Question 1:

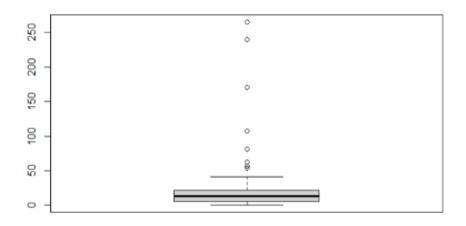
1. Consider the prostate cancer dataset available on eLearning as prostate cancer.csv. It consists of data on 97 men with advanced prostate cancer. A description of the variables is given in Figure 1. We would like to understand how PSA level is related to the other predictors in the dataset. Note that vesinv is a qualitative variable. You can treat gleason as a quantitative variable. Build a "reasonably good" linear model for these data by taking PSA level as the response variable. Carefully justify all the choices you make in building the model. Be sure to verify the model assumptions. In case a transformation of response is necessary, try the natural log transformation. Use the final model to predict the PSA level for a patient whose quantitative predictors are at the sample means of the variables and qualitative predictors are at the most frequent category.

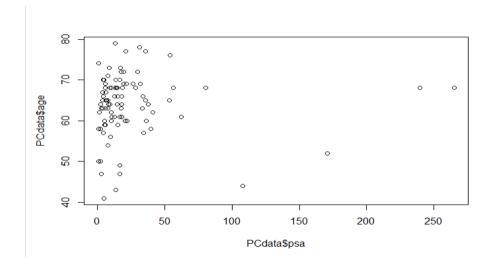
Section 1

Answers to the specific questions asked

- We read the prostate cancer data set and examined the summary and correlation between the features.
- Compared PSA level with each and every predictor after building a linear model and also found a summary of each.
- Built a model by selecting all the significant predictors which were obtained from the univariate model we developed.
- Altered model by not including some predictors to get significant predictors.
- Compared various model using ANOVA and predicted the value of PSA level and found the best model

