

FULL ADDER:

$$\begin{array}{r}
 28 \quad 11100 \quad A \\
 +22 \quad 10110 \quad B \\
 \hline
 50 \quad 110010
 \end{array}$$

* Inputs: Numbers (bits) to be added - A, B
Carry from adding 2 bits - C

* Outputs: Sum, Carry

INPUT			OUTPUT	
A	B	C _{in}	Sum	Count
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

K-MAP FOR SUM

A \ B C _{in}	00	01	11	10
	0	0	1	0
1	1	0	1	0

$$\begin{aligned}
 \text{Sum} = & A'B'C_{in} + A'BC_{in}' + \\
 & AB'C_{in}' + ABC_{in}
 \end{aligned}$$

K-MAP FOR CARRY

A \ B C _{in}	00	01	11	10
0	0	0	1	0
1	0	1	1	1

$$\begin{aligned}
 \text{Carry} = & AB + BC_{in} + C_{in}A \\
 = & AB + C_{in}(A+B)
 \end{aligned}$$

(Using XOR instead of OR,

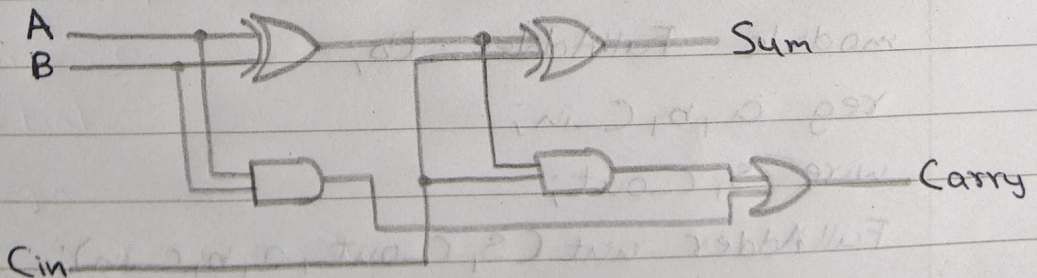
because in $A=1, B=1$ case,

AB is already 1, \Rightarrow OR gate will give 1 irrespective of using XOR or OR)

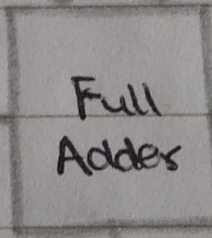
$$\begin{aligned}
 \text{Sum} &= A'BCin' + AB'cin' + ABCin + A'B'cin \\
 &= cin'(A'B + AB') + cin(AB + A'B') \\
 &= cin'(A'B + AB') + cin(A'B + AB')' \\
 &= cin \oplus (A'B + AB') \\
 &= cin \oplus A \oplus B
 \end{aligned}$$

$$\begin{aligned}
 \text{Carry} &= AB + ACin + BCin \\
 &= AB + ACin + BCin(A + A') \\
 &= ABCin + AB + ACin + A'BCin \\
 &= AB(cin + 1) + ACin + A'BCin \\
 &= AB + ACin + A'BCin \\
 &= AB + ACin(B + B') + A'BCin \\
 &= ABCin + AB + A'BCin + AB'cin \\
 &= AB(cin + 1) + cin(A'B + AB') \\
 &= AB + cin(A \oplus B)
 \end{aligned}$$

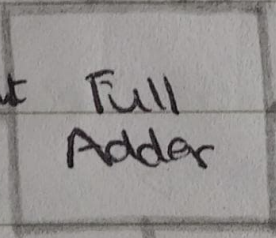
LOGIC DIAGRAM:



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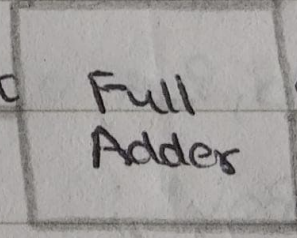
 $B_3 A_3$ $B_2 A_2$ $B_1 A_1$ $B_0 A_0$ 

Cin Cout



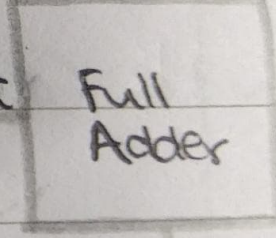
Cin

Cout



Cin

Cout



Cin

Cout

 S_3 S_2 S_1 S_0

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