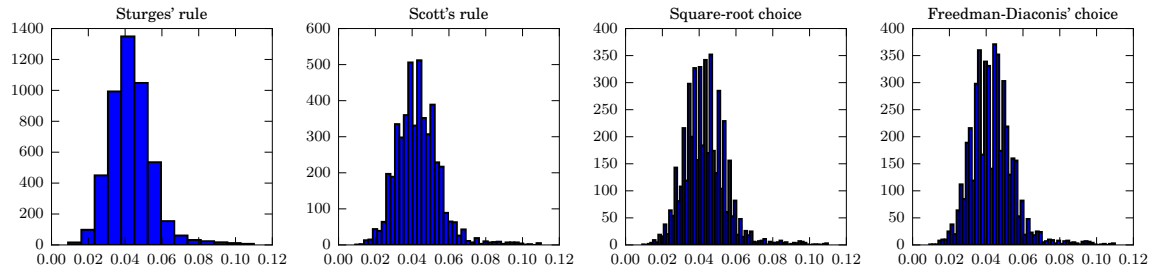


Figure 29: Histograms of attribute *chlorides* with outliers further than 3 standard deviations from the mean filtered

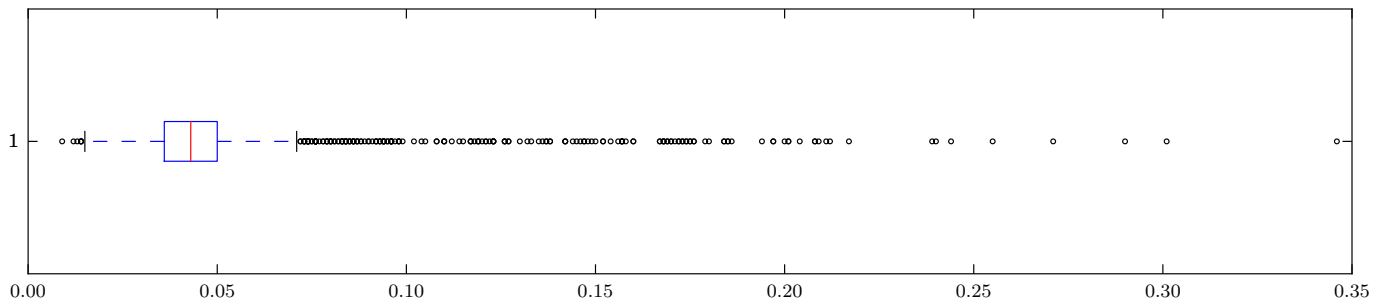


Figure 30: Boxplot of attribute *chlorides*

### 0.1.11 citric acid

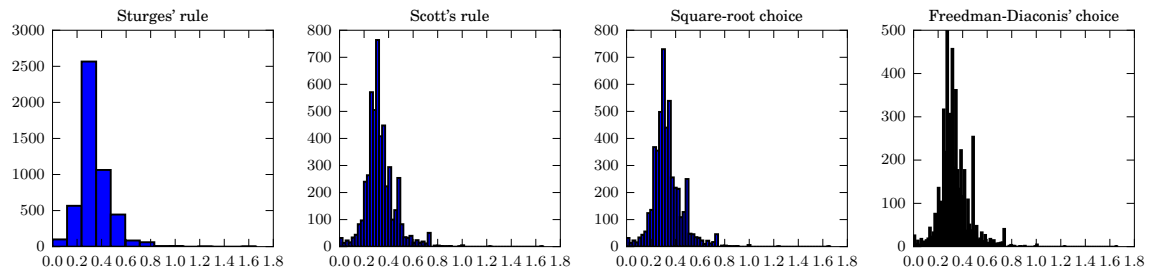


Figure 31: Histograms of attribute *citric acid* using different binning methods

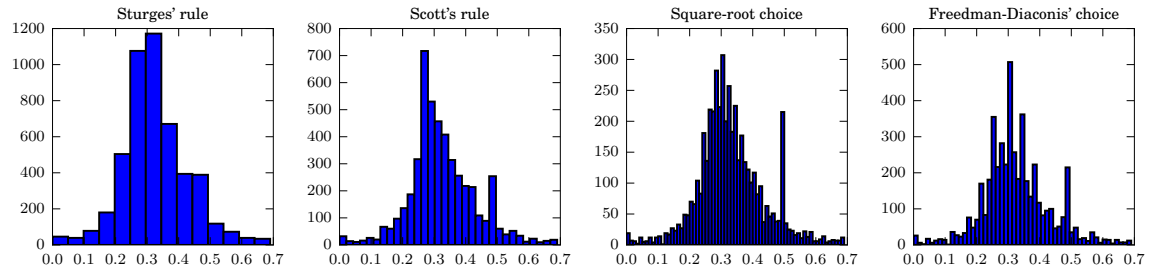


Figure 32: Histograms of attribute *citric acid* with outliers further than 3 standard deviations from the mean filtered