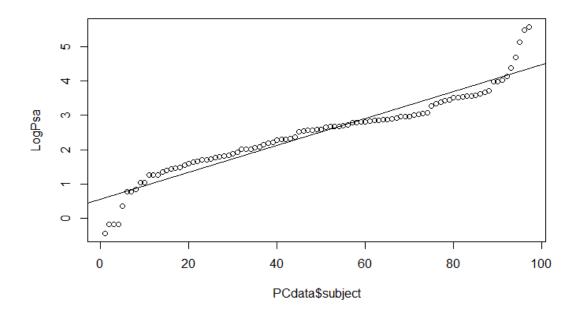
Box Plot of data and PSA

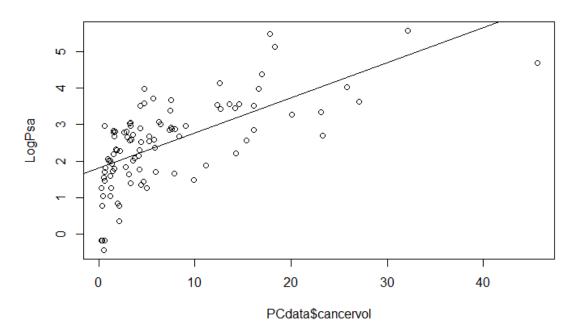


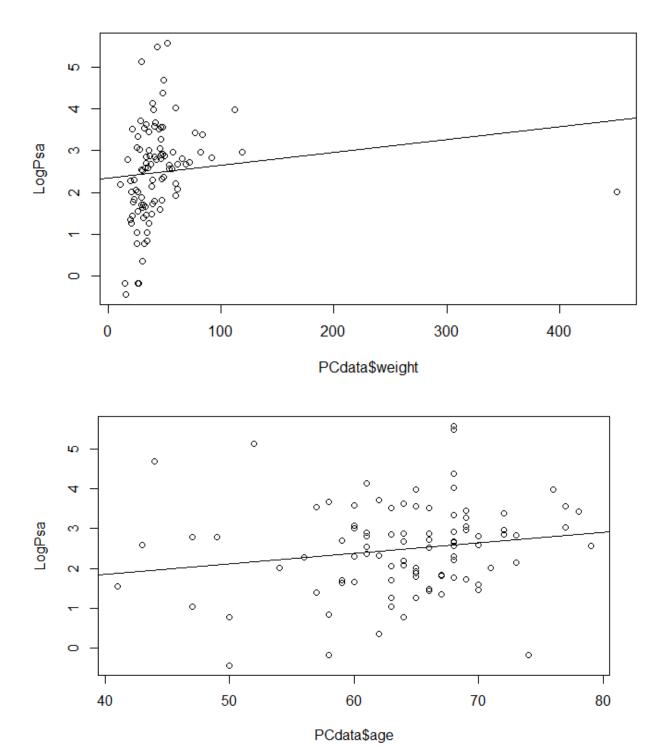


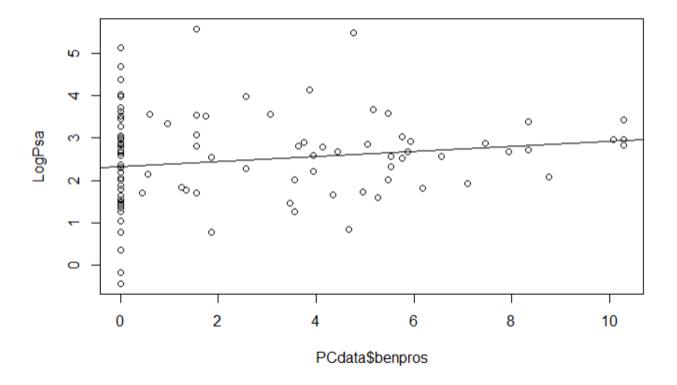
PSA is compared with features like subject, cancervol, weight, age, benpros, vesinv, capspen, gleason after building a linear model.

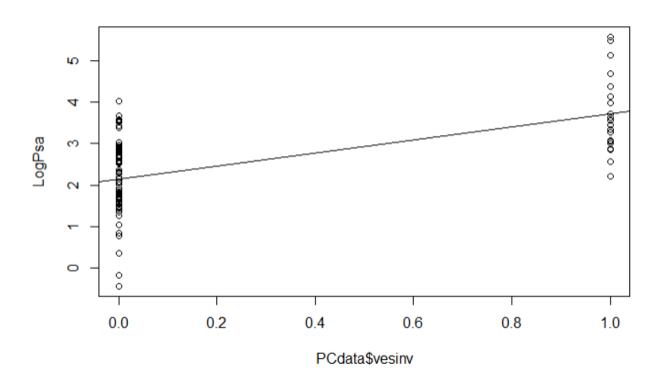
From the graphs below we can understand the relationship of PSA and predictors. Regression model is built after finding final predictors.

