Assignment 6

Nikita Pai & Abhilash Hemaraj

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library(readxl)

```
data <- read_excel('18 Toyota Corolla.xlsx')</pre>
str(data)
                                             1436 obs. of 38 variables:
## Classes 'tbl df', 'tbl' and 'data.frame':
   $ Id
                           1 2 3 4 5 6 7 8 9 10 ...
                    : num
## $ Model
                           "TOYOTA Corolla 2.0 D4D HATCHB TERRA 2/3-Doors" "TOYOTA Corolla 2.0 D4D HA
## $ Price
                   : num
                           13500 13750 13950 14950 13750 ...
## $ Age_08_04
                           23 23 24 26 30 32 27 30 27 23 ...
                   : num
   $ Mfg_Month
                          10 10 9 7 3 1 6 3 6 10 ...
                    : num
##
                           2002 2002 2002 2002 2002 ...
   $ Mfg_Year
                    : num
## $ KM
                    : num 46986 72937 41711 48000 38500 ...
## $ Fuel_Type
                    : chr
                           "Diesel" "Diesel" "Diesel" "Diesel"
## $ HP
                           90 90 90 90 90 90 90 192 69 ...
                    : num
## $ Met_Color
                    : num 1 1 1 0 0 0 1 1 0 0 ...
                          "Blue" "Silver" "Blue" "Black" ...
## $ Color
                   : chr
## $ Automatic
                   : num
                           0 0 0 0 0 0 0 0 0 0 ...
## $ cc
                    : num
                           2000 2000 2000 2000 2000 2000 2000 2000 1800 1900 ...
##
   $ Doors
                    : num 3 3 3 3 3 3 3 3 3 3 ...
## $ Cylinders
                    : num
                          4 4 4 4 4 4 4 4 4 . . .
## $ Gears
                           5 5 5 5 5 5 5 5 5 5 ...
                    : num
                    : num
## $ Quarterly Tax
                           210 210 210 210 210 210 210 210 100 185 ...
## $ Weight
                    : num 1165 1165 1165 1165 1170 ...
## $ Mfr_Guarantee
                   : num 0 0 1 1 1 0 0 1 0 0 ...
## $ BOVAG_Guarantee : num
                          1 1 1 1 1 1 1 1 1 1 ...
   $ Guarantee_Period: num
                           3 3 3 3 3 3 3 3 3 . . .
## $ ABS
                    : num 1 1 1 1 1 1 1 1 1 1 ...
## $ Airbag_1
                    : num 1 1 1 1 1 1 1 1 1 1 ...
## $ Airbag_2
                          1 1 1 1 1 1 1 1 0 1 ...
                    : num
## $ Airco
                    : num
                           0 1 0 0 1 1 1 1 1 1 ...
## $ Automatic_airco : num 0 0 0 0 0 0 0 0 0 ...
## $ Boardcomputer
                   : num 1 1 1 1 1 1 1 1 0 1 ...
## $ CD_Player
                           0 1 0 0 0 0 0 1 0 0 ...
                    : num
   $ Central_Lock
                    : num 1 1 0 0 1 1 1 1 1 0 ...
  ## $ Power_Steering : num 1 1 1 1 1 1 1 1 1 ...
## $ Radio
                    : num
                           0 0 0 0 0 0 0 0 1 0 ...
## $ Mistlamps
                    : num 0000110000...
## $ Sport_Model
                   : num 000001000...
## $ Backseat_Divider: num 1 1 1 1 1 1 1 1 0 1 ...
## $ Metallic Rim
                   : num 000000010...
