1

NCERT Mathematics 11.9.3 Q32

EE23BTECH11213 - MUTHYALA NIKHITHA SRI

Question: If A.M. and G.M. of roots of a quadratic equation are 8 and 5,respectively,then obtain the quadratic equation.

Solution:

Parameter	Description	Value
x_1, x_2	Roots of a quadratic equation	?
$\frac{x_1 + x_2}{2}$	A.M. of roots	8
$\sqrt{x_1 \cdot x_2}$	G.M. of roots	5
•	TABLE I	

INPUT PARAMETERS

$$x_1 \cdot x_2 = 25 \tag{1}$$

$$x_1 + x_2 = 16 (2)$$

$$\implies x^2 - 16x + 25 = 0 \tag{3}$$

$$\implies x_1 = 8 + \sqrt{39} \tag{4}$$

$$\implies x_2 = 8 - \sqrt{39} \tag{5}$$

(10)

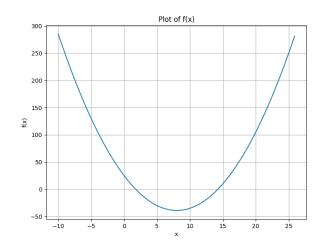


Fig. 1. Plot of $f(x) = x^2 - 16x + 25 = 0$

For AP.

$$x(0) = 8 + \sqrt{39} \tag{6}$$

$$d = -2\sqrt{39} \tag{7}$$

$$x(n) = (8 + \sqrt{39} + n(-2\sqrt{39}))u(n)$$
 (8)

$$X(z) = \frac{8 + \sqrt{39}}{1 - z^{-1}} + \frac{\left(-2\sqrt{39}\right) \cdot z^{-1}}{\left(1 - z^{-1}\right)^2} \quad |z| > |1|$$
(9)

 $\implies X(z) = \frac{8 + \sqrt{39} - \left(8 + 3\sqrt{39}\right) \cdot z^{-1}}{\left(1 - z^{-1}\right)^2} \quad |z| > |1|$

For GP.

$$x(0) = 8 + \sqrt{39} \tag{11}$$

$$r = \frac{8 - \sqrt{39}}{8 + \sqrt{39}} \tag{12}$$

$$x(n) = \left(\left(8 + \sqrt{39} \right) \cdot \left(\frac{8 - \sqrt{39}}{8 + \sqrt{39}} \right)^n \right) u(n)$$
 (13)

$$X(z) = \frac{8 + \sqrt{39}}{1 - \frac{(8 - \sqrt{39})z^{-1}}{8 + \sqrt{39}}} \quad |z| > \frac{103 - 16\sqrt{39}}{25} \quad (14)$$

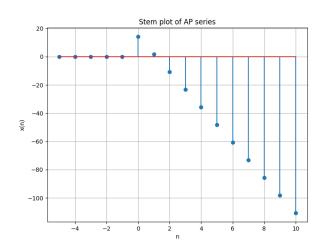


Fig. 2. Plot of $x(n) = (8 + \sqrt{39} + n(-2\sqrt{39})) u(n)$

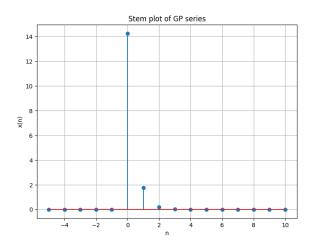


Fig. 3. Plot of $x(n) = \left(\left(8 + \sqrt{39} \right) \cdot \left(\frac{8 - \sqrt{39}}{8 + \sqrt{39}} \right)^n \right) u(n)$