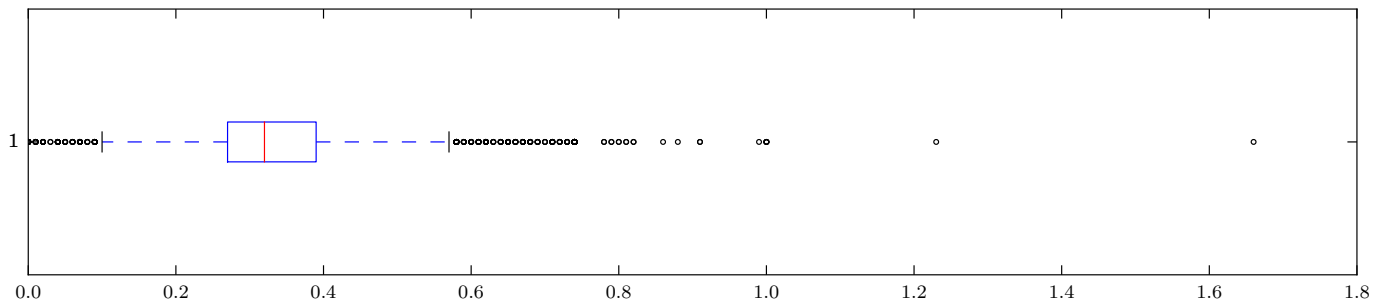


Figure 33: Boxplot of attribute *citric acid*

### 0.1.12 pH

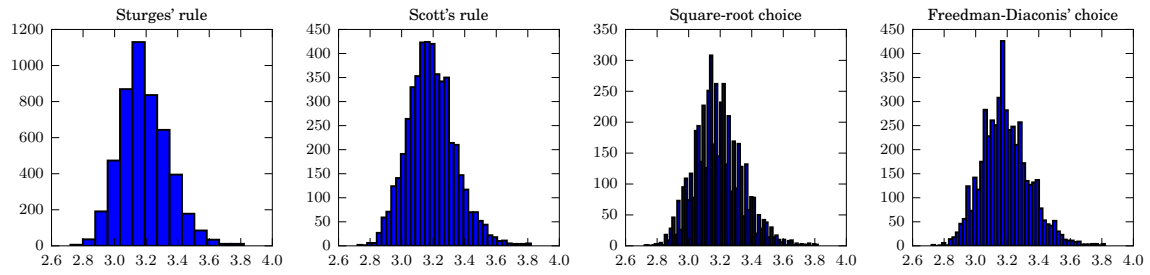


Figure 34: Histograms of attribute  $pH$  using different binning methods

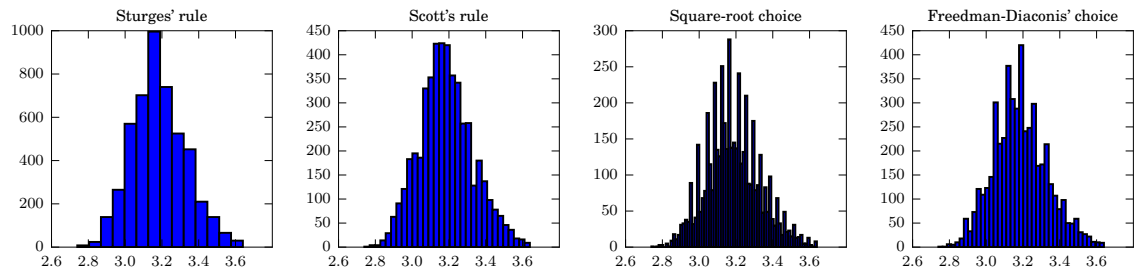


Figure 35: Histograms of attribute  $pH$  with outliers further than 3 standard deviations from the mean filtered

