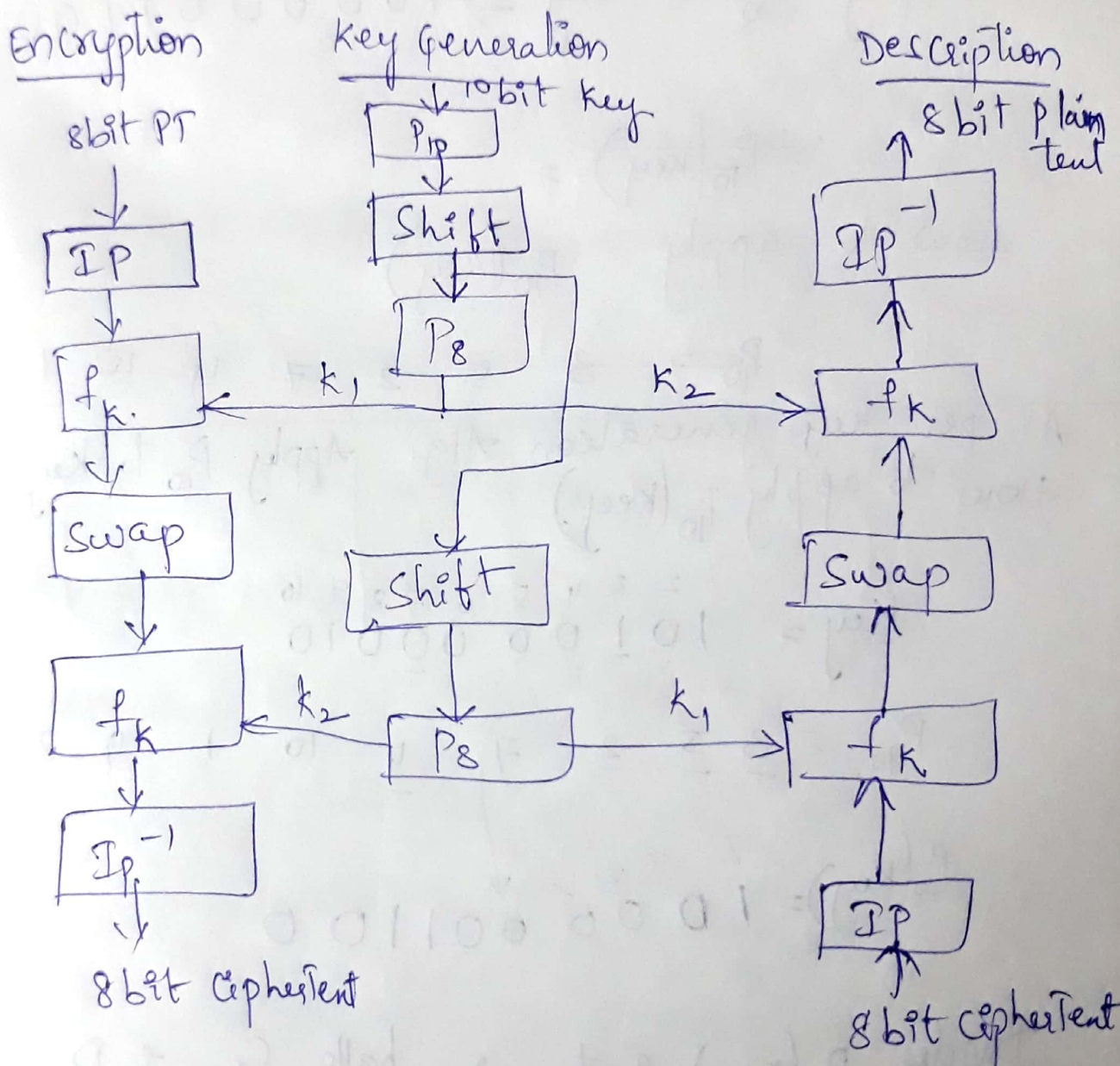


S-DES

S-DES Diagram.



Key generation Algorithm

key = $\begin{matrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \\ 10 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \end{matrix}$

$P_{10} = \begin{matrix} 3 & 5 & 2 & 7 & 4 & 10 & 1 & 9 & 8 & 6 \end{matrix}$
 $P_8 = \begin{matrix} 6 & 3 & 7 & 4 & 8 & 5 & 10 & 9 \end{matrix}$

As per key generation Alg. Apply P_{10} to key
 how to apply $P_{10}(\text{key})$

Key =

	1	2	3	4	5	6	7	8	9	10
	1	0	1	0	0	0	0	0	1	0

$P_{10} =$

3	5	2	7	4	10	1	9	8
---	---	---	---	---	----	---	---	---

$P_{10}(\text{key}) =$

1	0	0	0	0	0	1	1	0	0
---	---	---	---	---	---	---	---	---	---

Divide $P_{10}(\text{key})$ into 2 halves C_{i-1} & D_{i-1}

\Rightarrow

1	0	0	0	0	0	1	1	0	0
<u> </u>					<u> </u>				
C_{i-1}					D_{i-1}				

Left circular shift to C_{i-1} & D_{i-1}

$$LCS(C_{i-1}) = 00001 \quad LCS(D_{i-1}) = 11000$$

→ $LCS(C_{i-1})$ and $LCS(D_{i-1})$ ^{used} for next round
_{used}
 Apply P_8 to generate this round key.

