

Exchange Rate Arbitrage Analysis

Topic: Exchange Rate Conversion & Arbitrage Opportunities

Given data:

Bank A:

Bid: ¥100/\$

Ask: ¥120/\$

Bank B:

Bid: \$1.25/€

Ask: \$1.5/€

Bank C:

Bid: ¥200/€

Ask: ¥250/€

(a) Convert Bank A's Quote to American Terms

To convert the Bank A quote from Japanese Yen per Dollar (¥/\$) to U.S. Dollar per Yen (\$/¥), the reciprocal of the existing quotes must be taken.

Bid Price (Bank A):

$$\begin{aligned} \$\text{Bid} &= \frac{1}{\text{Ask in } ¥/\$} = \frac{1}{120} = \\ &= \$0.00833/\text{¥} \end{aligned}$$

Ask Price (Bank A):

$$\begin{aligned} \$\text{Ask} &= \frac{1}{\text{Bid in } ¥/\$} = \frac{1}{100} = \\ &= \$0.01/\text{¥} \end{aligned}$$

Explanation: The conversion involves taking the reciprocal to switch from an indirect quote (foreign currency per unit of domestic currency) to a direct quote (domestic currency per unit of foreign currency).

Supporting Statement: The quotes are now in American terms as \$/¥.

(b) Calculate the Cross Rates for Yen/Euro from Bank A and B

Utilize the Yen/Euro cross rate for both bid and ask prices based on Bank A and B.

Cross Rate Calculation:

$$\$ \text{Cross Rate Bid} (\text{¥}/\text{€}) = \text{Bid} (\text{¥}/\text{\$}) \times \text{Bid} (\text{\$}/\text{€})$$

$$\$ \text{Cross Rate Ask} (\text{¥}/\text{€}) = \text{Ask} (\text{¥}/\text{\$}) \times \text{Ask} (\text{\$}/\text{€})$$

From Bank A and Bank B:

$$\text{Bid (¥/€): } \$\text{Bid} (\text{¥}/\text{€}) = 100 \times 1.25 = ¥125/\text{€}$$

$$\text{Ask (¥/€): } \$\text{Ask} = 120 \times 1.5 = ¥180/\text{€}$$

Explanation: The cross rates use the product of the bid rates of USD/JPY and EUR/USD for bid and the same for ask.

Supporting Statement: Cross rates for ¥/€ calculated using Bank A (¥/\$) and Bank B (\$/€).

(c) Arbitrage Trading with Bank C

Check for arbitrage opportunities by comparing cross rates from step (b) with Bank C's quotes.

Bank C:

Bid (¥/€): ¥200/€

Ask (¥/€): ¥250/€

Comparison:

Arbitrage Buy (¥/€): from Bank B @ ¥125/€

Arbitrage Sell (¥/€): to Bank C @ ¥200/€

Explanation: Arbitrage profit exists if buying low and selling high in different markets/banks is possible.

Supporting Statement: Arbitrage trading involves divergence between derived cross rates and actual bank rates.

(d) Calculating Arbitrage Profit with \$10,000

Starting with \$10,000:

1. Convert \$10,000 to ¥ using Bank A:

$$\text{\text{Amount in ¥}} = 10,000 \times 100 = \text{\text{¥1,000,000}}$$

2. Convert ¥1,000,000 to € using Bank C (Bid rate):

$$\text{\text{Amount in €}} = \frac{1,000,000}{200} = \text{\text{€5,000}}$$

3. Convert €5,000 to \$ using Bank B:

$$\text{\text{Amount in \$}} = 5,000 \times 1.25 = \text{\text{\$6,250}}$$

Explanation: Track how \$10,000 initial capital converts through each step of arbitrage trading.

Supporting Statement: Each step accurately follows arbitrage conversion to find out profit.

Final Output:

Resulting profit by arbitrage:

$$\text{\text{Arbitrage Profit}} = \$6,250 - \$10,000 = \text{\text{\$250}}$$

Conclusion: The final arbitrage profit using triangular arbitrage with an initial capital of \$10,000 results in a final profit of \$250.