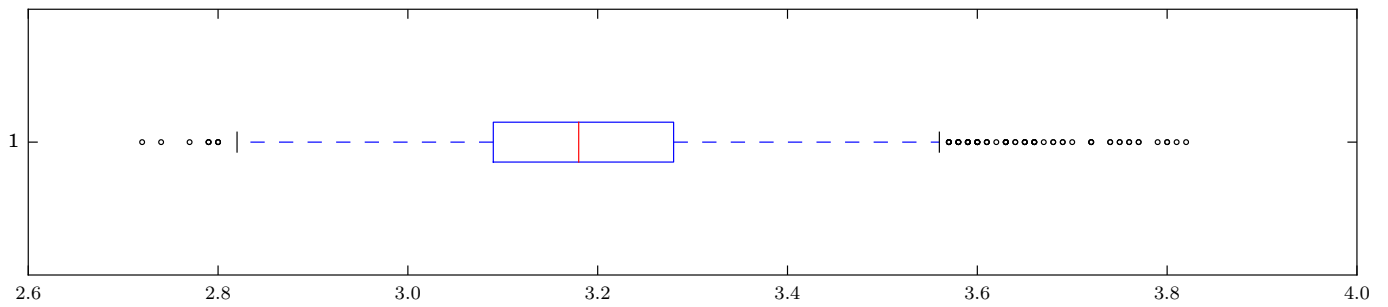


Figure 36: Boxplot of attribute  $pH$

## 0.2 Plots for the whole feature set

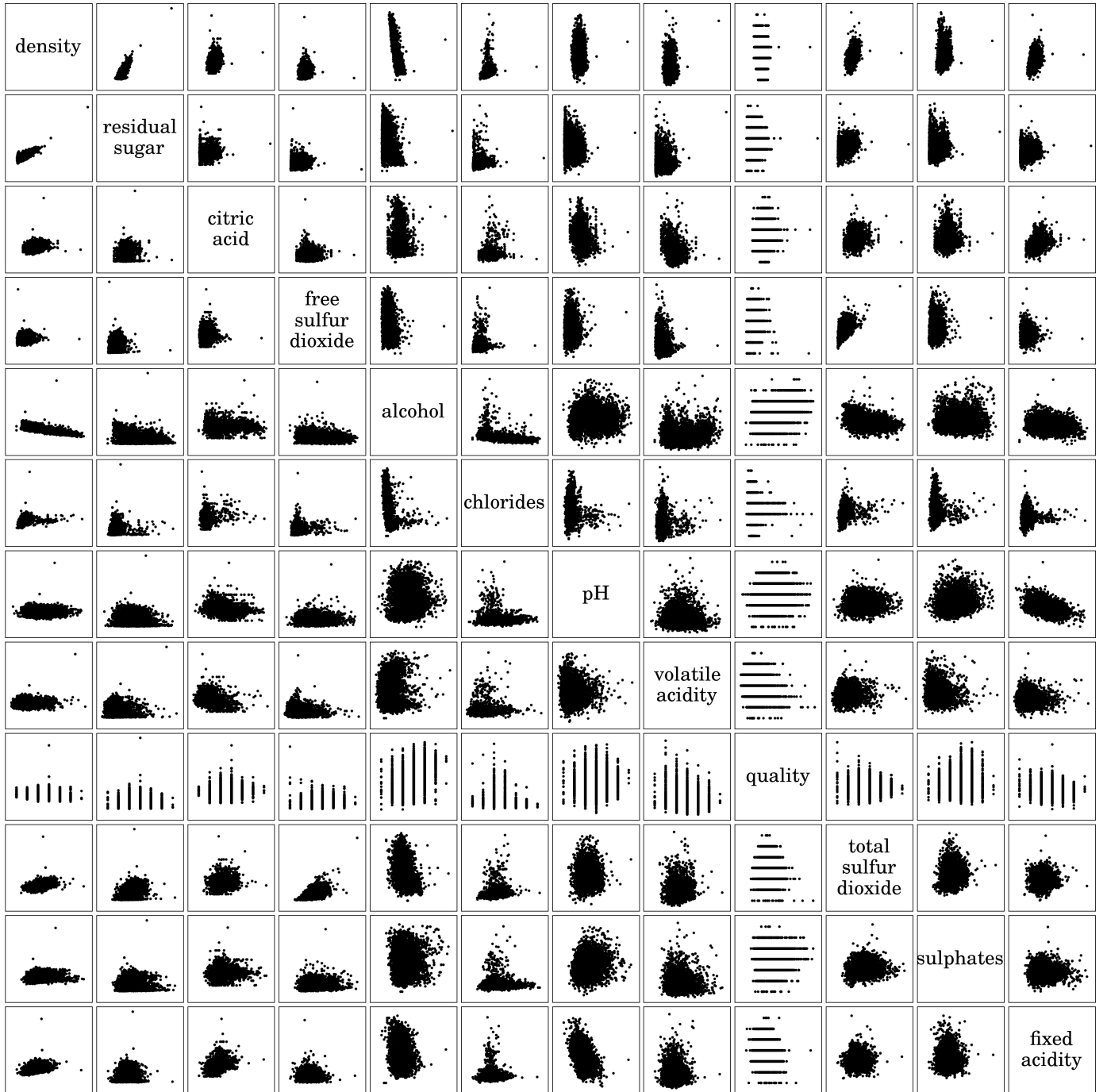


Figure 37: Scatter matrix of the whole feature set