$$\therefore LCS(C_{i-1}) + LCS(D_{i-1}) = 00001 \ 11000$$

Apply P_8 to above

$$P_8 = 6 \ 3 \ 7 \ 4 \ 8 \ 5 \ 10 \ 9$$

$$\therefore K_1 = P_8(LCS(C_{i-1}, D_{i-1})) = 10100100$$

To generate K_2

Take $LCS(C_{i-1}) + LCS(D_{i-1})$ as i/p.

$$C = LCS(C_{i-1}) \quad D_i = \{LCS(D_{i-1})\}$$

$$\therefore C = 00001 \quad D_i = 11000$$

Apply $LCS_2(C + D_i)$

$$\Rightarrow \begin{matrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \\ 00 & 100 & 000 & 11 \end{matrix}$$

Apply P_8 to above

$$K_2 = P_8(LCS_2(C, D_i)) = 010000011$$

Encryption

Plaintext (PT) = 11110011

$I_p = 2 \ 6 \ 3 \ 1 \ 4 \ 8 \ 5 \ 7$

$E/p = 4 \ 1 \ 2 \ 3 \ 2 \ 3 \ 4 \ 1$

(To convert 4 bits to 8 bits)

$P_4 = 2 \ 4 \ 3 \ 1$

$$S_0 = \begin{bmatrix} 1 & 0 & 3 & 2 \\ 3 & 2 & 1 & 0 \\ 0 & 2 & 1 & 3 \\ 3 & 1 & 3 & 2 \end{bmatrix} \quad S_1 = \begin{bmatrix} 0 & 1 & 2 & 3 \\ 2 & 0 & 1 & 3 \\ 3 & 0 & 1 & 2 \\ 2 & 1 & 0 & 3 \end{bmatrix}$$

S_0 & S_1 are S-boxes - used to convert 8 bits to 4 bits

Apply I_p to plaintext

$I_p = 2 \ 6 \ 3 \ 1 \ 4 \ 8 \ 5 \ 7$

PT = $\begin{matrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\ 1 & 1 & 1 & 1 & 0 & 0 & 1 & 1 \end{matrix}$

$IP(PT) \Rightarrow 10111101$

divide above into 2 halves.

$L_{-1} = 1011$

$R_{-1} = 1101$

Round, starts.

Round 1

Apply Ep on $R_{i-1} = 1101$

Ep = 41 2 3 2 3 41

$\therefore E/P(R_{i-1}) = 11101011$

To do \oplus with key - K_1

We need E/P.

$R_{i-1} = 4 \text{ bits}$ $K_1 = 8 \text{ bits}$

To Do XOR both must have Equal no. of bits.

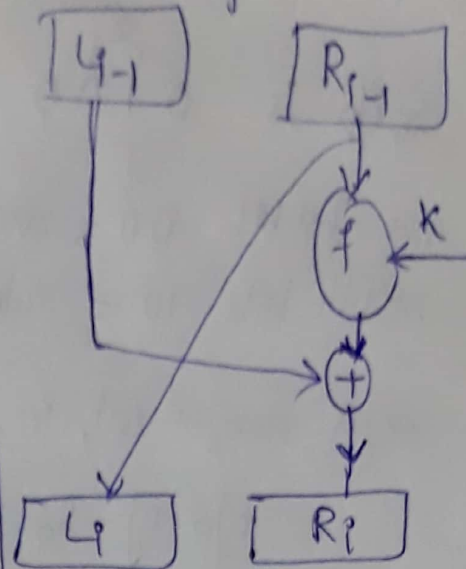
\therefore we expanded R_{i-1} using Expanded permutation (E/P).

$E/P(R_{i-1}) \oplus K_1$

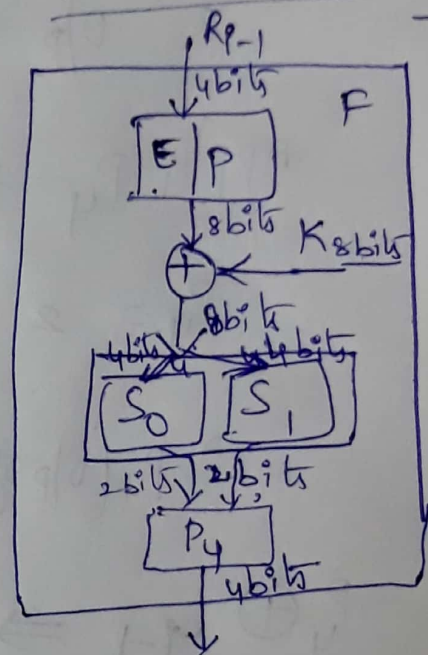
$$\begin{array}{r} \Rightarrow 11101011 \\ \oplus 10100100 \\ \hline 01001111 \text{ (8 bits)} \end{array}$$

- Divide above into 2 halves give first half (4 bits) to S_0 as i/p to get 2 bits as o/p and second half (4 bits) to S_1 as i/p to S_1 to get 2 bits as o/p.

