

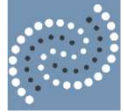
Анализ данных с использованием языка программирования R

Тема 6 Модели кластеризации данных

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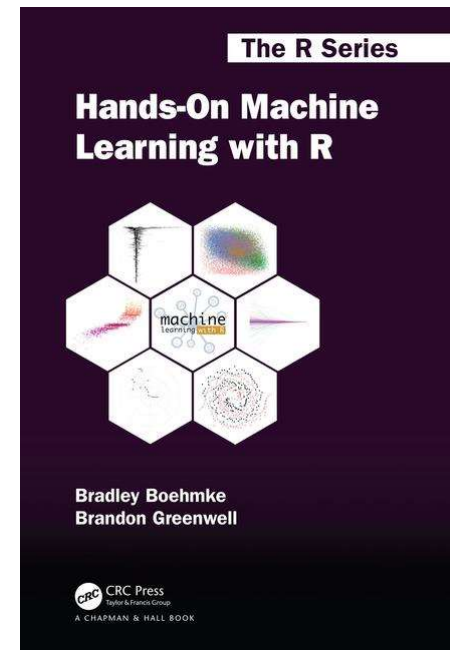


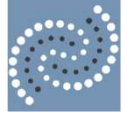
Reference

Hands-On Machine Learning with R

Bradley Boehmke & Brandon Greenwell

<https://bradleyboehmke.github.io/HOML/index.html>





Reference

Introduction to Machine Learning with R by Dr. Dimitrios Gouliermis

<http://www.mpia.de/homes/dgoulief/MLClasses/Course%20-%20Introduction%20to%20Machine%20Learning%20for%20Scientists%20with%20R.html>



Reference

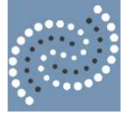


DataCamp

INTERACTIVE COURSE

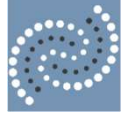
Introduction to Machine Learning

<https://learn.datacamp.com/courses/introduction-to-machine-learning-with-r>



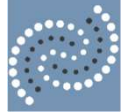
Supervised vs. Unsupervised Learning

Supervised		Unsupervised
Data: 1) n observations; 2) p variables X_1, X_2, \dots, X_p , measured on each observation; 3) response Y measured on same n observations		Data: 1) n observations; 2) p variables X_1, X_2, \dots, X_p , measured on each observation
Y		Clustering...
Continuous Regression	Discrete Classification	



Clustering, what?

- Cluster: collection of objects
 - *Similar* within cluster
 - *Dissimilar* between clusters
- Clustering: grouping objects in clusters
 - No labels: *unsupervised* classification
 - Plenty possible clusterings



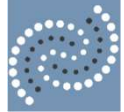
Clustering, why?

- Pattern Analysis
- Visualise Data
- pre-Processing Step
- Outlier Detection
- ...
- Targeted Marketing Programs
- Student Segmentations
- Data Mining
- ...



Clustering methods

- k-means
- Hierarchical (*many variations*)



Compactness and Separation

- Within Cluster Sums of Squares (WSS):

$$WSS = \sum_{i=1}^{N_C} \sum_{x \in C_i} d(\mathbf{x}, \bar{\mathbf{x}}_{C_i})^2$$

Measure of compactness

$\bar{\mathbf{x}}_{C_i}$	Cluster Centroid
\mathbf{x}	Object
C_i	Cluster
N_C	#Clusters



Minimise WSS

- Between Cluster Sums of Squares (BSS):

$$BSS = \sum_{i=1}^{N_C} |C_i| \cdot d(\bar{\mathbf{x}}_{C_i}, \bar{\mathbf{x}})^2$$

Measure of separation

$\bar{\mathbf{x}}_{C_i}$	Cluster Centroid
N_C	#Clusters
$ C_i $	#Objects In Cluster
$\bar{\mathbf{x}}$	Sample Mean



Maximise BSS

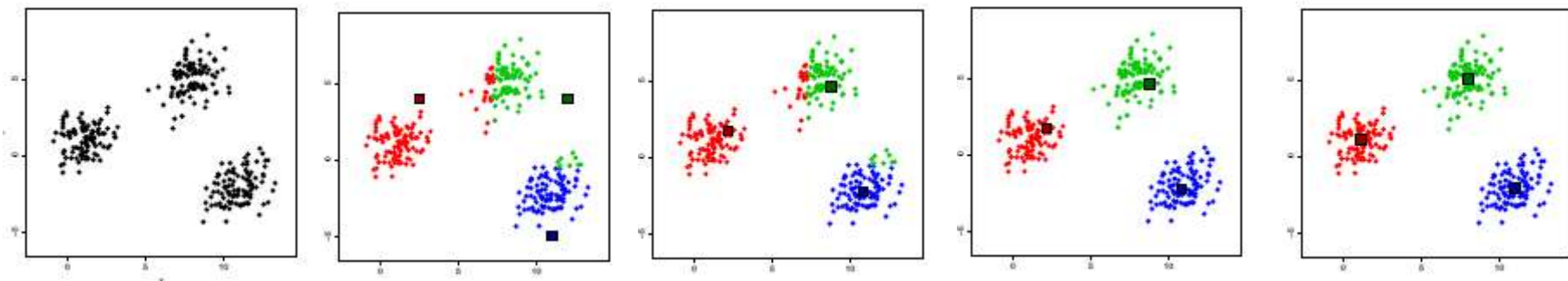


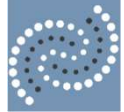
K-means algorithm

Goal: Partition data in k disjoint subsets

1. Randomly assign k centroids
2. Assign data to closest centroid
3. Moves centroids to *average* location
4. Repeat step 2 and 3