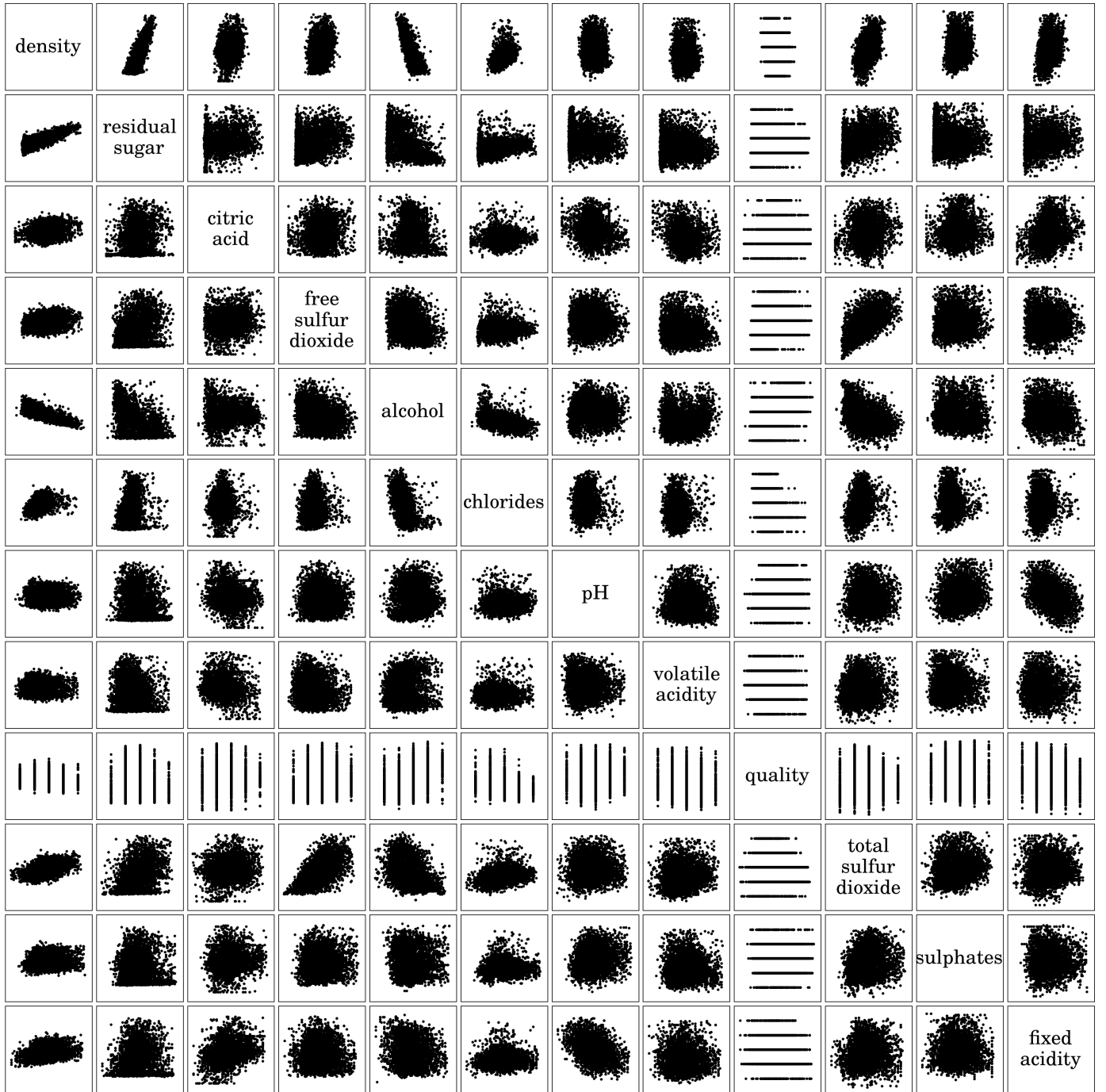


Figure 38: Scatter matrix of the whole feature set with outliers further than 3 standard deviations from the mean filtered

