

Title: Implementation of PCA with ANN algorithm for Face recognition

design a face recognition system using Python.

Use of following libraries are allowed:

- Numpy, Scipy for matrix multiplication, finding SVD or Eigen vector etc.
- Open CV- Python library for inputting/reading images etc.

For step-by-step directions you may use the following link.

Steps involved in training: 1.

Generate the face database:

Each face image is represented in the form a matrix having m rows and n columns, where each pixel (x,y) such that $x \leq m$, and $y \leq n$ shows pixel location of the image as well as the direction.

For the simplicity we are assuming each face image as a column vector, if we have p images then the size of the face database will be $mn \times p$. Let's say face database is denoted as $(Face_Db)_{mn \times p}$

2. Mean Calculation:

Calculate the mean of each observation

$$M_i = \sum_{j=1}^p \sum_{i=1}^{mn} Face_Db(i, j)$$

here mean vector will have the dimension $(M)_{mn \times 1}$

3. Do mean Zero

Subtract mean face from each face image, let's say this mean zero face data as Φ , and calculated as

$$(\Phi(i))_{mn \times p} = (Face_Db(i))_{mn \times p} - (M)_{mn \times 1} \quad \text{Where } i=1,2,3, \dots, p.$$

4. Calculate Co-Variance of the Mean aligned faces (Φ)

Here there is a slightly variation in calculation of covariance, generally we prefer to calculate the covariance of data by:

$$C = \sum_{i=1}^n (X_i - \bar{X}) ((Y_i - \bar{Y}))^t$$

Where \bar{X}, \bar{Y} are the mean of X_i and Y_i , and C is the covariance matrix. If we will follow the same convention on face data we will get.

$$C(mn, mn) = \sum_{z=1}^{mn} \sum_{y=1}^{mn} \sum_{i=1}^p (\Delta(z, i) - M_{z,i}) * (\Delta(y, i) - M_{y,i})$$

Here we will get mn direction, which is very hard to compute, store and process. It also increases the program complexity, hence in 1991 Turk and Peterland [1] two researches suggested a new way to calculate the co-variance that is basically known as surrogate covariance, that is:

$$C(p, p) = \sum_{z=1}^p \sum_{y=1}^p \sum_{i=1}^{mn} (\Delta(z, i) - M_{z,i}) * (\Delta(y, i) - M_{y,i})$$

Hence here will get only p * p dimension, which is easy to compute and process, the idea behind computing the surrogate covariance suggested by Turk and Peterland that, these are only the valid direction where we will get maximum variances, and rest of the directions are insignificant to us. Means these are direction where we will get the eigenvalues and for rest we will get eigenvalues equal to zero.

5. Do eigenvalue and eigenvector decomposition:

Now we have covariance matrix $(C)_{p \times p}$, find out the eigenvectors and eigenvalues. Let we have eigenvector

$(V)_{p \times p}$ and eigenvalues $(\lambda)_{p \times p}$.

6. Find the best direction (Generation of feature vectors)

Now select the best direction from p directions, for this sort the eigenvalues in the descending order and decide a k value, which represents the number of selected eigenvectors to extract k direction from all p direction. On the basis of k value we can generate the Feature vector $(\Phi)_{p \times k}$.

7. Generating Eigenfaces:

For generating the eigenfaces (Φ) project the each mean aligned face to the generated feature vector.

$$(\Phi)_{k \times mn} = (\Phi)_{tk \times p} * (\Phi)_{tp \times mn}$$

8. Generate Signature of Each Face:

For generating signature of each face (Φ) , project each mean aligned face to the eigenfaces.

$$(\Phi)_{k \times i} = (\Phi)_{k \times mn} * (\Phi)_{mn \times i}$$

Where $i \in 1, 2, 3, \dots, p$. hence Φ will have the size $k * p$.

9. Apply ANN for training:

After getting the best eigen vector apply back propagation neural network as discussed in the video.

Steps involved in Testing:

1. For testing, let we have an image (I), make it as a column vector say $(I)^{1_{mn*1}}$ 2.

Do mean Zero, by subtracting mean face (M) to this test face, say it $(I)^2$.

$$(I)^{2_{mn*1}} = (I)^{1_{mn*1}} - (M)^{mn*1}$$

3. Project this mean aligned face $(I)^2$ to eigenfaces (\square), we will get the projected test face (\square).

$$(\square)^{k*1} = (\square)^{k*mn} * (I)^{2_{mn*1}}$$

4. Now we have projected test face \square and signature of each face \square , use the trained ANN model to predict the unknown face.

Take 60% data as training set and 40 % data as test set, evaluate your classifier on the following Factors:

- a) Change the value of k and then, see how it changes the classification accuracy. Plot a graph between accuracy and k value to show the comparative study.
- b) Add imposters (who do not belong to the training set) into the test set and then recognize it as the not enrolled person.