Let's take $k = 3$





Choosing k

- Goal: Find k that minimizes WSS
- Problem: WSS keeps decreasing as k increases!
- Solution: WSS starts decreasing slowly }
WSS / TSS < 0.2 } Fix k

$$TSS = WSS + BSS$$

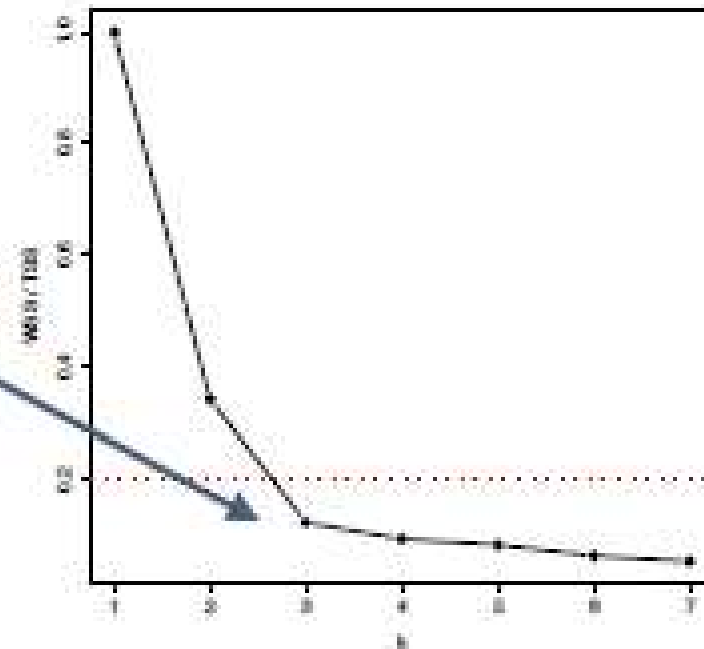


Choosing k: Scree Plot

Scree Plot: Visualizing the ratio WSS / TSS as function of k

Look for the *elbow* in the plot

Choose $k = 3$





K-means in R

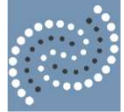
```
> my_km <- kmeans(data, centers, nstart)
```

- **centers:** Starting centroid or #clusters
- **nstart:** #times R restarts with different centroids

Distance: Euclidean metric

```
> my_km$tot.withinss ← WSS
```

```
> my_km$betweenss ← BSS
```



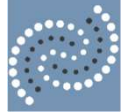
Cluster evaluation

Not trivial! There is no truth

- No true labels
- No true response

Evaluation methods? Depends on the goal

Goal: Compact and Separated ← Measurable!



Cluster measures

WSS and BSS: Good indication

Underlying idea:

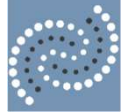
- Variance within clusters
- Separation between clusters



Compare

Alternative:

- Diameter
- Intercluster Distance



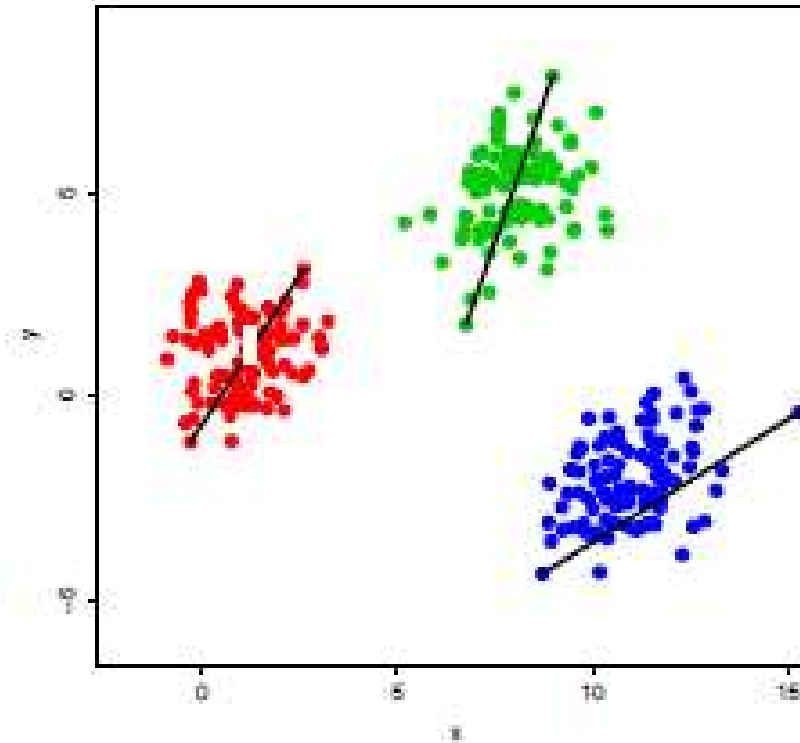
Diameter

$$\text{Dia}_i = \max_{x,y \in C_i} d(x,y)$$

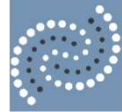
x, y : Objects

C_i : Cluster

d : Distance (objects)