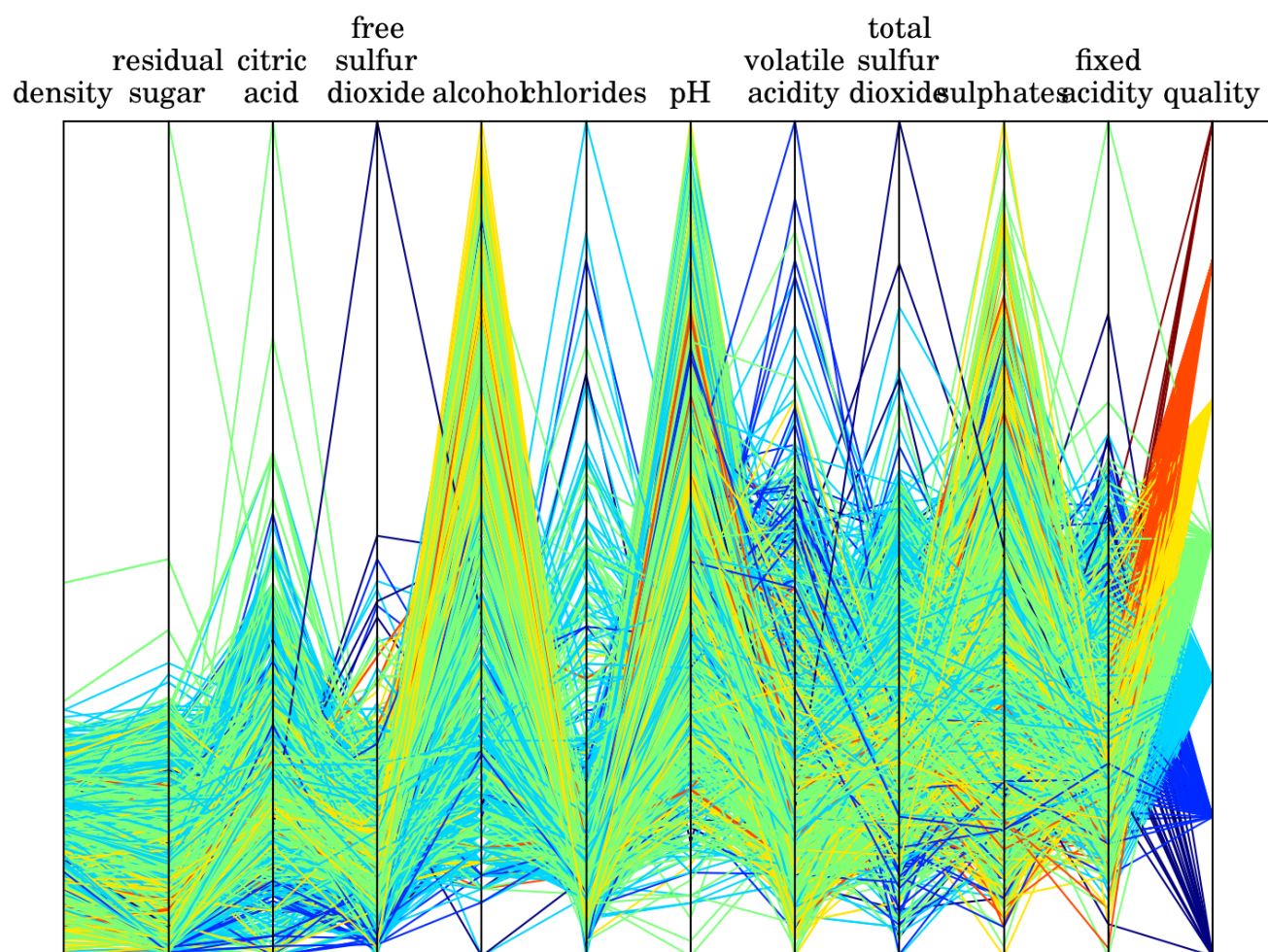


Figure 39: Parallel coordinates representation of the data set

### 0.2.1 Principal component analysis

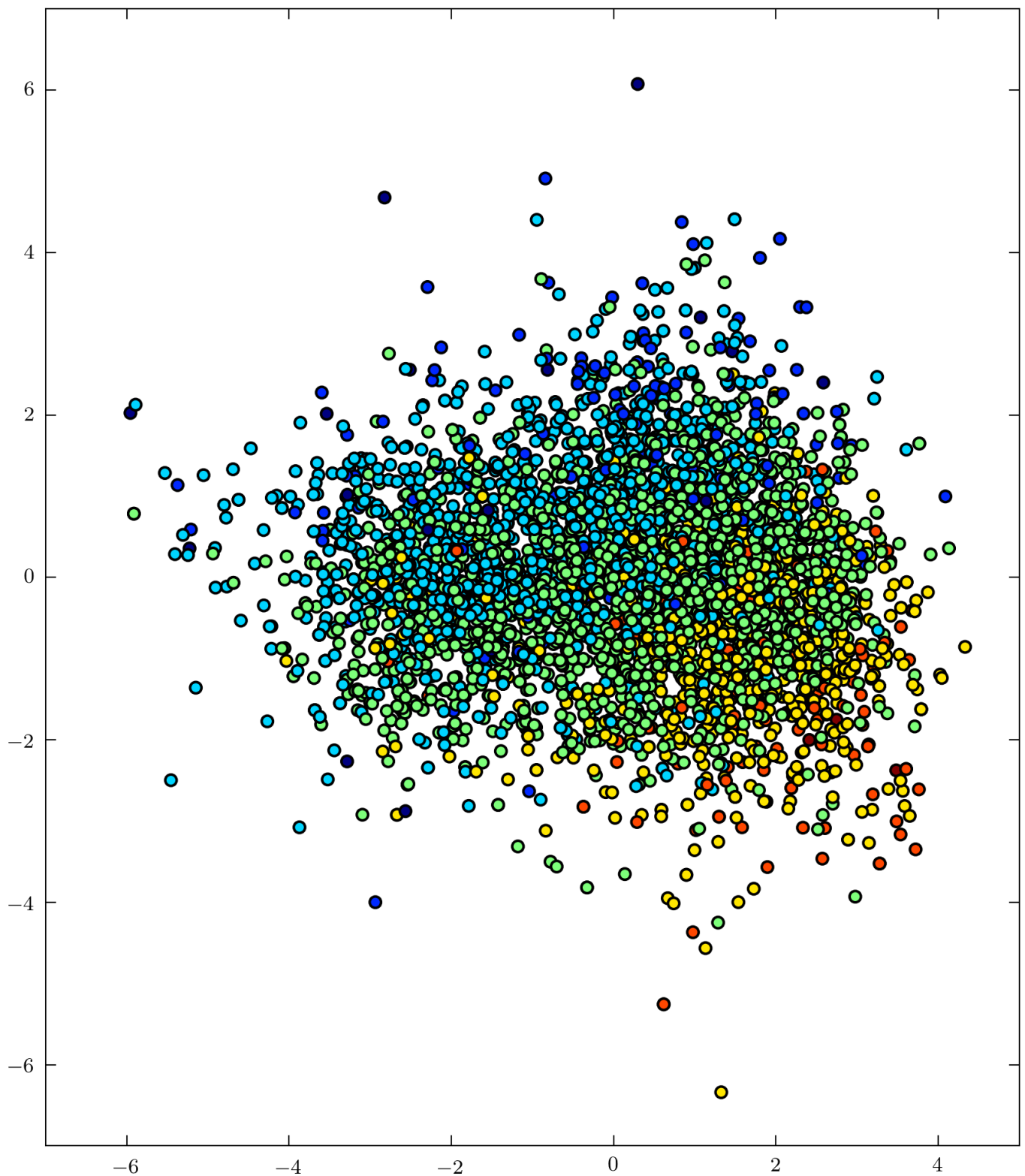


Figure 40: 2D projection of the data using PCA

|                        | PC1    | PC2    | PC3    | PC4    | PC5    | PC6    | PC7    | PC8    | PC9    | PC10   | PC11   | PC12   |
|------------------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| Proportion of variance | 0.2746 | 0.1317 | 0.1170 | 0.0923 | 0.0856 | 0.0746 | 0.0654 | 0.0581 | 0.0469 | 0.0293 | 0.0226 | 0.0017 |
| Cumulative variance    | 0.2746 | 0.4063 | 0.5234 | 0.6157 | 0.7013 | 0.7760 | 0.8414 | 0.8995 | 0.9464 | 0.9757 | 0.9983 | 1.0000 |



