

Subject: Physics | Topic: Electric Fields

Given:

Charge $(q_1) = +8.97 \mu\text{C} = +8.97 \times 10^{-6} \text{ C}$

Position of $(q_1) (x_1) = +3.18 \text{ cm} = +0.0318 \text{ m}$

Charge $(q_2) = -21.8 \mu\text{C} = -21.8 \times 10^{-6} \text{ C}$

Position of $(q_2) (x_2) = +8.64 \text{ cm} = +0.0864 \text{ m}$

Objective:

Calculate the x-component of the net electric field at:

1. $(x = 0) \text{ cm}$

2. $(x = 6) \text{ cm}$

Step 1: Calculate the x-component of the electric field at $(x = 0) \text{ cm}$

Formula:

$$E = \frac{k \cdot |q|}{r^2}$$

where,

(E) = Electric field,

(k) = Coulomb's constant = $(8.99 \times 10^9) \text{ N}\cdot\text{m}^2/\text{C}^2$,

(q) = magnitude of the charge,

(r) = distance between the charge and the point of interest.

Calculation of (E_1) from (q_1) at $(x=0)$:

$$(r_1) = x_1 - 0 = 0.0318 \text{ m}$$

$$(E_1) = \frac{8.99 \times 10^9 \times 8.97 \times 10^{-6}}{(0.0318)^2}$$

$$(E_1) = \frac{8.99 \times 10^9 \times 8.97 \times 10^{-6}}{0.00101124}$$

$$(E_1) \approx 7.968 \times 10^5 \text{ N/C}$$

Direction: The direction of (E_1) due to (q_1) (positive charge) at $(x = 0)$ is along the negative x-axis.

Calculation of (E_2) from (q_2) at $(x=0)$:

$$(r_2) = x_2 - 0 = 0.0864 \text{ m}$$

$$(E_2) = \frac{8.99 \times 10^9 \times 21.8 \times 10^{-6}}{(0.0864)^2}$$

$$(E_2) = \frac{8.99 \times 10^9 \times 21.8 \times 10^{-6}}{0.00746496}$$

$$(E_2) \approx 2.627 \times 10^6 \text{ N/C}$$

Direction: The direction of (E_2) due to (q_2) (negative charge) at $(x = 0)$ is along the positive x-axis.

Net Electric Field at $(x = 0) \text{ cm}$:

$$(E_{\text{net}}) = E_2 - E_1$$

$$(E_{\text{net}}) = 2.627 \times 10^6 - 7.968 \times 10^5$$

$$(E_{\text{net}}) = 1.83 \times 10^6 \text{ N/C}$$

Supporting Statement: The net electric field at a point is the vector sum of fields due to all charges. Here, (E_2) was greater and in the positive x-direction.

Step 2: Calculate the x-component of the electric field at x=6 cm

Position of the charges relative to x=6 cm:

$$r_{1,6} = |0.06 - 0.0318| = 0.0282 \text{ m from } q_1$$

$$r_{2,6} = |0.06 - 0.0864| = 0.0264 \text{ m from } q_2$$

Calculation of $E_{1,6}$ from q_1 at x=6 cm:

$$E_{1,6} = \frac{8.99 \times 10^9 \times 8.97 \times 10^{-6}}{0.0282^2}$$

$$E_{1,6} = \frac{8.99 \times 10^9 \times 8.97 \times 10^{-6}}{0.00079524}$$

$$E_{1,6} \approx 1.01 \times 10^6 \text{ N/C}$$

Direction: The field $E_{1,6}$ due to q_1 (positive charge) at x = 6 cm is along the positive x-axis.

Calculation of $E_{2,6}$ from q_2 at x=6 cm:

$$E_{2,6} = \frac{8.99 \times 10^9 \times 21.8 \times 10^{-6}}{0.0264^2}$$

$$E_{2,6} = \frac{8.99 \times 10^9 \times 21.8 \times 10^{-6}}{0.00069696}$$

$$E_{2,6} \approx 2.81 \times 10^6 \text{ N/C}$$

Direction: The field $E_{2,6}$ due to q_2 (negative charge) at x = 6 cm is along the positive x-axis.

Net Electric Field at x = 6 cm:

$$E_{\text{net},6} = E_{1,6} + E_{2,6}$$

$$E_{\text{net},6} = 1.01 \times 10^6 + 2.81 \times 10^6$$

$$E_{\text{net},6} = 3.82 \times 10^6 \text{ N/C}$$

Supporting Statement: Both electric fields $E_{1,6}$ and $E_{2,6}$ are in the same direction (positive x-axis), hence they add up.

Final Solution:

1. The x-component of the net electric field at x = 0 cm is $1.83 \times 10^6 \text{ N/C}$ (positive direction).
2. The x-component of the net electric field at x = 6 cm is $3.82 \times 10^6 \text{ N/C}$ (positive direction).