```

```
## $ Radio_cassette : num 0 0 0 0 0 0 0 1 0 ...
## $ Tow Bar : num 0 0 0 0 0 0 0 0 0 ...
#Factor variables which is equivalent to creating dummy variables
data$Fuel_Type <- factor(data$Fuel_Type)</pre>
data$Color <- factor(data$Color)</pre>
data$Price <- (data$Price - min(data$Price))/(max(data$Price) - min(data$Price))</pre>
\label{lem:data-MfgMonth} $$\operatorname{Mfg_Month} - \min(\operatorname{data}_{Mfg_Month}) / (\max(\operatorname{data}_{Mfg_Month}) - \min(\operatorname{data}_{Mfg_Month})) / (\max(\operatorname{data}_{Mfg_Month})) / (\max(\operatorname{da
data$Mfg_Year <- (data$Mfg_Year - min(data$Mfg_Year))/(max(data$Mfg_Year)-min(data$Mfg_Year))
data$Guarantee_Period <- (data$Guarantee_Period - min(data$Guarantee_Period))/(max(data$Guarantee_Period)
data$Weight <- (data$Weight - min(data$Weight))/(max(data$Weight) - min(data$Weight))
data$Quarterly_Tax <- (data$Quarterly_Tax - min(data$Quarterly_Tax))/(max(data$Quarterly_Tax)-min(data$
data$cc <- (data$cc - min(data$cc))/(max(data$cc) - min(data$cc))</pre>
data$Doors <- (data$Doors - min(data$Doors))/(max(data$Doors) - min(data$Doors))</pre>
data$Cylinders <- (data$Cylinders - min(data$Cylinders))/(max(data$Cylinders)-min(data$Cylinders))
data$Gears <- (data$Gears - min(data$Gears))/(max(data$Gears)-min(data$Gears))</pre>
data$KM <- (data$KM - min(data$KM))/(max(data$KM) - min(data$KM))</pre>
data$HP <- (data$HP - min(data$HP))/(max(data$HP) - min(data$HP))</pre>
#creating data set
set.seed(222)
ind \leftarrow sample(2, nrow(data), replace = TRUE, prob = c(0.75, 0.25))
training <- data[ind==1,]</pre>
testing <- data[ind==2,]</pre>
str(training)
## Classes 'tbl_df', 'tbl' and 'data.frame': 1096 obs. of 38 variables:
                                             : num 2 3 4 7 8 9 10 11 12 13 ...
## $ Id
## $ Model
                                            : chr "TOYOTA Corolla 2.0 D4D HATCHB TERRA 2/3-Doors" " TOYOTA Corolla 2.0 D4D H
## $ Price
                                           : num 0.334 0.341 0.377 0.446 0.506 ...
## $ Age_08_04 : num 0.278 0.291 0.316 0.329 0.367 ...
## $ Mfg_Month : num 0.818 0.727 0.545 0.455 0.182 ...
## $ Mfg_Year : num 0.667 0.667 0.667 0.667 0.667 ...
## $ KM
                                           : num 0.3 0.172 0.198 0.389 0.312 ...
                                           : Factor w/ 3 levels "CNG", "Diesel", ...: 2 2 2 2 2 3 2 3 3 3 ...
## $ Fuel_Type
## $ HP
                                            : num 0.171 0.171 0.171 0.171 0.171 ...
## $ Met_Color : num 1 1 0 1 1 0 0 0 0 0 ...
## $ Color : Factor w/ 10 levels "Beige",
## $ Automatic : num 0 0 0 0 0 0 0 0 0 ...
                                           : Factor w/ 10 levels "Beige", "Black", ...: 7 3 2 5 5 6 3 7 6 6 ...
                                             : num 0.0476 0.0476 0.0476 0.0476 0.0476 ...
## $ cc
## $ Doors
                                           : num 0.333 0.333 0.333 0.333 ...
## $ Cylinders
                                           : num 0.667 0.667 0.667 0.667 0.667 ...
## $ Gears
## $ Quarterly_Tax : num 0.723 0.723 0.723 0.723 0.723 ...
                                              : num 0.268 0.268 0.268 0.398 0.398 ...
