

Perfectly-Secure Asynchronous MPC for General Adversaries

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Secure Multi-Party Computation (MPC)

Secure Multi-Party Computation (MPC)

x_n



x_1



x_{n-1}



x_2



x_3

Secure Multi-Party Computation (MPC)

x_n



$$y = f(x_1, \dots, x_n)$$



x_1



x_{n-1}



x_2



x_3

Secure Multi-Party Computation (MPC)

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x_3

Secure Multi-Party Computation (MPC)

x_n



$$y = f(x_1, \dots, x_n)$$

- Privacy



x_1



x_{n-1}



x_2



x_3

Secure Multi-Party Computation (MPC)

x_n



$$y = f(x_1, \dots, x_n)$$

- Privacy
- Correctness



x_1



x_{n-1}

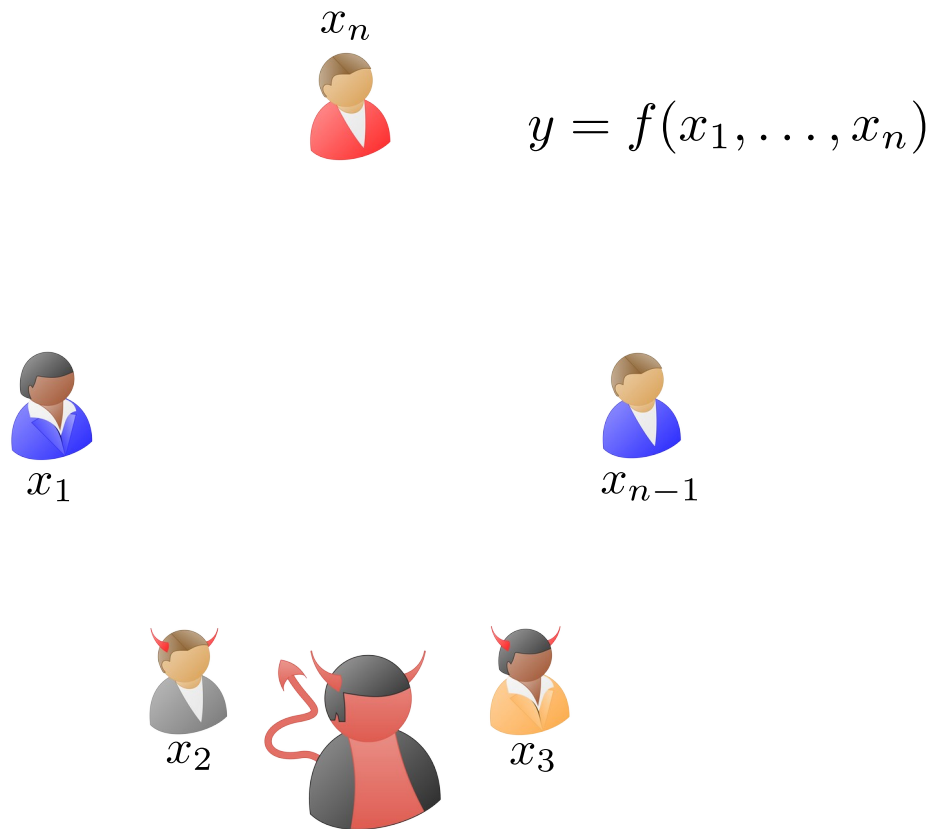


x_2



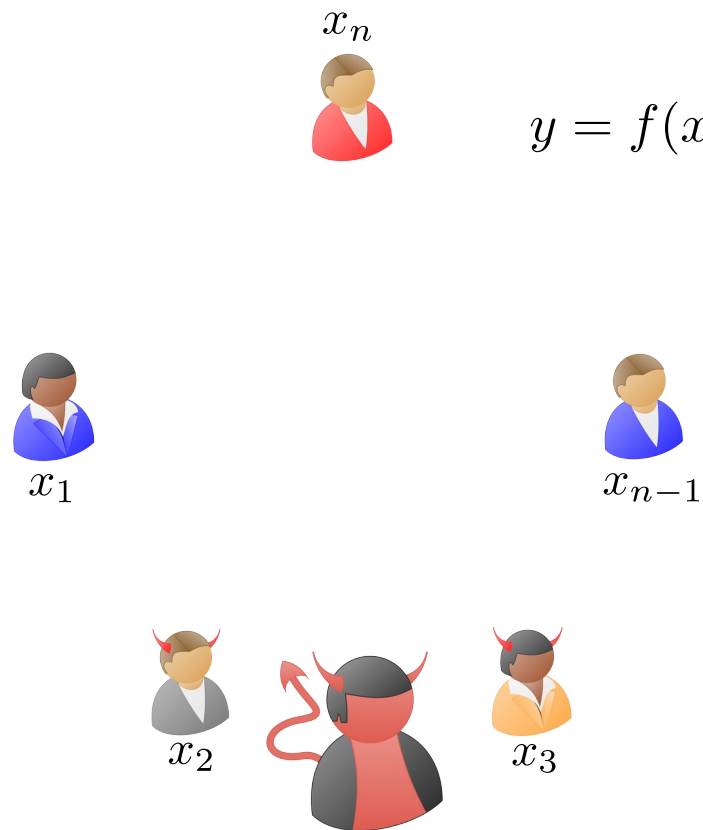
x_3

Secure Multi-Party Computation (MPC)



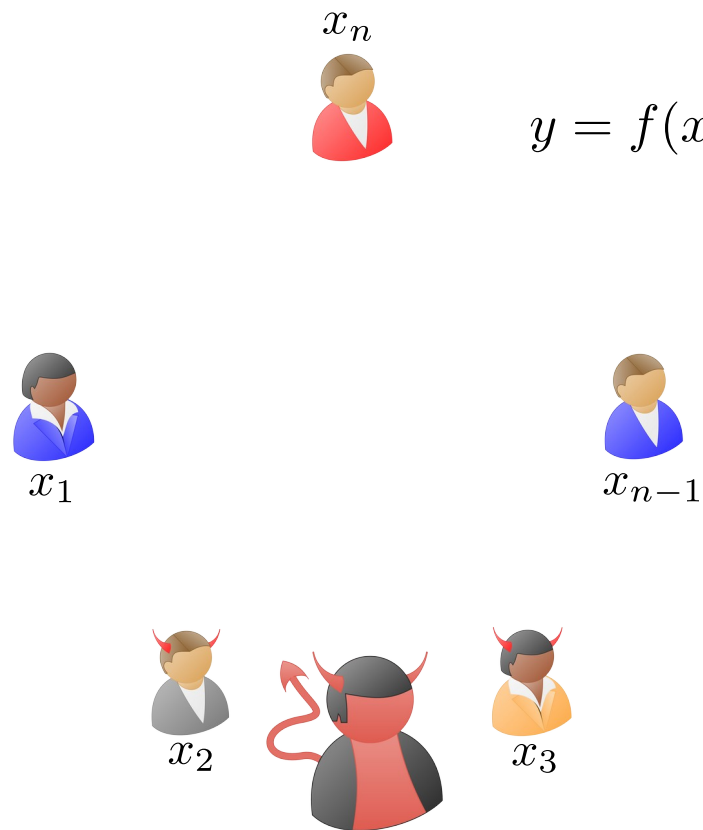
- Privacy
- Correctness
- Independence of Inputs

Secure Multi-Party Computation (MPC)



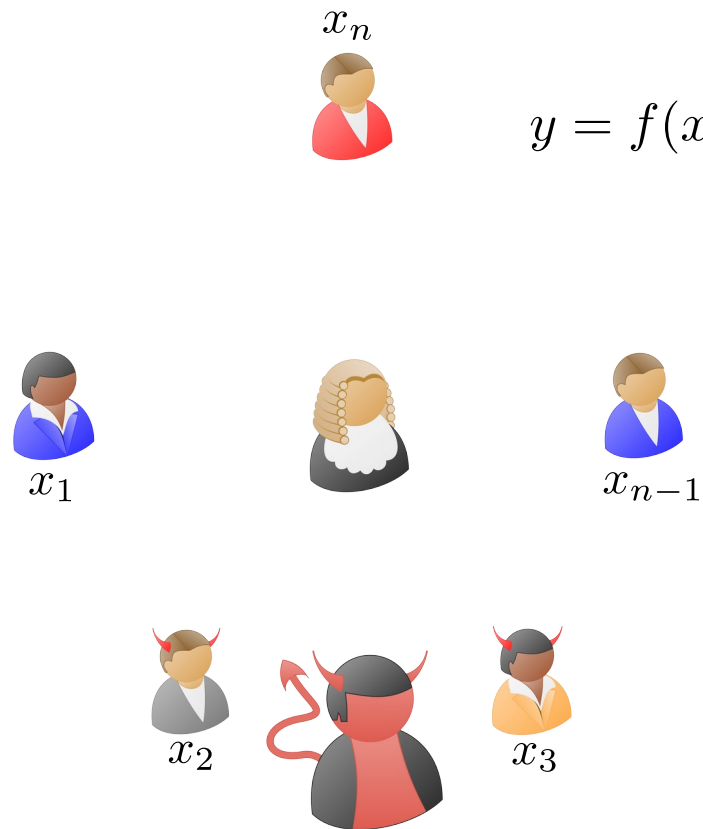
- Privacy
- Correctness
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- Guaranteed Output Delivery

Secure Multi-Party Computation (MPC)



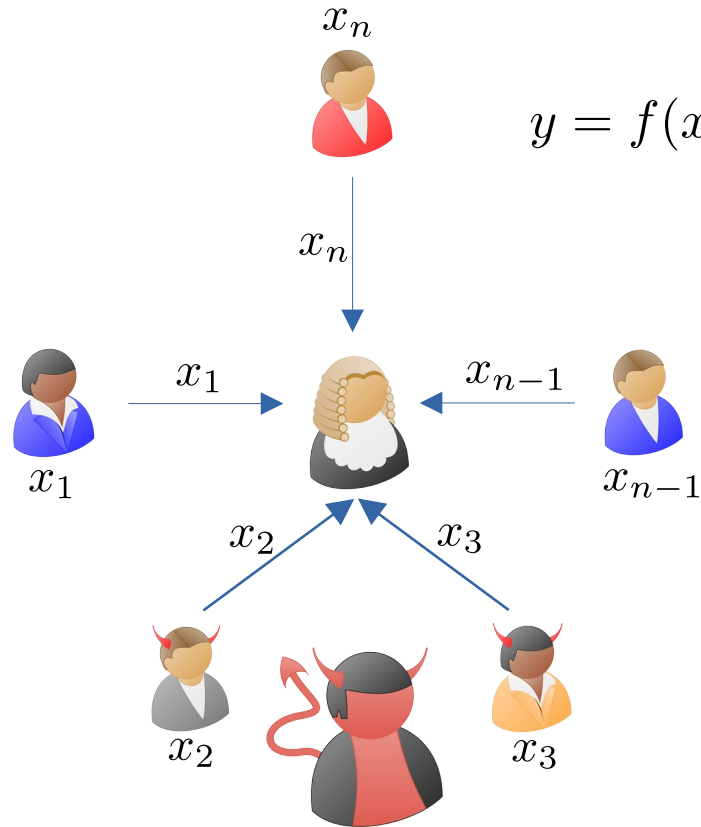
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Secure Multi-Party Computation (MPC)



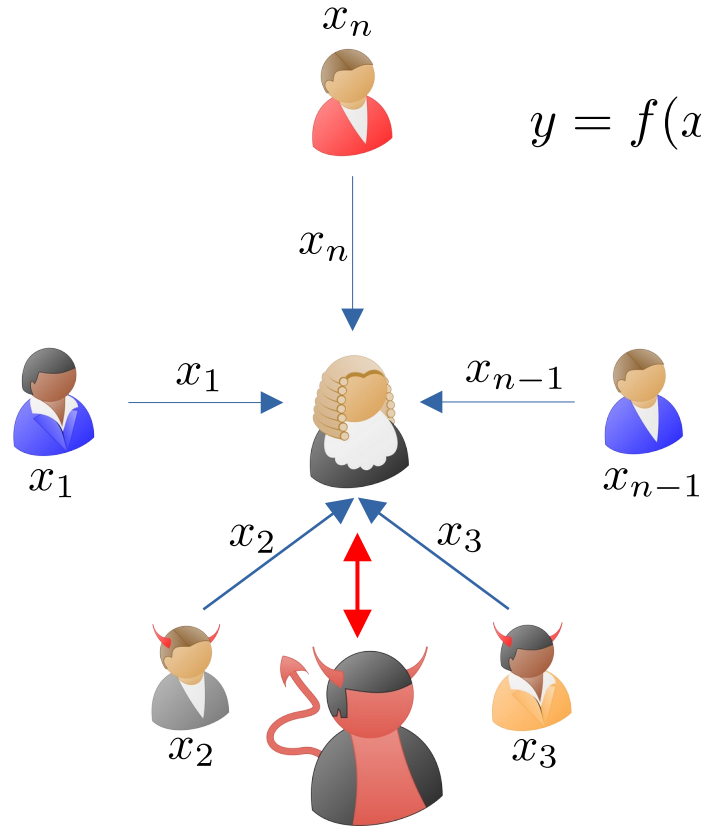
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Secure Multi-Party Computation (MPC)



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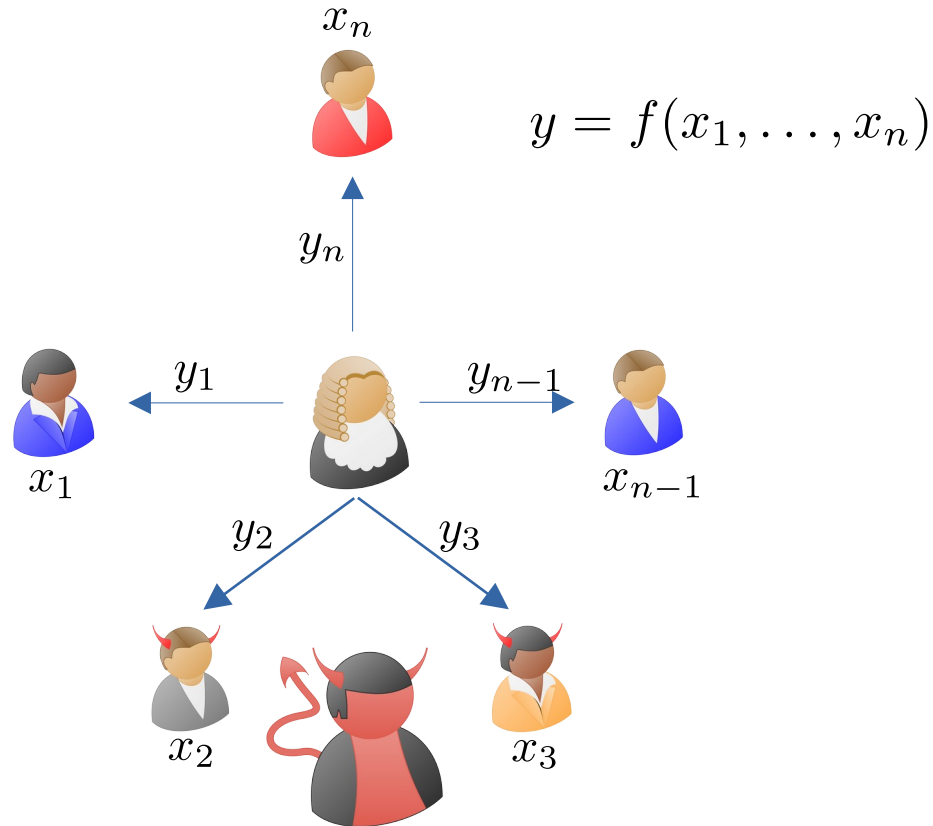
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Communication Models

Communication Models

Synchronous Model

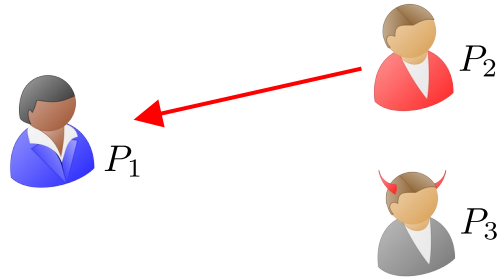
Communication Models

Synchronous Model



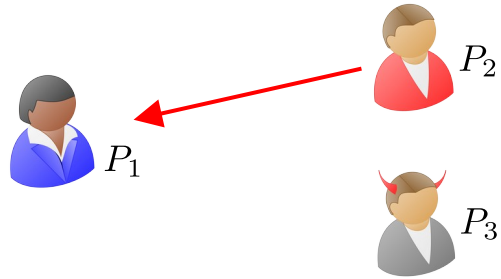
Communication Models

Synchronous Model



Communication Models

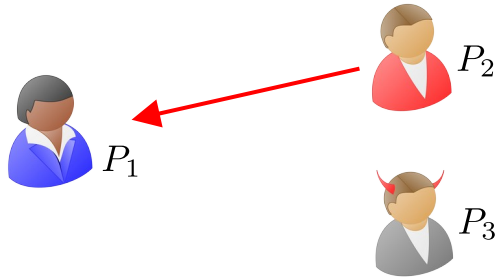
Synchronous Model



- Message Delays $< \Delta$

Communication Models

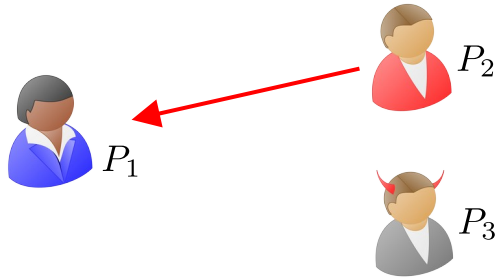
Synchronous Model



- Message Delays $< \Delta$
- Synchronized Clocks

Communication Models

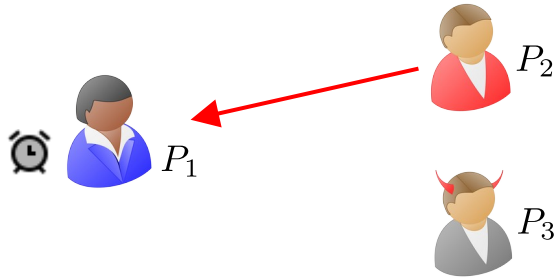
Synchronous Model



- Message Delays $< \Delta$
- Synchronized Clocks
- Computation in Rounds

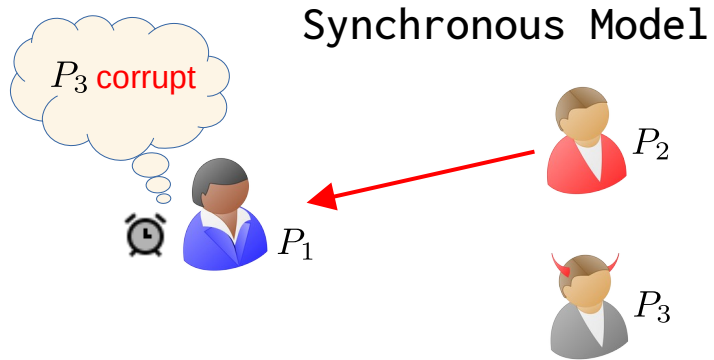
Communication Models

Synchronous Model



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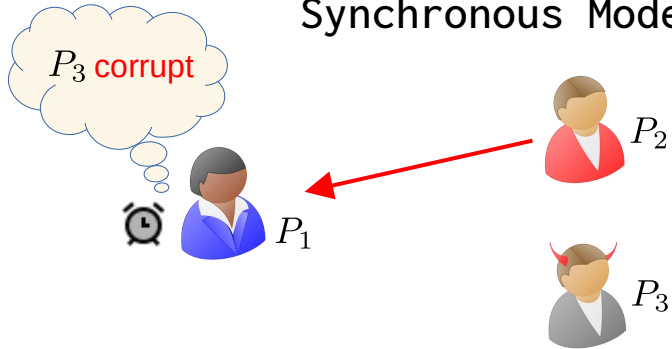
Communication Models



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Communication Models

Synchronous Model

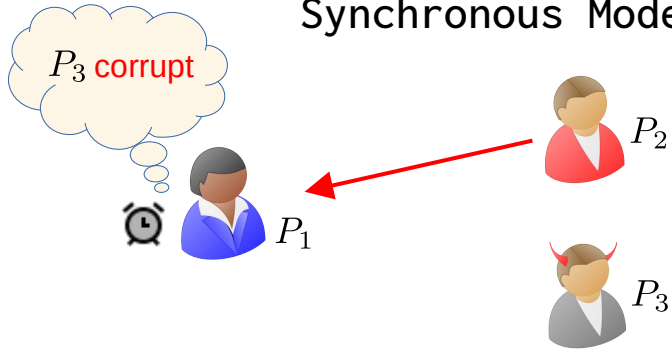


Asynchronous Model [\[BCG93\]](#)

- Message Delays $< \Delta$
- Synchronized Clocks
- Computation in Rounds

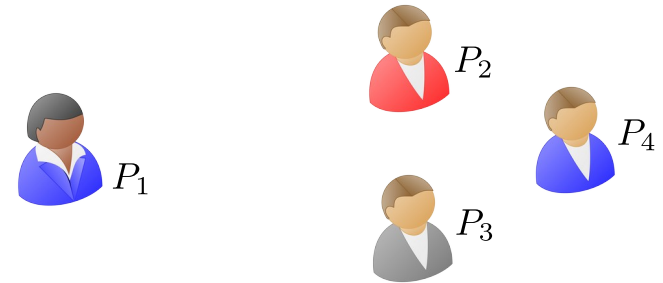
Communication Models

Synchronous Model



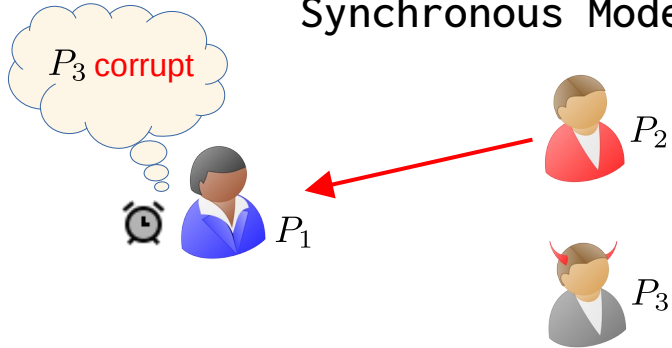
- Message Delays $< \Delta$
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Asynchronous Model [BCG93]



Communication Models

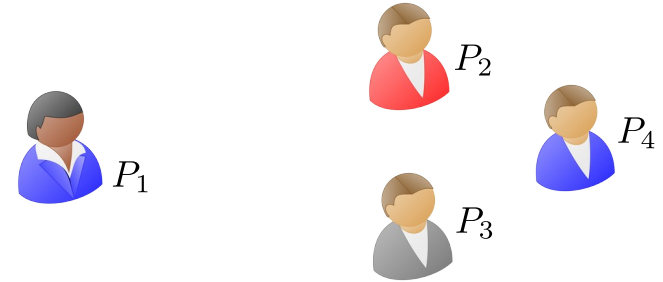
Synchronous Model



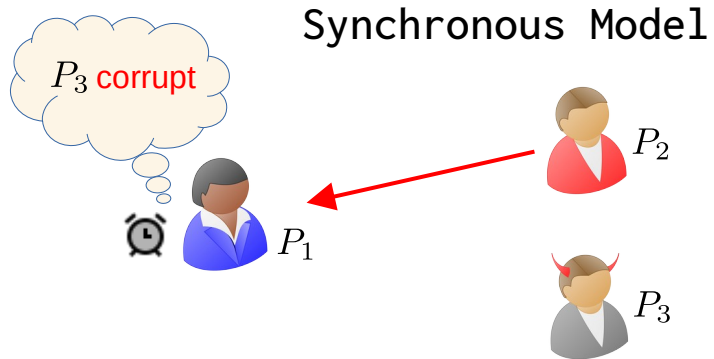
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Asynchronous Model [BCG93]

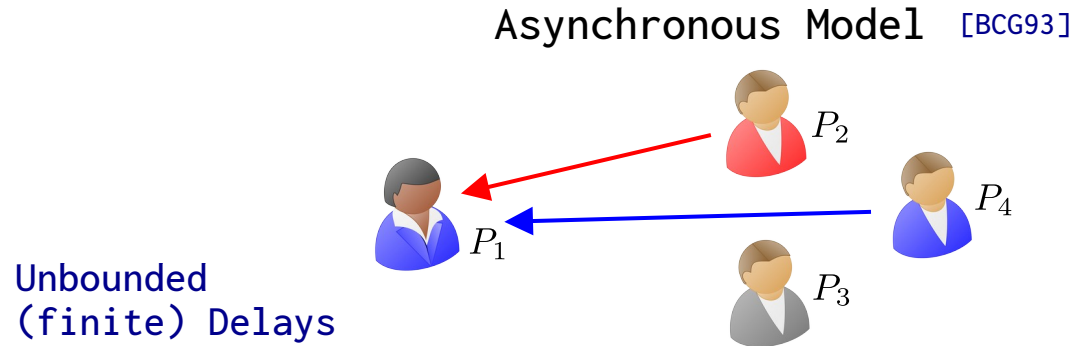
Unbounded
(finite) Delays



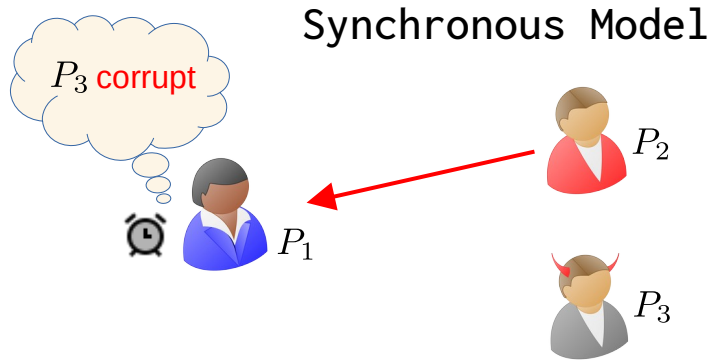
Communication Models



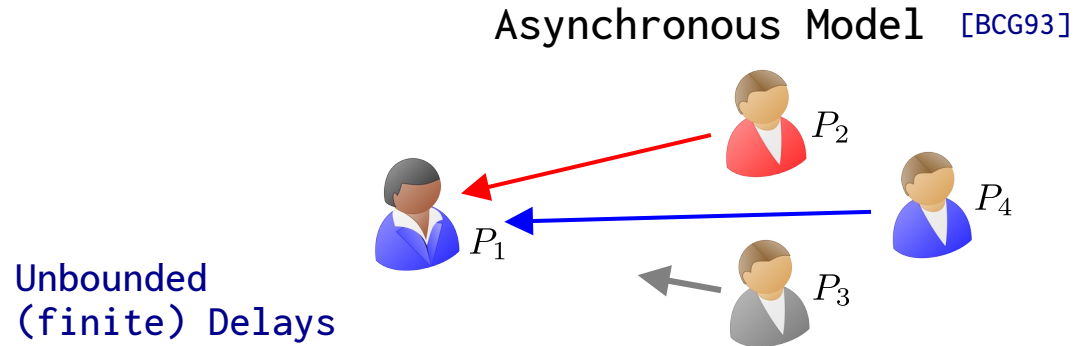
- Message Delays $< \Delta$
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- Computation in Rounds



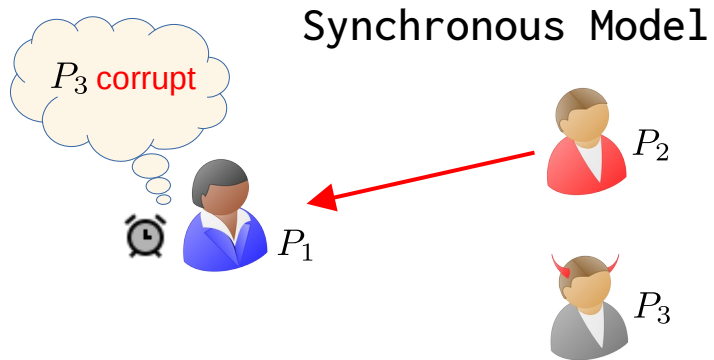
Communication Models



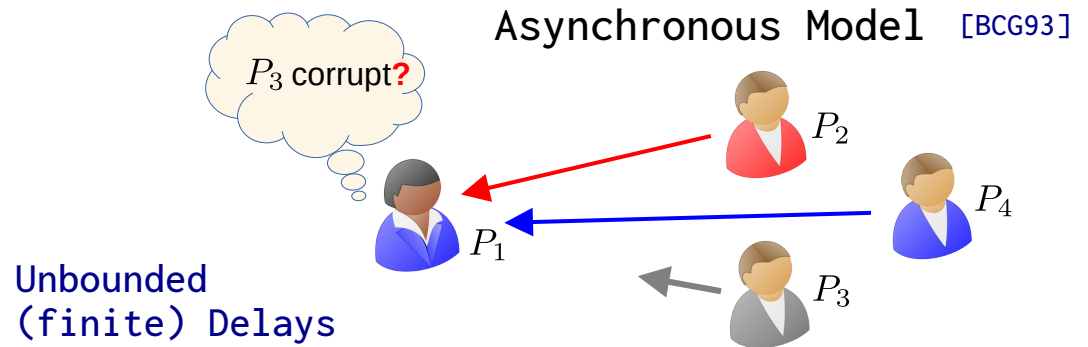
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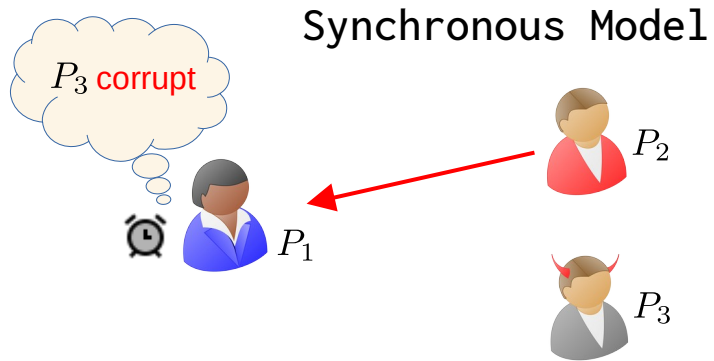
Communication Models



