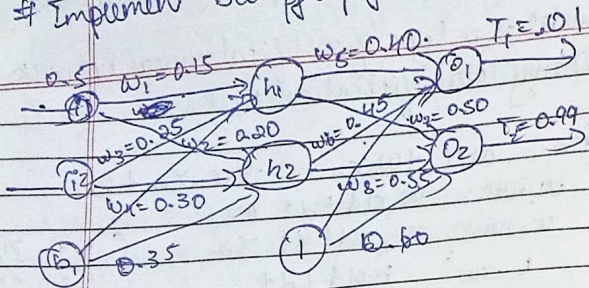


Implement backpropagation model algorithm.



$$S(x) = 1 / (1 + e^{-x})$$

$$h_{in} = S(w_1 x_1 + w_2 x_2 + w_3 x_3 + b_1)$$

$$= S(0.15 \times 0.5 + 0.25 \times 0.1 + 0.35 \times 0.1 + 0.35)$$

$$= S(0.3775) = 0.59327$$

$$h_{in} = 1 / (1 + e^{-(0.3775)}) = 0.59327$$

$$h_{2in} = (0.3 \times 0.1) + (0.25 \times 0.05) + 0.35$$

$$= 0.3925$$

$$h_{2in} = 1 / (1 + e^{-(0.3925)}) = 0.59689$$

$$O_{1in} = (w_5 \times h_{1in} + w_6 \times h_{2in} + b_2)$$

$$O_{2in} = (w_7 \times h_{1in} + w_8 \times h_{2in} + b_3)$$

$$O_{1in} = (0.40 \times 0.59327 + 0.45 \times 0.59689 + 0.60)$$

$$= 1.10591$$

$$E(1.10591) = 1 / (1 + e^{-(1.10591)}) = 0.75137$$

$$O_{2in} = (0.5 \times 0.59327 + 0.55 \times 0.59689 + 0.6)$$

$$= 1.22493$$

$$E(1.22493) = 1 / (1 + e^{-1.22493}) = 0.77293$$

$$Error = \frac{1}{2} (target - output)^2$$

$$E = \frac{1}{2} (T_1 - out_1)^2 + \frac{1}{2} (T_2 - out_2)^2$$

$$= \frac{1}{2} (0.01 - 0.75137)^2 + \frac{1}{2} (0.99 - 0.77293)^2$$

$$= 0.292371$$

$$\delta O_1 = (T_1 - out_1) \times O_{1in} \times (1 - O_{1in})$$

$$= (0.01 - 0.75137) \times 0.75137 \times (1 - 0.75137)$$

$$= -0.13850$$

$$w_5^{new} = w_5^{old} + \alpha \times \delta O_1 \times h_{1in}$$

$$= 0.4 + 0.5 \times (-0.13850) \times 0.59327$$

$$= 0.35892$$

$$w_6^{new} = w_6^{old} + \alpha \times \delta O_1 \times h_{2in}$$

$$= 0.45 + 0.5 \times (-0.13850) \times 0.59689$$

$$= 0.40867$$

$$b_3^{+} = b_3 + \alpha \times \delta O_2 \times 1$$

$$= 0.60 + 0.5 \times (-0.13850) \times 1 = 0.53075$$

$$\begin{aligned} \delta_{02} &= (T_2 - 0.77293) \times 0.77293 \times (1 - 0.77293) \\ &= (0.99 - 0.77293) \times 0.77293 \times (1 - 0.77293) \\ &= 0.03810 \end{aligned}$$

$$\begin{aligned} w_{7new} &= w_7 + \alpha \times \delta_{02} \times i_{07} \\ &= 0.50 + 0.5 \times 0.03810 \times 0.59327 \\ &= 0.51130 \end{aligned}$$

$$\begin{aligned} w_{8new} &= w_8 + \alpha \times \delta_{02} \times i_{08} \\ &= 0.55 \times 0.5 \times 0.03810 \times 0.59689 \\ &= 0.56137 \end{aligned}$$

$$\begin{aligned} b_4 &= b_4 + \alpha \times \delta_{02} \times 1 \\ &= 0.60 + 0.5 \times 0.03810 \times 1 = 0.61905 \end{aligned}$$

$$\begin{aligned} \delta_{h1} &= (\delta_{01} + w_5 + \delta_{02} \times w_7) \times 0.1 \times (1 - 0.00877) \\ &= (-0.13850 \times 0.40 + 0.03810 \times 0.50) \times 0.59327 \\ &\quad (1 - 0.59327) \\ &= -0.00877. \end{aligned}$$

$$\begin{aligned} w_i^+ &= w_i + \alpha \times \delta_{h1} \times i_i \\ &= 0.15 + 0.5 \times (-0.00877) \times 0.05 \\ &= 0.14978 \end{aligned}$$

$$\begin{aligned} w_2 &= w_2 + \alpha \times \delta_{h1} \times i_2 \\ &= 0.20 + 0.5 \times (-0.00877) \times 0.10 \\ &= 0.19956. \end{aligned}$$

$$\begin{aligned} b_1 &= b_1 + \alpha \times \delta_{h1} \times 1 \\ &= 0.35 \times 0.5 \times (-0.00877) \end{aligned}$$

$$b_1 = 0.34562.$$

$$\begin{aligned} \delta_{h2} &= (\delta_{01} \times w_6 + \delta_{02} \times w_8) \times 0.2 \times (1 - 0.00995) \\ &= (-0.13850) \times 0.45 + 0.03810 \times 0.55 \times 0.59689 \\ &\quad (1 - 0.59689) \\ &= -0.00995. \end{aligned}$$

$$\begin{aligned} w_3 &= w_3 + \alpha \times \delta_{h2} \times i_3 \\ &= 0.25 + 0.5 \times (-0.00995) \times 0.05 \\ &= 0.24975 \end{aligned}$$

$$\begin{aligned} w_4 &= w_4 + \alpha \times \delta_{h2} \times i_4 \\ &= 0.30 + 0.5 \times (-0.00995) \times 0.10 \\ w_4 &= 0.29950 \end{aligned}$$

$$\begin{aligned} w_5^+ &= b_2 + \alpha \times \delta_{h2} \times 1 \\ &= 0.35 \times 0.5 \times (-0.00995) \times 1 \\ &= 0.34503. \end{aligned}$$

$$\begin{aligned} w_1 &= 0.14978 \quad w_2 = 0.19956 \quad w_3 = 0.24975 \\ w_4 &= 0.29950 \quad w_5 = 0.35842 \quad w_6 = 0.53075 \\ w_7 &= 0.51130 \quad w_8 = 0.56137 \\ b_1 &= 0.34562 \quad b_2 = 0.3450 \quad b_3 = 0.53075 \\ b_4 &= 0.61905 \end{aligned}$$