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NCERT Mathematics 10.5.2 Q10

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Question: The 17th term of an AP exceeds its 10th term by 7. Find the common difference.

Solution:

Parameter	Value
First term of AP	x(0)
Common difference of AP	d
x(16) - x(9)	7

Using the formula for the nth term of an AP (x(n) = x(0) + (n)d), where (x(n)) represents the (n+1)th term of an arithmetic progression (AP)

$$x(16) = x(0) + 16d$$
 (1)

$$x(9) = x(0) + 9d \tag{2}$$

$$(x(0) + 16d) - (x(0) + 9d) = 7 (3)$$

$$7d = 7 \tag{4}$$

$$d = 1 \tag{5}$$

Now,

$$f(n) = x(n) \cdot u(n) = (x(0) + nd)u(n)$$
 (6)

The z-transform of u(n) is given by

$$F(z) = \sum_{n = -\infty}^{\infty} f(n)z^{-n}$$
(7)

$$F(z) = \sum_{n = -\infty}^{\infty} (x(0) + nd)u(n)z^{-n}$$
 (8)

$$F(z) = \sum_{n=0}^{\infty} (x(0) + nd)z^{-n}$$
 (9)

$$F(z) = x(0) \cdot \frac{1}{1 - z^{-1}} + d \cdot \frac{z^{-1}}{(1 - z^{-1})^2}; ROC : |z| > 1$$
(10)