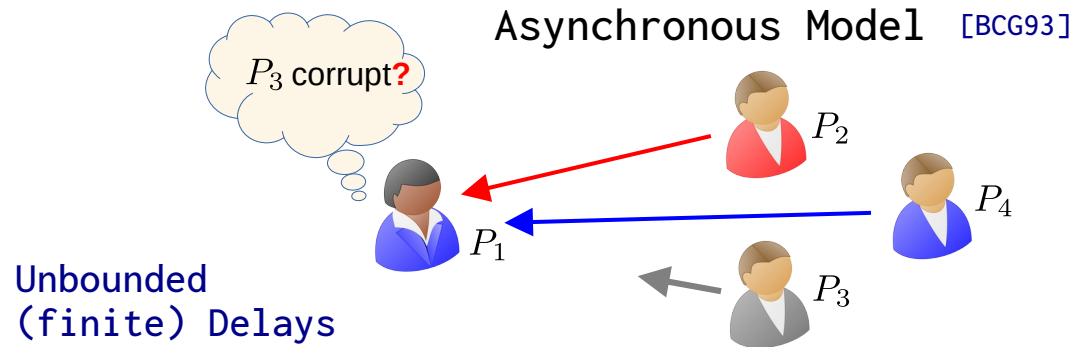
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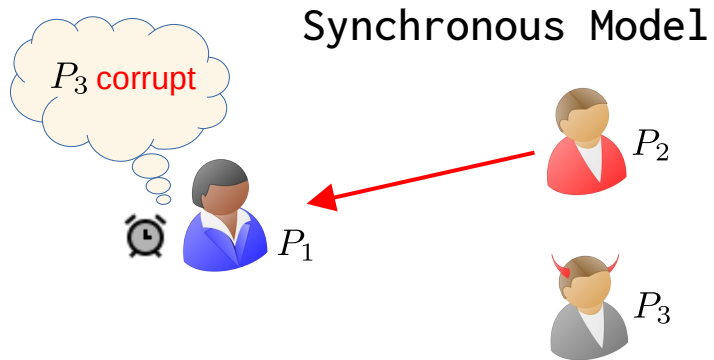


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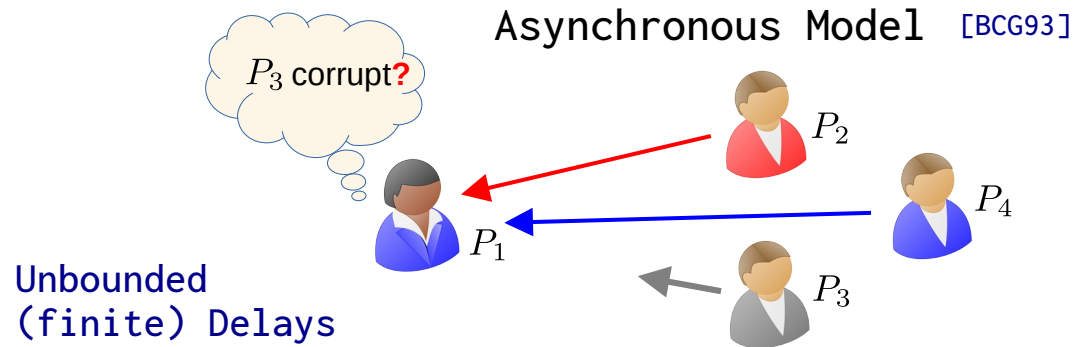


- No Input Provision

Communication Models

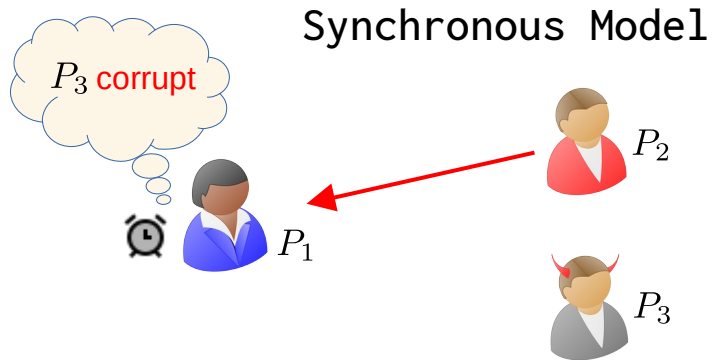


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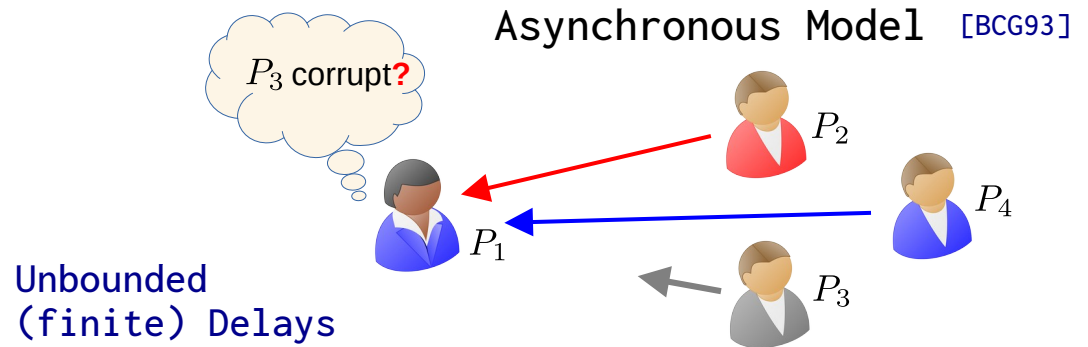


- No Input Provision $f(x_1, x_2, \cdot, x_4)$

Communication Models

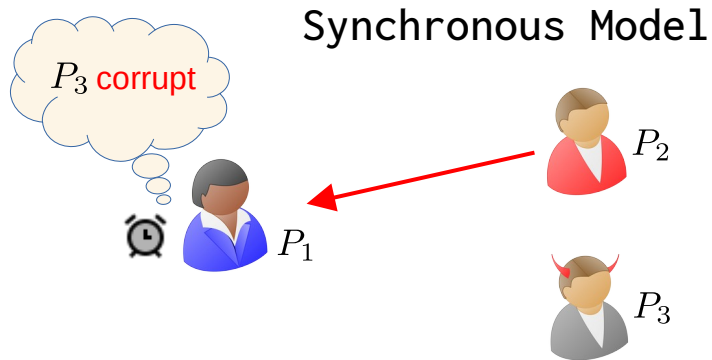


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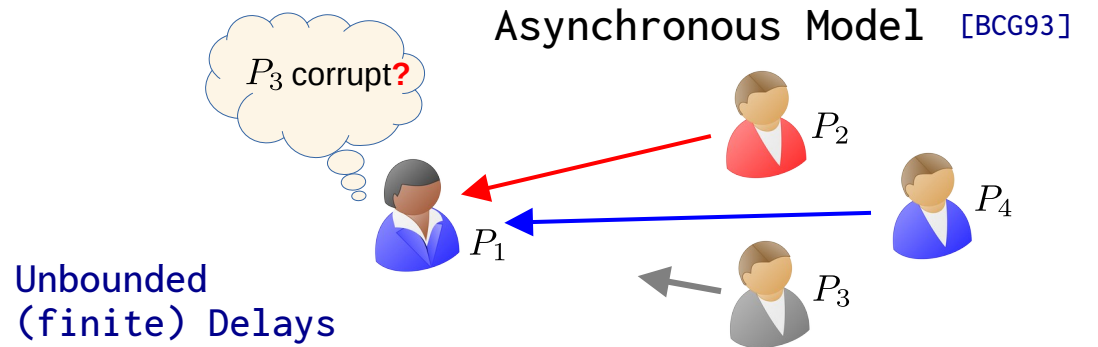


- No Input Provision $f(x_1, x_2, \cdot, x_4)$
- Worse Resilience

Communication Models

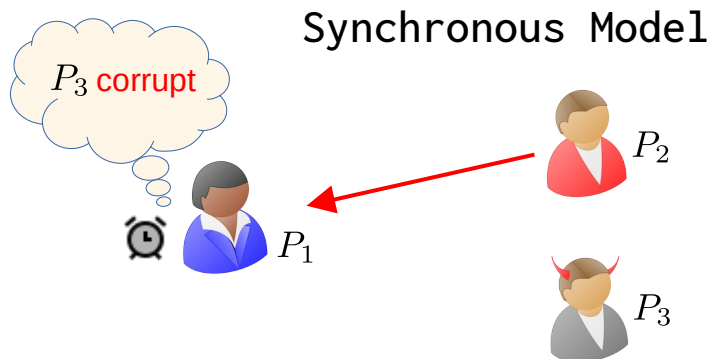


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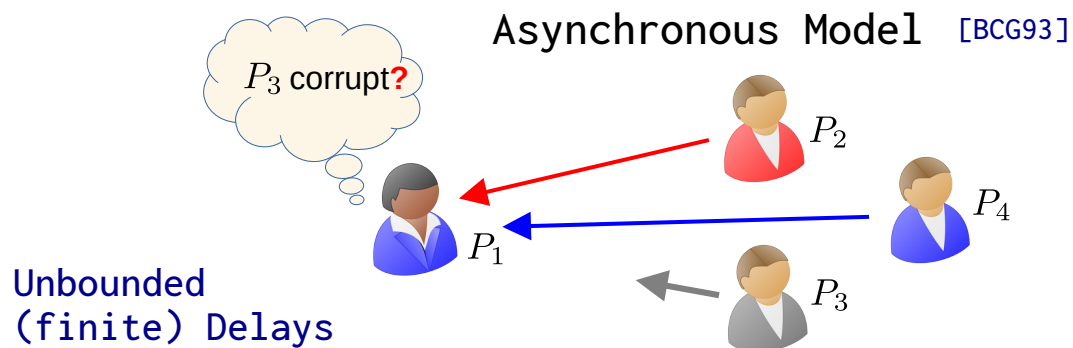



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- Worse Resilience
- Worse Communication and Computation (Known Protocols)

Communication Models

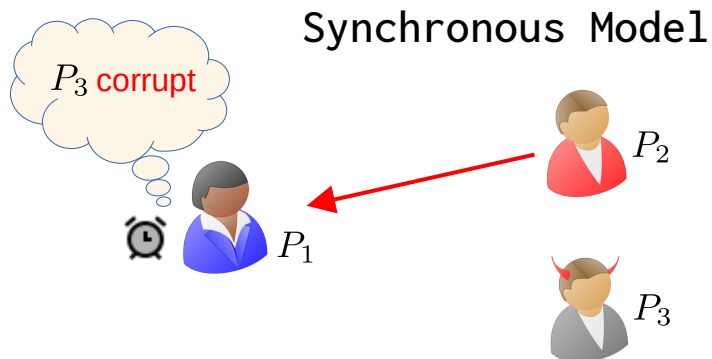


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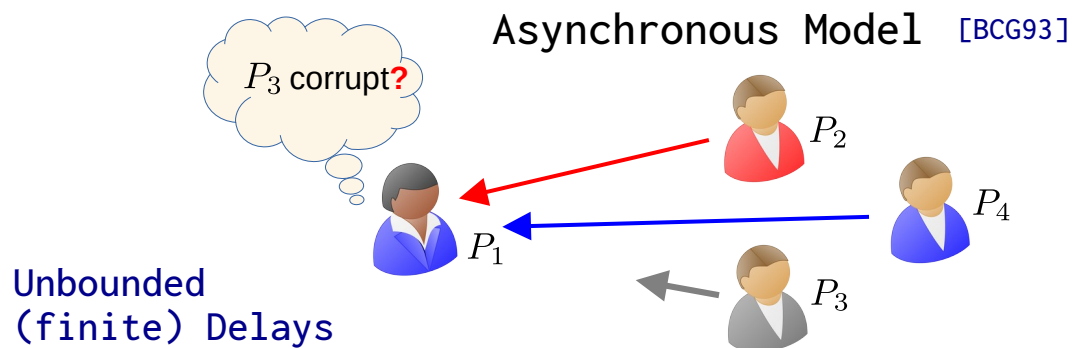




- No Input Provision $f(x_1, x_2, \cdot, x_4)$
- Worse Resilience
- Worse Communication and Computation (Known Protocols)
- Real-World Networks 

Communication Models



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- No Input Provision $f(x_1, x_2, \cdot, x_4)$
- Worse Resilience
- Worse Communication and Computation (Known Protocols)
- Real-World Networks 
- Responsiveness 

General Adversaries

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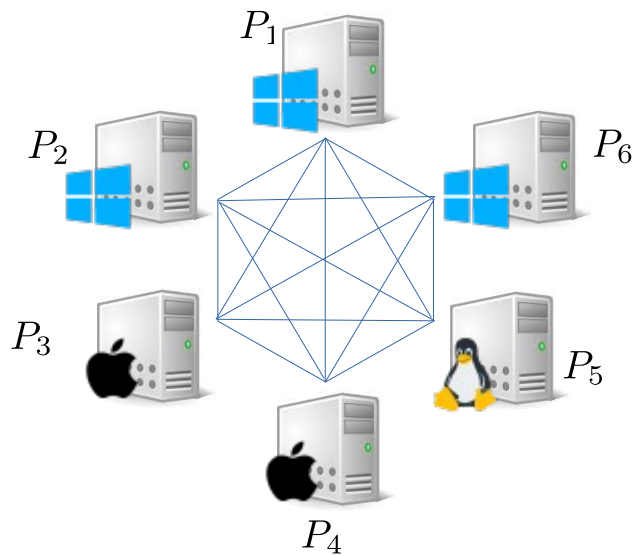
Most MPC protocols: $t < \frac{n}{k}$

General Adversaries

Most MPC protocols: $t < \frac{n}{k}$ Can be limiting...

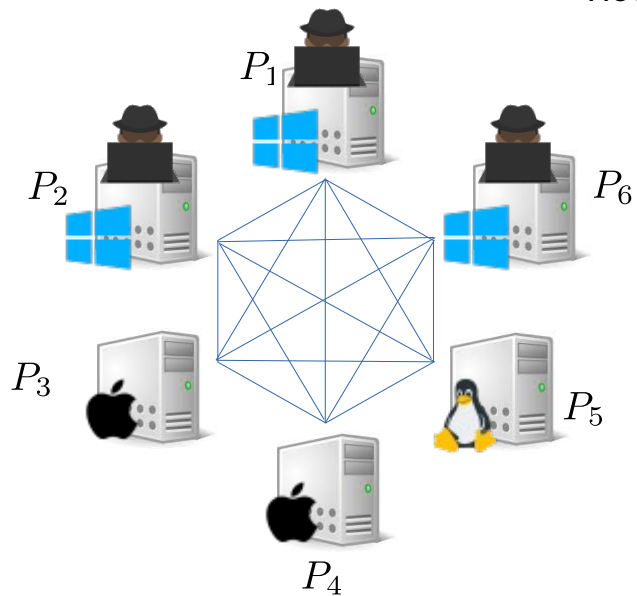
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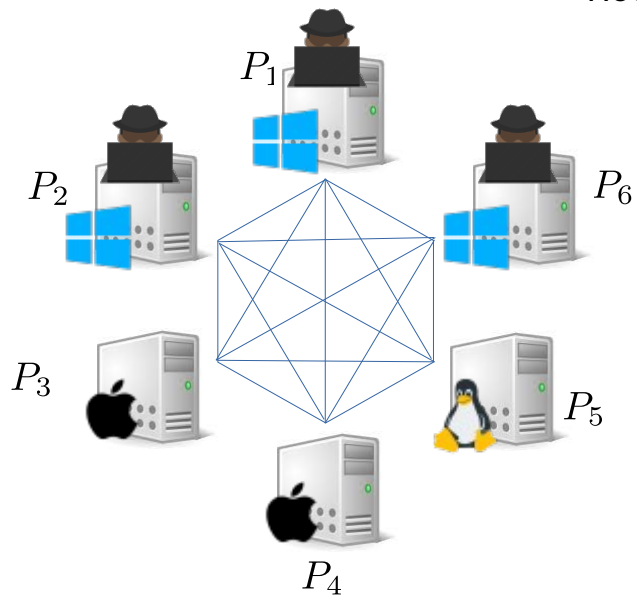
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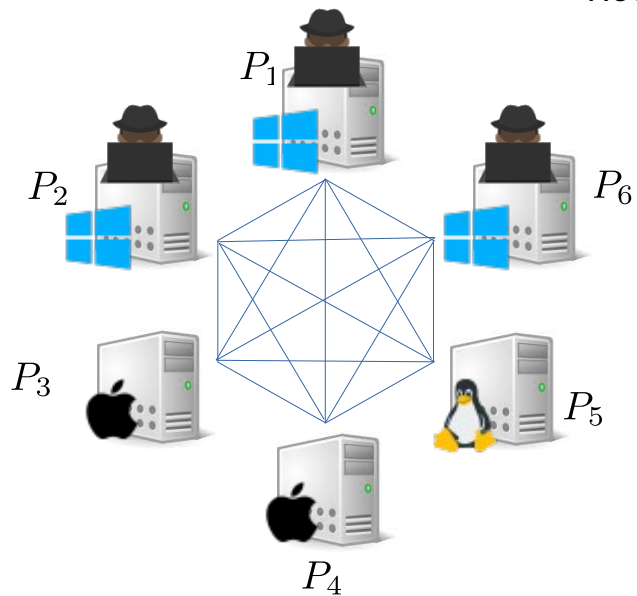
Most MPC protocols: $t < \frac{n}{k}$ Can be limiting...



- Computational-Security

General Adversaries

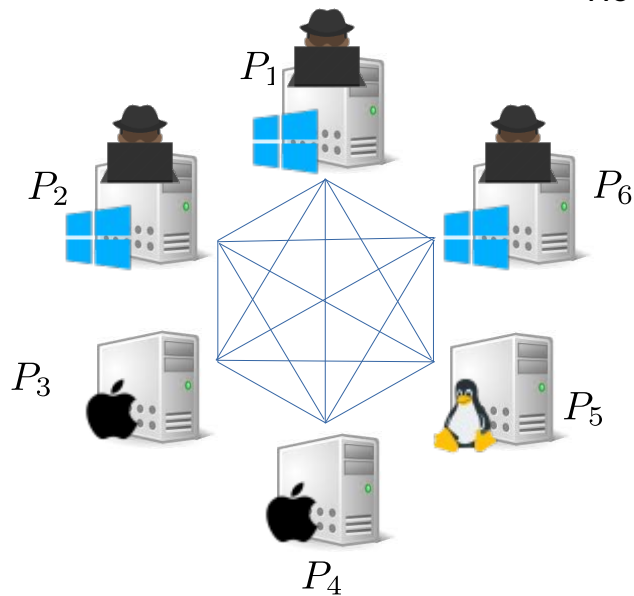
Most MPC protocols: $t < \frac{n}{k}$ Can be limiting...



- Computational-Security
- Guaranteed Output Delivery

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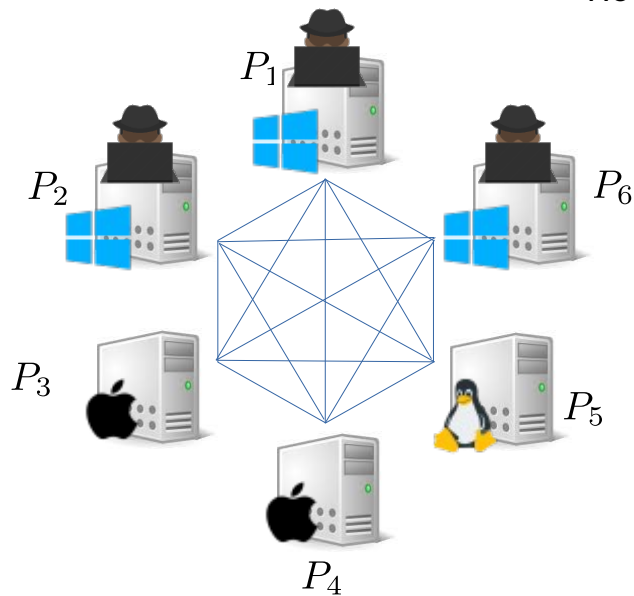


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$$t < 6/2 \implies t \leq 2$$

General Adversaries

Most MPC protocols: $t < \frac{n}{k}$ Can be limiting...



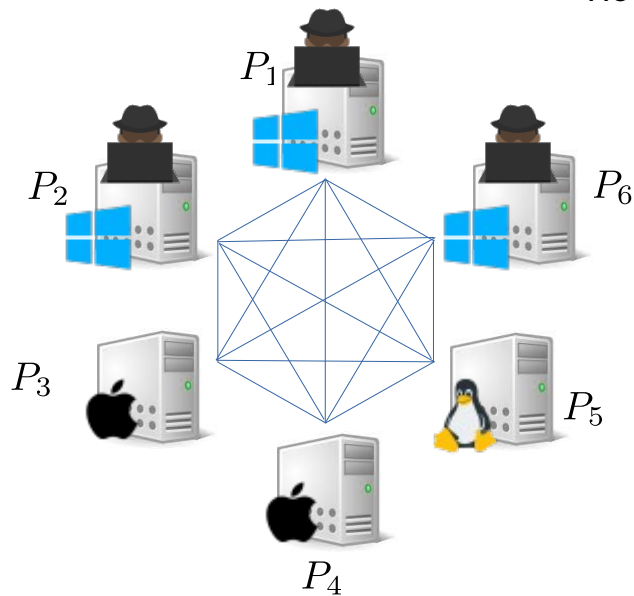
$$\mathcal{Z} = \{\{P_1, P_2, P_6\}, \{P_3, P_4\}, \{P_5\}\} \quad [\text{HM97}]$$

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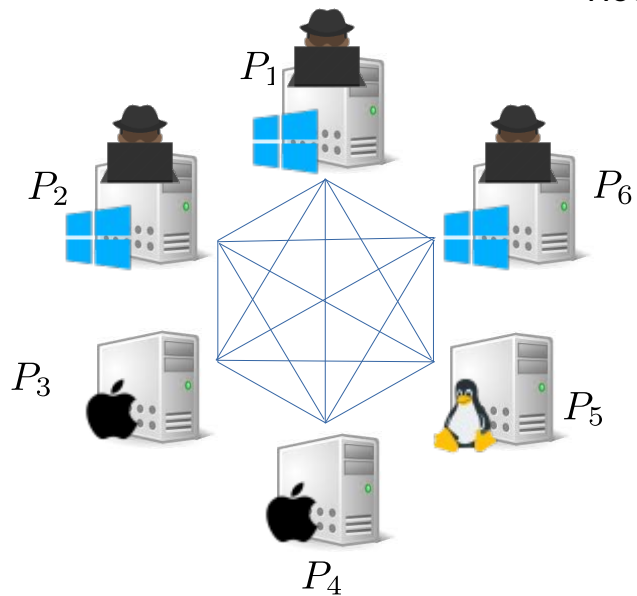
- monotone, maximal

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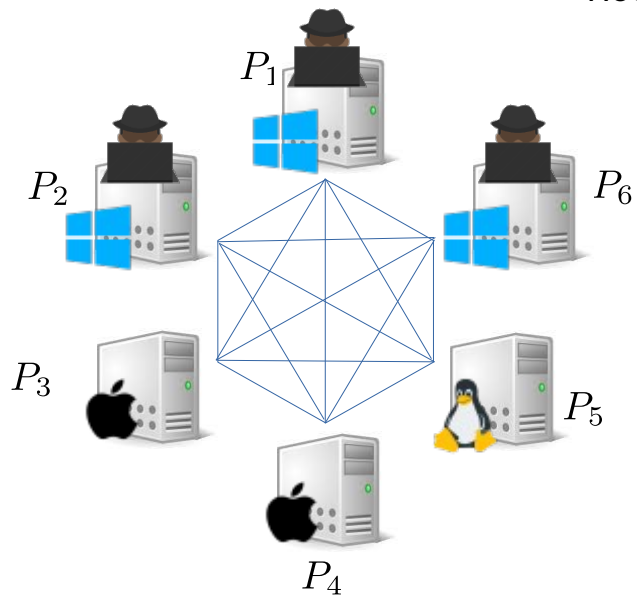
- monotone, maximal
- Size possibly exp in n

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General Adversaries

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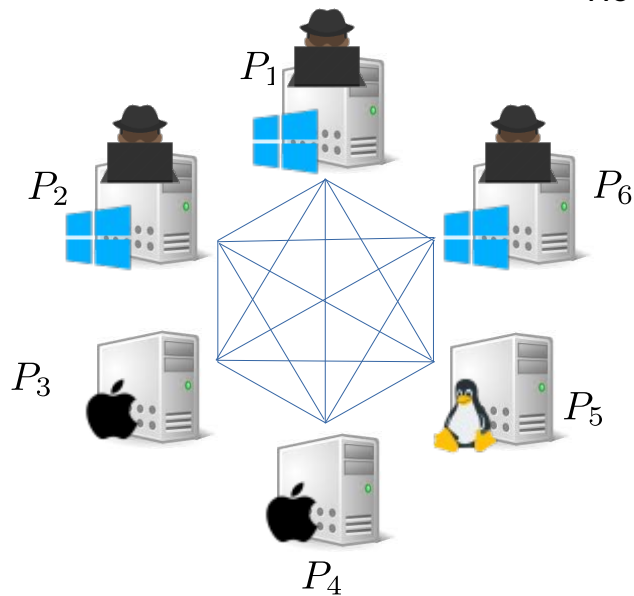
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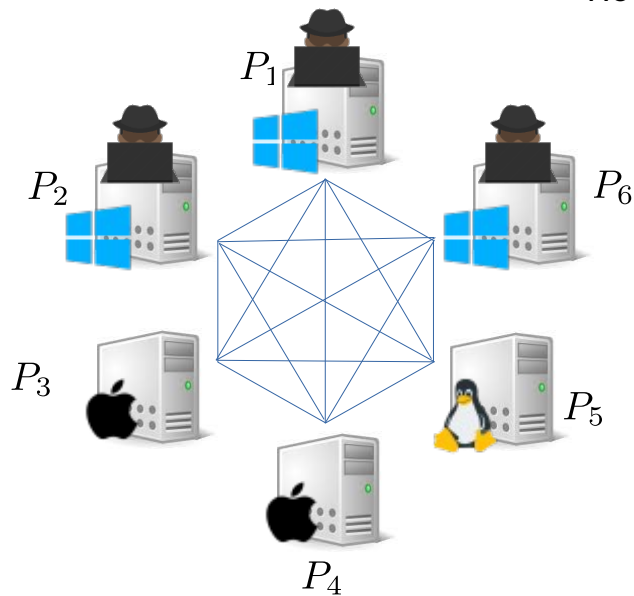
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- Communication Complexity $|\mathcal{Z}|^{\mathcal{O}(1)}$ (Known Protocols)

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- Size possibly exp in n

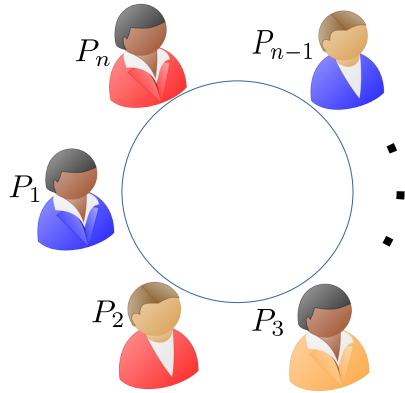
- Increased flexibility
- Communication Complexity $|\mathcal{Z}|^{\mathcal{O}(1)}$ (Known Protocols)
- Computational Complexity Lower Bound $\Omega(|\mathcal{Z}|)$ [HM00]

- Computational-Security
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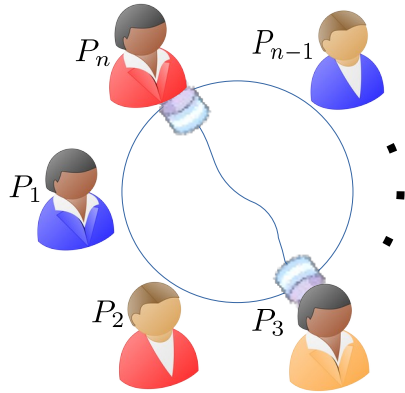
$$t < 6/2 \implies t \leq 2$$

Setting

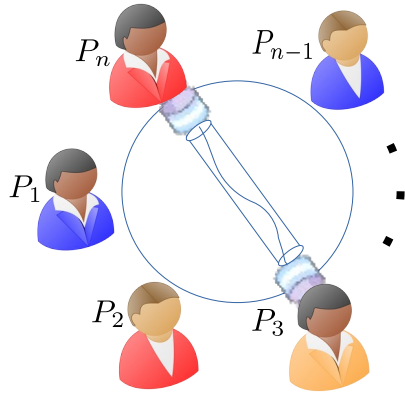
Setting



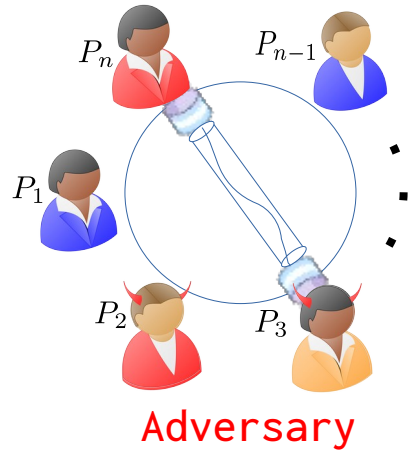
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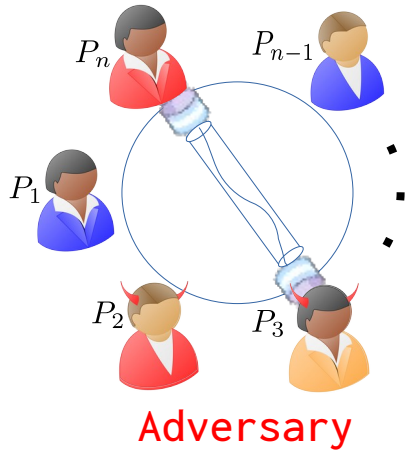
Setting



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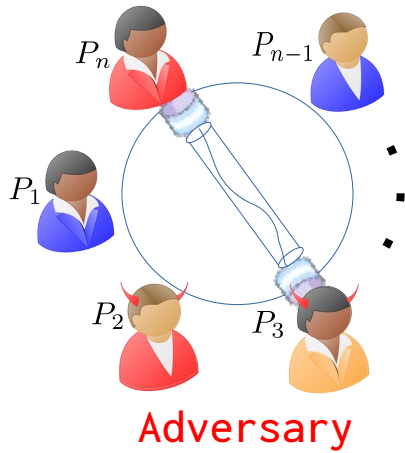
Setting



- Computationally-Unbounded



Setting

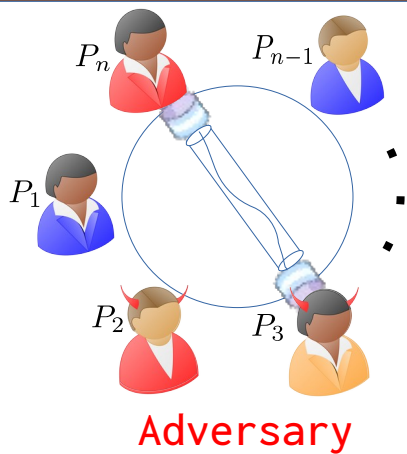


- Computationally-Unbounded

Perfect-Security 0% ⚠



Setting



- Computationally-Unbounded

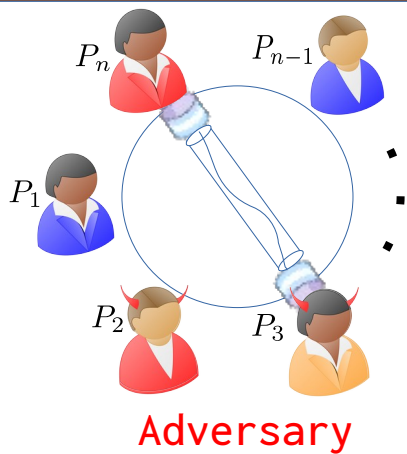
Perfect-Security 0% !