## 0.3 Correlation coefficients using different functions

### 0.3.1 Correlation coefficients using Pearson's correlation coefficient

|                      | residual<br>sugar | fixed<br>acidity | density        | volatile<br>acidity | total<br>sulfur<br>dioxide | alcohol        | quality       | sulphates     | free<br>sulfur<br>dioxide | chlorides     | citric<br>acid | pH            |
|----------------------|-------------------|------------------|----------------|---------------------|----------------------------|----------------|---------------|---------------|---------------------------|---------------|----------------|---------------|
| residual sugar       | <b>1.0000</b>     | 0.0890           | <b>0.8390</b>  | 0.0643              | 0.4014                     | -0.4506        | -0.0976       | -0.0267       | 0.2991                    | 0.0887        | 0.0942         | -0.1941       |
| fixed acidity        | 0.0890            | <b>1.0000</b>    | 0.2653         | -0.0227             | 0.0911                     | -0.1209        | -0.1137       | -0.0171       | -0.0494                   | 0.0231        | 0.2892         | -0.4259       |
| density              | <b>0.8390</b>     | 0.2653           | <b>1.0000</b>  | 0.0271              | <b>0.5299</b>              | <b>-0.7801</b> | -0.3071       | 0.0745        | 0.2942                    | 0.2572        | 0.1495         | -0.0936       |
| volatile acidity     | 0.0643            | -0.0227          | 0.0271         | <b>1.0000</b>       | 0.0893                     | 0.0677         | -0.1947       | -0.0357       | -0.0970                   | 0.0705        | -0.1495        | -0.0319       |
| total sulfur dioxide | 0.4014            | 0.0911           | <b>0.5299</b>  | 0.0893              | <b>1.0000</b>              | -0.4489        | -0.1747       | 0.1346        | <b>0.6155</b>             | 0.1989        | 0.1211         | 0.0023        |
| alcohol              | -0.4506           | -0.1209          | <b>-0.7801</b> | 0.0677              | -0.4489                    | <b>1.0000</b>  | 0.4356        | -0.0174       | -0.2501                   | -0.3602       | -0.0757        | 0.1214        |
| quality              | -0.0976           | -0.1137          | -0.3071        | -0.1947             | -0.1747                    | 0.4356         | <b>1.0000</b> | 0.0537        | 0.0082                    | -0.2099       | -0.0092        | 0.0994        |
| sulphates            | -0.0267           | -0.0171          | 0.0745         | -0.0357             | 0.1346                     | -0.0174        | 0.0537        | <b>1.0000</b> | 0.0592                    | 0.0168        | 0.0623         | 0.1560        |
| free sulfur dioxide  | 0.2991            | -0.0494          | 0.2942         | -0.0970             | <b>0.6155</b>              | -0.2501        | 0.0082        | 0.0592        | <b>1.0000</b>             | 0.1014        | 0.0941         | -0.0006       |
| chlorides            | 0.0887            | 0.0231           | 0.2572         | 0.0705              | 0.1989                     | -0.3602        | -0.2099       | 0.0168        | 0.1014                    | <b>1.0000</b> | 0.1144         | -0.0904       |
| citric acid          | 0.0942            | 0.2892           | 0.1495         | -0.1495             | 0.1211                     | -0.0757        | -0.0092       | 0.0623        | 0.0941                    | 0.1144        | <b>1.0000</b>  | -0.1637       |
| pH                   | -0.1941           | -0.4259          | -0.0936        | -0.0319             | 0.0023                     | 0.1214         | 0.0994        | 0.1560        | -0.0006                   | -0.0904       | -0.1637        | <b>1.0000</b> |

### 0.3.2 Correlation coefficients using Spearman's rho

|                      | residual<br>sugar | fixed<br>acidity | density        | volatile<br>acidity | total<br>sulfur<br>dioxide | alcohol        | quality       | sulphates     | free<br>sulfur<br>dioxide | chlorides      | citric<br>acid | pH            |
|----------------------|-------------------|------------------|----------------|---------------------|----------------------------|----------------|---------------|---------------|---------------------------|----------------|----------------|---------------|
| residual sugar       | <b>1.0000</b>     | 0.1067           | <b>0.7804</b>  | 0.1086              | 0.4313                     | -0.4453        | -0.0821       | -0.0038       | 0.3461                    | 0.2278         | 0.0246         | -0.1800       |
| fixed acidity        | 0.1067            | <b>1.0000</b>    | 0.2700         | -0.0429             | 0.1126                     | -0.1068        | -0.0845       | -0.0132       | -0.0245                   | 0.0947         | 0.2979         | -0.4183       |
| density              | <b>0.7804</b>     | 0.2700           | <b>1.0000</b>  | 0.0101              | <b>0.5638</b>              | <b>-0.8219</b> | -0.3484       | 0.0951        | 0.3278                    | <b>0.5083</b>  | 0.0914         | -0.1101       |
| volatile acidity     | 0.1086            | -0.0429          | 0.0101         | <b>1.0000</b>       | 0.1176                     | 0.0340         | -0.1966       | -0.0169       | -0.0812                   | -0.0049        | -0.1504        | -0.0452       |
| total sulfur dioxide | 0.4313            | 0.1126           | <b>0.5638</b>  | 0.1176              | <b>1.0000</b>              | -0.4766        | -0.1967       | 0.1578        | <b>0.6186</b>             | 0.3752         | 0.0932         | -0.0118       |
| alcohol              | -0.4453           | -0.1068          | <b>-0.8219</b> | 0.0340              | -0.4766                    | <b>1.0000</b>  | 0.4404        | -0.0449       | -0.2726                   | <b>-0.5708</b> | -0.0292        | 0.1489        |
| quality              | -0.0821           | -0.0845          | -0.3484        | -0.1966             | -0.1967                    | 0.4404         | <b>1.0000</b> | 0.0333        | 0.0237                    | -0.3145        | 0.0183         | 0.1094        |
| sulphates            | -0.0038           | -0.0132          | 0.0951         | -0.0169             | 0.1578                     | -0.0449        | 0.0333        | <b>1.0000</b> | 0.0523                    | 0.0939         | 0.0798         | 0.1402        |
| free sulfur dioxide  | 0.3461            | -0.0245          | 0.3278         | -0.0812             | <b>0.6186</b>              | -0.2726        | 0.0237        | 0.0523        | <b>1.0000</b>             | 0.1670         | 0.0883         | -0.0063       |
| chlorides            | 0.2278            | 0.0947           | <b>0.5083</b>  | -0.0049             | 0.3752                     | <b>-0.5708</b> | -0.3145       | 0.0939        | 0.1670                    | <b>1.0000</b>  | 0.0327         | -0.0540       |
| citric acid          | 0.0246            | 0.2979           | 0.0914         | -0.1504             | 0.0932                     | -0.0292        | 0.0183        | 0.0798        | 0.0883                    | 0.0327         | <b>1.0000</b>  | -0.1462       |
| pH                   | -0.1800           | -0.4183          | -0.1101        | -0.0452             | -0.0118                    | 0.1489         | 0.1094        | 0.1402        | -0.0063                   | -0.0540        | -0.1462        | <b>1.0000</b> |