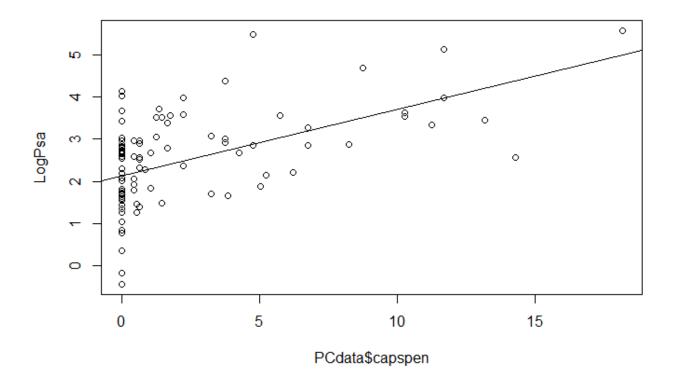


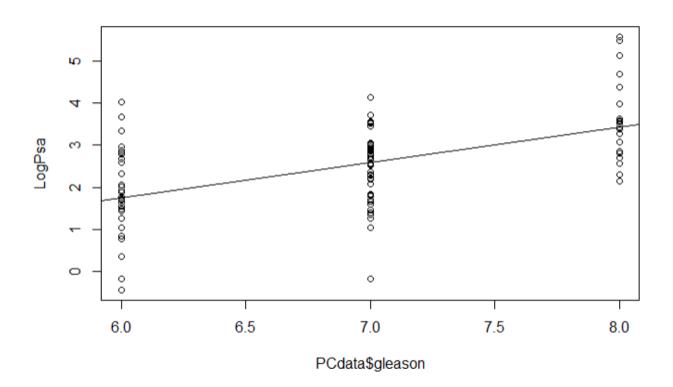


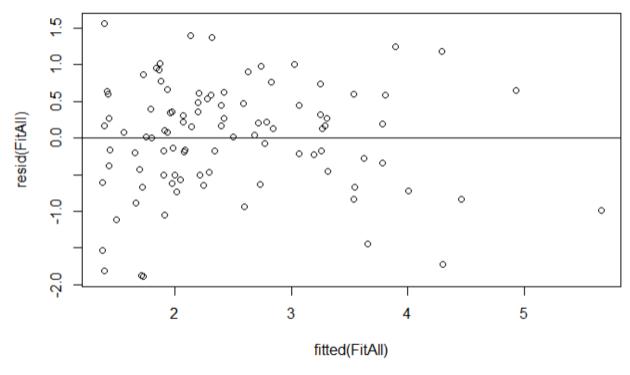


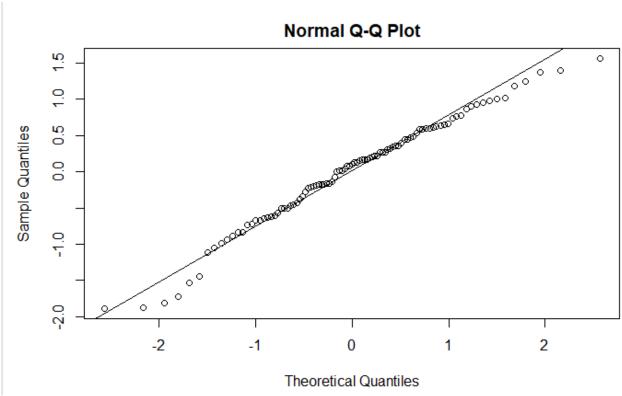












```
anova(Fit10, Fit9)
 Analysis of Variance Table
 Model 1: LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) + PCdata$gleason
Model 2: LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) + PCdata$gleason +
PCdataScapspen
Res. Df RSS Df Sum of Sq F Pr(>F)
93 60.340
2 92 60.039 1 0.30134 0.4617 0.4985
# Capsapen is not a significant predictor as pval is >=0.05
# Using all significant predictors
# Using all significant predictors
                                                                                                                                                                    @ X >
FitAll = lm(LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) + PCdata$gleason + PCdata$benpros, data = PCdata )
summary(FitAll)
 lm(formula = LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) +
      PCdata$gleason + PCdata$benpros, data = PCdata)
 Residuals:
 Min 1Q Median 3Q Max
-1.88531 -0.50276 0.09885 0.53687 1.56621
 Coefficients:
                              (Intercept)
 PCdata$cancervol 0.06488
factor(PCdata$vesinv)1 0.68421
 PCdata$@leason
                       0.09136
 PCdata$benpros
 Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
 Residual standard error: 0.7606 on 92 degrees of freedom
Multiple R-squared: 0.5834, Adjusted R-squared: 0.56
F-statistic: 32.21 on 4 and 92 DF, p-value: < 2.2e-16
```

```
anova(Fit9, FitAll)
Analysis of Variance Table
Model 1: LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) + PCdata$gleason +
      PCdata$capspen
Model 2: LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) + PCdata$qleason +
     PCdata$benpros
Res.Df RSS Df
1 92 60.039
2 92 53.229 0
             RSS Df Sum of Sq F Pr(>F)
                          6.8101
anova(FitAll, Fit10)
Analysis of Variance Table
Model 1: LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) + PCdata$gleason +
Pcdata$benpros

Model 2: LogPsa ~ Pcdata$cancervol + factor(Pcdata$vesinv) + Pcdata$gleason

Res.Df R5s Df Sum of Sq F Pr(>F)

1 92 53.229
1 2
       93 60.340 -1 -7.1115 12.291 0.0007054 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Removed the predictors which are not significant using ANOVA test of different models. Capspen has p value 0.49 which is greater than 0.05 so we removed that from the model because it is not a significant predictor. FitAll has the lowest standard error among all the Fit.

Predicted the PSA value based on the model and its coefficient standard error

```
| X1 = -0.65013

x2 = 0.06488

x3 = 0.68421

x4 = 0.33376

x5 = 0.09136

PredictingAns = exp(x1 + x2 * CancervolMean + x3 * 0 + x4* GleasonMean + x5 * BenprosMean)

PredictingAns
```

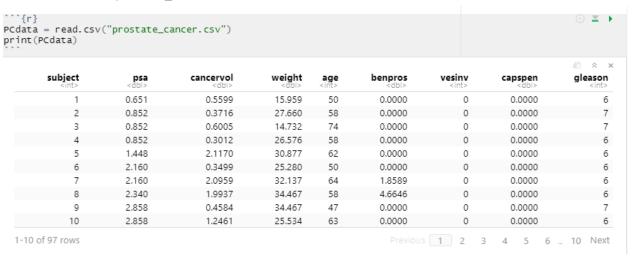
Assumptions:

From the residual graph one can observe that errors are centered around zero with constant variance also they are normally distributed as seen from the QQ plot. The QQ line fits well.

Section 2

Rcode

Read the dataset prostate_cancer

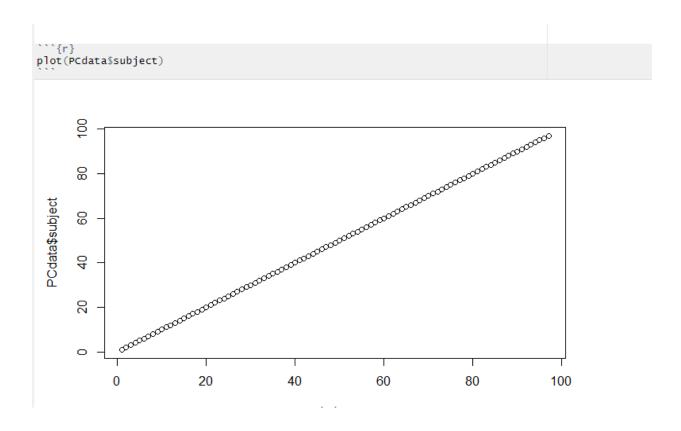


Summary of the dataset



Correlations between the feature variables.