- Malicious (Byzantine)



Setting



- Computationally-Unbounded

Perfect-Security 0% !



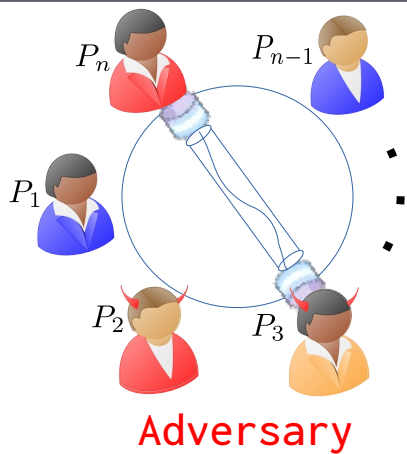
- Malicious (Byzantine)



- Message Scheduler



Setting



- Computationally-Unbounded

Perfect-Security 0% !



- Malicious (Byzantine)



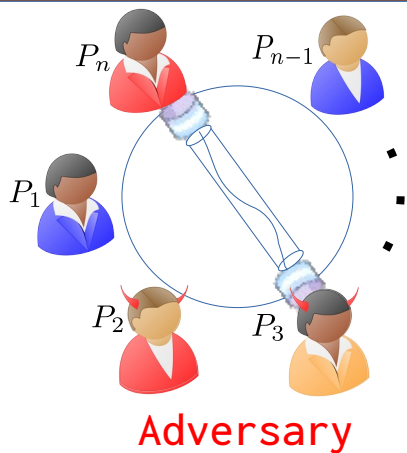
- Message Scheduler



Adversary Structure $\mathcal{Z} = \{\dots, Z_i, \dots\}$



Setting



- Computationally-Unbounded

Perfect-Security 0% !



- Malicious (Byzantine)



- Message Scheduler

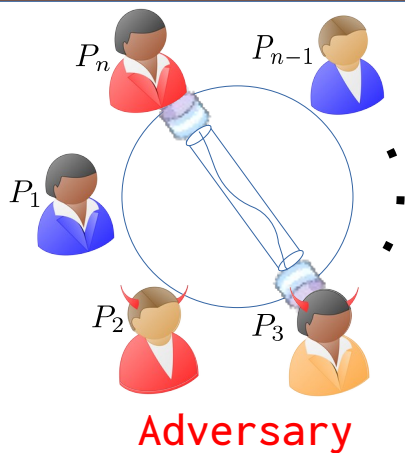


Adversary Structure $\mathcal{Z} = \{\dots, Z_i, \dots\}$



Requires $Q^{(4)}$
[KSR02]

Setting



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Perfect-Security 0% !



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Adversary Structure $\mathcal{Z} = \{\dots, Z_i, \dots\}$

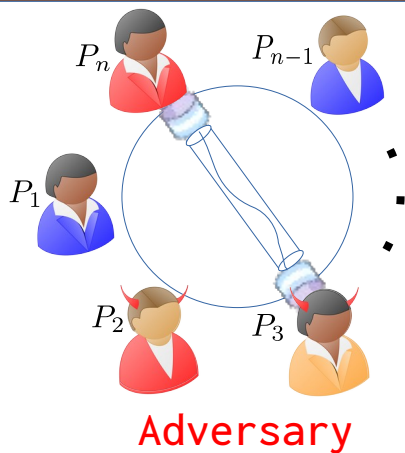
Partysset \mathcal{P}



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Setting



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Perfect-Security 0% !



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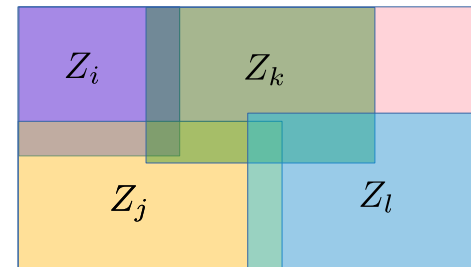


Adversary Structure $\mathcal{Z} = \{\dots, Z_i, \dots\}$

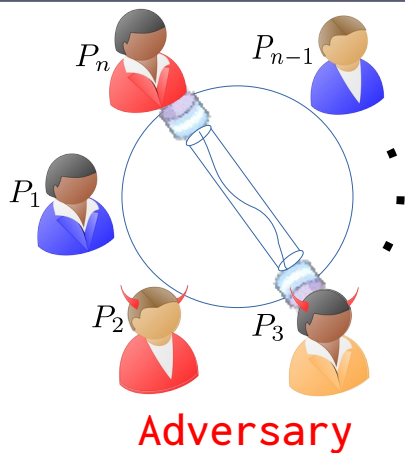


Requires $Q^{(4)}$
[KSR02]

Partysset \mathcal{P}



Setting



$f(x_1, x_2, x_3, x_4)$



- **Computationally-Unbounded**

Perfect-Security 0% !



- **Malicious (Byzantine)**



- **Message Scheduler**

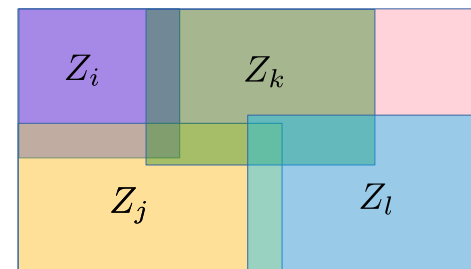


Adversary Structure $\mathcal{Z} = \{\dots, Z_i, \dots\}$

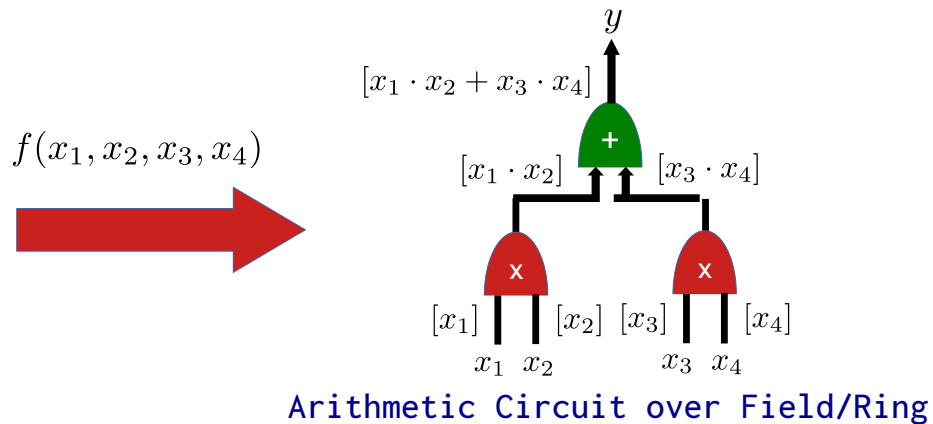
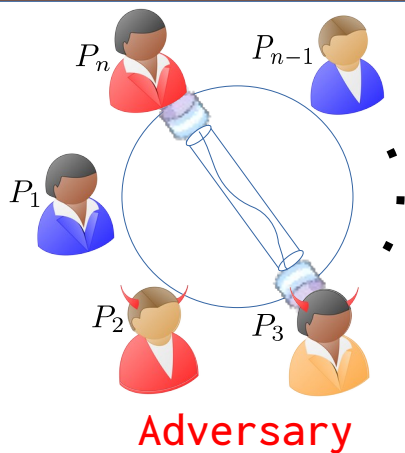


Requires $Q^{(4)}$
[KSR02]

Partysset \mathcal{P}



Setting



- **Computationally-Unbounded**

Perfect-Security 0% !



- **Malicious (Byzantine)**



- **Message Scheduler**

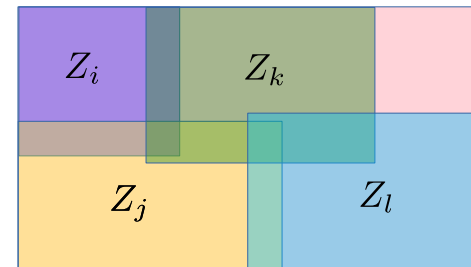


Adversary Structure $\mathcal{Z} = \{\dots, Z_i, \dots\}$

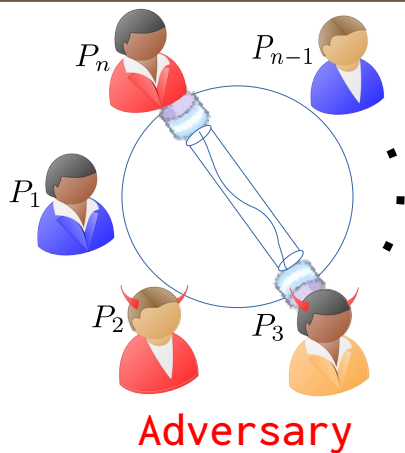


Requires $Q^{(4)}$
[KSR02]

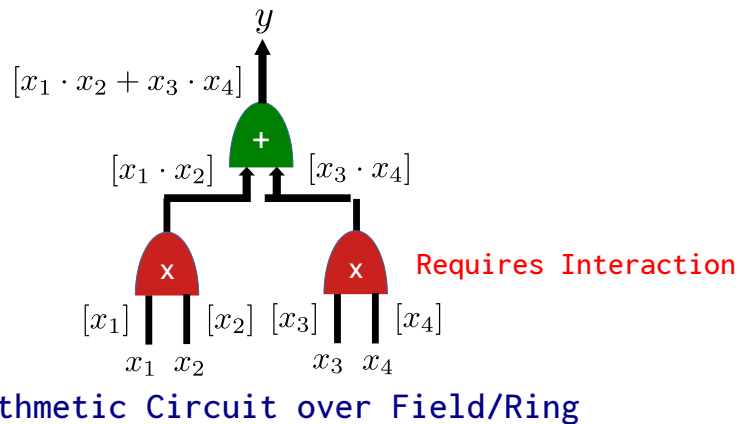
Partysset \mathcal{P}



Setting



$f(x_1, x_2, x_3, x_4)$



- **Computationally-Unbounded**

Perfect-Security 0% !



- **Malicious (Byzantine)**



- **Message Scheduler**

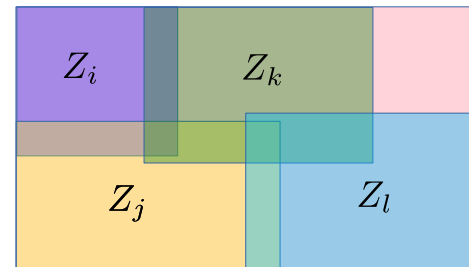


Adversary Structure $\mathcal{Z} = \{\dots, Z_i, \dots\}$

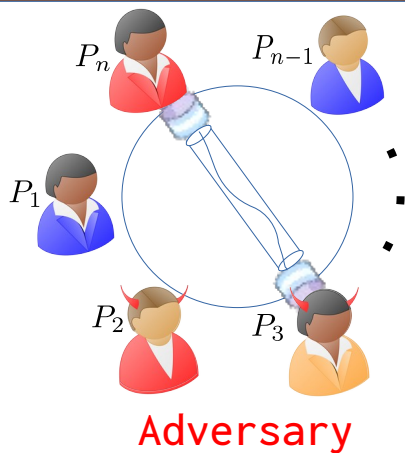


Requires $Q^{(4)}$
[KSR02]

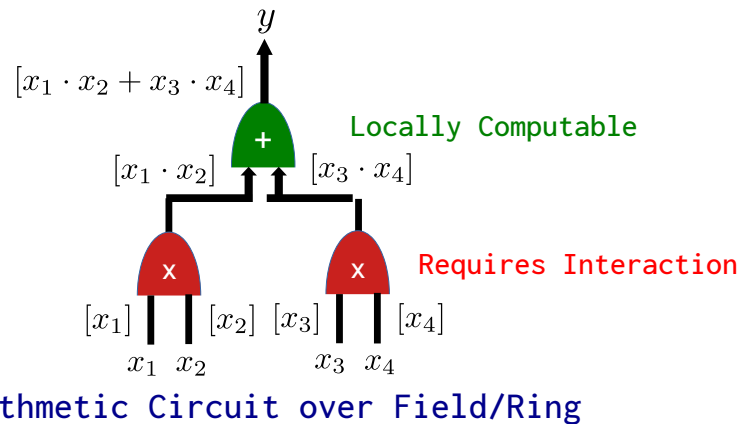
Partysset \mathcal{P}



Setting



$f(x_1, x_2, x_3, x_4)$



- Computationally-Unbounded

Perfect-Security 0%



- Malicious (Byzantine)



- Message Scheduler

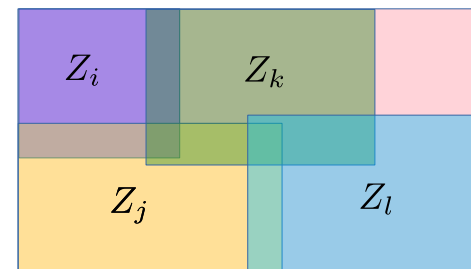


Adversary Structure $\mathcal{Z} = \{\dots, Z_i, \dots\}$



Requires $Q^{(4)}$
[KSR02]

Partyset \mathcal{P}



Work on General Adversaries

Work on General Adversaries

Synchronous Model

Work on General Adversaries

Synchronous Model

- [\[HM97, HM00\]](#)
Feasibility Results

Work on General Adversaries

Synchronous Model

- [HM97, HM00]
Feasibility Results
- [CDD+99, CDM00, FHM99, Mau02, SS99]
Polynomial (in $|Z|$) complexities

Work on General Adversaries

Synchronous Model

- [HM97, HM00]
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Polynomial (in $|Z|$) complexities
- [HT13, L013]
Improved Efficiency

Work on General Adversaries

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Work on General Adversaries

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Work on General Adversaries

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 - Mixed Model [BFH+08, HMZ08]
 - Cryptographic Setting [KRS+18, SW19]

Work on General Adversaries

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etc...

Work on General Adversaries

Synchronous Model

Asynchronous Model

- [HM97, HM00]
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Work on General Adversaries

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etc...

Asynchronous Model

- [KSR02]

Work on General Adversaries

Synchronous Model

- [HM97, HM00]
Feasibility Results
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- Others...
 - Byzantine Agreement [FM98, AFM03]
 - Mixed Model [BFH+08, HMZ08]
 - Cryptographic Setting [KRS+18, SW19]
etc...

Asynchronous Model

- [KSR02]
 - Perfect-Security Setting

Work on General Adversaries

Synchronous Model

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 - Cryptographic Setting [KRS+18, SW19]
etc...

Asynchronous Model


- [KSR02]
 - Perfect-Security Setting
 - MSP-based AVSS Protocol

Work on General Adversaries

Synchronous Model

- [HM97, HM00]
Feasibility Results
- [CDD+99, CDM00, FHM99, Mau02, SS99]
Polynomial (in $|Z|$) complexities
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etc...

Asynchronous Model


- [KSR02]
 - Perfect-Security Setting
 - MSP-based AVSS Protocol
 - AMPC Protocol 

Work on General Adversaries

Synchronous Model

- [HM97, HM00]
Feasibility Results
- [CDD+99, CDM00, FHM99, Mau02, SS99]
Polynomial (in $|\mathcal{Z}|$) complexities
- [HT13, L013]
Improved Efficiency
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 - Byzantine Agreement [FM98, AFM03]
 - Mixed Model [BFH+08, HMZ08]
 - Cryptographic Setting [KRS+18, SW19]
etc...

Asynchronous Model


- [KSR02]
 - Perfect-Security Setting
 - MSP-based AVSS Protocol
 - AMPC Protocol 
- Our Work

Work on General Adversaries

Synchronous Model

- [HM97, HM00]
Feasibility Results
- [CDD+99, CDM00, FHM99, Mau02, SS99]
Polynomial (in $|Z|$) complexities
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 - Byzantine Agreement [FM98, AFM03]
 - Mixed Model [BFH+08, HMZ08]
 - Cryptographic Setting [KRS+18, SW19]
etc...

Asynchronous Model


- [KSR02]
 - Perfect-Security Setting
 - MSP-based AVSS Protocol
 - AMPC Protocol 
- Our Work
 - Perfectly-Secure Additive SS-based ([Mau02]) AVSS Protocol

Work on General Adversaries

Synchronous Model

- [HM97, HM00]
Feasibility Results
- [CDD+99, CDM00, FHM99, Mau02, SS99]
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- [HT13, L013]
Improved Efficiency
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 - Byzantine Agreement [FM98, AFM03]
 - Mixed Model [BFH+08, HMZ08]
 - Cryptographic Setting [KRS+18, SW19]
etc...

Asynchronous Model


- [KSR02]
 - Perfect-Security Setting
 - MSP-based AVSS Protocol
 - AMPC Protocol 
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 - Perfectly-Secure Additive SS-based ([Mau02]) AVSS Protocol
 - Perfectly-Secure AMPC Protocol

Work on General Adversaries

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Feasibility Results
- [CDD+99, CDM00, FHM99, Mau02, SS99]
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- Others...
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 - Mixed Model [BFH+08, HMZ08]
 - Cryptographic Setting [KRS+18, SW19]
etc...

Asynchronous Model

- [KSR02]
 - Perfect-Security Setting
 - MSP-based AVSS Protocol
 - AMPC Protocol 
- Our Work
 - Perfectly-Secure Additive SS-based ([Mau02]) AVSS Protocol
 - Perfectly-Secure AMPC Protocol
 - ABA Protocol (Generalization of [CR93])

Flaw in [KSR02]

Flaw in [KSR02]

Player Elimination Framework [\[HMP00\]](#)

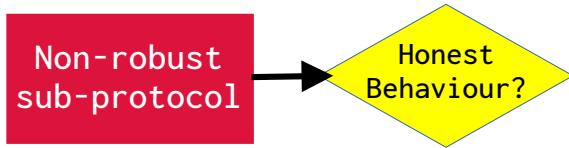
Flaw in [KSR02]

Player Elimination Framework [HMP00]

Non-robust
sub-protocol

Flaw in [KSR02]

Player Elimination Framework [HMP00]



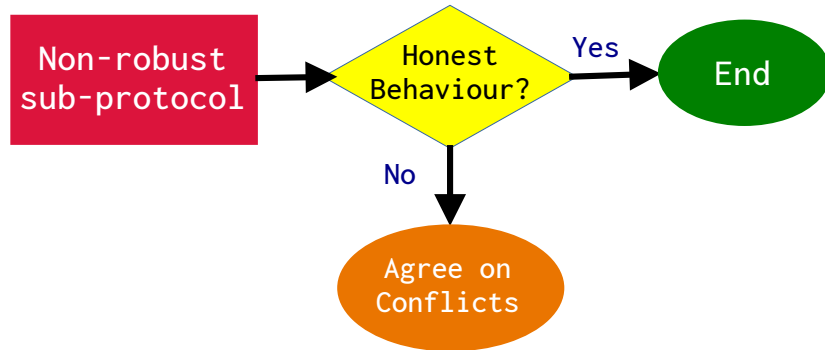
Flaw in [KSR02]

Player Elimination Framework [HMP00]



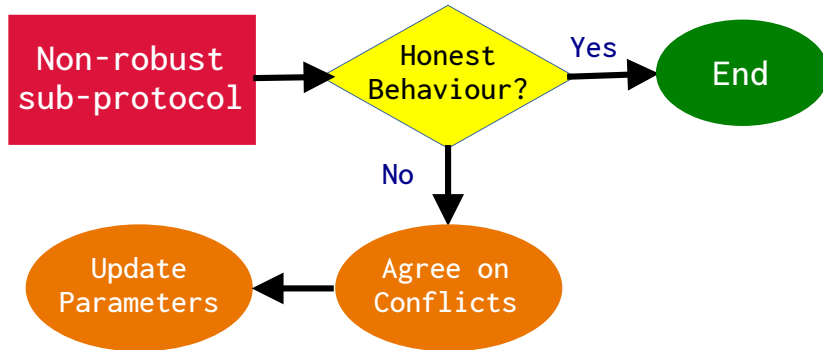
Flaw in [KSR02]

Player Elimination Framework [HMP00]



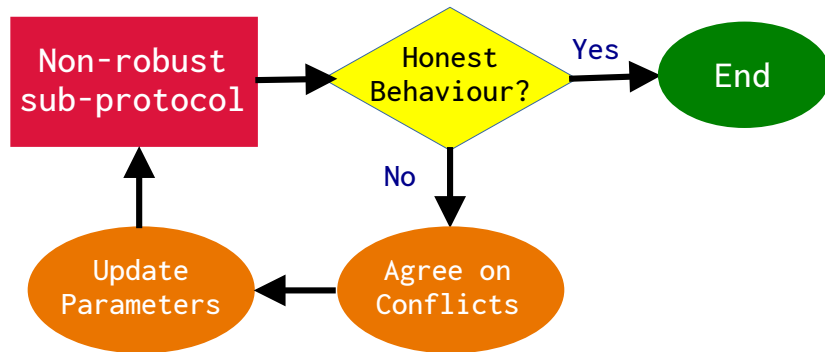
Flaw in [KSR02]

Player Elimination Framework [HMP00]



Flaw in [KSR02]

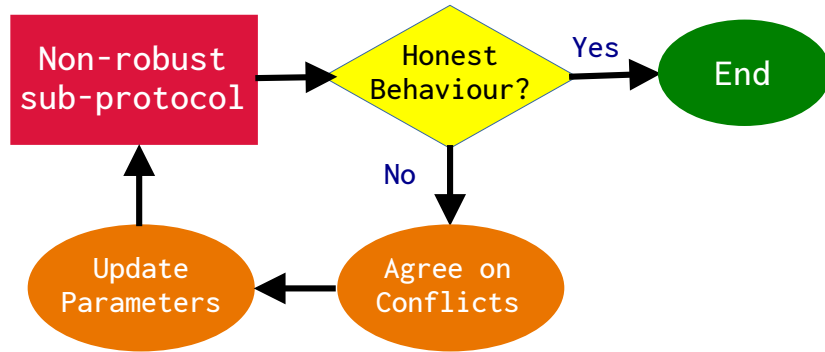
Player Elimination Framework [HMP00]



Flaw in [KSR02]

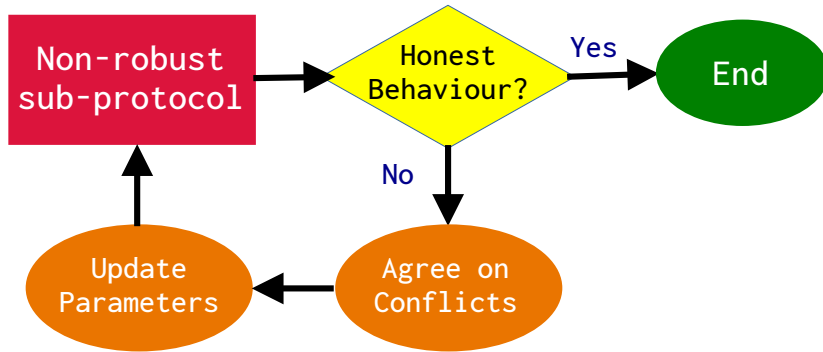
Player Elimination Framework [HMP00]

Example Execution



Flaw in [KSR02]

Player Elimination Framework [HMP00]

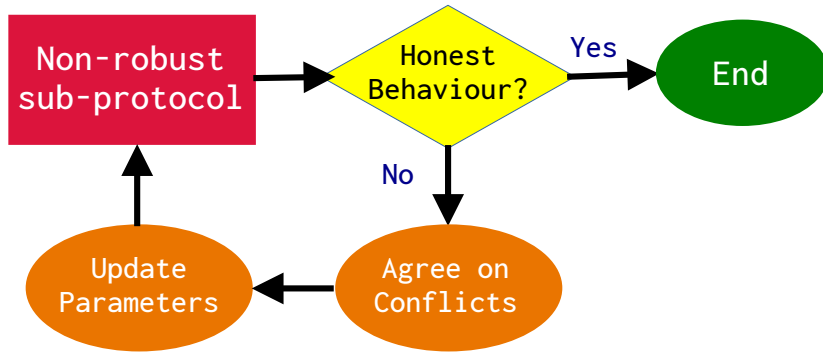


Example Execution

Partyset $\mathcal{P} = \{P_1, P_2, P_3, P_4, P_5, P_6, P_7\}$

Flaw in [KSR02]

Player Elimination Framework [HMP00]



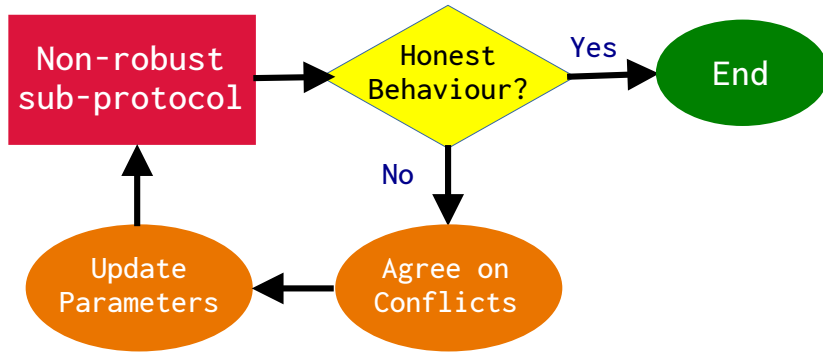
Example Execution

Partyset $\mathcal{P} = \{P_1, P_2, P_3, P_4, P_5, P_6, P_7\}$

Adversary Structure satisfying $\mathcal{Q}^{(4)}$

Flaw in [KSR02]

Player Elimination Framework [HMP00]



Example Execution

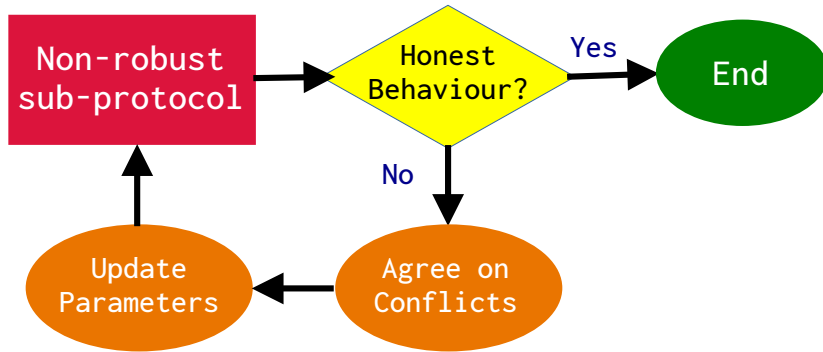
Partyset $\mathcal{P} = \{P_1, P_2, P_3, P_4, P_5, P_6, P_7\}$

Adversary Structure satisfying $\mathcal{Q}^{(4)}$

$$\mathcal{Z} = \{\{P_1, P_2\}, \{P_1, P_3\}, \{P_1, P_4\}, \{P_1, P_5, P_6\}, \{P_7\}\}$$

Flaw in [KSR02]

Player Elimination Framework [HMP00]



Example Execution

Partyset $\mathcal{P} = \{P_1, P_2, P_3, P_4, P_5, P_6, P_7\}$

Adversary Structure satisfying $\mathcal{Q}^{(4)}$

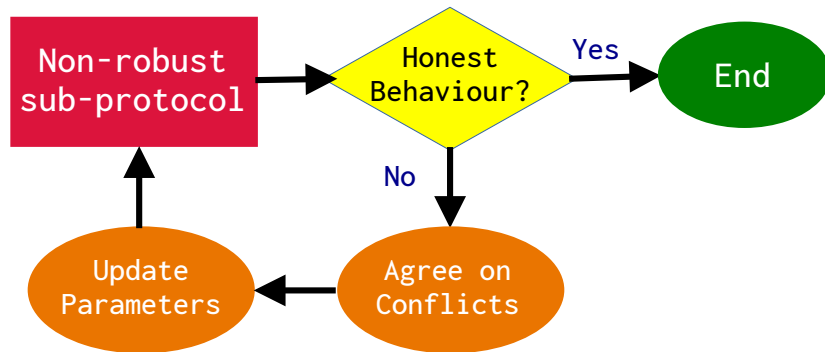
$\mathcal{Z} = \{\{P_1, P_2\}, \{P_1, P_3\}, \{P_1, P_4\}, \{P_1, P_5, P_6\}, \{P_7\}\}$