## $ Weight
## $ Mfr_Guarantee : num 0 1 1 0 1 0 0 1 1 1 ...
## $ BOVAG_Guarantee : num 1 1 1 1 1 1 1 1 1 ...
## $ Guarantee_Period: num 0 0 0 0 0 ...
## $ ABS
                                           : num 1 1 1 1 1 1 1 1 1 1 ...
## $ Airbag_1
                                           : num 1 1 1 1 1 1 1 1 1 1 ...
## $ Airbag_2
                                            : num 1 1 1 1 1 0 1 1 1 1 ...
```

```
## $ Airco
              : num 1001111111...
## $ Automatic_airco : num 0 0 0 0 0 0 1 1 1 ...
## $ Boardcomputer : num 1 1 1 1 1 0 1 0 1 1 ...
## $ CD_Player
                   : num 1000100100...
## $ Central_Lock : num 1 0 0 1 1 1 0 1 1 1 ...
## $ Powered Windows : num 0 0 0 1 1 1 0 1 1 1 ...
## $ Power Steering : num 1 1 1 1 1 1 1 1 1 ...
## $ Radio
                    : num 0000010000...
                   : num 000000011...
## $ Mistlamps
## $ Sport_Model : num 0 0 0 1 0 0 0 0 1 1 ...
## $ Backseat_Divider: num 1 1 1 1 1 0 1 0 1 1 ...
## $ Metallic_Rim : num 0 0 0 0 0 1 1 1 1 ...
## $ Radio_cassette : num 0 0 0 0 1 0 0 0 0 ...
## $ Tow_Bar
                   : num 0000000000...
Creating models
library(neuralnet)
## Warning: package 'neuralnet' was built under R version 3.6.3
nmodel1 <- neuralnet(Price~. -Cylinders -Color -Fuel_Type -Model-Id,</pre>
                   data = training,
                   hidden=1,
                   threshold = 1,
                   learningrate.limit = NULL,
                   algorithm = "rprop+")
plot(nmodel1)
nmodel2 <- neuralnet(Price~. -Cylinders -Color -Fuel_Type -Model-Id,</pre>
                    data= training, hidden=1,
                   threshold = 0.1,
                   learningrate.limit = NULL,
                   algorithm = "rprop+")
plot(nmodel2)
nmodel3 <- neuralnet(Price~. -Cylinders -Color -Fuel_Type -Model-Id, data = training, hidden=1,</pre>
                   threshold = 0.05,
                   learningrate.limit = NULL,
                   algorithm = "rprop+")
plot(nmodel3)
nmodel4 <- neuralnet(Price~. -Cylinders -Color -Fuel_Type -Model-Id, data = training, hidden=1,
                   threshold = 0.01,
                   learningrate.limit = NULL,
                   algorithm = "rprop+")
plot(nmodel4)
nmodel5 <- neuralnet(Price~. -Cylinders -Color -Fuel_Type -Model-Id, data = training, hidden=1,
                   threshold = 0.005,
```

```
learningrate.limit = NULL,
                    algorithm = "rprop+")
plot(nmodel5)
nmodel6 <- neuralnet(Price~. -Cylinders -Color -Fuel_Type -Model-Id, data = training, hidden=1,</pre>
                    threshold = 0.001,
                    learningrate.limit = NULL,
                    algorithm = "rprop+")
plot(nmodel6)
nmodel7 <- neuralnet(Price~. -Cylinders -Color -Fuel_Type -Model-Id,</pre>
                    data = training, hidden=1,
                    threshold = 0.0001,
                    learningrate.limit = NULL,
                    algorithm = "rprop+")