```
```{r}
 ③ ▼ ▶
cor(PCdata)
 subject
 cancervol
 weight
 benpros
 vesinv
 0.60268375
subject
 1.0000000
 0.620997842
 0.113741022 0.19655569
 0.16500536
 0.566780347
psa.
 0.6026837
 1.00000000
 0.624150588
 0.026213430 0.01719938 -0.01648649
 0.528618785
cancervol 0.6209978
 0.62415059
 1.000000000
 0.005107148 0.03909442 -0.13320943
 0.581741687
weight
 0.1137410
 0.02621343
 0.005107148
 1.000000000 0.16432371
 0.32184875 -0.002410475
 0.1965557
 0.01719938
 0.039094423
 0.164323714 1.00000000
 0.36634121
 0.117658038
benpros
 0.1650054 -0.01648649 -0.133209431
 0.321848748 0.36634121
 1.00000000 -0.119553192
vesinv
 0.5667803 0.52861878
 0.581741687 -0.002410475 0.11765804 -0.11955319
 1.000000000
capspen
 0.4767525 0.55079252
 gleason
 0.5379241 0.42957975 0.481438397 -0.024206925 0.22585181 0.02682555
 capspen
 gleason
 0.476752459
 0.53792405
subject
 0.550792517
 0.42957975
psa
cancervol
 0.692896688
 0.48143840
 0.001578905 -0.02420693
weight
 0.099555351
 0.22585181
age
benpros
 -0.083008649
 0.02682555
vesinv
 0.680284092
 0.42857348
 1.000000000
 0.46156590
capspen
 0.461565896 1.00000000
gleason
```

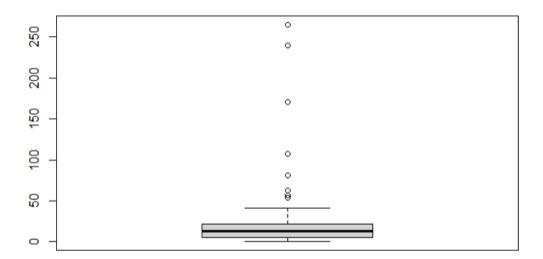


# # Taking log to scale the psa and box plot of data and psa

```
Scaling psa
LogPsa = log(PCdata$psa)

""{r}
boxplot(PCdata$psa)

A x
```



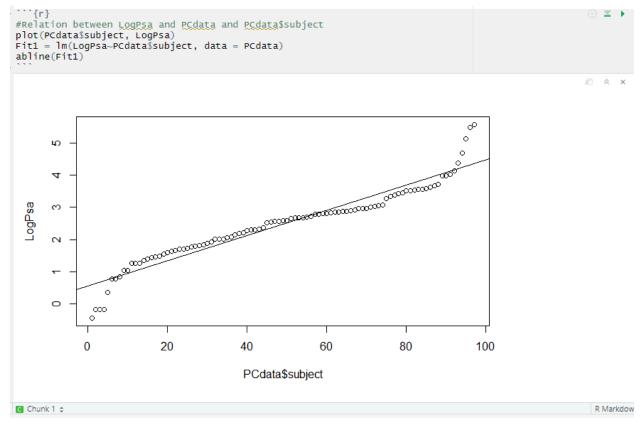
# # Column names

```
#Column Names
ColNames = colnames(PCdata)
ColNames

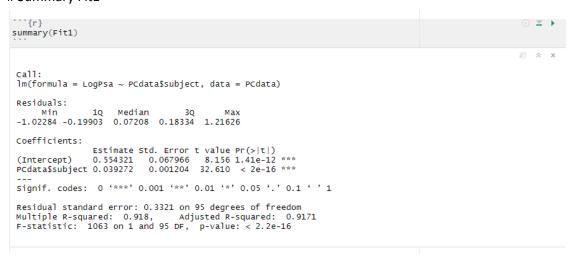
[1] "subject" "psa" "cancervol" "weight" "age" "benpros" "vesinv" "capspen"

[9] "gleason"
```