Conflict Set

$\{P_1, P_2, P_7\}$

Flaw in [KSR02]

Player Elimination Framework [HMP00]



Example Execution

Partyset $\mathcal{P} = \{P_1, P_2, P_3, P_4, P_5, P_6, P_7\}$

Adversary Structure satisfying $\mathcal{Q}^{(4)}$

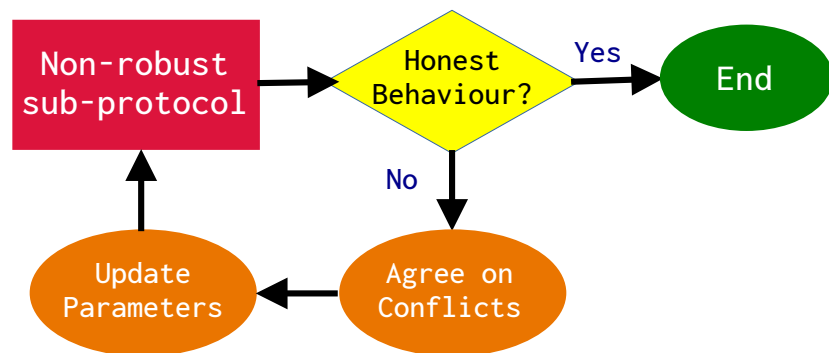
$$\mathcal{Z} = \{\{P_1, P_2\}, \{P_1, P_3\}, \{P_1, P_4\}, \{P_1, P_5, P_6\}, \{P_7\}\}$$

Conflict Set

$\{P_1, P_2, P_7\}$ Choice of Adversary

Flaw in [KSR02]

Player Elimination Framework [HMP00]



Example Execution

Partyset $\mathcal{P} = \{P_1, P_2, P_3, P_4, P_5, P_6, P_7\}$

Adversary Structure satisfying $\mathcal{Q}^{(4)}$

$$\mathcal{Z} = \{\{P_1, P_2\}, \{P_1, P_3\}, \{P_1, P_4\}, \{P_1, P_5, P_6\}, \{P_7\}\}$$

Conflict Set

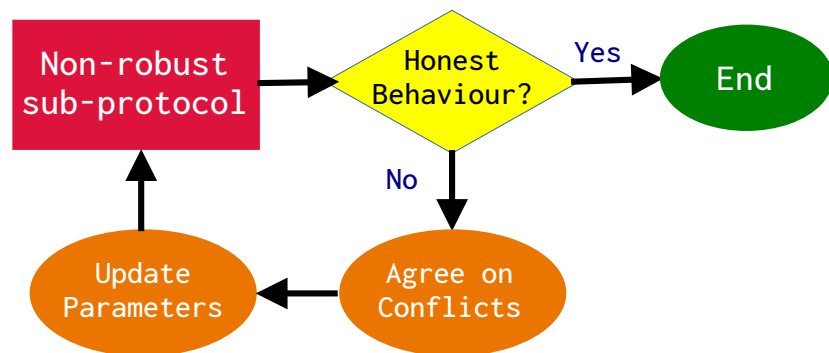
$\{P_1, P_2, P_7\}$ Choice of Adversary

Updated Parameters

$$\mathcal{P} = \{P_3, P_4, P_5, P_6\}$$

Flaw in [KSR02]

Player Elimination Framework [HMP00]



Example Execution

Partyset $\mathcal{P} = \{P_1, P_2, P_3, P_4, P_5, P_6, P_7\}$

Adversary Structure satisfying $\mathcal{Q}^{(4)}$

$$\mathcal{Z} = \{\{P_1, P_2\}, \{P_1, P_3\}, \{P_1, P_4\}, \{P_1, P_5, P_6\}, \{P_7\}\}$$

Conflict Set

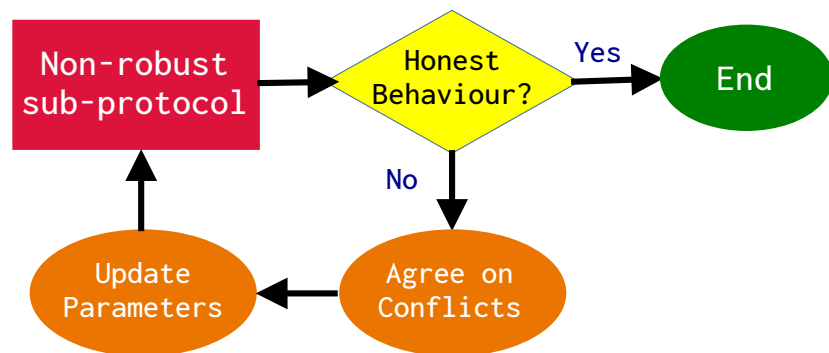
$\{P_1, P_2, P_7\}$ Choice of Adversary

Updated Parameters

$\mathcal{P} = \{P_3, P_4, P_5, P_6\}$ \mathcal{Z} remains same

Flaw in [KSR02]

Player Elimination Framework [HMP00]



Example Execution

Partyset $\mathcal{P} = \{P_1, P_2, P_3, P_4, P_5, P_6, P_7\}$

Adversary Structure satisfying $\mathcal{Q}^{(4)}$

$$\mathcal{Z} = \{\{P_1, P_2\}, \{P_1, P_3\}, \{P_1, P_4\}, \{P_1, P_5, P_6\}, \{P_7\}\}$$

Conflict Set

$\{P_1, P_2, P_7\}$ Choice of Adversary

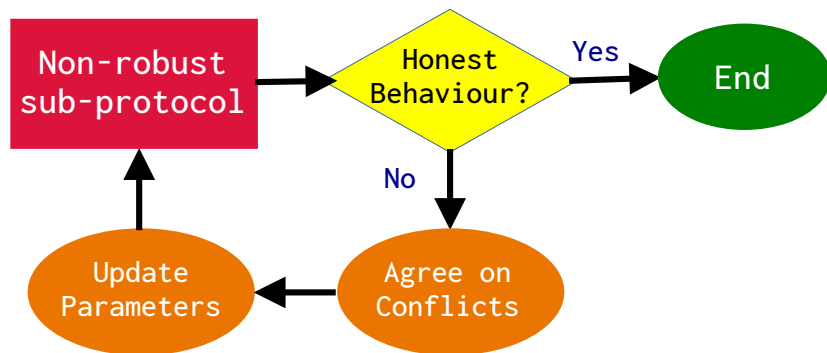
Updated Parameters

$\mathcal{P} = \{P_3, P_4, P_5, P_6\}$ \mathcal{Z} remains same

$$\mathcal{P} \subseteq \{P_1, P_3\} \cup \{P_1, P_4\} \cup \{P_1, P_5, P_6\}$$

Flaw in [KSR02]

Player Elimination Framework [HMP00]



Example Execution

Partyset $\mathcal{P} = \{P_1, P_2, P_3, P_4, P_5, P_6, P_7\}$

Adversary Structure satisfying $Q^{(4)}$

$$\mathcal{Z} = \{\{P_1, P_2\}, \{P_1, P_3\}, \{P_1, P_4\}, \{P_1, P_5, P_6\}, \{P_7\}\}$$

Conflict Set

$\{P_1, P_2, P_7\}$ Choice of Adversary

Updated Parameters

$\mathcal{P} = \{P_3, P_4, P_5, P_6\}$ \mathcal{Z} remains same

$$\mathcal{P} \subseteq \{P_1, P_3\} \cup \{P_1, P_4\} \cup \{P_1, P_5, P_6\} \quad Q^{(3)} \text{ Fails}$$

