

Chemical Equilibrium - Finding Equilibrium Pressure

Given:

- Reaction: $2 \text{NO(g)} \leftrightarrow 2 \text{NO(g)} + \text{O}_2\text{(g)}$
- $K_p = 1.11 \times 10^{-5}$ at 200°C
- Volume of the vessel: 2.50 L
- Initial pressure of NO: 4.00 atm

Objective:

To find the pressure of NO at equilibrium.

1. Introduction and Setup:

The balanced chemical equation for the reaction is given, and the equilibrium constant in terms of pressure (K_p) is provided. The task involves determining the equilibrium pressure of NO gas when the system reaches equilibrium.

2. Determine Changes in Pressure:

Let x be the change in the pressure of NO as the system comes to equilibrium.

The initial pressures are:

- Initial $P_{\text{NO}} = 4.00$ atm
- $P_{\text{O}_2} = 0$ atm

The changes in pressure at equilibrium will be:

- P_{NO} decreases by $2x$
- P_{O_2} increases by x

The equilibrium pressures will be:

- $P_{\text{NO}} = 4.00 - 2x$
- $P_{\text{O}_2} = x$

3. Express K_p in Terms of Equilibrium Pressures:

The expression for K_p for the equilibrium reaction:

$$K_p = \frac{(P_{\text{NO}_2})^2 (P_{\text{O}_2})}{(P_{\text{NO}})^2}$$

Substituting the equilibrium pressures:

$$K_p = \frac{x (4.00 - 2x)^2}{(4.00 - 2x)^2}$$

Simplify:

$$K_p = x (4.00 - 2x)^2$$

4. Solve the Equilibrium Equation:

Set up the quadratic equation:

$$1.11 \times 10^{-5} = x (4.00 - 2x)^2$$

5. Solve for x :

Simplify the equation carefully to avoid errors:

$$1.11 \times 10^{-5} = x (16 - 16x + 4x^2)$$

6. Calculate Equilibrium Pressure:

Once x is determined, calculate the equilibrium pressure of NO:

$$P_{\text{NO}} = 4.00 - 2x$$

7. Final Solution:

The equilibrium pressure $P_{\text{NO}} = 4.00 - 2x$ atm.