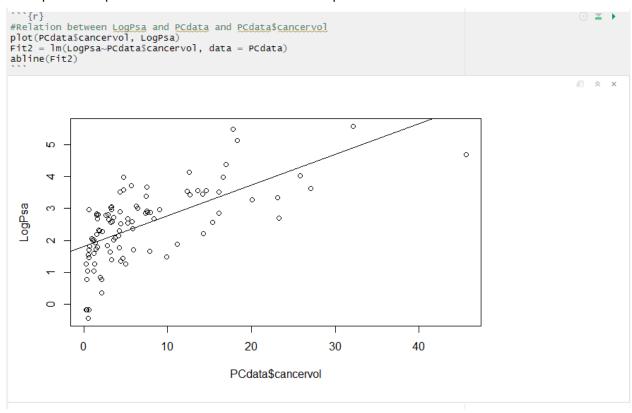
# # Comparison of psa and subject feature with the help of linear model



# # Summary Fit1



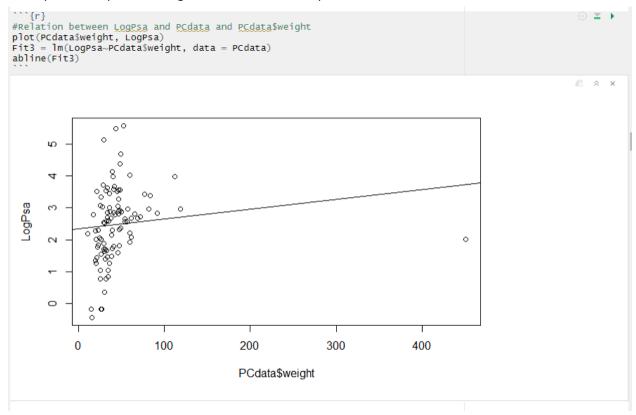
#### # Comparison of psa and cancervol feature with the help of linear model



## # summary Fit2

```
```{r}
summary(Fit2)
                                                                                                                               call:
 lm(formula = LogPsa ~ PCdata$cancervol, data = PCdata)
 Residuals:
                 1Q Median
     Min
                                      3Q
                                               Max
 -2.2886 -0.6590 0.1493 0.5769 1.9610
 Coefficients:
                       Estimate Std. Error t value Pr(>|t|)
                                    0.11899 15.174 < 2e-16 ***
0.01132 8.496 2.69e-13 ***
 (Intercept)
                        1.80549
 PCdata$cancervol 0.09619
 Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Residual standard error: 0.8742 on 95 degrees of freedom
Multiple R-squared: 0.4317, Adjusted R-squared: 0.4258
F-statistic: 72.18 on 1 and 95 DF, p-value: 2.688e-13
```

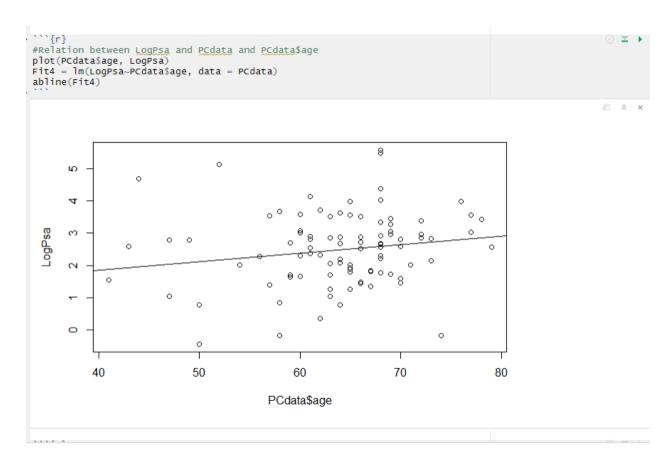
Comparison of psa and weight feature with the help of linear model



Summary Fit3

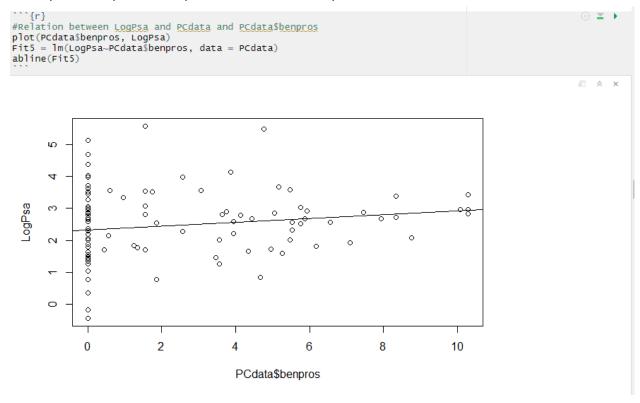
```
```{r}
summary(Fit3)
 lm(formula = LogPsa ~ PCdata$weight, data = PCdata)
 Residuals:
 1Q Median
 3Q
 мах
 -2.8172 -0.7291 0.1300 0.6144 3.0783
 Coefficients:
 Estimate Std. Error t value Pr(>|t|)
 2.338901 0.165328 14.147 <2e-16 ***
0.003072 0.002570 1.195 0.235
 (Intercept)
 PCdata$weight 0.003072
 Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
 Residual standard error: 1.151 on 95 degrees of freedom
Multiple R-squared: 0.01482, Adjusted R-squared: 0.004446
F-statistic: 1.429 on 1 and 95 DF, p-value: 0.235
```