Verifiable Secret-Sharing

Verifiable Secret-Sharing

Dealer



Verifiable Secret-Sharing

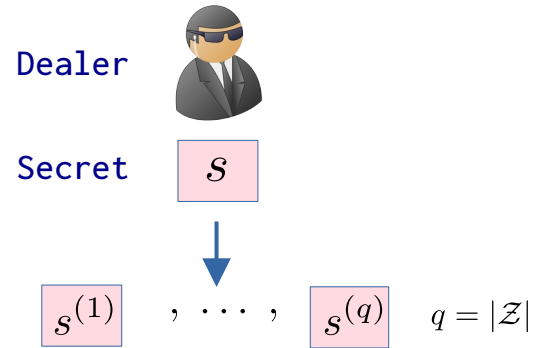
Dealer



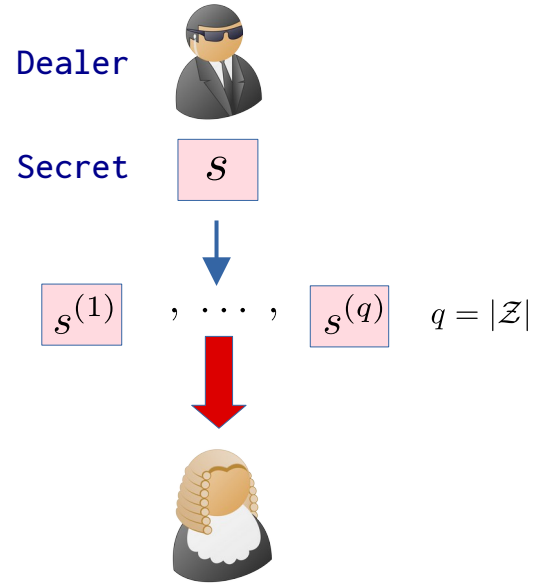
Secret



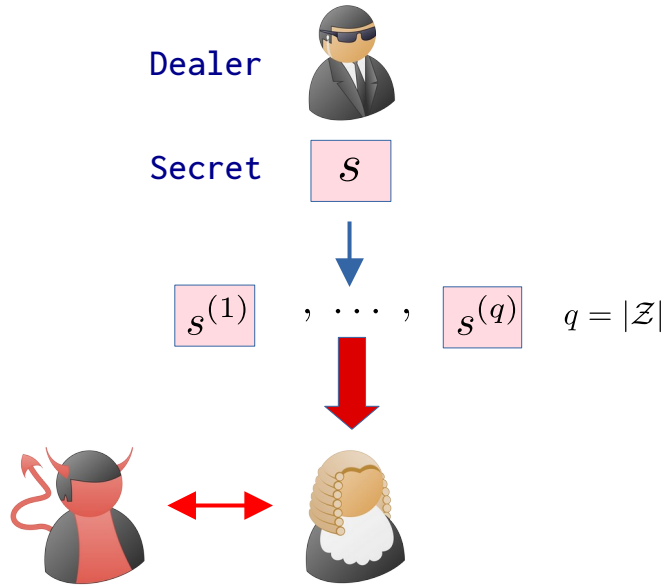
Verifiable Secret-Sharing



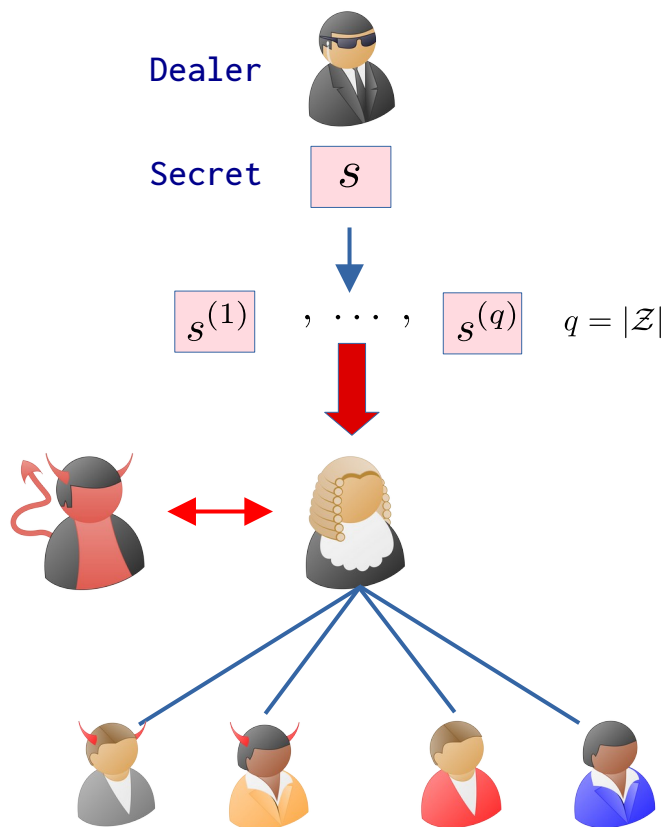
Verifiable Secret-Sharing



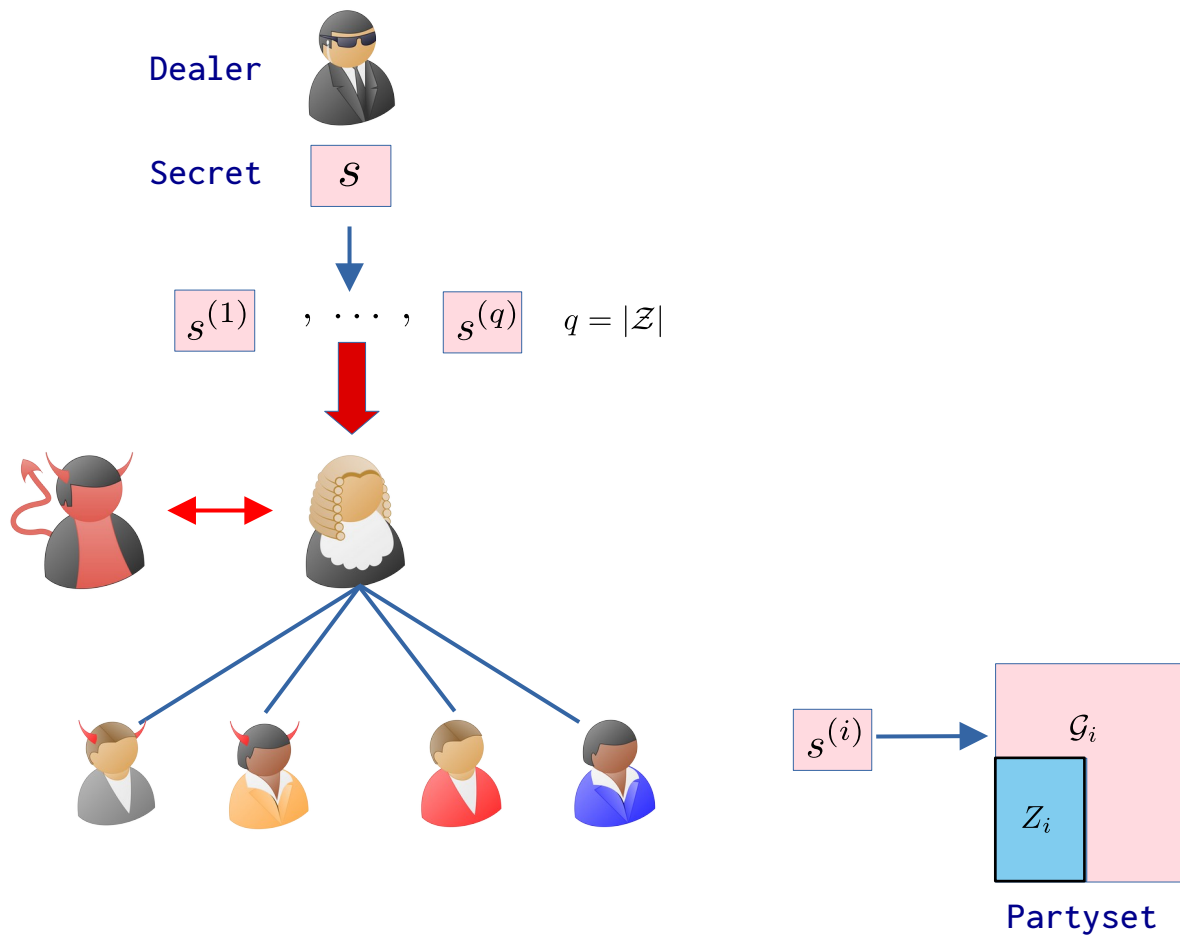
Verifiable Secret-Sharing



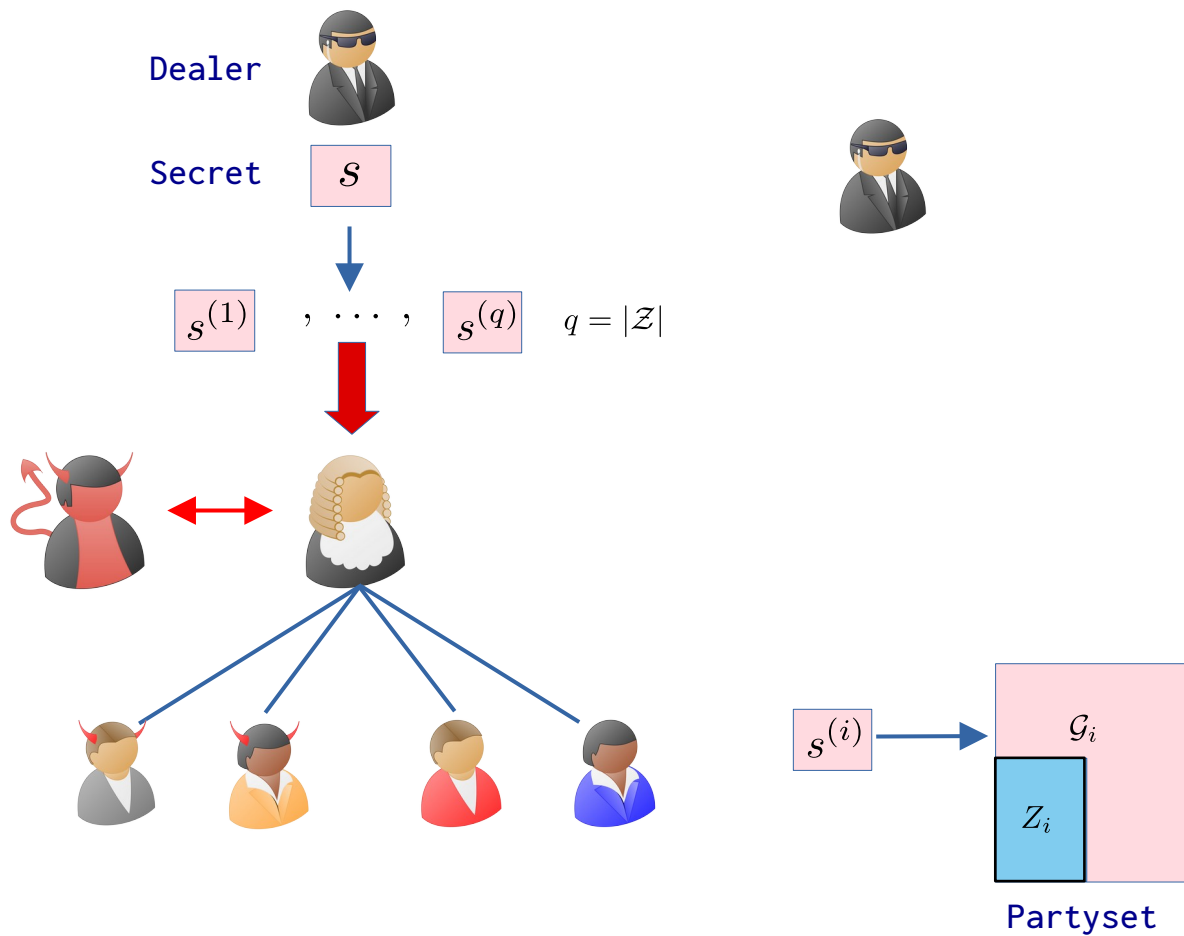
Verifiable Secret-Sharing



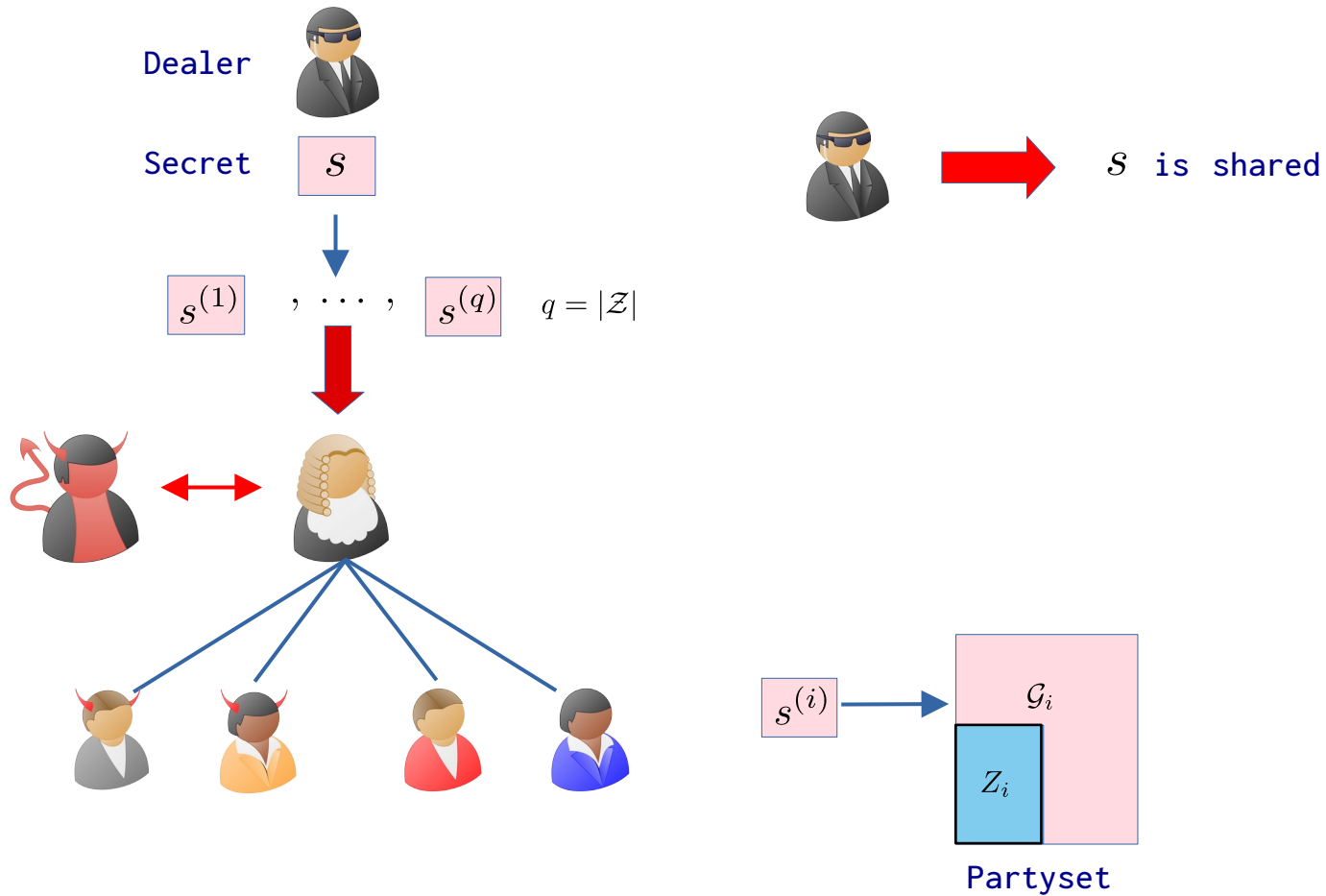
Verifiable Secret-Sharing



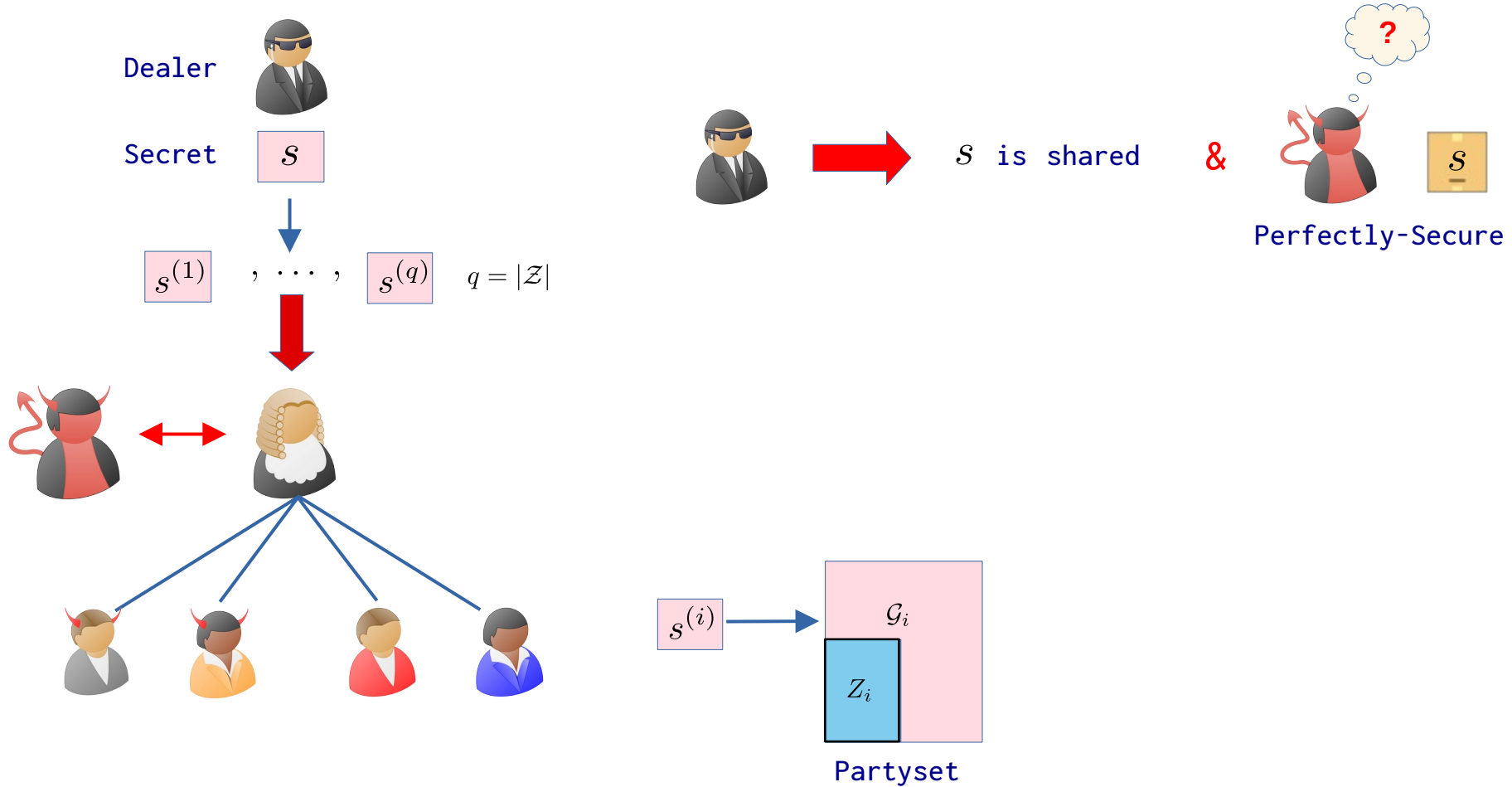
Verifiable Secret-Sharing



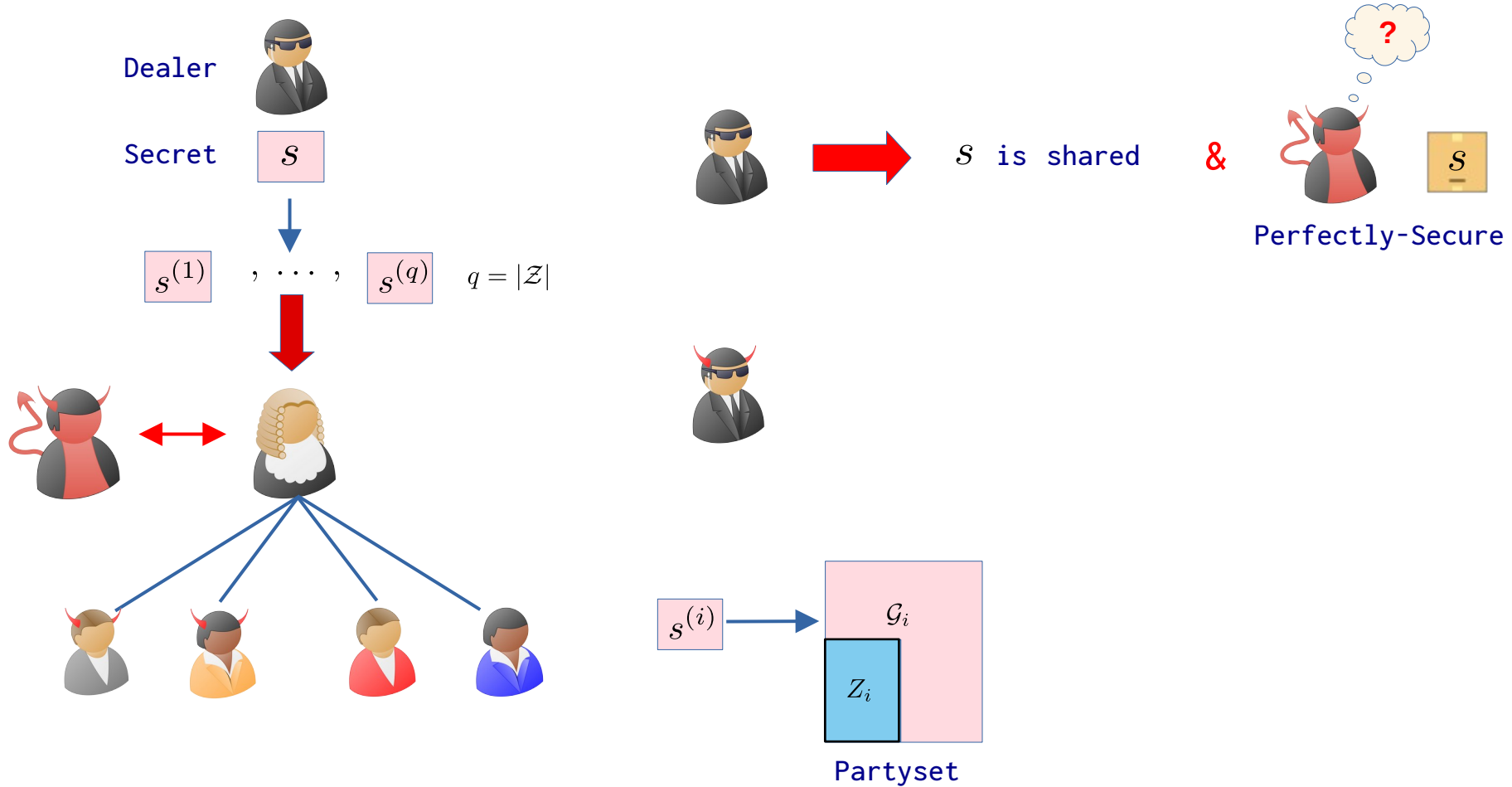
Verifiable Secret-Sharing



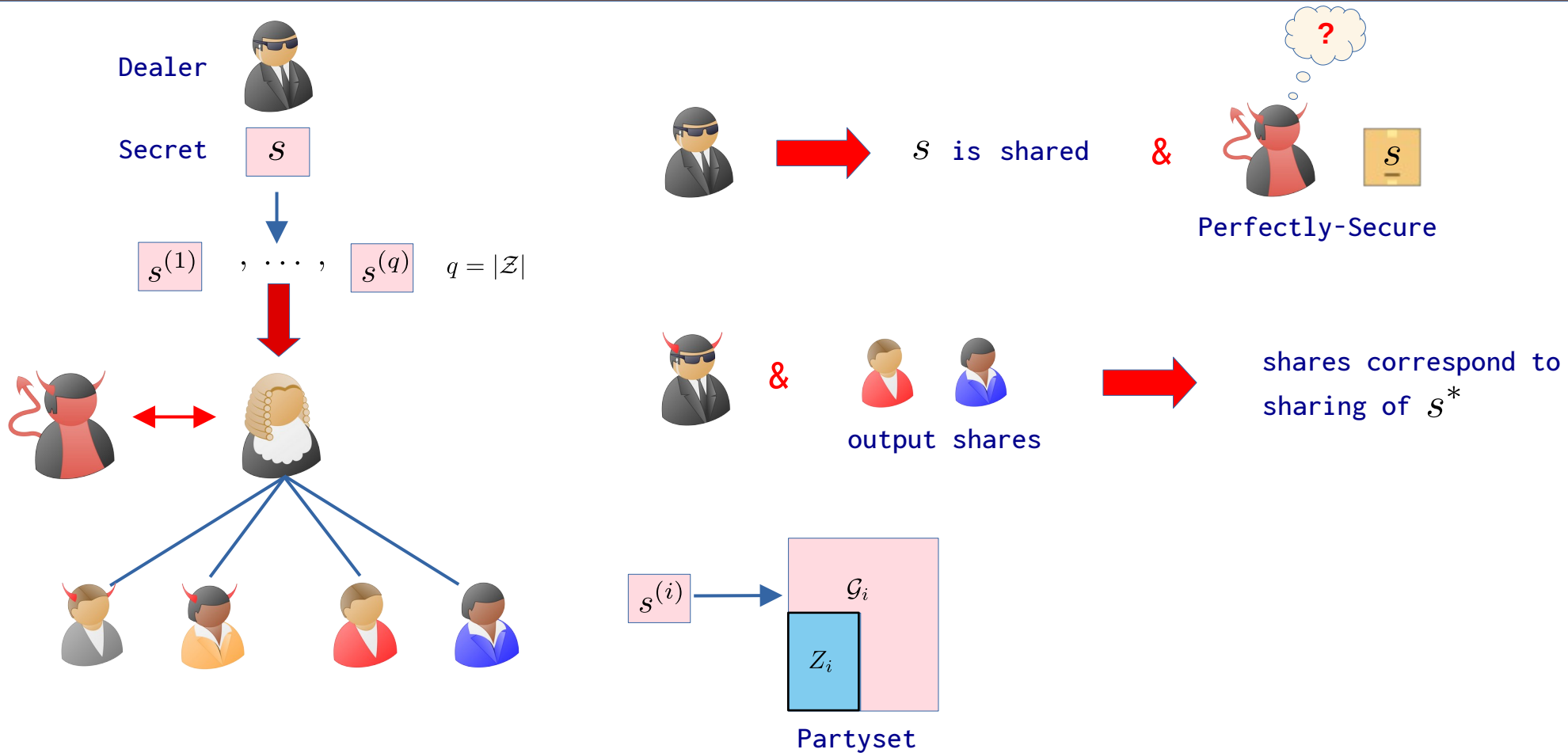
Verifiable Secret-Sharing



Verifiable Secret-Sharing



Verifiable Secret-Sharing



Verifiable Secret-Sharing

Verifiable Secret-Sharing

Verifiable Secret-Sharing

$$\mathcal{Z} = \{\{P_1, P_2\}, \{P_1, P_3\}, \{P_1, P_4\}, \{P_1, P_5, P_6\}, \{P_7\}\}$$

Verifiable Secret-Sharing

$$\mathcal{Z} = \{\{P_1, P_2\}, \{P_1, P_3\}, \{P_1, P_4\}, \{P_1, P_5, P_6\}, \{P_7\}\}$$



Dealer

Verifiable Secret-Sharing

$$\mathcal{Z} = \{\{P_1, P_2\}, \{P_1, P_3\}, \{P_1, P_4\}, \{P_1, P_5, P_6\}, \{P_7\}\}$$



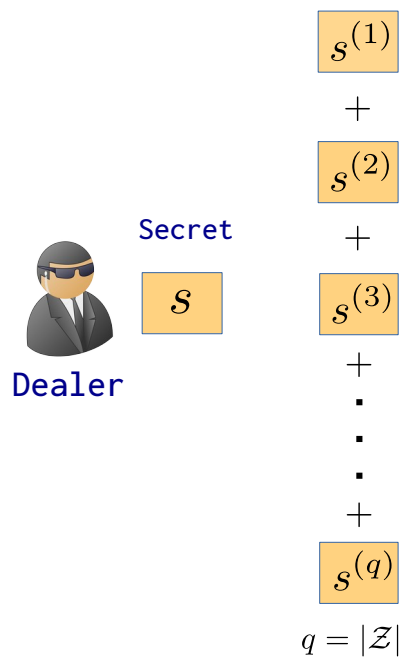
Secret

s

Dealer

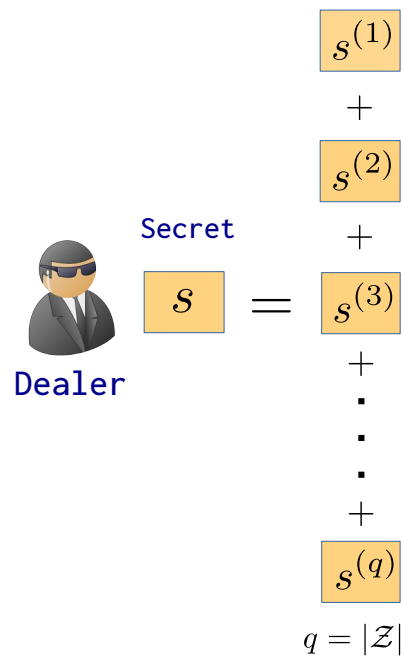
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$$\mathcal{Z} = \{\{P_1, P_2\}, \{P_1, P_3\}, \{P_1, P_4\}, \{P_1, P_5, P_6\}, \{P_7\}\}$$



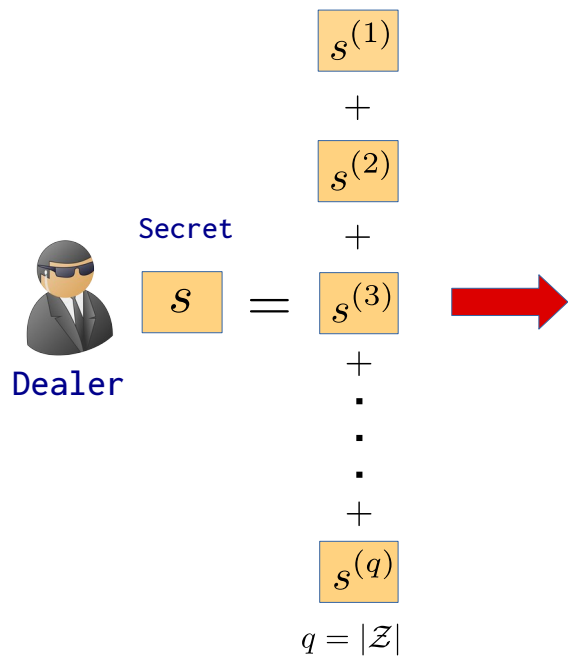
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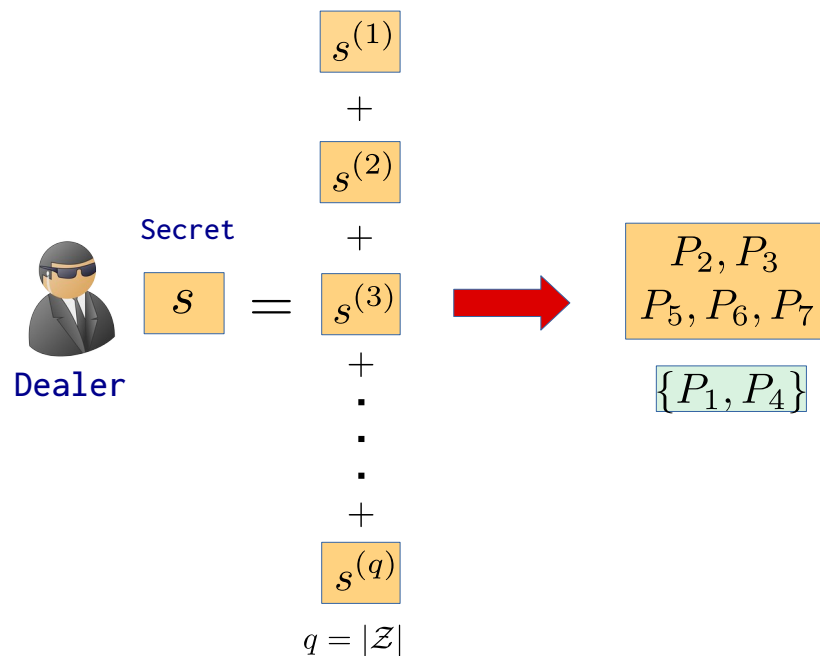
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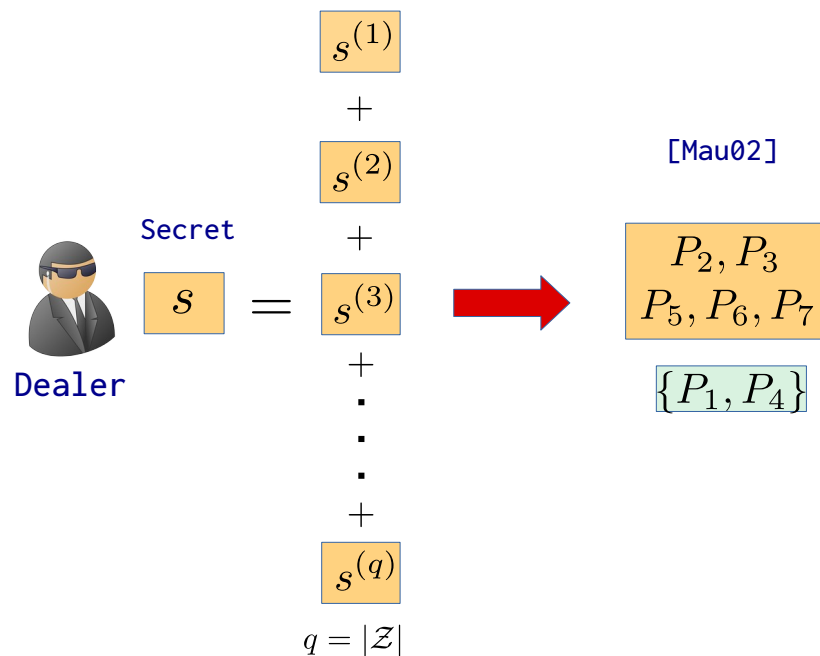
Verifiable Secret-Sharing

$$\mathcal{Z} = \{\{P_1, P_2\}, \{P_1, P_3\}, \{P_1, P_4\}, \{P_1, P_5, P_6\}, \{P_7\}\}$$



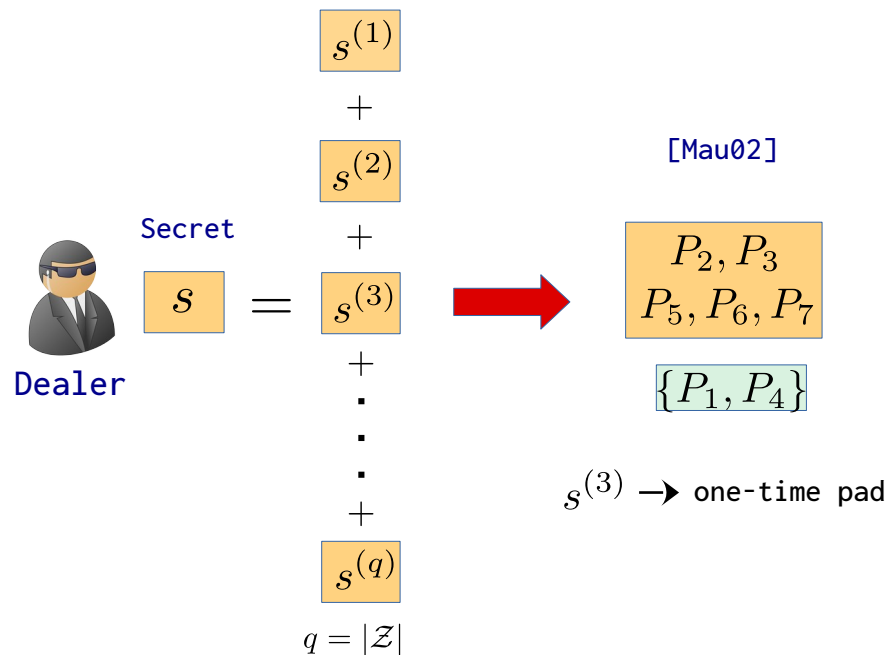
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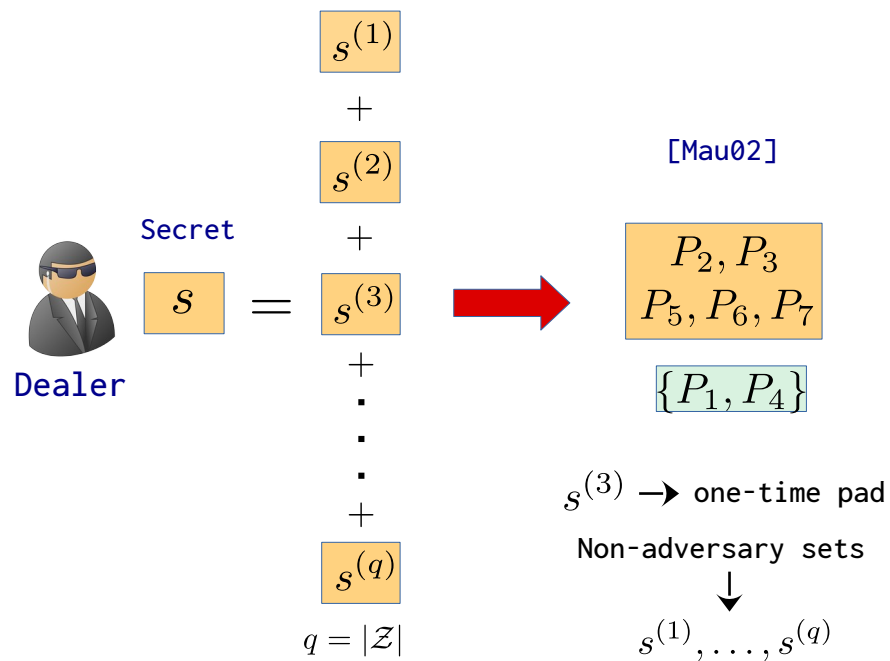
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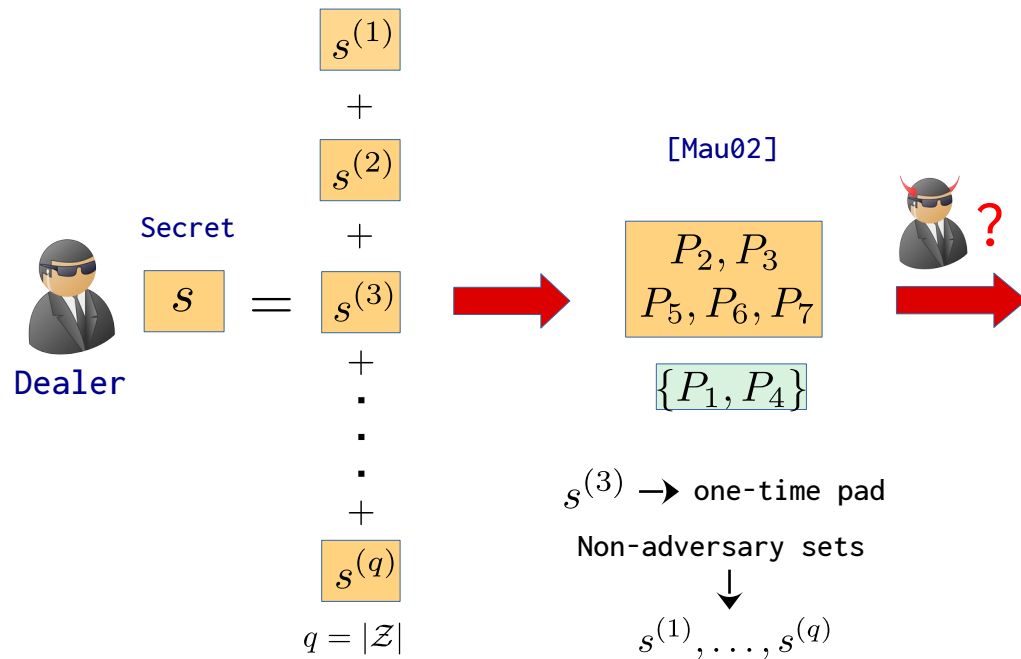
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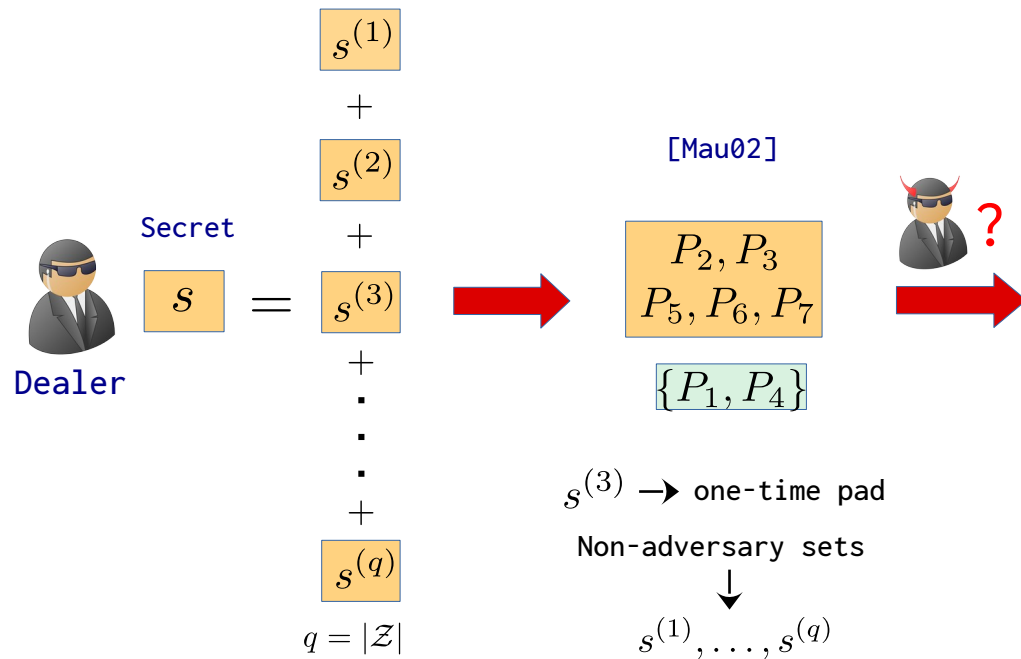
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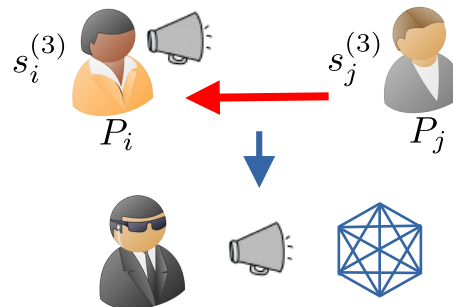
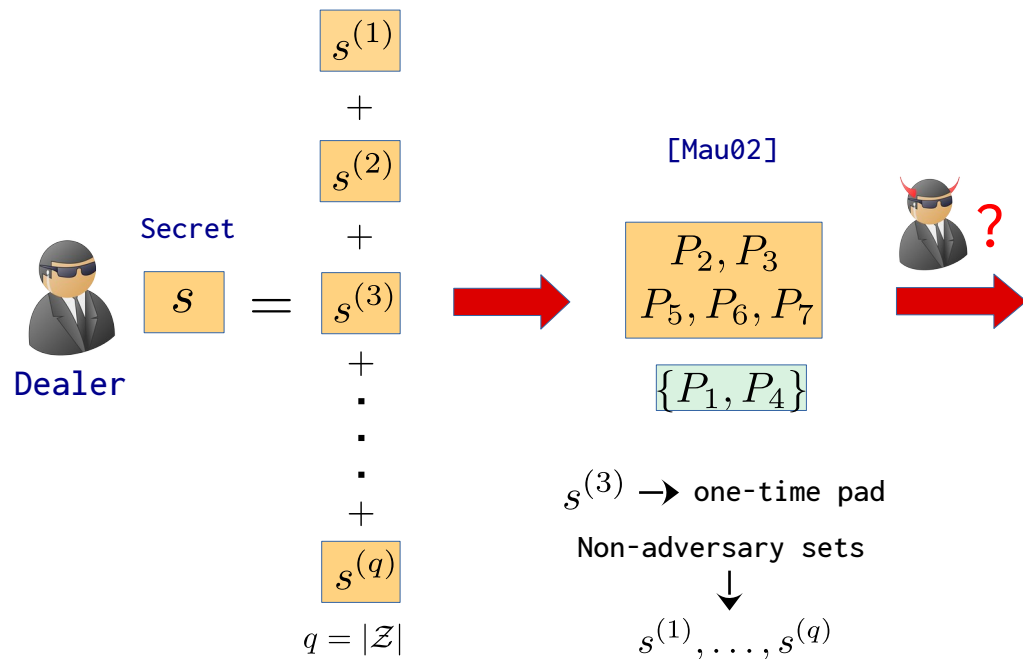
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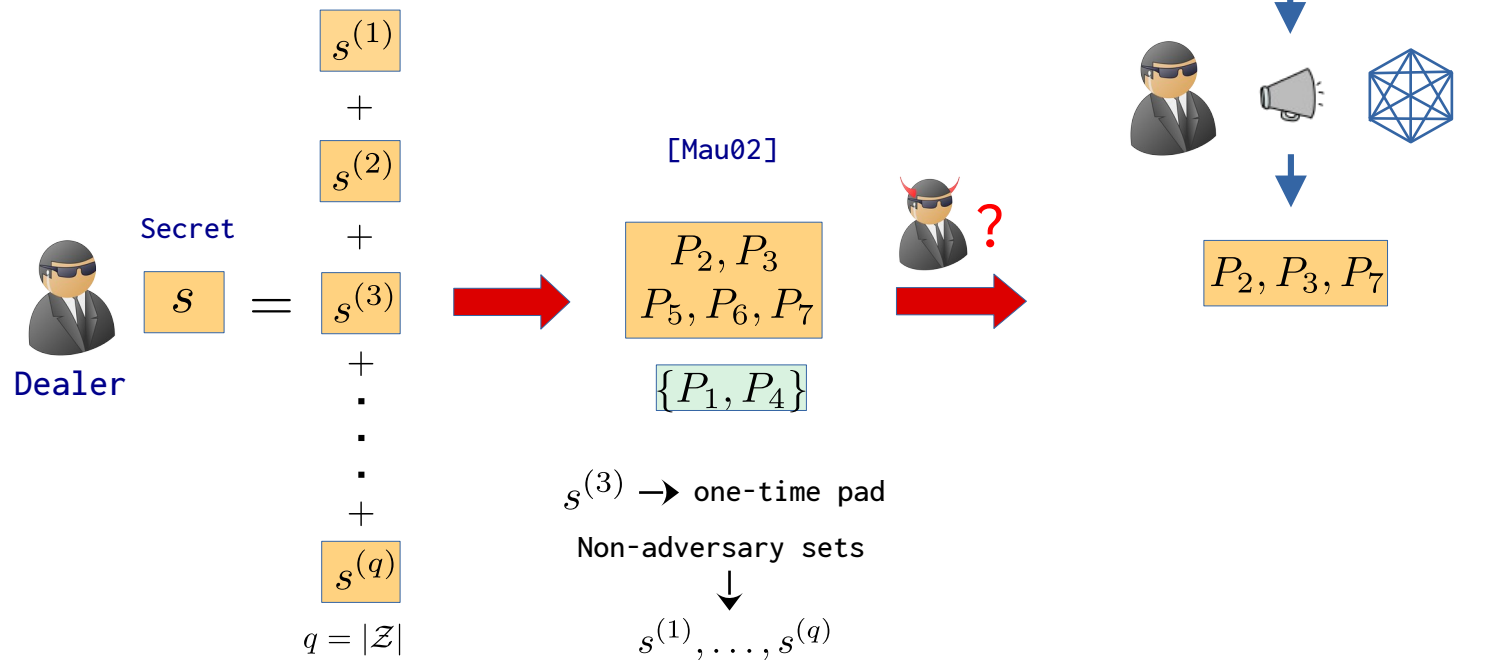
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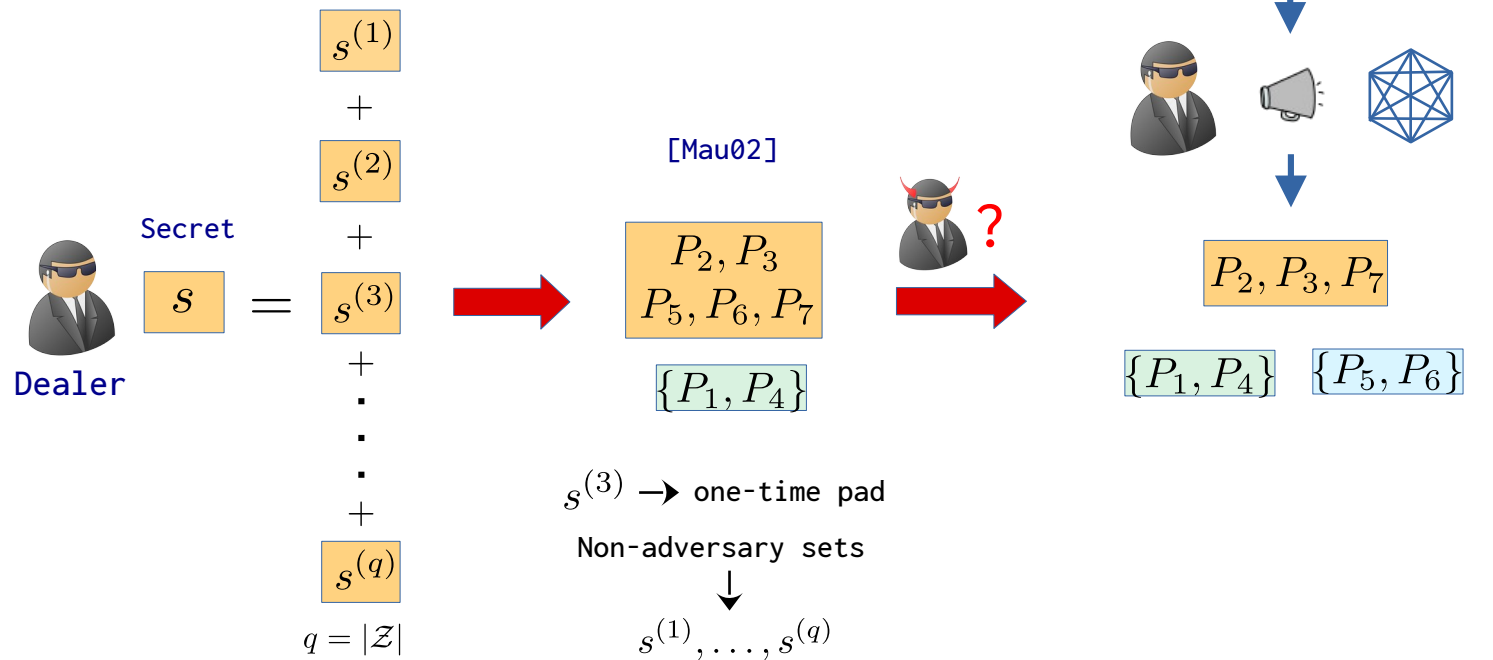
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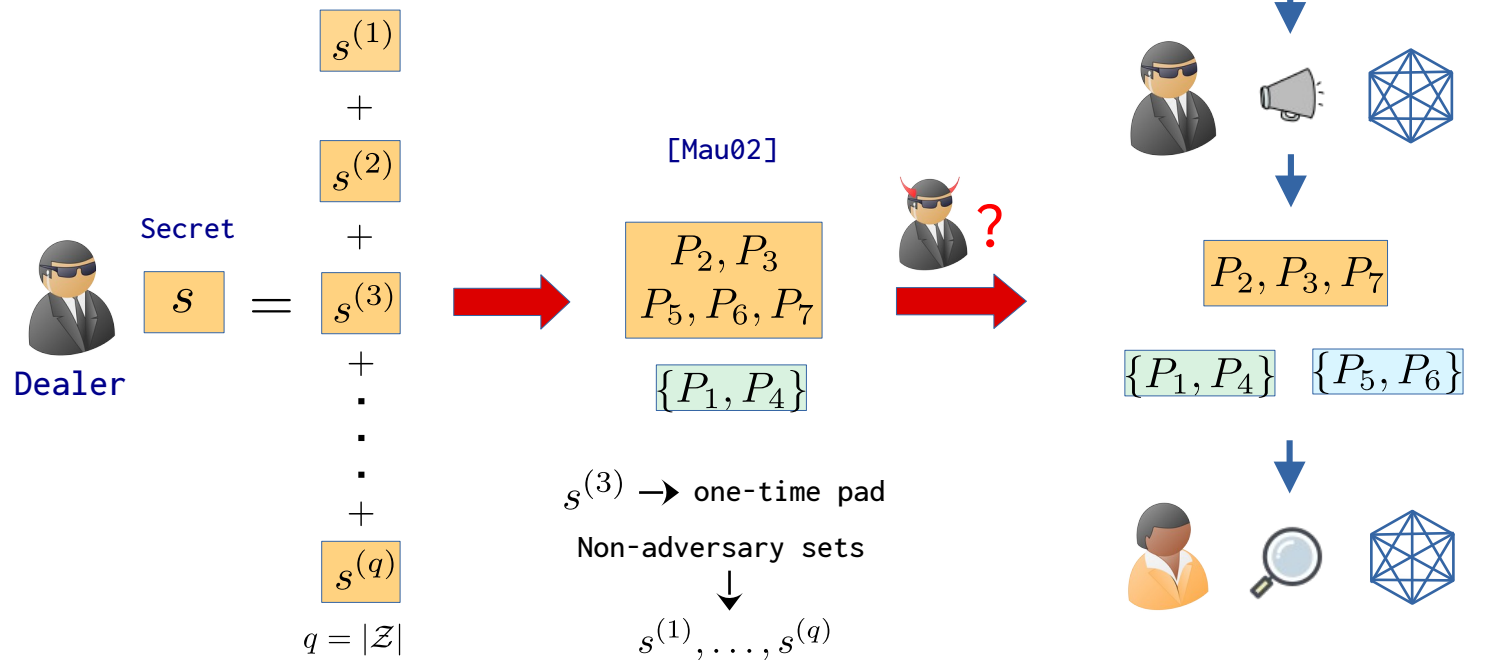
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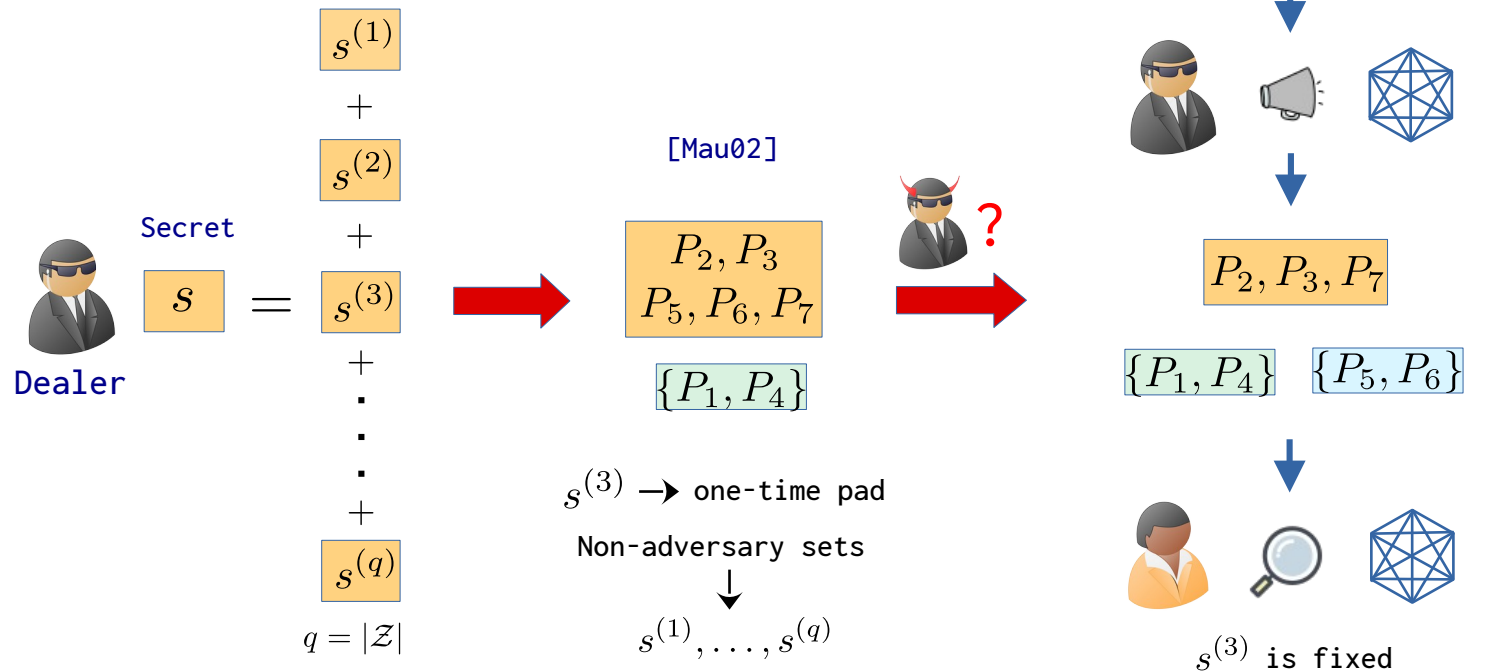
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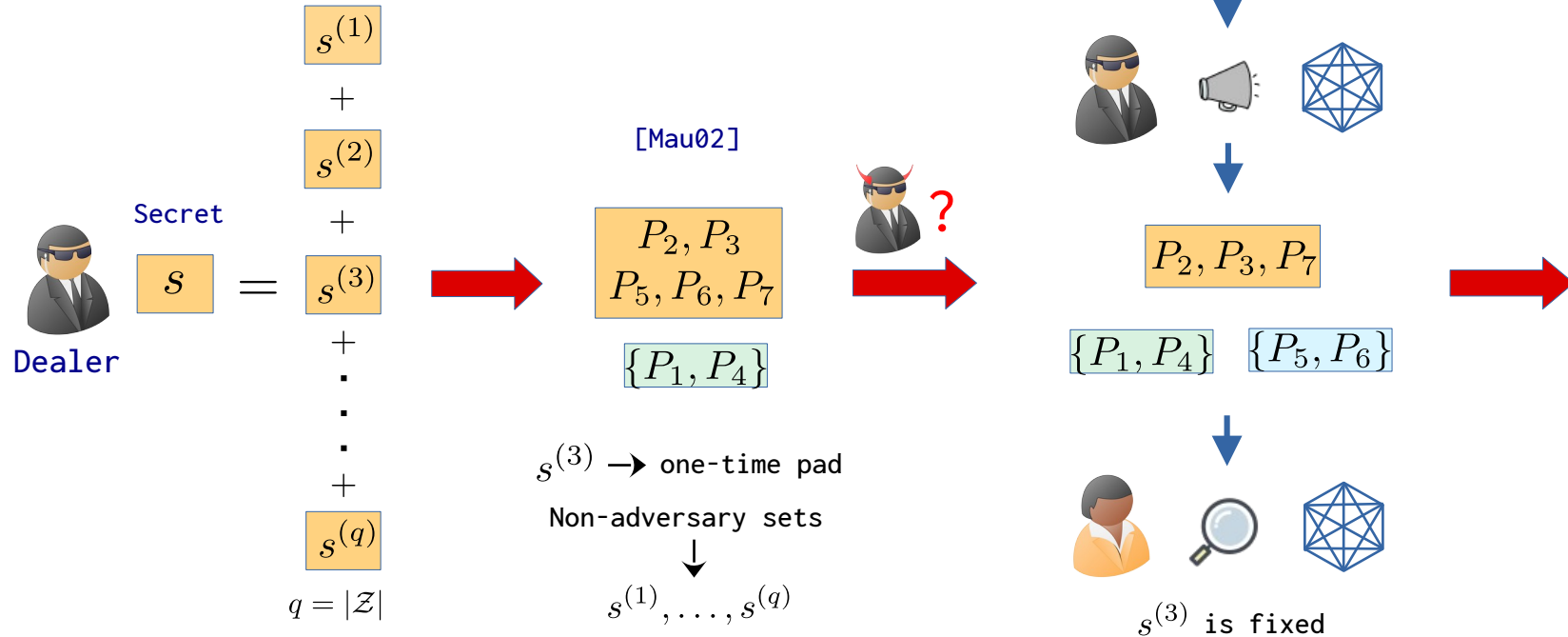
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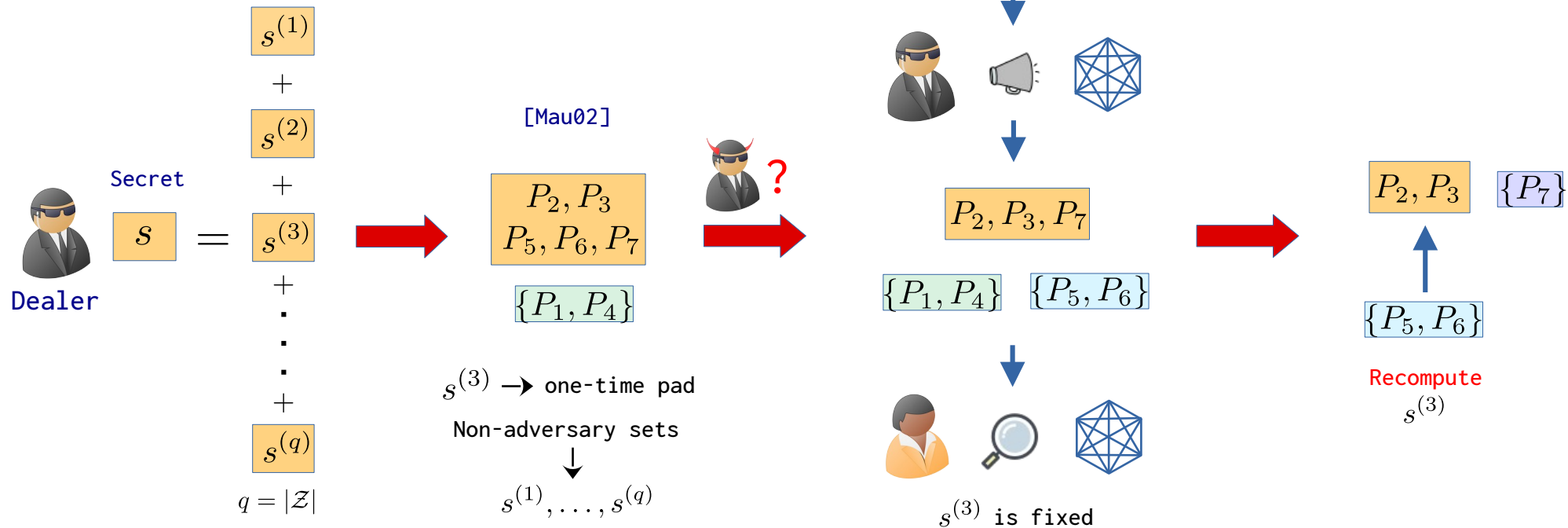
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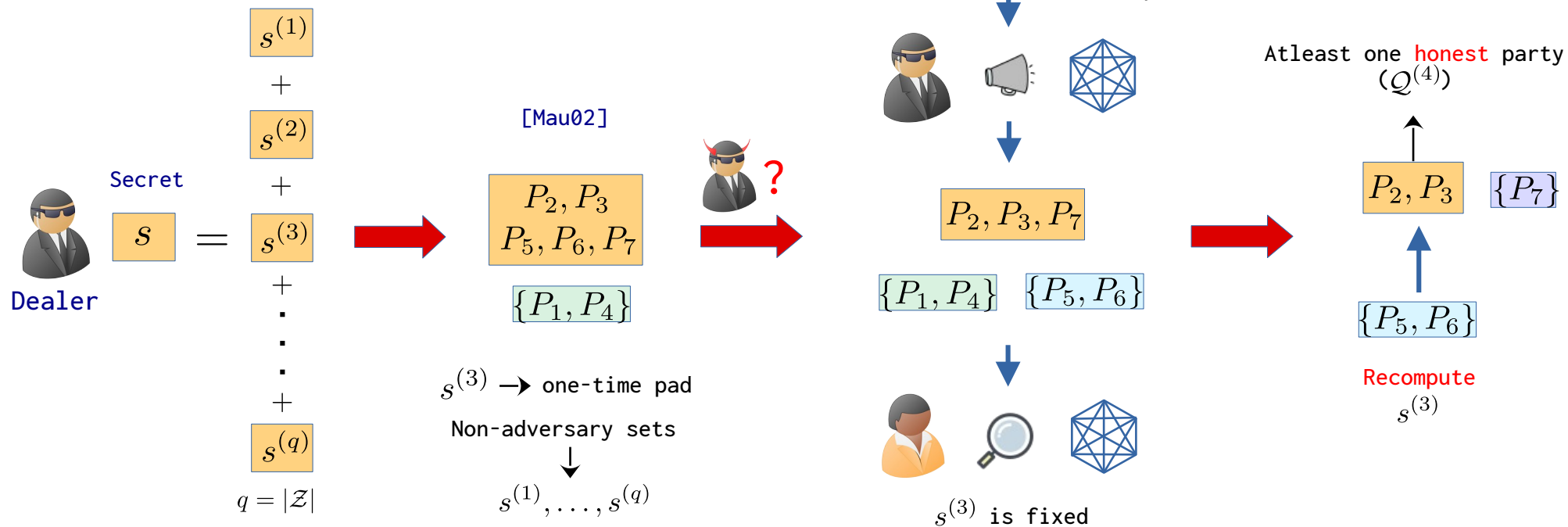
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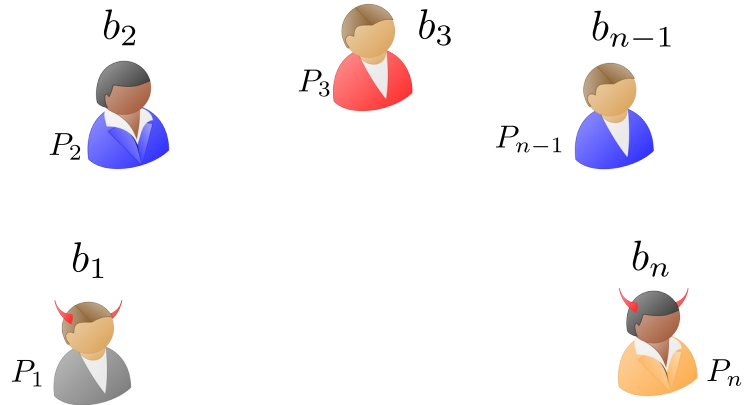
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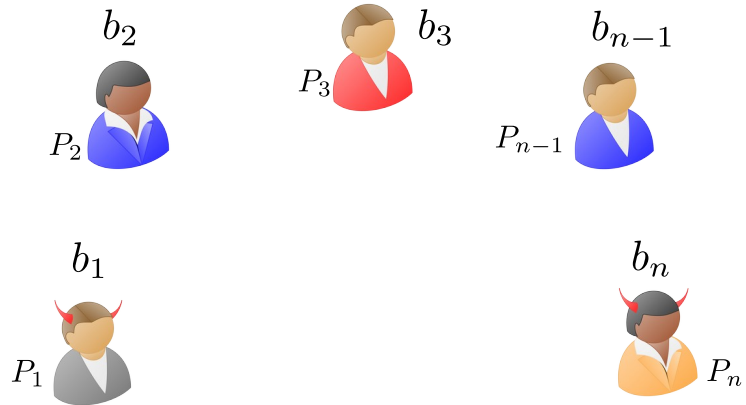
Asynchronous Byzantine Agreement (ABA)