## Warning: Algorithm did not converge in 1 of 1 repetition(s) within the stepmax.
output1 <- compute(nmodel1, training[,-3])</pre>
head(output1$net.result)
##
             [,1]
## [1,] 0.2261974
## [2,] 0.2261973
## [3,] 0.2261973
## [4,] 0.2261974
## [5,] 0.2261974
## [6,] 0.2261974
head(training[3,])
## # A tibble: 1 x 38
        Id Model Price Age_08_04 Mfg_Month Mfg_Year
##
                                                        KM Fuel_Type
                                                                        HP Met_Color
##
     <dbl> <chr> <dbl>
                           <dbl>
                                      <dbl>
                                               <dbl> <dbl> <fct>
                                                                     <dbl>
                                                                                <dbl>
## 1
         4 TOYO~ 0.377
                           0.316
                                      0.545
                                               0.667 0.198 Diesel
                                                                     0.171
## # ... with 28 more variables: Color <fct>, Automatic <dbl>, cc <dbl>,
       Doors <dbl>, Cylinders <dbl>, Gears <dbl>, Quarterly_Tax <dbl>,
## #
       Weight <dbl>, Mfr_Guarantee <dbl>, BOVAG_Guarantee <dbl>,
       Guarantee_Period <dbl>, ABS <dbl>, Airbag_1 <dbl>, Airbag_2 <dbl>,
## #
       Airco <dbl>, Automatic_airco <dbl>, Boardcomputer <dbl>, CD_Player <dbl>,
## #
## #
       Central_Lock <dbl>, Powered_Windows <dbl>, Power_Steering <dbl>,
       Radio <dbl>, Mistlamps <dbl>, Sport_Model <dbl>, Backseat_Divider <dbl>,
## #
## #
       Metallic_Rim <dbl>, Radio_cassette <dbl>, Tow_Bar <dbl>
library(caret)
## Warning: package 'caret' was built under R version 3.6.3
## Loading required package: lattice
```

```
## Loading required package: ggplot2
nmodel1.pred1 <- compute(nmodel1, training[,-3])</pre>
RMSE(nmodel1.pred1$net.result, training$Price)
## [1] 0.125237
nmodel2.pred2 <- compute(nmodel2, training[,-3])</pre>
RMSE(nmodel2.pred2$net.result, training$Price)
## [1] 0.03889802
nmodel3.pred3 <- compute(nmodel3, training[,-3])</pre>
RMSE(nmodel3.pred3$net.result, training$Price)
## [1] 0.03649143
nmodel4.pred4 <- compute(nmodel4, training[,-3])</pre>
RMSE(nmodel4.pred4$net.result, training$Price)
## [1] 0.03527904
nmodel4.pred4 <- compute(nmodel4, training[,-3])</pre>
RMSE(nmodel4.pred4$net.result, training$Price)
## [1] 0.03527904
nmodel5.pred5 <- compute(nmodel5, training[,-3])</pre>
RMSE(nmodel5.pred5$net.result, training$Price)
## [1] 0.03524061
nmodel6.pred6 <- compute(nmodel6, training[,-3])</pre>
RMSE(nmodel6.pred6$net.result, training$Price)
## [1] 0.03520978
#What happens to the RMS error (or Sum of Squares Error) for the training data as the value of threshold
The value of RMSE error decreases for the training data as the the value of threshold decreases from 1 to
0.0001
nmodel1.red1 <- compute(nmodel1, testing[,-3])</pre>
RMSE(nmodel1.red1$net.result, testing$Price)
```

[1] 0.1396461

```
nmodel2.red2 <- compute(nmodel2, testing[,-3])</pre>
RMSE(nmodel2.red2$net.result, testing$Price)
## [1] 0.04920632
nmodel3.red3 <- compute(nmodel3, testing[,-3])</pre>
RMSE(nmodel3.red3$net.result, testing$Price)
## [1] 0.04388745
nmodel4.red4 <- compute(nmodel4, testing[,-3])</pre>
RMSE(nmodel4.red4$net.result, testing$Price)
## [1] 0.04209523
nmodel5.red5 <- compute(nmodel5, testing[,-3])</pre>
RMSE(nmodel5.red5$net.result, testing$Price)
## [1] 0.04173473
nmodel6.red6 <- compute(nmodel6, testing[,-3])</pre>
RMSE(nmodel6.red6$net.result, testing$Price)
## [1] 0.04124369
#What happens to the RMS error Sum of Squares Error for the validation data?