## # Comparison of psa and age feature with the help of linear model



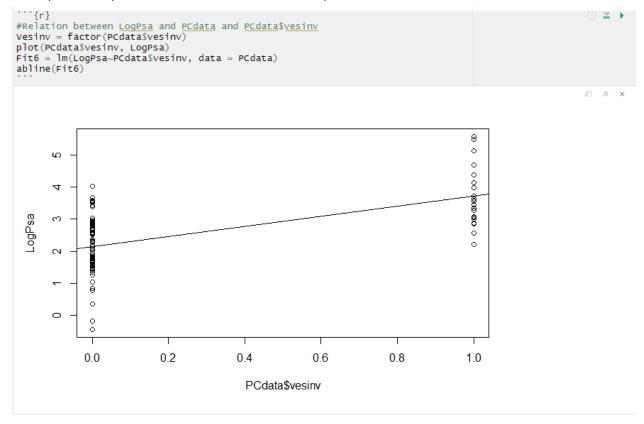
```
```{r}
summary(Fit4)
 call:
 lm(formula = LogPsa ~ PCdata$age, data = PCdata)
 Residuals:
                         Median
       Min
                   1Q
                                                    Max
 -2.90564 -0.71115 0.07247 0.66617
 Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                                           0.791
 (Intercept) 0.79721
                              1.00729
                                                     0.4307
 PCdata$age 0.02633
                              0.01567
                                           1.680
                                                     0.0961 .
 Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Residual standard error: 1.143 on 95 degrees of freedom
Multiple R-squared: 0.02887, Adjusted R-squared: 0.01865
F-statistic: 2.824 on 1 and 95 DF, p-value: 0.09615
```

Comparison of psa and benpros feature with the help of linear model

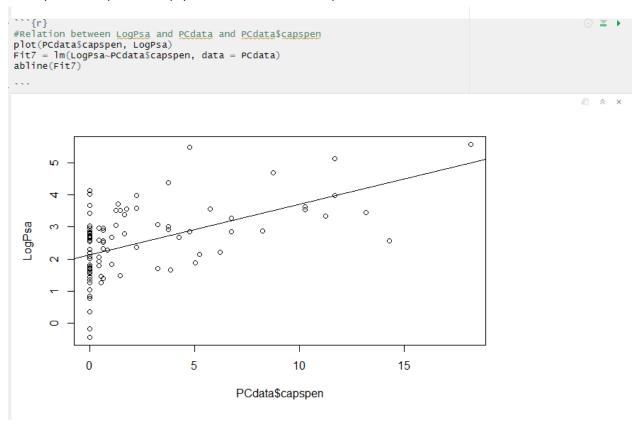


```
· ```{r}
                                                                                                   ⊕ ≚ ▶
summary(Fit5)
                                                                                                   call:
 lm(formula = LogPsa ~ PCdata$benpros, data = PCdata)
 Residuals:
                1Q Median
      Min
                                  3Q
 -2.75607 -0.76149 -0.01686 0.63318 3.16016
 Coefficients:
                <2e-16 ***
 (Intercept)
 PCdata$benpros 0.05991
                            0.03856 1.554
                                              0.124
 Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
 Residual standard error: 1.145 on 95 degrees of freedom
 Multiple R-squared: 0.02478, Adjusted R-squared: 0.01451
F-statistic: 2.413 on 1 and 95 DF, p-value: 0.1236
```

Comparison of psa and vesinvt feature with the help of linear model

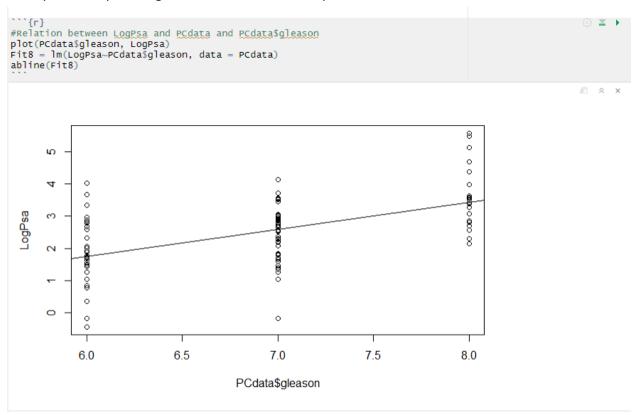


Comparison of psa and capspent feature with the help of linear model