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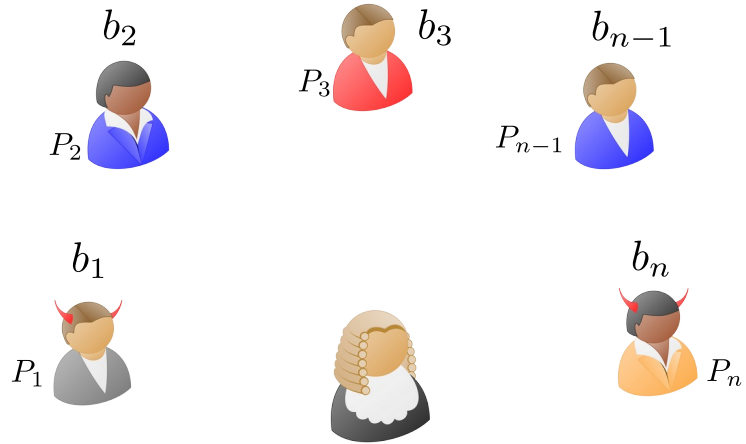
Asynchronous Byzantine Agreement (ABA)

Agree on a common bit



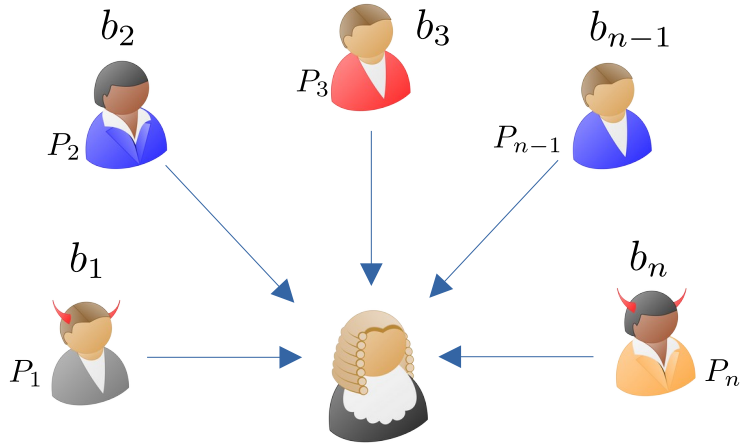
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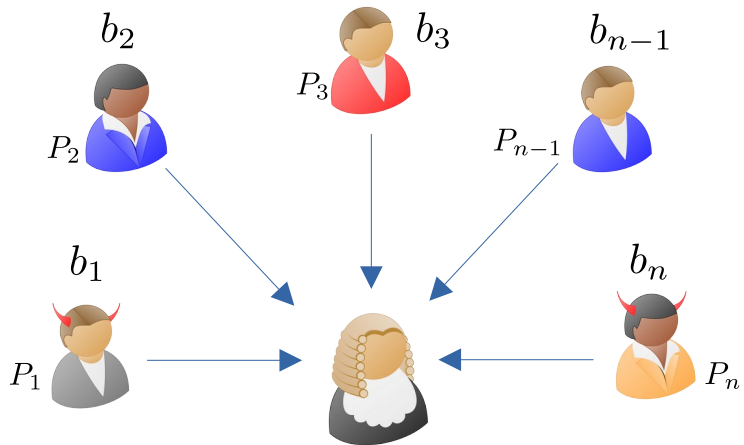
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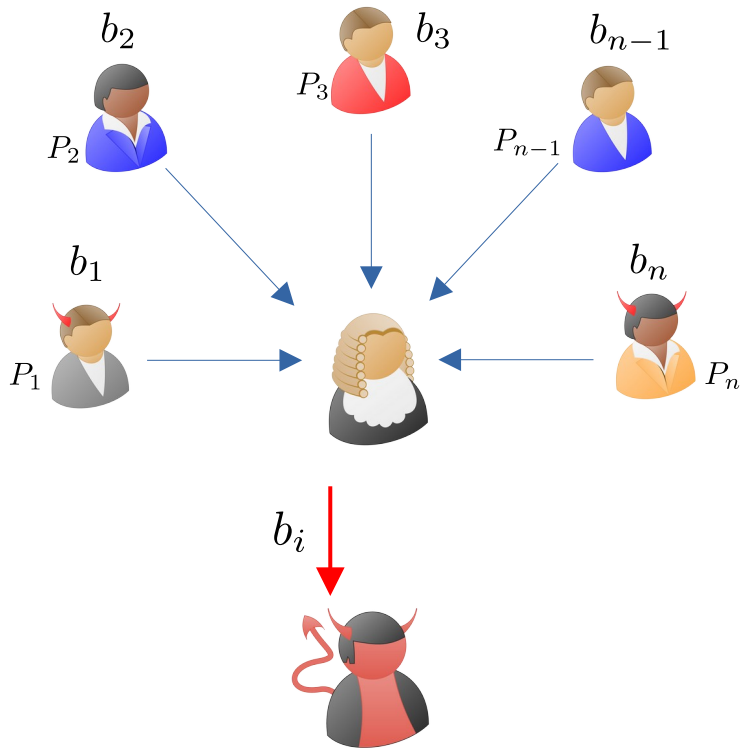
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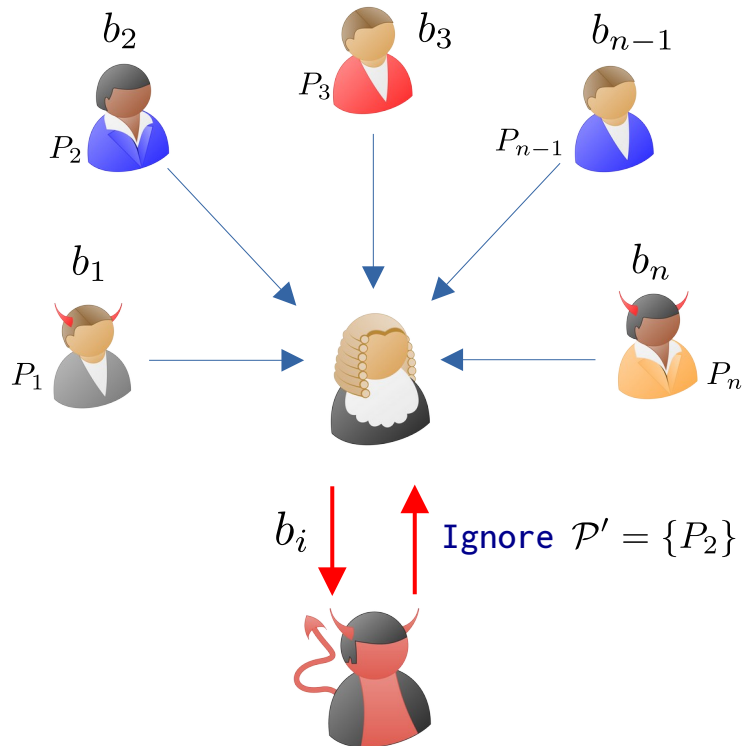
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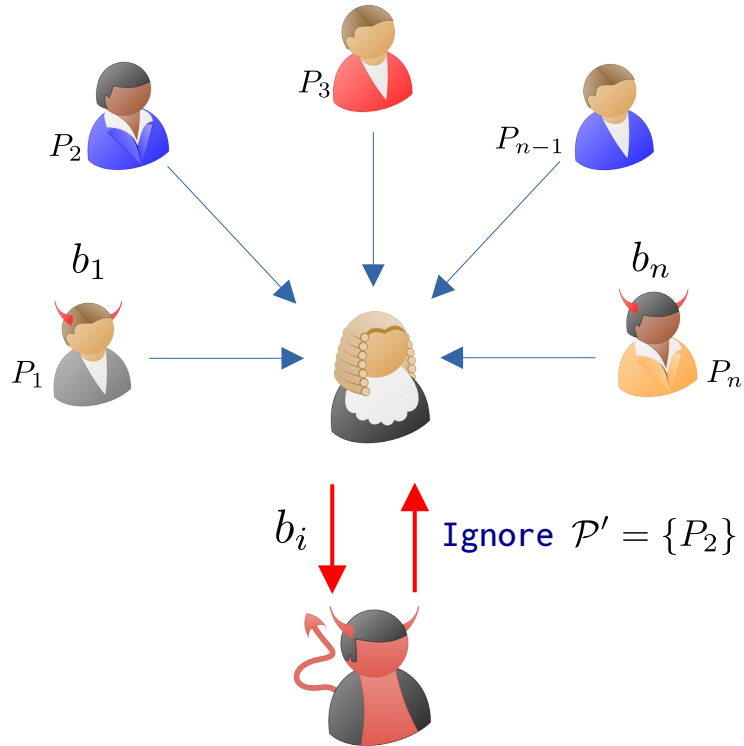
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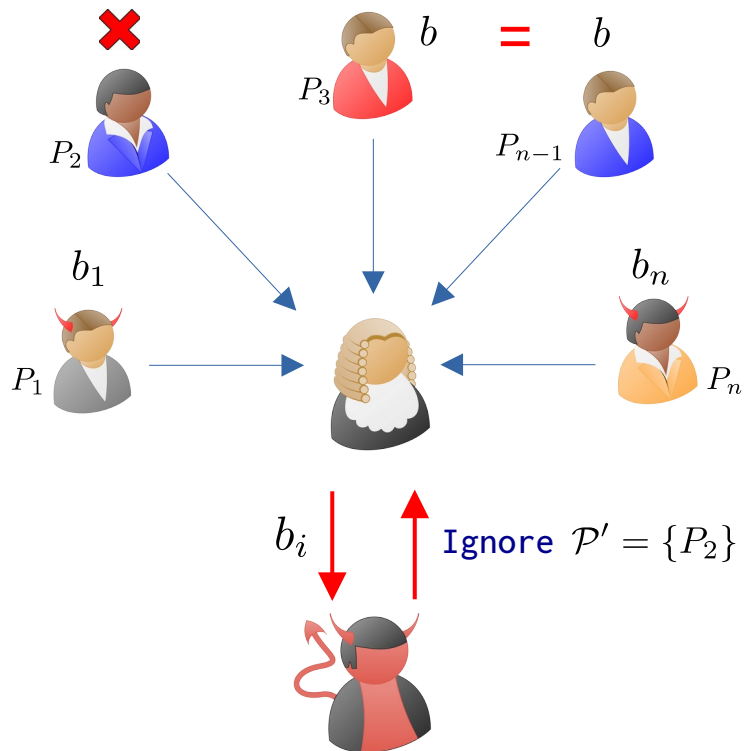
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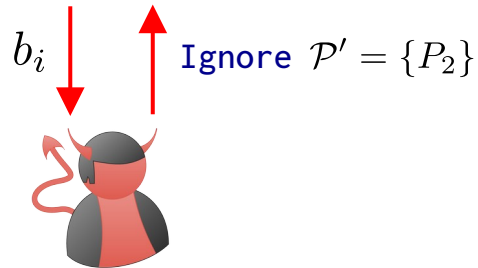
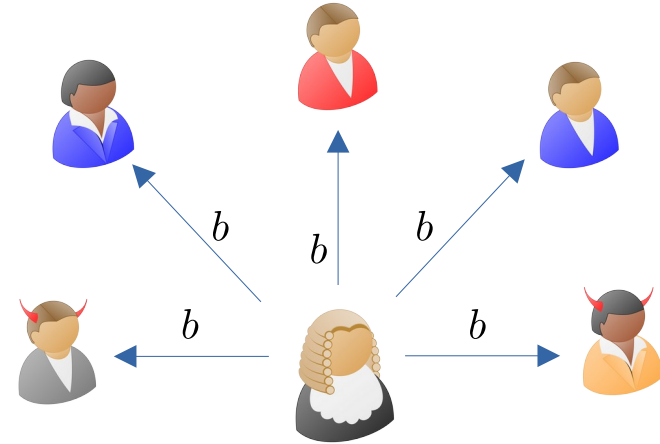
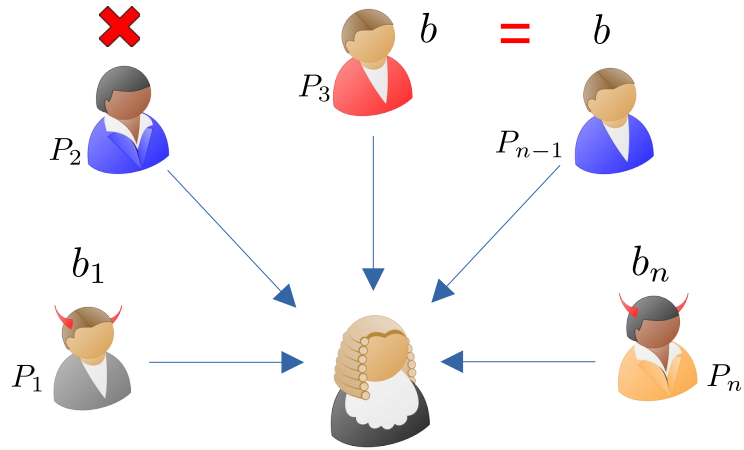
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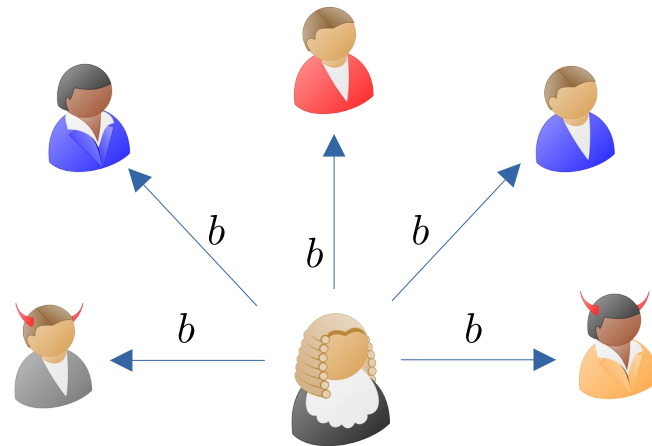
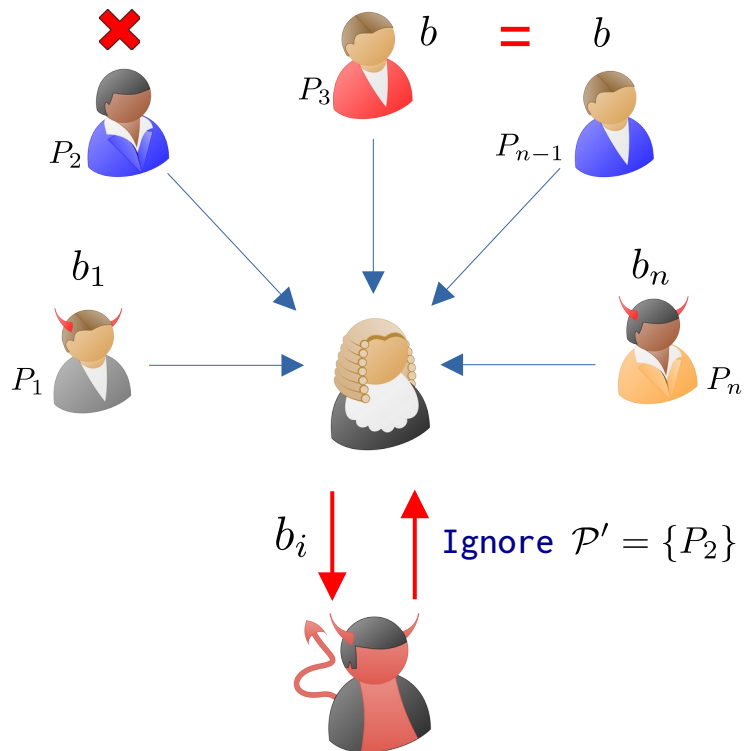
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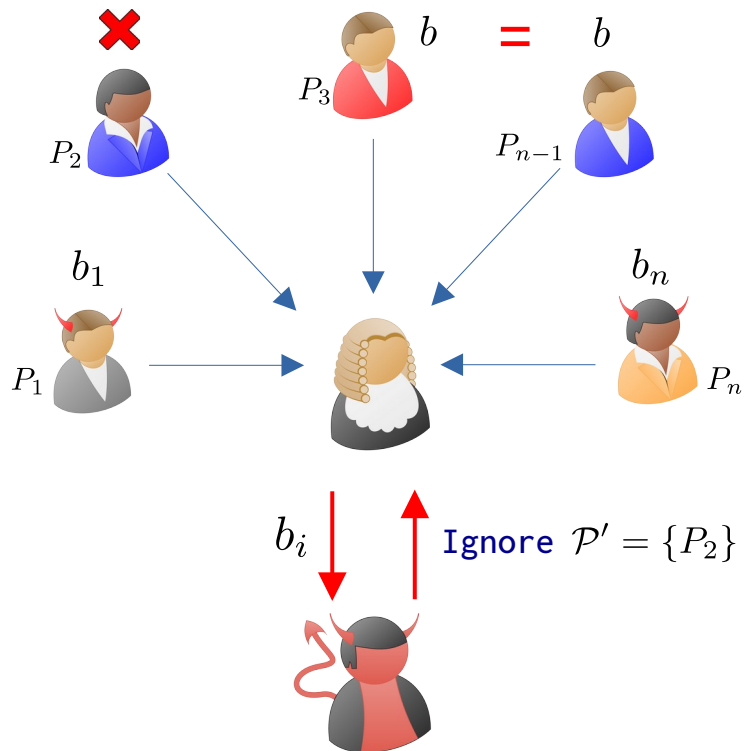
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Validity