### 0.3.3 Correlation coefficients using Kendall's tau

|                      | residual<br>sugar | fixed<br>acidity | density        | volatile<br>acidity | total<br>sulfur<br>dioxide | alcohol        | quality       | sulphates     | free<br>sulfur<br>dioxide | chlorides     | citric<br>acid | pH            |
|----------------------|-------------------|------------------|----------------|---------------------|----------------------------|----------------|---------------|---------------|---------------------------|---------------|----------------|---------------|
| residual sugar       | <b>1.0000</b>     | 0.0749           | <b>0.5890</b>  | 0.0728              | 0.2933                     | -0.3056        | -0.0631       | -0.0025       | 0.2367                    | 0.1553        | 0.0153         | -0.1256       |
| fixed acidity        | 0.0749            | <b>1.0000</b>    | 0.1855         | -0.0296             | 0.0773                     | -0.0732        | -0.0655       | -0.0087       | -0.0169                   | 0.0654        | 0.2086         | -0.2948       |
| density              | <b>0.5890</b>     | 0.1855           | <b>1.0000</b>  | 0.0066              | 0.3884                     | <b>-0.6351</b> | -0.2666       | 0.0642        | 0.2173                    | 0.3491        | 0.0615         | -0.0756       |
| volatile acidity     | 0.0728            | -0.0296          | 0.0066         | <b>1.0000</b>       | 0.0813                     | 0.0235         | -0.1548       | -0.0116       | -0.0548                   | -0.0035       | -0.1040        | -0.0304       |
| total sulfur dioxide | 0.2933            | 0.0773           | 0.3884         | 0.0813              | <b>1.0000</b>              | -0.3258        | -0.1512       | 0.1087        | 0.4447                    | 0.2571        | 0.0622         | -0.0084       |
| alcohol              | -0.3056           | -0.0732          | <b>-0.6351</b> | 0.0235              | -0.3258                    | <b>1.0000</b>  | 0.3467        | -0.0264       | -0.1825                   | -0.4040       | -0.0200        | 0.1026        |
| quality              | -0.0631           | -0.0655          | -0.2666        | -0.1548             | -0.1512                    | 0.3467         | <b>1.0000</b> | 0.0264        | 0.0172                    | -0.2449       | 0.0146         | 0.0844        |
| sulphates            | -0.0025           | -0.0087          | 0.0642         | -0.0116             | 0.1087                     | -0.0264        | 0.0264        | <b>1.0000</b> | 0.0356                    | 0.0626        | 0.0545         | 0.0958        |
| free sulfur dioxide  | 0.2367            | -0.0169          | 0.2173         | -0.0548             | 0.4447                     | -0.1825        | 0.0172        | 0.0356        | <b>1.0000</b>             | 0.1139        | 0.0608         | -0.0052       |
| chlorides            | 0.1553            | 0.0654           | 0.3491         | -0.0035             | 0.2571                     | -0.4040        | -0.2449       | 0.0626        | 0.1139                    | <b>1.0000</b> | 0.0223         | -0.0379       |
| citric acid          | 0.0153            | 0.2086           | 0.0615         | -0.1040             | 0.0622                     | -0.0200        | 0.0146        | 0.0545        | 0.0608                    | 0.0223        | <b>1.0000</b>  | -0.1013       |
| pH                   | -0.1256           | -0.2948          | -0.0756        | -0.0304             | -0.0084                    | 0.1026         | 0.0844        | 0.0958        | -0.0052                   | -0.0379       | -0.1013        | <b>1.0000</b> |