```
```{r}
 ⊕ ¥ →
summary(Fit7)
lm(formula = LogPsa ~ PCdata$capspen, data = PCdata)
Residuals:
 Min
 1Q Median
 3Q
 Max
-2.5532 -0.6740 0.0071 0.6660 2.6043
Coefficients:
 (Intercept)
PCdata$capspen 0.15796
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Residual standard error: 0.992 on 95 degrees of freedom
Multiple R-squared: 0.2683, Adjusted R-squared: 0.2606
F-statistic: 34.84 on 1 and 95 DF, p-value: 5.503e-08
```

## # Comparison of psa and gleason feature with the help of linear model



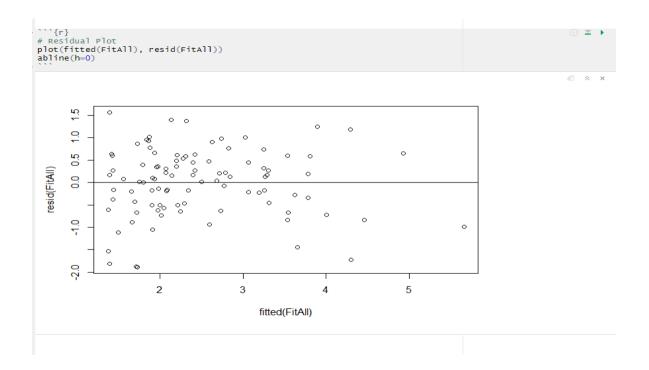
```
One can conclude that carcervol, gleason, vesinv, benepros and capspen are significant and show considerable relationship with PSA level.
To predict PSA we use different combinations of above predictors
```{r}
Fit9 = lm(LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) + PCdata$gleason + PCdata$capspen, data =
PCdata )
```{r}
 ∰ ¥ ▶
summary(Fit9)
 lm(formula = LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) +
 PCdata$gleason + PCdata$capspen, data = PCdata)
 Residuals:
 Min 1Q Median 3Q Max
-2.1747 -0.4497 0.1049 0.6215 1.6135
 Coefficients:
 (Intercept)
 PCdata$cancervol
 4.238 5.35e-05 ***
 0.28024 2.522 0.01339 *
0.13100 3.020 0.00327 **
 factor(PCdata$vesinv)1 0.70675
 PCdata$gleason
 0.39566
 0.03455 -0.680 0.49852
 -0.02348
 PCdata$capspen
 Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
 Residual standard error: 0.8078 on 92 degrees of freedom
Multiple R-squared: 0.5301, Adjusted R-squared: 0.50
F-statistic: 25.95 on 4 and 92 DF, p-value: 2.075e-14
To analyze changes in the model by including some of the predictors like PCdata$cancervol,
factor(PCdata$vesinv), PCdata$gleason
```{r}
                                                                                                                        Fit10 = lm(LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) + PCdata$gleason, data = PCdata )
```{r}
 ⊕ ¥ ▶
summary(Fit10)
 lm(formula = LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) +
 PCdata$gleason, data = PCdata)
 Residuals:
 Min 1Q Median 3Q Max
-2.16928 -0.44558 0.08431 0.60719 1.64082
 Coefficients:
 Estimate Std. Error t value Pr(>|t|)
 -0.72120 0.85749 -0.841 0.4025
 (Intercept)
 0.01352 4.425 2.62e-05 ***
0.24962 2.488 0.0146 *
0.12966 2.969 0.0038 **
 PCdata$cancervol
 0.05981
 factor(PCdata$vesinv)1 0.62117
 PCdata$gleason
 0.38491
 Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
 Residual standard error: 0.8055 on 93 degrees of freedom
 Multiple R-squared: 0.5277, Adjusted R-squared: 0.5125
F-statistic: 34.64 on 3 and 93 DF, p-value: 4.022e-15
```

```
```{r}
                                                                                                  ∰ ¥ ▶
anova(FitAll, Fit10)
 Analysis of Variance Table
 Model 1: LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) + PCdata$qleason +
     PCdata$benpros
 Model 2: LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) + PCdata$gleason
            RSS Df Sum of Sq
  Res.Df
                                 F
                                      Pr(>F)
      92 53.229
 2
      93 60.340 -1 -7.1115 12.291 0.0007054 ***
 Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```{r}
 ∅ ¥ ▶
anova(Fit10, Fit9)
Analysis of Variance Table
Model 1: LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) + PCdata$gleason
Model 2: LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) + PCdata$gleason +
 PCdata$capspen
 RSS Df Sum of Sq
 F Pr(>F)
 Res. Df
 93 60.340
 92 60.039 1 0.30134 0.4617 0.4985
```

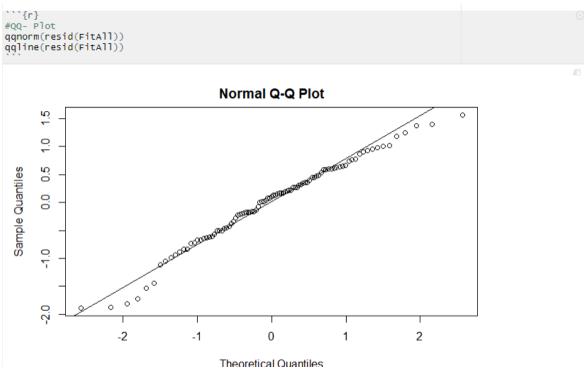
# Capsapen has p value = 0.49 which is greater than 0.05. It is not a significant predictor so we can remove it from model