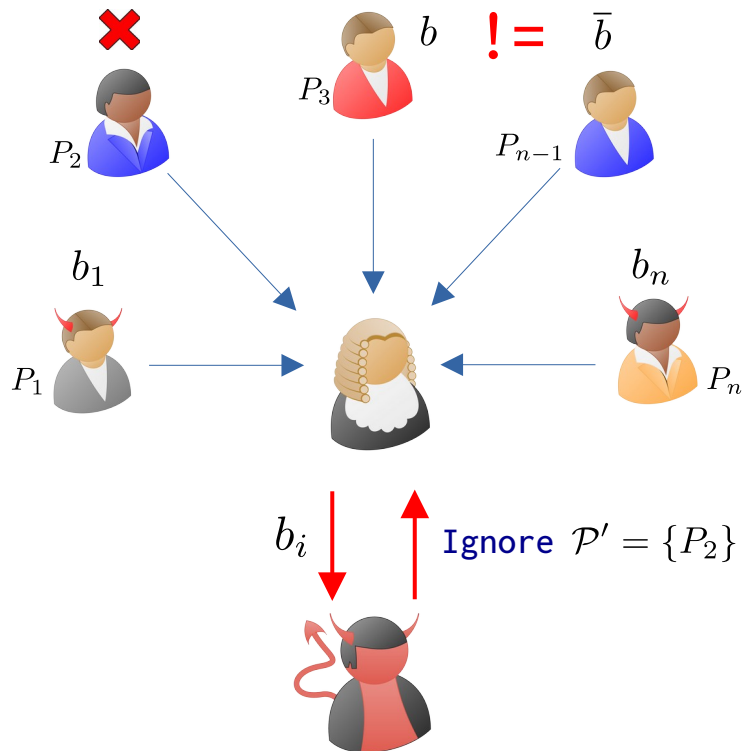
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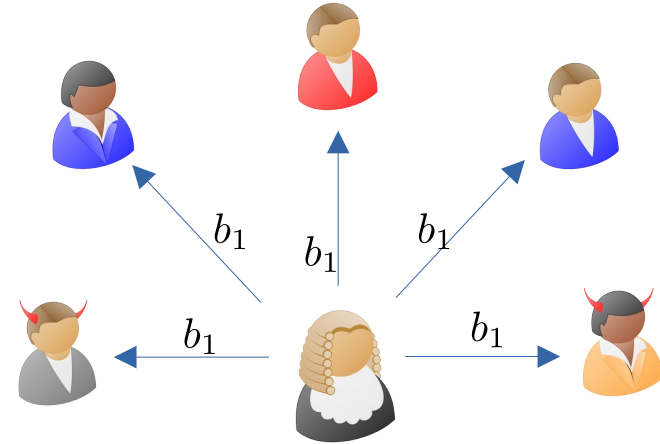
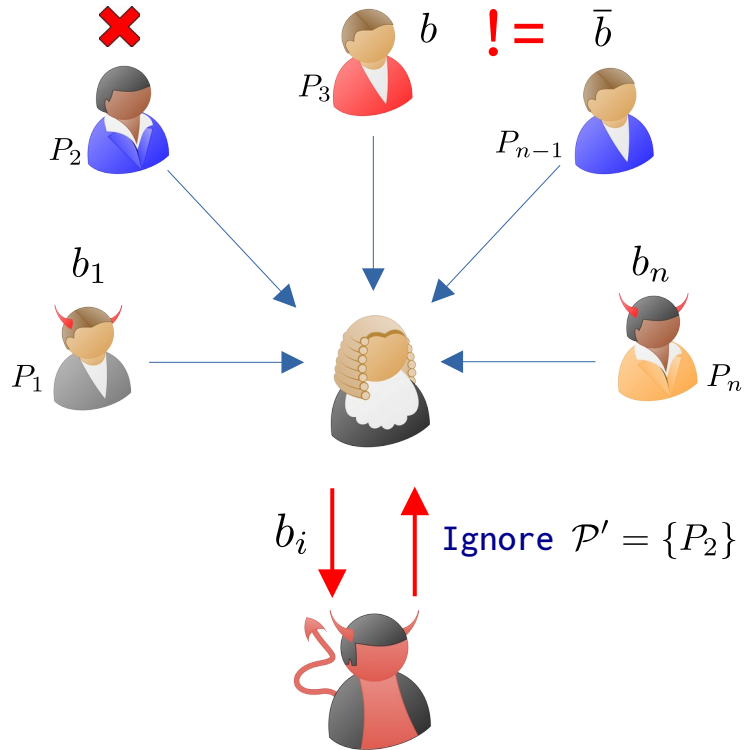
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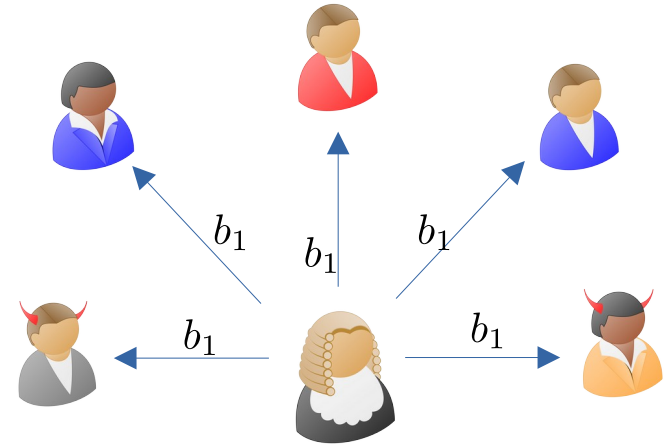
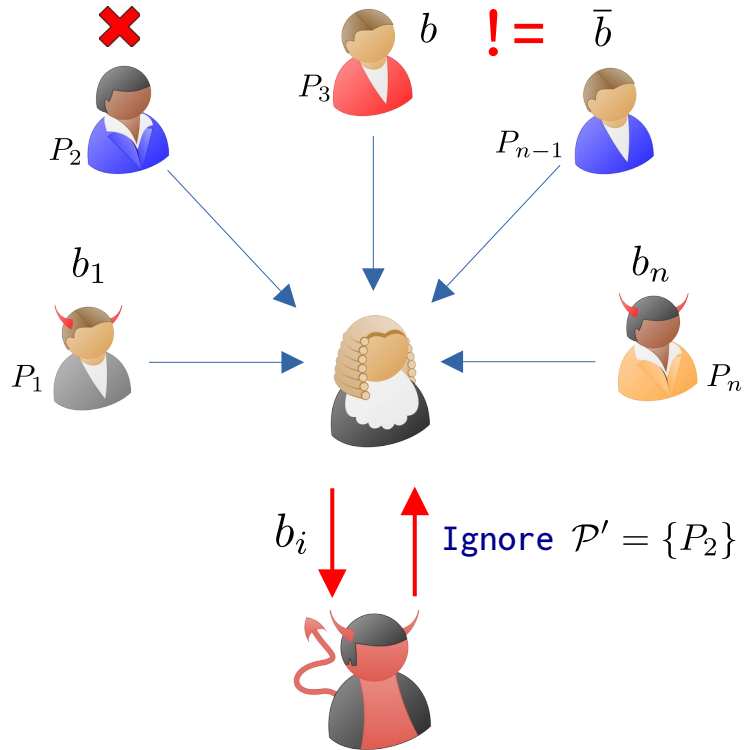
Asynchronous Byzantine Agreement (ABA)

Agree on a common bit



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Agreement

Asynchronous Byzantine Agreement (ABA)

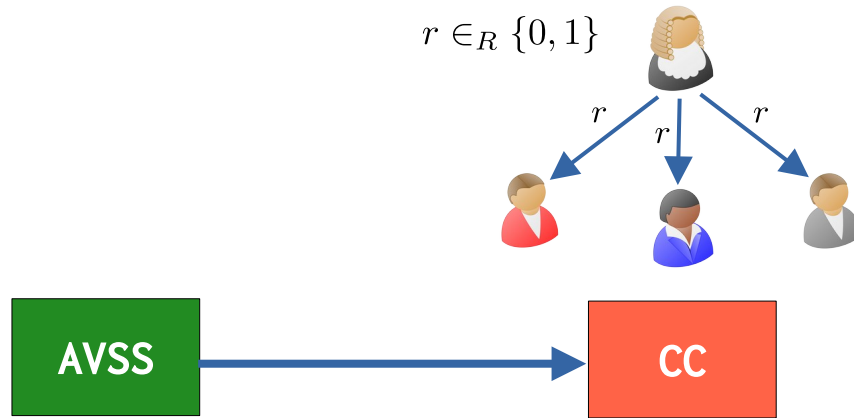
Asynchronous Byzantine Agreement (ABA)

AVSS

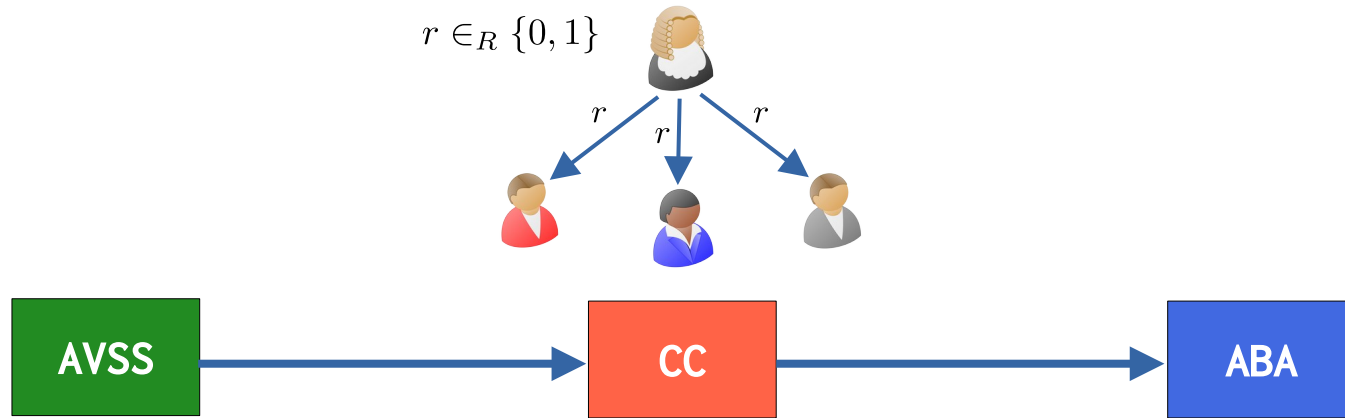
Asynchronous Byzantine Agreement (ABA)



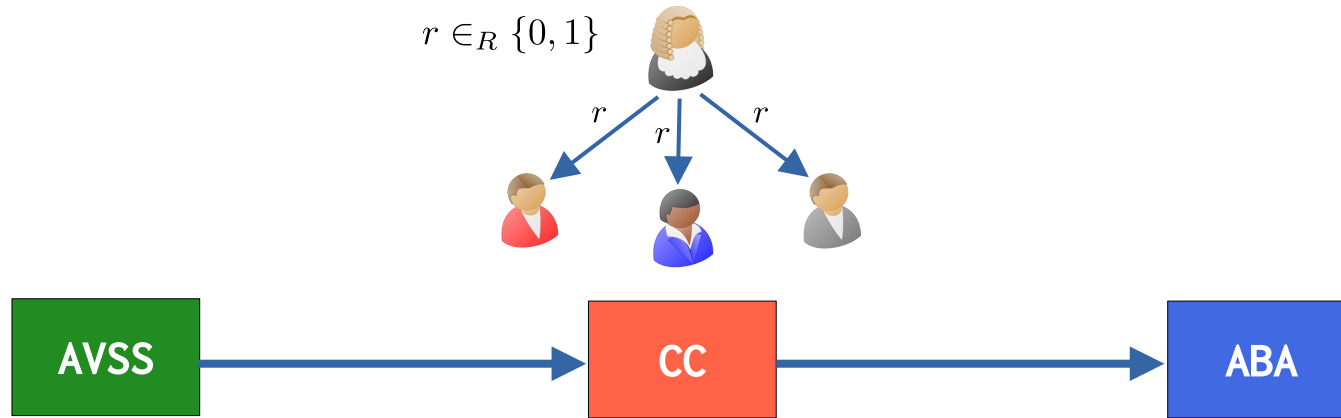
Asynchronous Byzantine Agreement (ABA)



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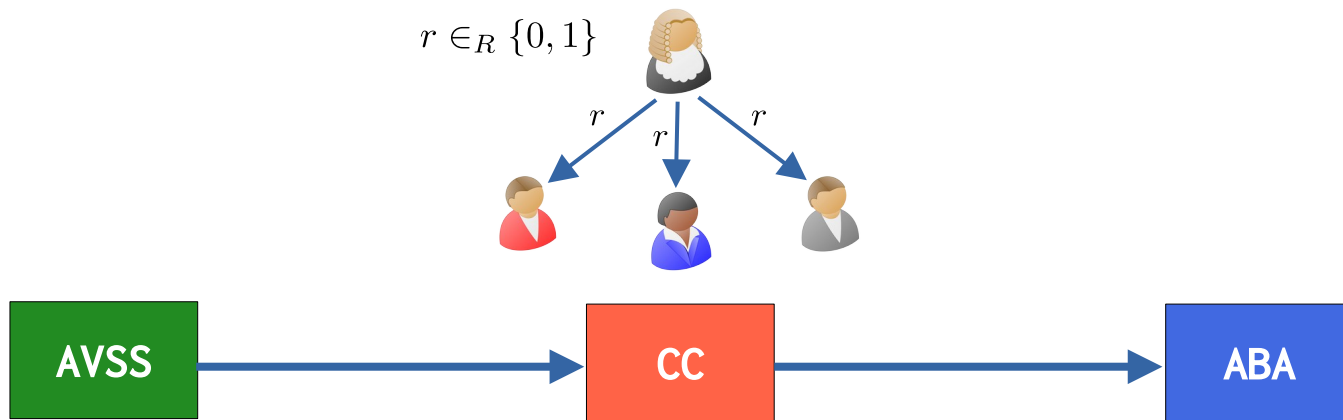


Asynchronous Byzantine Agreement (ABA)



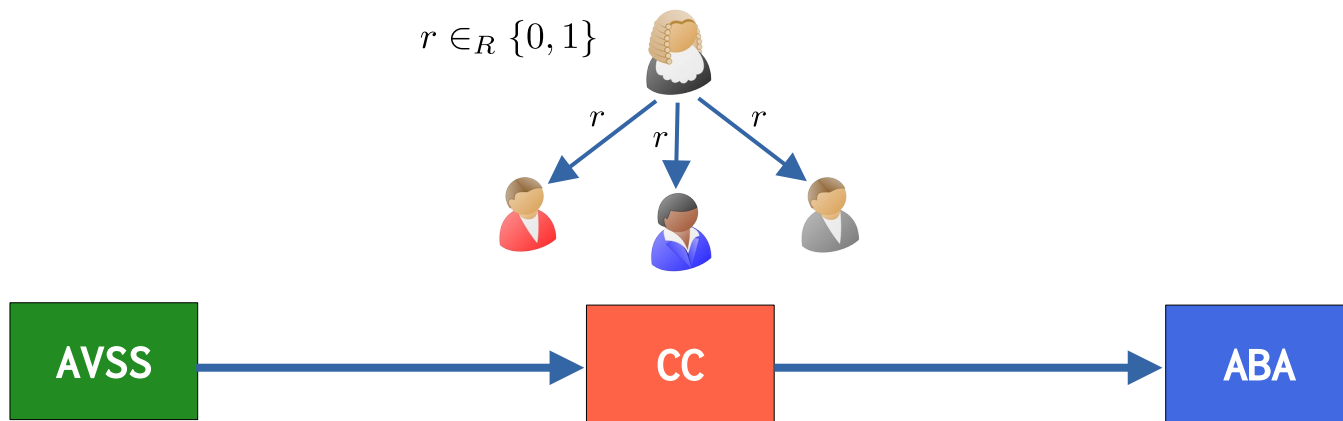
- Perfectly-Secure

Asynchronous Byzantine Agreement (ABA)



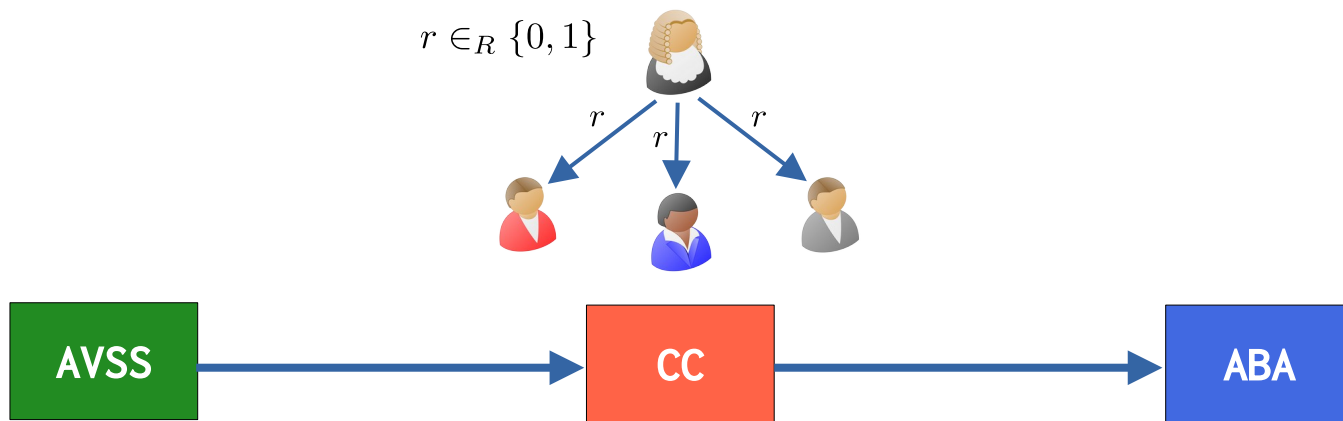
- Perfectly-Secure
- Generalization of [CR93]

Asynchronous Byzantine Agreement (ABA)



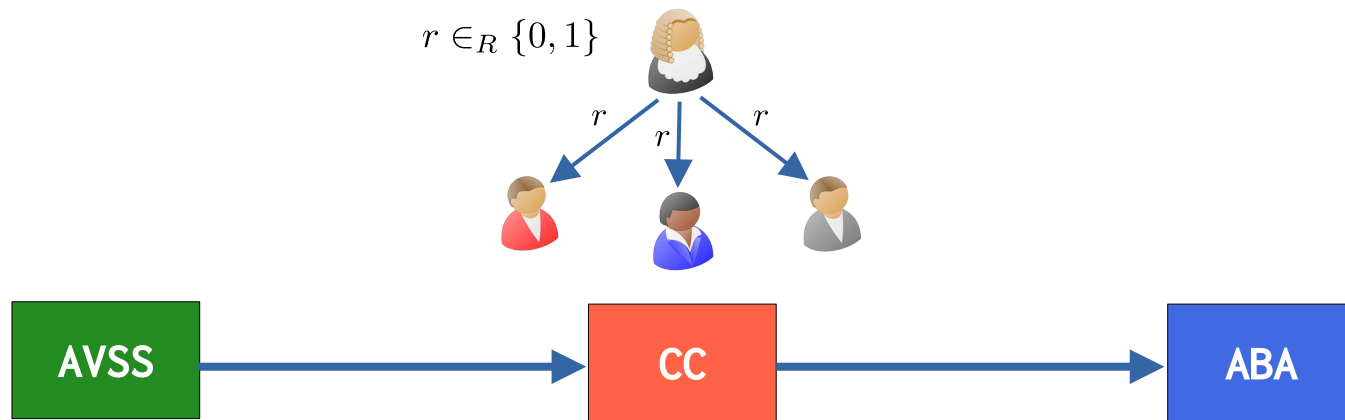
- Perfectly-Secure
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- Success Probability $> 1/n$

Asynchronous Byzantine Agreement (ABA)



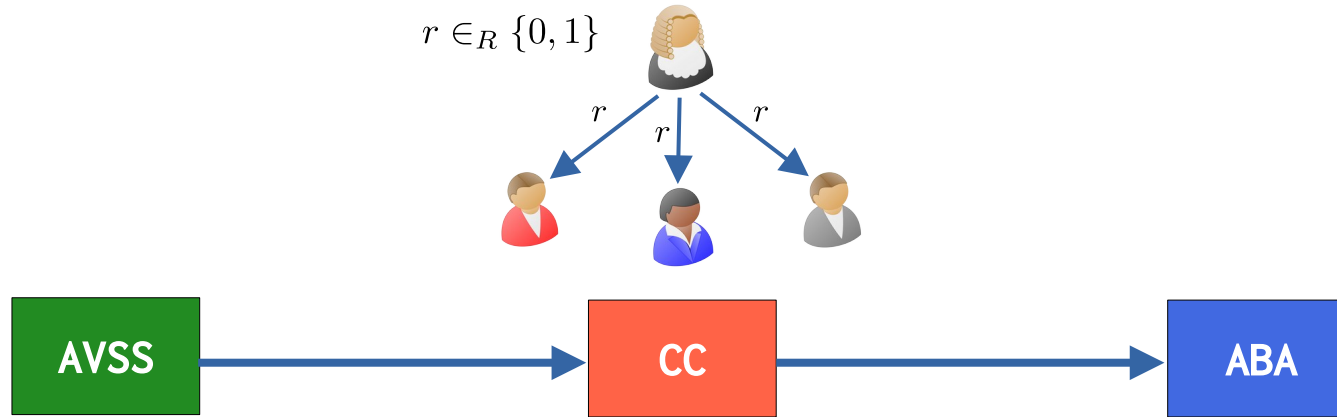
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Depends on largest set in \mathcal{Z}

Asynchronous Byzantine Agreement (ABA)



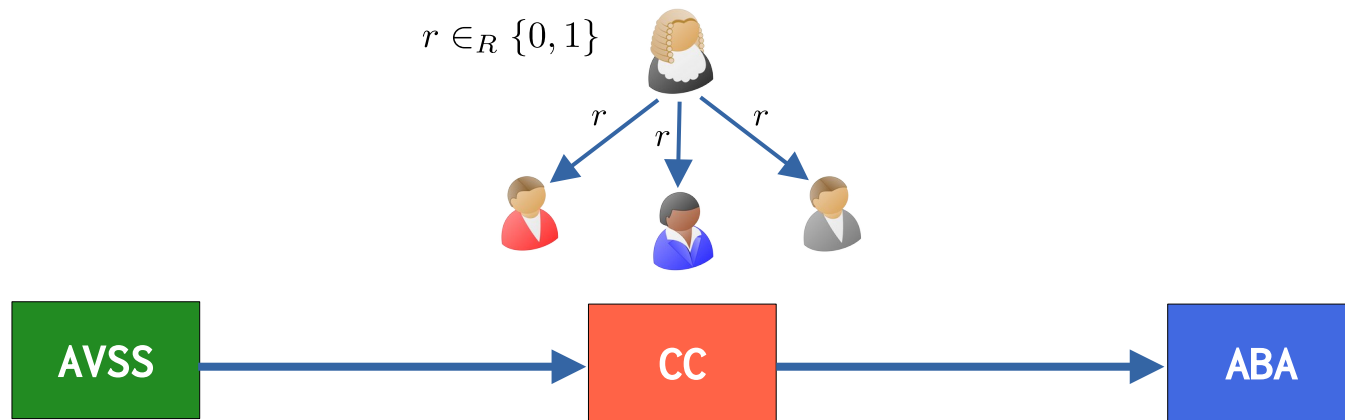
- Perfectly-Secure
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Asynchronous Byzantine Agreement (ABA)



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Depends on largest set in \mathcal{Z}
- Expected Running Time
 $R = \mathcal{O}(n^2)$

Asynchronous Byzantine Agreement (ABA)



- Perfectly-Secure
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Depends on largest set in \mathcal{Z}
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 $R = \mathcal{O}(n^2)$

The MPC Protocol

The MPC Protocol



The MPC Protocol

Mult

The MPC Protocol

$[a]$ $[b]$

Mult

The MPC Protocol

$$[a] \quad [b] \quad \text{Mult} \quad [a \cdot b] = \sum_{(l,m) \in \{1 \dots q\} \times \{1 \dots q\}} [a^{(l)} \cdot b^{(m)}]$$

The MPC Protocol

$$[a] \quad [b] \quad \text{Mult} \quad [a \cdot b] = \sum_{(l,m) \in \{1 \dots q\} \times \{1 \dots q\}} [a^{(l)} \cdot b^{(m)}]$$

