

Electrical Engineering: Transformer and Generator Specifications

Part (a): Transformer Calculations

Given:

Primary Voltage (V_1) = 11000V

Secondary Voltage (V_2) = 400V

Transformer Rating (S) = 100 kVA

Secondary Turns (N_2) = 160 turns

Reactance (X) = 0.1 pu

Step 1: Calculate the primary and secondary currents you would expect to measure on full load (i)

Transformer rating formula:

$$S = V_1 \cdot I_1 = V_2 \cdot I_2$$

- For primary current (I_1):
- $I_1 = S / V_1 = 100000 / 11000 \sim 9.09$ Amps
- For secondary current (I_2):
- $I_2 = S / V_2 = 100000 / 400 = 250$ Amps

Step 2: Calculate the number of primary turns (ii)

Transformer turns ratio formula:

$$N_1 / N_2 = V_1 / V_2$$

$$N_1 = N_2 \cdot (V_1 / V_2) = 160 \cdot (11000 / 400) = 4400 \text{ turns}$$

Step 3: Calculate the reactance in Ohms, referred to the secondary (iii)

Per Unit System:

$$X_{\text{pu}} = 0.1$$

Calculating base impedance (Z_{base}):

$$Z_{\text{base,secondary}} = V_2^2 / S = 400^2 / 100000 = 1.6 \text{ Ohms}$$

Actual reactance on secondary ($X_{\text{secondary}}$):

$$X_{\text{secondary}} = X_{\text{pu}} \cdot Z_{\text{base}} = 0.1 \cdot 1.6 = 0.16 \text{ Ohms}$$

Part (b): Generator Characteristics for an Isolated Power System

Given:

Load = 330 kVA

Load Voltage (V_{load}) = 33 kV

Power Factor (pf) = 0.9 (lagging)

Transmission Line Impedance (z) = 0.4 + j0.6 Ω /km

Line Length = 20 km

Step 1: Calculate the generator current requirement, including the angle (i)

Complex Power (S) = Apparent Power:

$$S = 330 \text{ kVA} = 330 \times 10^3$$

Power Factor (pf) = 0.9 (lagging):

Real Power (P):

$$P = S \cdot \text{pf} = 330000 \cdot 0.9 = 297 \text{ kW}$$

Reactive Power (Q):

$$Q = S \cdot \sin(\cos^{-1}(0.9))$$

$$Q = 330000 \cdot \sin(\cos^{-1}(0.9)) \approx 330000 \cdot 0.4359 = 143847 \text{ VAR}$$

Current (I):

$$I = S / \sqrt{3} \cdot V_{\text{load}}$$

$$I = 330000 / \sqrt{3} \cdot 33000 \approx 5.774 \text{ Amps}$$

Power Angle (ϕ):

$$\cos \phi = 0.9$$

$$\phi = \cos^{-1}(0.9) \approx 25.84^\circ$$

Step 2: Calculate the generator voltage requirement, including the angle (ii)

Line Impedance (Z_{line}):

$$Z_{\text{line}} = Z_{\text{total}} = 20 \cdot (0.4 + j0.6) = 8 + j12 \text{ Ohms}$$

Voltage Drop (V_{drop}):

$$V_{\text{drop}} = I \cdot Z_{\text{line}}$$

$$V_{\text{drop}} = 5.774 \cdot (8 + j12) \approx (46.19 + j69.29) \text{ Volts}$$

$$V_{\text{drop}} = \sqrt{46.19^2 + 69.29^2} \approx 83.3 \text{ Volts}$$

Generator Voltage (V_g):

$$V_g = V_{\text{load}} + V_{\text{drop}} = 33 \text{ kV} + 83.3 \text{ V} = 33.0833 \text{ kV}$$

Final Solution:

(a)

- (i) The primary and secondary currents are approximately 9.09 Amps and 250 Amps, respectively.
- (ii) The number of primary turns is 4400 turns.
- (iii) The reactance referred to the secondary is 0.16 Ohms.

(b)

- (i) The generator current requirement is approximately 5.774 Amps with a power angle of 25.84 degrees.
- (ii) The generator voltage requirement is approximately 33.0833 kV.