The RMSE value decreases from model 1 to model 7. Hence, suggesting that there is a strong dependent
correlation\ between\ lowering\ threshold\ with\ that\ of\ RMSE\ value
nmodel5.1 <- neuralnet(Price~. -Cylinders -Color -Fuel_Type -Model-Id, data = training, hidden=1,</pre>
                     threshold = 0.005,
                     learningrate.limit = NULL,
                     algorithm = "rprop+")
plot(nmodel5.1)
nmodel5.2 <- neuralnet(Price~. -Cylinders -Color -Fuel_Type -Model-Id, data = training, hidden=2,
                     threshold = 0.005,
                     learningrate.limit = NULL,
                     algorithm = "rprop+")
plot(nmodel5)
nmodel5.3 <- neuralnet(Price~. -Cylinders -Color -Fuel_Type -Model-Id, data = training, hidden=4,
                     threshold = 0.005,
                     learningrate.limit = NULL,
                     algorithm = "rprop+")
plot(nmodel5)
```

```
nmodel5.4 <- neuralnet(Price~. -Cylinders -Color -Fuel_Type -Model-Id, data = training, hidden=8,
                     threshold = 0.005,
                     learningrate.limit = NULL,
                     algorithm = "rprop+")
plot(nmodel5)
nmodel5.1.pred5 <- compute(nmodel5.1, training[,-3])</pre>
RMSE(nmodel5.1.pred5$net.result, training$Price)
## [1] 0.03523865
nmodel5.1.red5 <- compute(nmodel5.1, testing[,-3])</pre>
RMSE(nmodel5.1.red5$net.result, testing$Price)
## [1] 0.04172574
nmodel5.2.pred5 <- compute(nmodel5.2, training[,-3])</pre>
RMSE(nmodel5.2.pred5$net.result, training$Price)
## [1] 0.03330954
nmodel5.2.red5 <- compute(nmodel5.2, testing[,-3])</pre>
RMSE(nmodel5.2.red5$net.result, testing$Price)
## [1] 0.04231841
nmodel5.3.pred5 <- compute(nmodel5.3, training[,-3])</pre>
RMSE(nmodel5.3.pred5$net.result, training$Price)
## [1] 0.03069817
nmodel5.3.red5 <- compute(nmodel5.3, testing[,-3])</pre>
RMSE(nmodel5.3.red5$net.result, testing$Price)
## [1] 0.0434862
nmodel5.4.pred5 <- compute(nmodel5.4, training[,-3])</pre>
RMSE(nmodel5.4.pred5$net.result, training$Price)
## [1] 0.02605389
nmodel5.4.red5 <- compute(nmodel5.4, testing[,-3])</pre>
RMSE(nmodel5.4.red5$net.result, testing$Price)
```

[1] 0.04761447

#Conduct an experiment to assess the effect of changing the number of hidden layer nodes (default 1), e.g., 1,2,4,8. The increase in hidden layer does not lead to decrease in RMSE value in testing data which is quite contradictory than that of the training data. This shows that increasing the number of hidden layers much more than the sufficient number of layers will cause accuracy in the test set to decrease. It causes the network to overfit to the training set, i.e., it will learn the training data, but it won't be able to generalize to new unseen data(testing data).