Single Round



In Each Round function



S_0 i/p is $\begin{array}{c} \text{column} \\ \uparrow \\ 0 \ 1 \ 0 \ 0 \\ \downarrow \end{array}$

first & last bit $00 = \text{row}_0$

Middle bits $10 = \text{column}_2$

refer $\text{row}_0 \leftarrow \text{col}$, in $S_0 = 03$

\therefore o/p of $S_0 = 11$

S_1 i/p is $\begin{array}{c} \text{col} \\ \uparrow \\ 1 \ 1 \\ \downarrow \\ \text{row} \end{array}$

$11 = \text{row}_3$

$11 = \text{column}_3$

In S_1 , $3^{\text{rd}} \text{ row} + \text{col} = 3$

\therefore o/p of $S_1 = 11$

\therefore o/p of $S_0 + S_1 = \overset{1}{1} \overset{2}{1} \overset{3}{1} \overset{4}{1}$

Apply P_4 to o/p of $S_0 + S_1$

$P_4 = 2 \ 4 \ 3 \ 1$

$\Rightarrow P_4(\text{o/p of } S_0 + S_1) = 1 \ 1 \ 1 \ 1$

$$\begin{array}{rcl} P_4 \oplus L_{i-1} & \Rightarrow & \begin{array}{cccc} 1 & 1 & 1 & 1 \\ 1 & 0 & 1 & 1 \\ \hline 0 & 1 & 0 & 0 \end{array} \end{array}$$

$P_4(\text{o/p of } S_0 + S_1)$
 L_{i-1}

$$L_i = R_{i-1} \quad R_i = (L_{i-1} \oplus f(R_{i-1}, K_i))$$

$$\therefore L_i = 1101 \quad R_i = 0100$$

Round 2

$$R_i = \begin{matrix} 1 & 2 & 3 & 4 \\ 0 & 1 & 0 & 0 \end{matrix}$$

$$E/P = \begin{matrix} 4 & 1 & 2 & 3 & 2 & 3 & 4 & 1 \end{matrix}$$

$$E/P(R_i) = 00101000$$

$$E/P(R_i) \oplus k_2 \Rightarrow 00101000$$

$$\begin{array}{r} \oplus \quad 01000011 \\ \hline 01101011 \\ \hline \end{array}$$

$\underbrace{\quad\quad\quad}_{S_0} \quad \underbrace{\quad\quad\quad}_{S_1}$

$$S_0 = \begin{matrix} 3 \text{ col} \\ 0110 \\ \hline 0 \text{ row} \end{matrix}$$

$$S_0 - 0 \text{ row} = 2$$

$$S_0 = 10$$

$$S_1 = 1011$$

$$\begin{matrix} 11 - 3 \text{ row} \\ 01 - 1 \text{ col} \end{matrix} = 1$$

$$S_1 = 01$$

$$\therefore \text{op of } S_0 S_1 = 1001$$

$$P_4(\text{op of } S_0 S_1) = 0101$$

$$\begin{array}{r} P_4(\text{op of } S_0 S_1) \oplus L_i \Rightarrow \begin{matrix} 0101 \\ \oplus 1101 \\ \hline 1000 \end{matrix} \end{array}$$

$$\therefore L_{i+1} = R_i \quad R_{i+1} = (L_i \oplus f(R_i, k_2))$$

$$\therefore R_{i+1} = \begin{matrix} 1 & 2 & 3 & 4 \\ 0 & 1 & 0 & 0 \end{matrix} \quad R_{i+1} = \begin{matrix} 5 & 6 & 7 & 8 \\ 1 & 0 & 0 & 0 \end{matrix}$$

Apply I_P^{-1} to $L_{i+1} \oplus R_{i+1}$

$$I_P = \begin{matrix} 1 & 2 & 3 & 4 \\ 2 & 6 & 3 & 1 \\ \hline 4 & 1 & 3 & 5 \end{matrix} \quad \begin{matrix} 5 & 6 & 7 & 8 \\ 4 & 8 & 5 & 7 \end{matrix}$$

$$I_P^{-1} = \begin{matrix} 4 & 1 & 3 & 5 & 7 & 2 & 8 & 6 \end{matrix}$$

$$\Rightarrow I_P^{-1}(L_{i+1}, R_{i+1}) = \text{Cipher Text}$$

$$\boxed{\begin{matrix} 00010100 \\ \downarrow \\ \text{Cipher Text} \end{matrix}}$$