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The MPC Protocol

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$a^{(1)}$

$b^{(3)}$

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$\{P_1, P_2\}$

P_3, P_4
 P_5, P_6, P_7

$a^{(1)}$

$b^{(3)}$

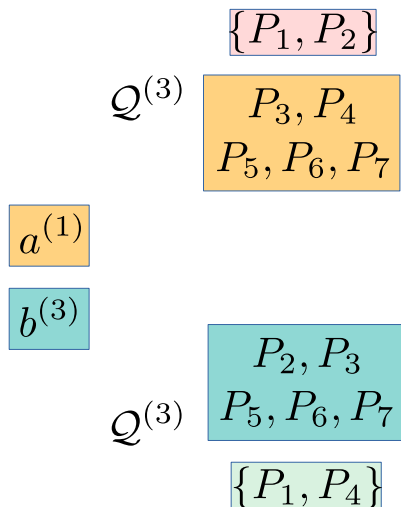
P_2, P_3
 P_5, P_6, P_7

$\{P_1, P_4\}$

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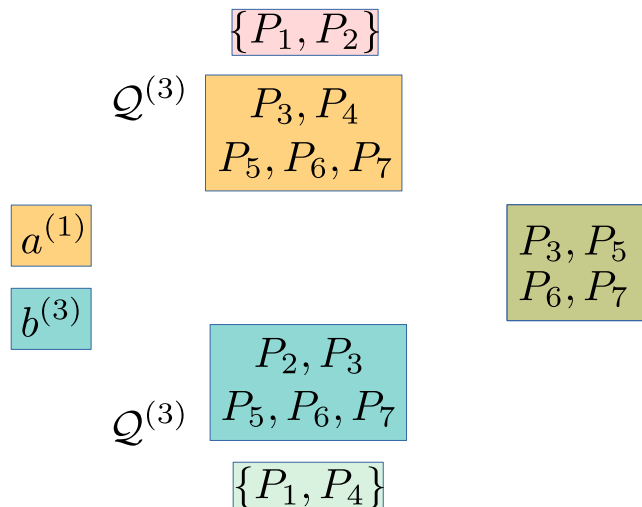
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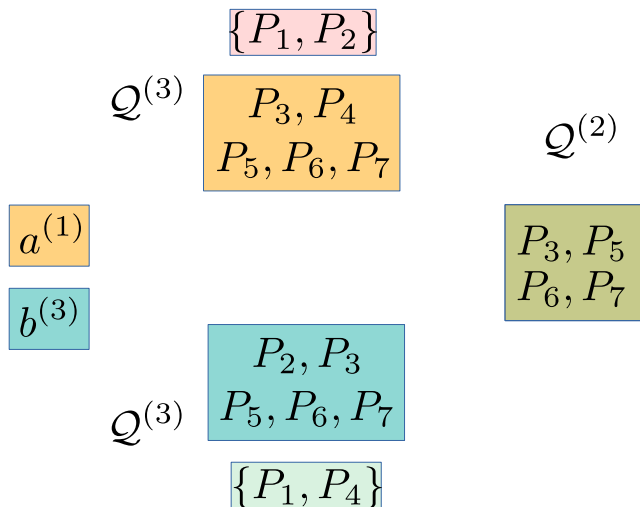
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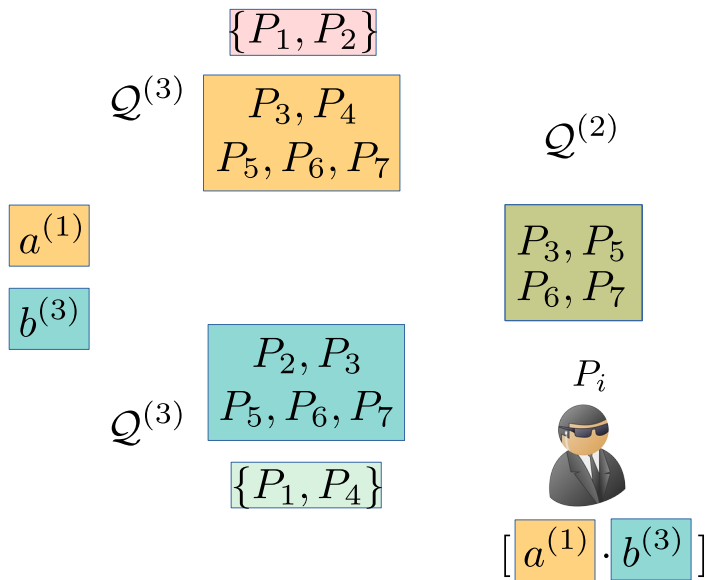
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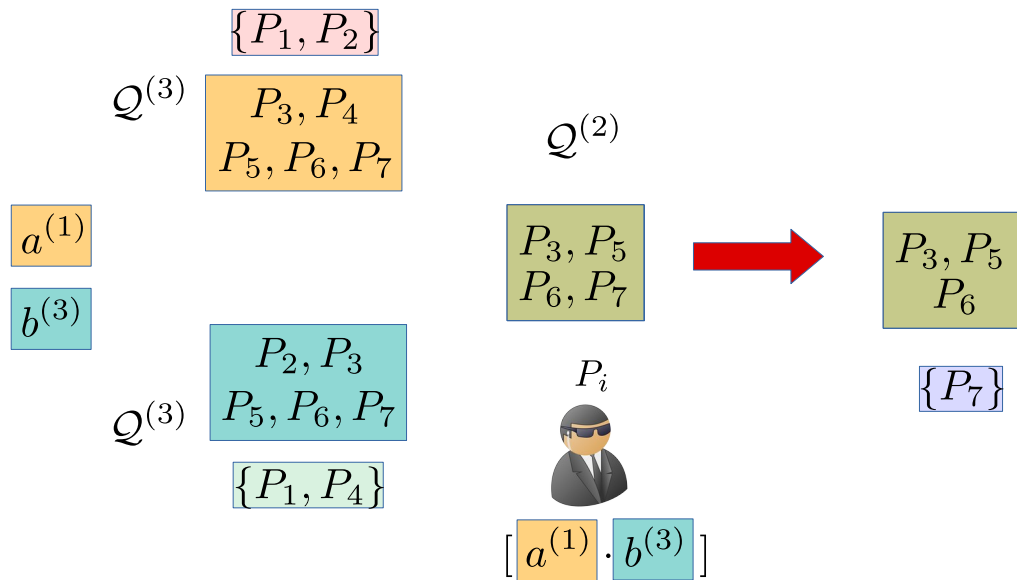
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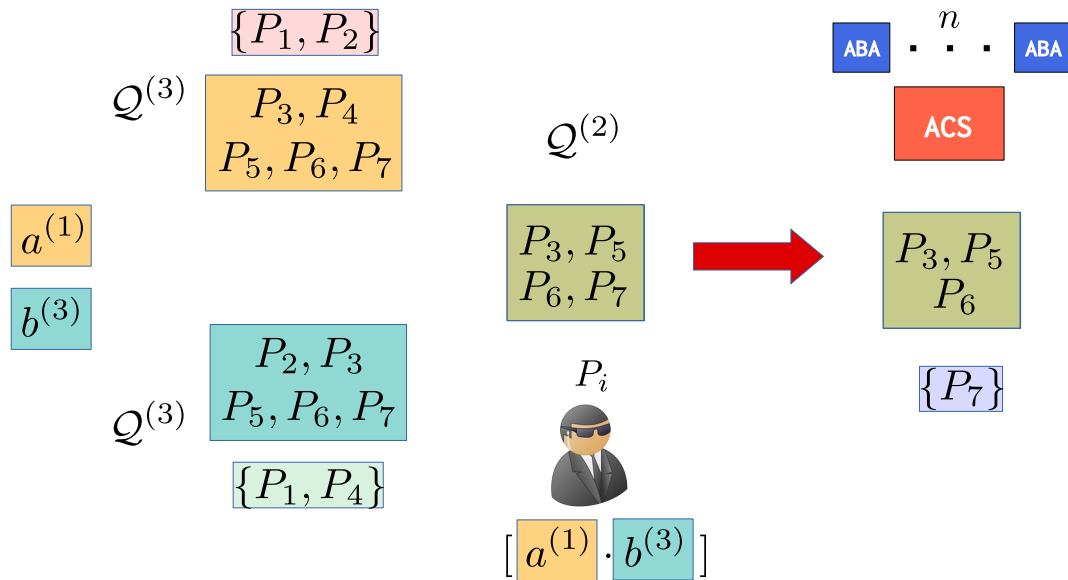
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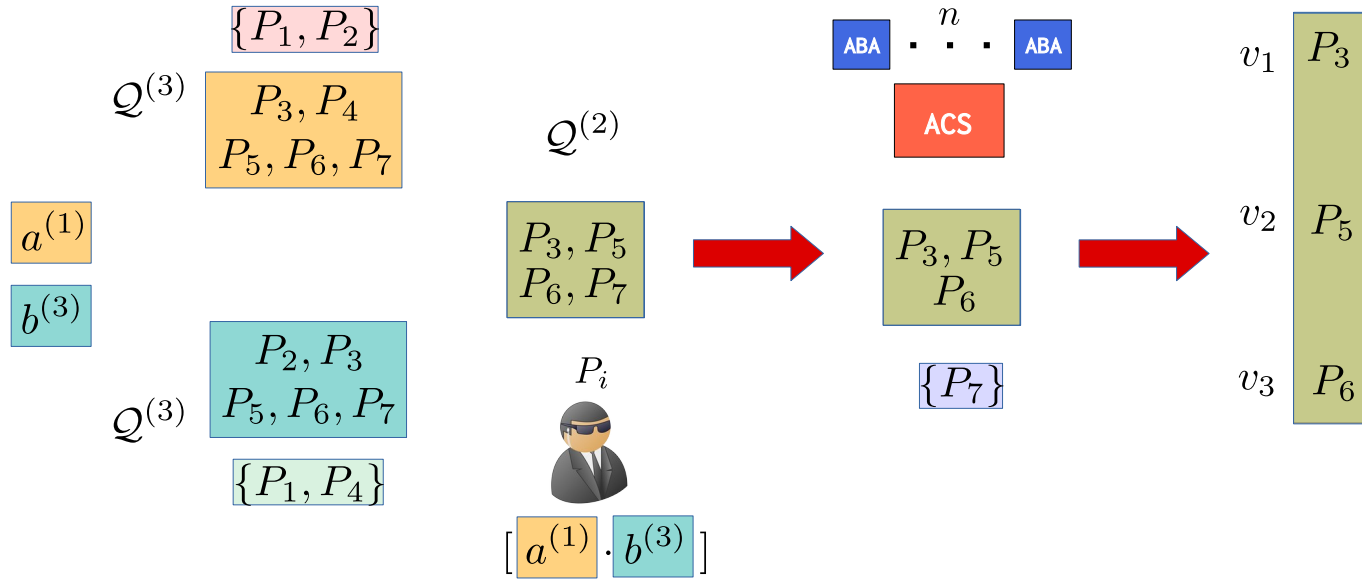
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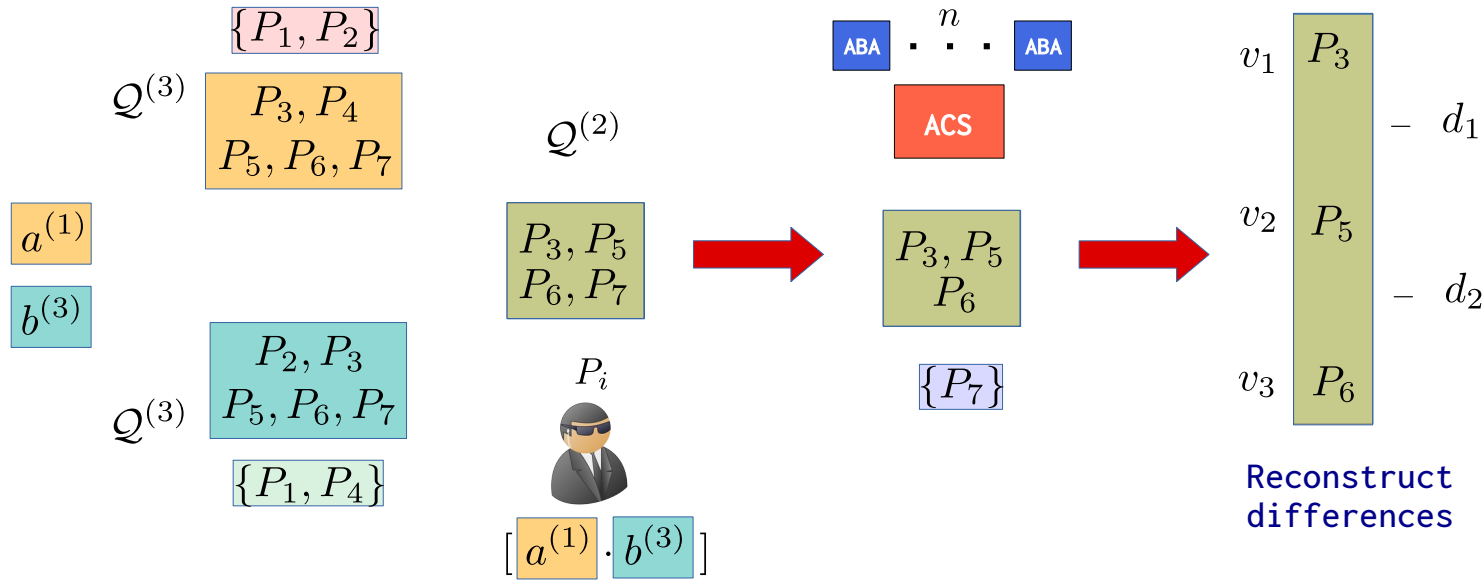
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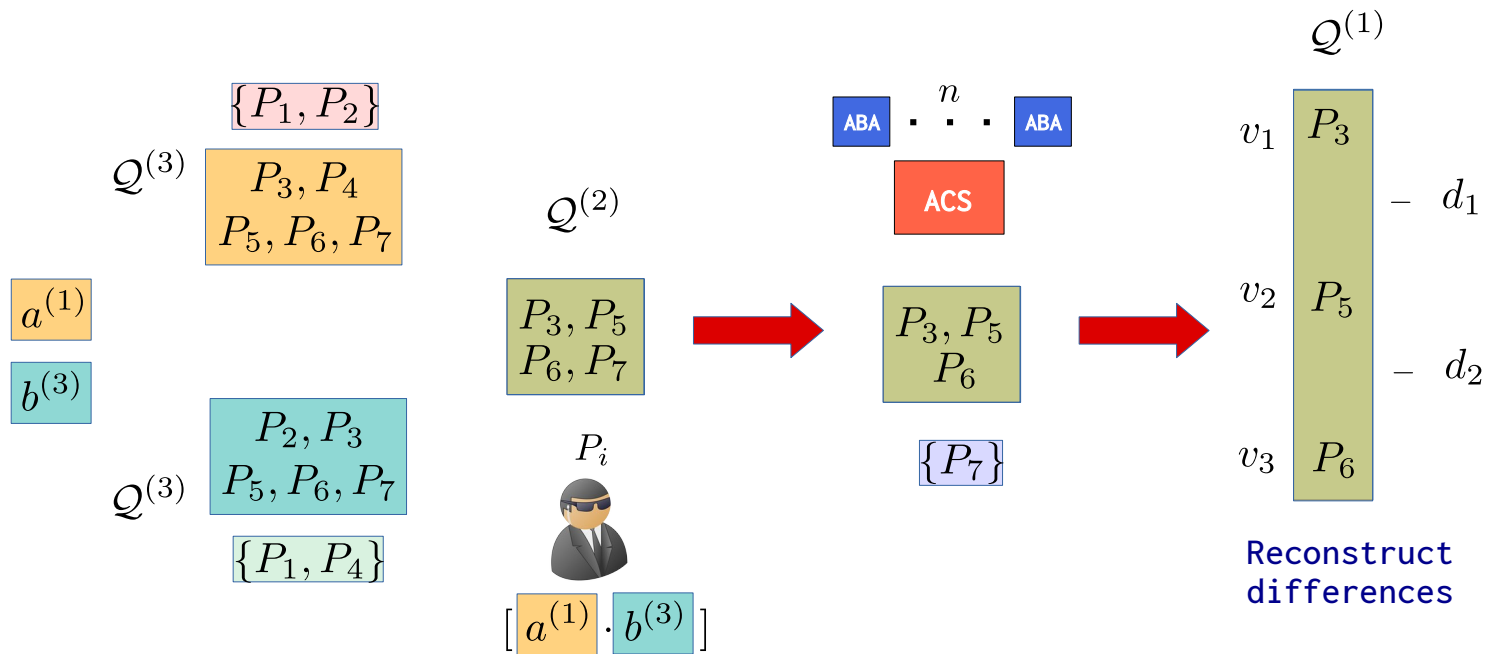
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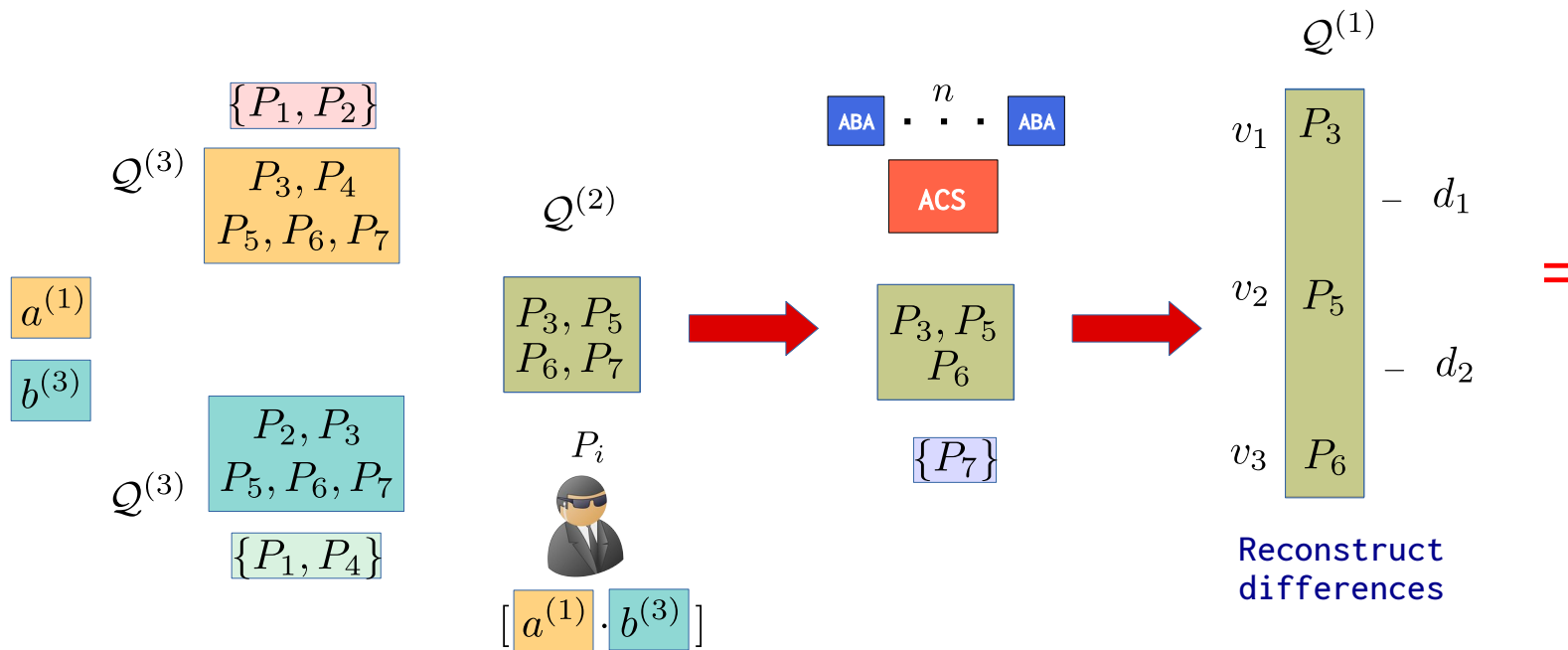
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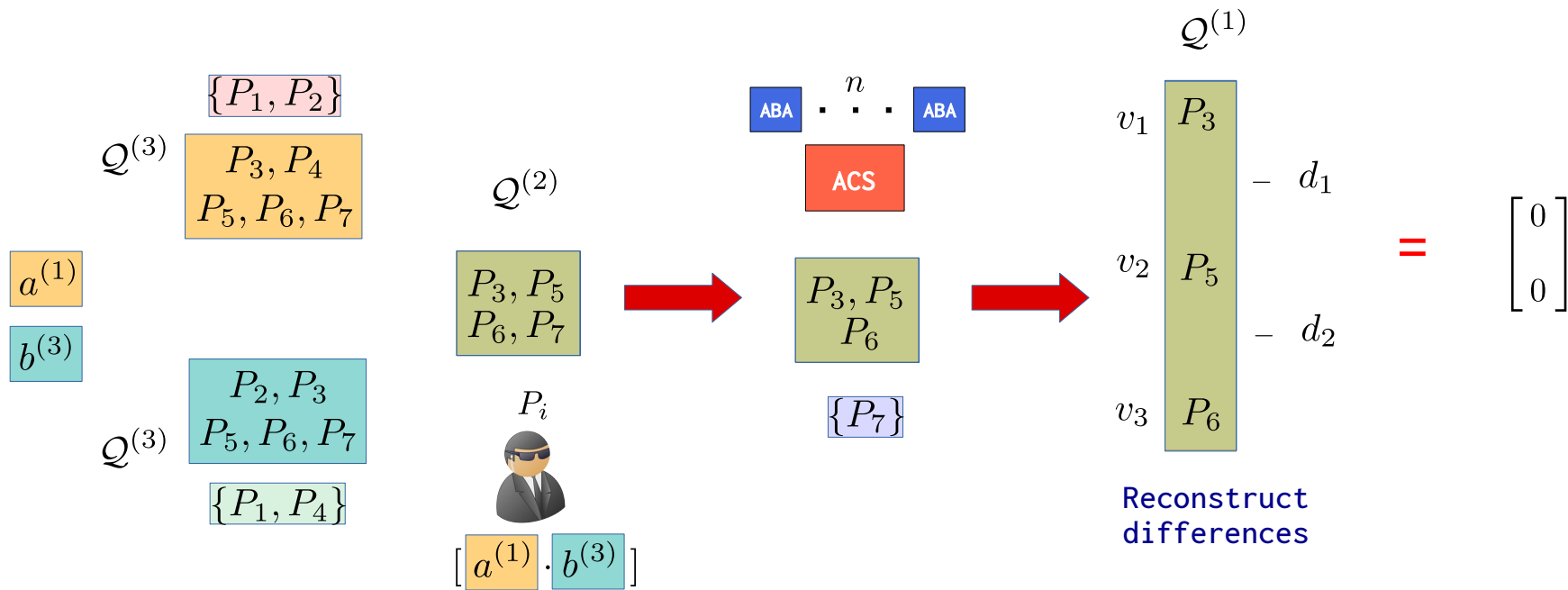
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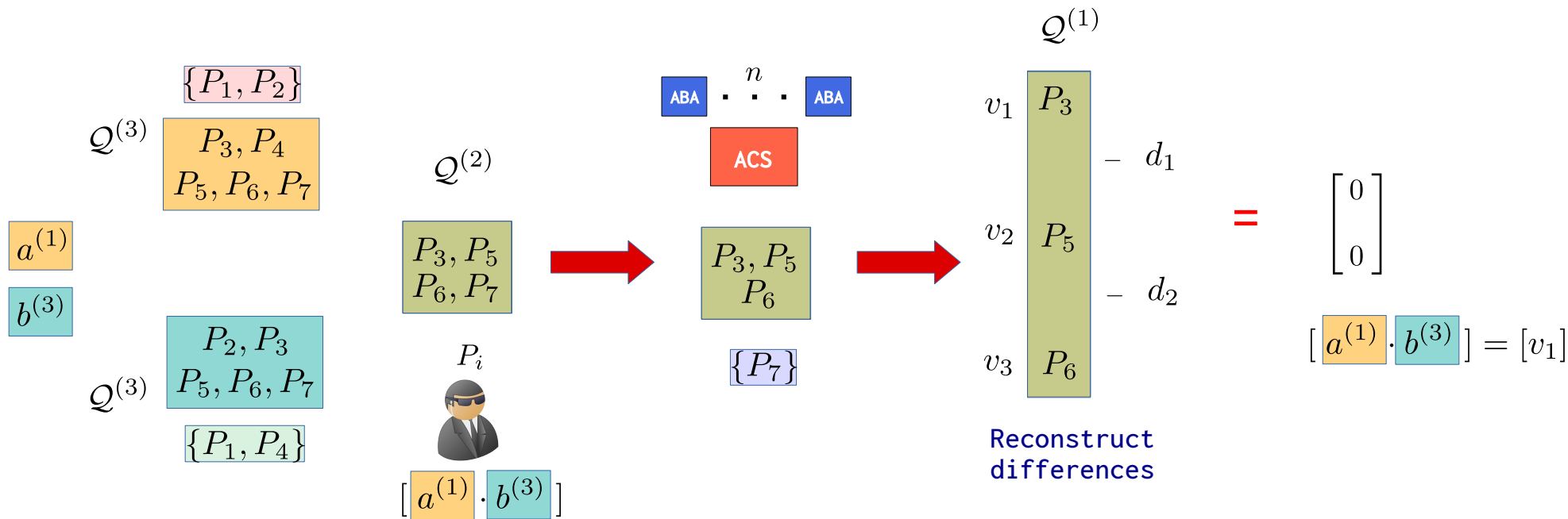
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The MPC Protocol

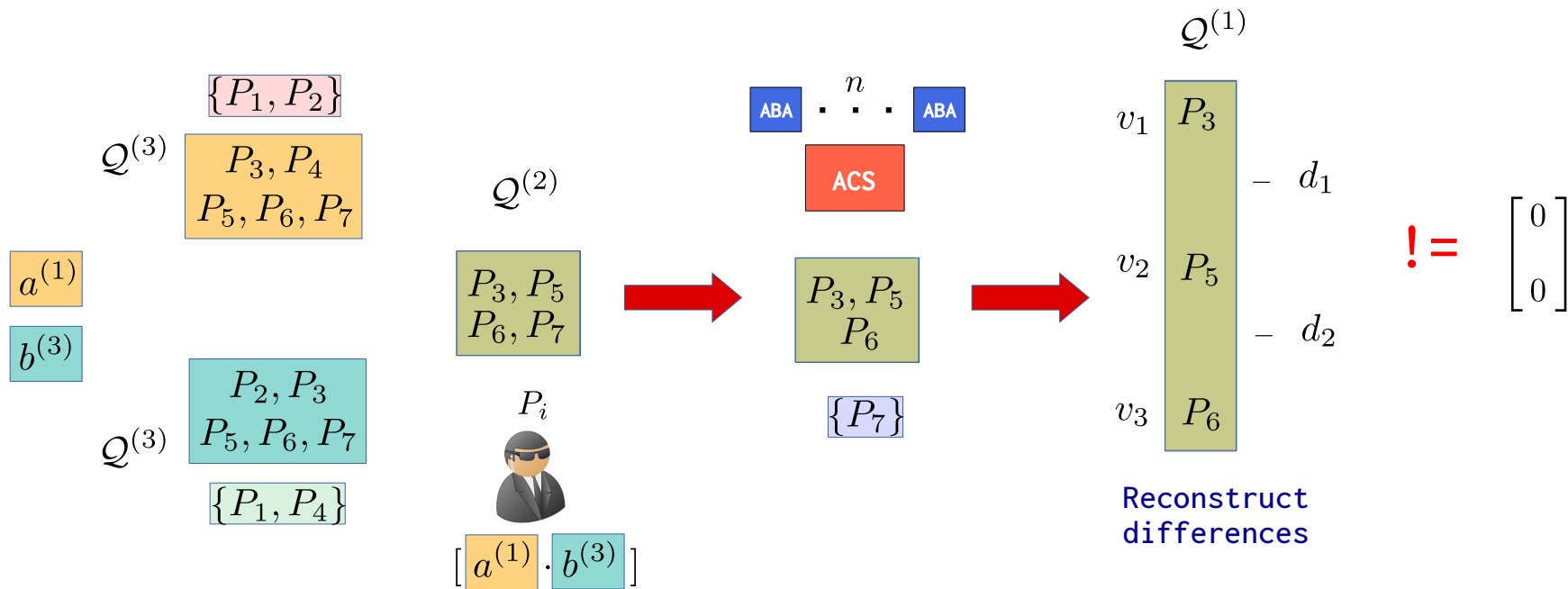
$$[a] \quad [b] \quad \text{Mult} \quad [a \cdot b] = \sum_{(l,m) \in \{1 \dots q\} \times \{1 \dots q\}} [a^{(l)} \cdot b^{(m)}]$$



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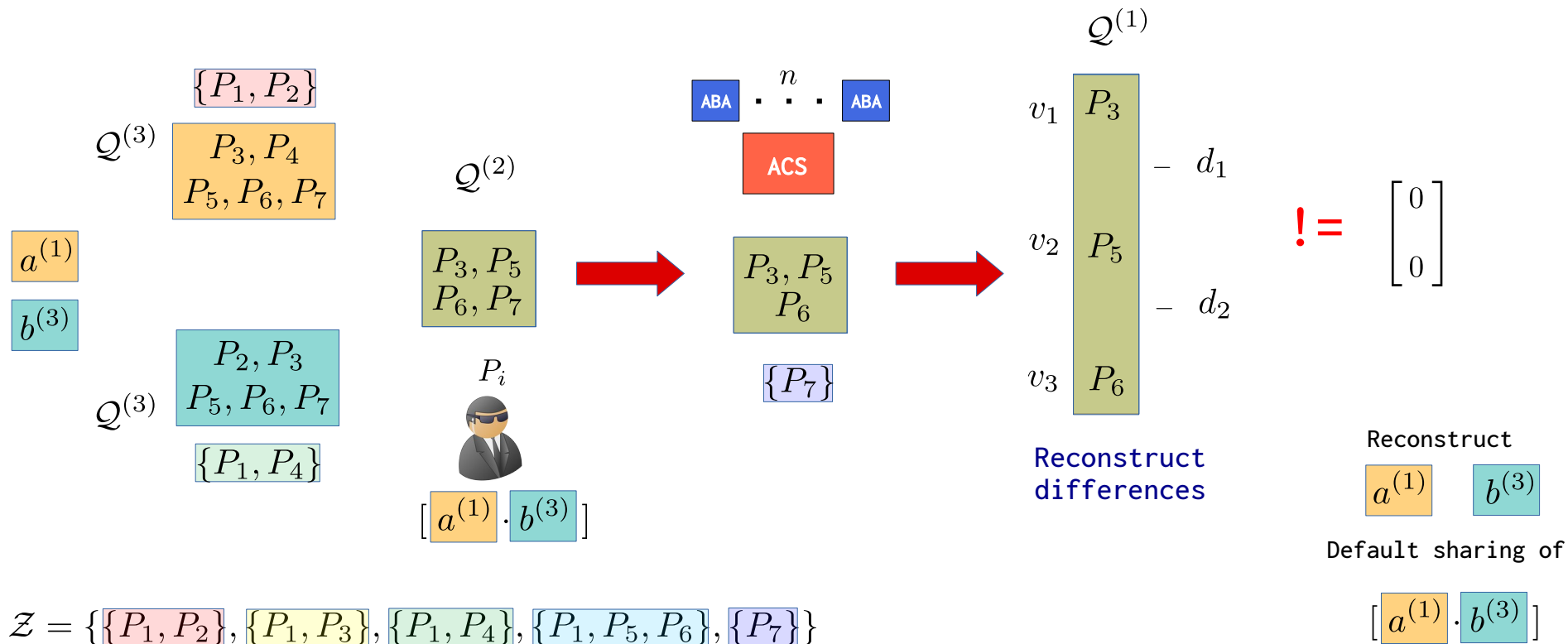
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Thanks!