```
Capsapen is not a significant predictor as pval is >=0.05 ```\{r\}
Using all significant predictors
FitAll = lm(LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) + PCdata$gleason + PCdata$benpros, data =
PCdata)
```{r}
                                                                                                  ## ▼ ▶
summary(FitAll)
                                                                                                  lm(formula = LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) +
    PCdata$gleason + PCdata$benpros, data = PCdata)
              1Q Median
                                3Q
 -1.88531 -0.50276 0.09885 0.53687 1.56621
Coefficients:
                       Estimate Std. Error t value Pr(>|t|)
                       -0.65013 0.80999 -0.803 0.424253
 (Intercept)
                        0.06488
 PCdata$cancervol
                                  0.01285
                                            5.051 2.22e-06 ***
                                  0.23640 2.894 0.004746 **
 factor(PCdata$vesinv)1 0.68421
 PCdata$gleason
                        0.33376
                                  0.12331
                                            2.707 0.008100 **
                                  0.02606 3.506 0.000705 ***
 PCdata$benpros
                        0.09136
 Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
 Residual standard error: 0.7606 on 92 degrees of freedom
Multiple R-squared: 0.5834, Adjusted R-squared: 0.5653
F-statistic: 32.21 on 4 and 92 DF, p-value: < 2.2e-16
```

This is the minimum residual standard error obtained so this is the best model.



Errors are centered around zero with constant variance



Errors are normally distributed and also QQ line fits well

```
# Question - Use the final model to predict the PSA level for a patient whose quantitative predictors are at
the sample means of the variables and qualitative predictors are at the most frequent category.
# taking mean of quantitative and qualitative predictors ```\{r\}
CancervolMean = mean(PCdata$cancervol)
CancervolMean
                                                                                                [1] 6.998682
```{r}
 ⊕ × ►
GleasonMean = mean(PCdata$gleason)
GleasonMean
 [1] 6.876289
```{r}
                                                                                                ⊕ ≚ ▶
BenprosMean = mean(PCdata$benpros)
BenprosMean
                                                                                                [1] 2.534725
                                                                                                63 × 1
MfVesinv = names(which.max(table(factor(PCdata$vesinv))))
MfVesinv
                                                                                                [1] "0"
```

Predicting the PSA value based on model and its coefficient error.

```
```{r}
anova(FitAll, Fit10)
 Analysis of Variance Table
Model 1: LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) + PCdata$gleason +
 PCdata$benpros
Model 2: LogPsa ~ PCdata$cancervol + factor(PCdata$vesinv) + PCdata$gleason Res.Df RSS Df Sum of Sq F Pr(>F)
 92 53.229
2
 93 60.340 -1
 -7.1115 12.291 0.0007054 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```{r}
                                                                                                             ⊕ ¥ ▶
x1 = -0.65013
x2 = 0.06488
x3 = 0.68421
x4 = 0.33376
x5 = 0.09136
PredictingAns = \exp(x1 + x2 + \text{CancervolMean} + x3 + 0 + x4 + \text{GleasonMean} + x5 + \text{BenprosMean})
PredictingAns
                                                                                                             [1] 10.28357
```