

## Portfolio Performance Measures

### Given Data:

- Risk-free rate ( $r_f$ ): 4%
- Market's average return ( $r_m$ ): 12%
- Excess return regression results for Stocks A and B:
  - Stock A:  $\alpha_A = 1\%$ ,  $\beta_A = 1.2$
  - Stock B:  $\alpha_B = 2\%$ ,  $\beta_B = 0.8$
- R-squared and standard deviations:
  - Stock A:  $R^2 = 0.689$ ,  $\sigma(e_A) = 12.2\%$ ,  $\sigma(A) = 23.5\%$
  - Stock B:  $R^2 = 0.493$ ,  $\sigma(e_B) = 21\%$ ,  $\sigma(B) = 28.7\%$

### Calculations:

#### i. Alpha:

Given  $\alpha$  values:

- Stock A:  $\alpha_A = 1\%$
- Stock B:  $\alpha_B = 2\%$

*Supporting Statement and Explanation:*

Alpha is given directly for each stock.

#### ii. Information Ratio:

Information Ratio =  $\alpha / \sigma(e)$

For Stock A:

Information Ratio\_A =  $1\% / 12.2\% = 0.0819672 \approx 0.0820$

For Stock B:

Information Ratio\_B =  $2\% / 21\% = 0.0952381 \approx 0.0952$

*Supporting Statement and Explanation:*

The Information Ratio measures the risk-adjusted return of the portfolio by dividing alpha by the residual standard deviation.

#### iii. Sharpe Ratio:

Sharpe Ratio =  $(r_i - r_f) / \sigma_i$

For Stock A:

Sharpe Ratio\_A =  $(12\% - 4\%) / 23.5\% = 0.3404255 \approx 0.3404$

For Stock B:

Sharpe Ratio\_B =  $(12\% - 4\%) / 28.7\% = 0.278042 \approx 0.2780$

*Supporting Statement and Explanation:*

The Sharpe Ratio provides a measure of risk-adjusted return, comparing the return in excess of the risk-free rate to the standard deviation of the portfolio returns.

#### iv. Treynor Measure:

Treynor Measure =  $(r_i - r_f) / \beta_i$

For Stock A:

Treynor Measure\_A =  $(12\% - 4\%) / 1.2 = 6.6666667 \approx 6.6667$

For Stock B:

Treynor Measure\_B =  $(12\% - 4\%) / 0.8 = 10$

*Supporting Statement and Explanation:*

The Treynor Measure evaluates how much excess return is generated per unit of market risk, with market risk measured by beta.

**Summary Table:**

|                       | Stock A | Stock B |
|-----------------------|---------|---------|
| i. Alpha              | 1.0000  | 2.0000  |
| ii. Information Ratio | 0.0820  | 0.0952  |
| iii. Sharpe Ratio     | 0.3404  | 0.2780  |
| iv. Treynor Measure   | 6.6667  | 10.0000 |

**Best Choice Under Circumstances:**

**I. This is the only risky asset to be held by the investor:**

Use Sharpe Ratio since the Total Risk matters.  
Stock A has a higher Sharpe Ratio (0.3404).

**II. This stock will be mixed with the rest of the investor's portfolio, currently composed solely of holdings in the market-index fund:**

Use Treynor Measure since Market Risk matters.  
Stock B has a higher Treynor Measure (10.0000).

**III. This is one of many stocks that the investor is analyzing to form an actively managed stock portfolio:**

Use Information Ratio since Specific Risk is analyzed.  
Stock B has a higher Information Ratio (0.0952).

*Supporting Statement and Explanation:*

Different scenarios require different performance measures to find the optimal choice considering the risk and return tradeoff.