```
nmodel5.a <- neuralnet(Price~. -Cylinders -Color -Fuel_Type -Model-Id, data = training, hidden=c(2),
                    threshold = 0.005,
                    learningrate.limit = NULL,
                    learningrate.factor =
                         list(minus = 0.5, plus = 1.2),
                    algorithm = "rprop+")
plot(nmodel5)
nmodel5.b <- neuralnet(Price~. -Cylinders -Color -Fuel_Type -Model-Id, data = training, hidden=c(2,2),
                    threshold = 0.005,
                    learningrate.limit = NULL,
                    learningrate.factor =
                         list(minus = 0.5, plus = 1.2),
                    algorithm = "rprop+")
plot(nmodel5)
nmodel5.a.pred5 <- compute(nmodel5.a, training[,-3])</pre>
RMSE(nmodel5.a.pred5$net.result, training$Price)
## [1] 0.03359912
nmodel5.a.red5 <- compute(nmodel5.a, testing[,-3])
RMSE(nmodel5.a.red5$net.result, testing$Price)
## [1] 0.04041993
nmodel5.b.pred5 <- compute(nmodel5.b, training[,-3])</pre>
RMSE(nmodel5.b.pred5$net.result, training$Price)
## [1] 0.03245532
nmodel5.b.red5 <- compute(nmodel5.b, testing[,-3])</pre>
RMSE(nmodel5.b.red5$net.result, testing$Price)
```

[1] 0.04073952

#Conduct a similar experiment to assess the effect of changing the number of layers from 1 to 2 in the network.

#Neural network model capacity is controlled both by the number of nodes and the number of layers in the model. A model with a single hidden layer and sufficient number of nodes has the capability of learning any mapping function, but the chosen learning algorithm may or may not be able to realize this capability. Increasing the number of layers provides a short-cut to increasing the capacity of the model with fewer resources, and modern techniques allow learning algorithms to successfully train deep models. #Whether changing the number of layers from 1 to 2 in a network would be profitable or not depends on the data itself. As for this data, it is only decrementing the accuracy level sugguesting that the model has been overfitted.

```
nmodel11 <- neuralnet(Price~. -Cylinders -Color -Fuel_Type -Model-Id, data = training, hidden=1,</pre>
                     threshold = 1,
                     learningrate = 0.1,
                     algorithm = "rprop+")
plot(nmodel11)
nmodel12 <- neuralnet(Price~. -Cylinders -Color -Fuel_Type -Model-Id, data = training, hidden=1,
                     threshold = 1,
                     learningrate = 0.01,
                     algorithm = "rprop+")
plot(nmodel2)
nmodel13 <- neuralnet(Price~. -Cylinders -Color -Fuel_Type -Model-Id, data = training, hidden=1,
                     threshold = 1,
                     learningrate = 0.001,
                     algorithm = "rprop+")
plot(nmodel13)
nmodel11pred <- compute(nmodel11, training[,-3])</pre>
RMSE(nmodel11pred$net.result, training$Price)
## [1] 0.1252575
nmodel11red <- compute(nmodel11, testing[,-3])</pre>
RMSE(nmodel11red$net.result, testing$Price)
## [1] 0.139653
nmodel12pred <- compute(nmodel12, training[,-3])</pre>
RMSE(nmodel12pred$net.result, training$Price)
## [1] 0.1099406
nmodel12red <- compute(nmodel12, testing[,-3])</pre>
RMSE(nmodel12red$net.result, testing$Price)
## [1] 0.1242203
nmodel13pred <- compute(nmodel13, training[,-3])</pre>
RMSE(nmodel13pred$net.result, training$Price)
## [1] 0.08550215
nmodel13red <- compute(nmodel13, testing[,-3])</pre>
RMSE(nmodel13red$net.result, testing$Price)
```

[1] 0.09941224

"" #Study the effect of gradient descent step size (learning rate) on the training process and the network performance. #Dereasing learning rate means leaning to smaller steps (from model 1 to model 3), which is leading to decrement in RMSE value. A learning rate that is too large can cause the model to converge too quickly to a suboptimal solution, whereas a learning rate that is too small can cause the process to get stuck. Hence, the optimum solution lies in testing with sufficient number of epochs and then selecting the learning rate.