Measure of Compactness



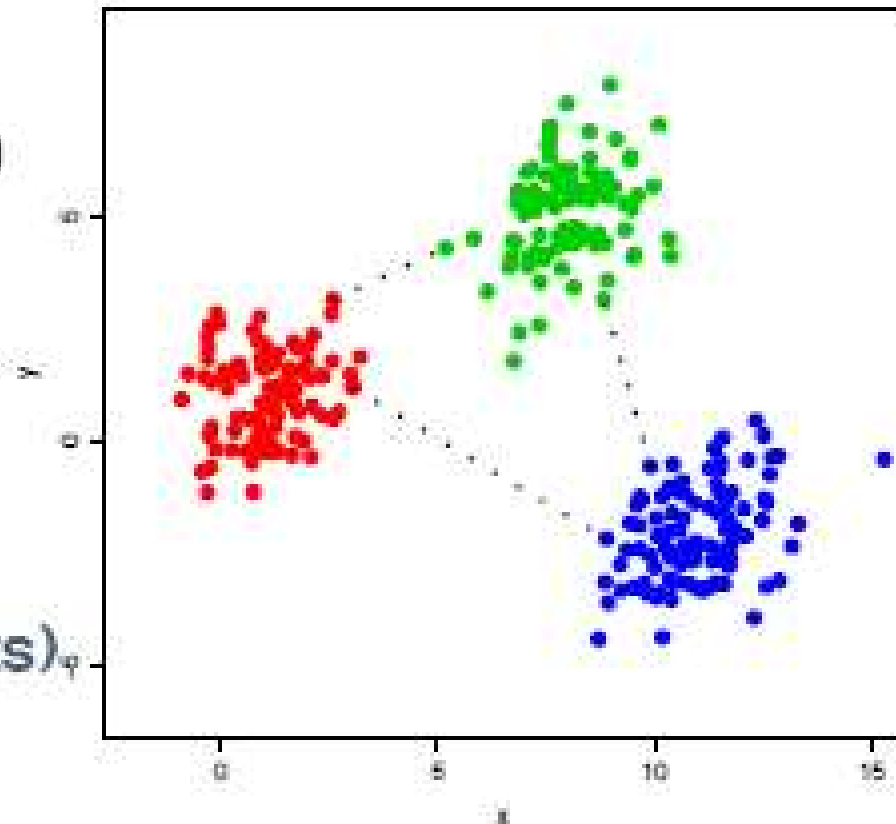
Intercluster distance

$$\delta(C_i, C_j) = \min_{x \in C_i, y \in C_j} d(x, y)$$

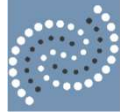
x, y : Objects

C_i, C_j : Clusters

d : Distance (objects)

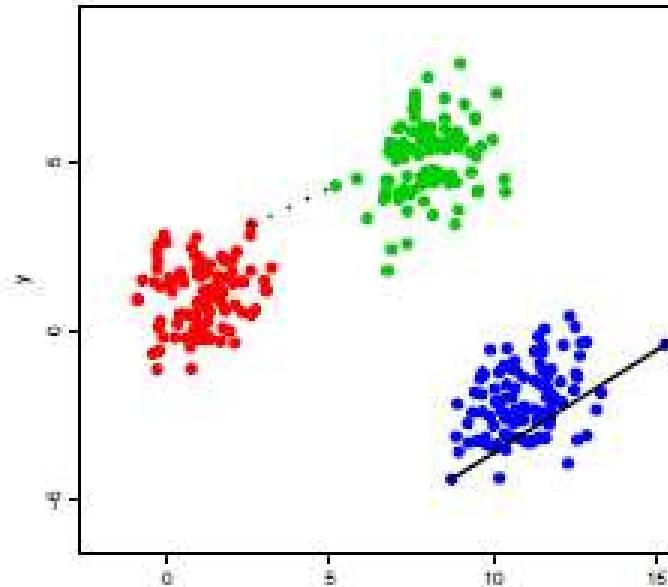


Measure of Separation



Dunn's index

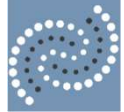
$$\frac{\min_{1 \leq i < j \leq k} \delta(C_i, C_j)}{\max_{1 \leq m \leq k} \text{Dia}_m}$$



Higher Dunn \longrightarrow Better separated / more compact

Notes:

- High computational cost
- Worst case indicator



Evaluating in R

Libraries: cluster and clValid

Dunn's Index:

```
> dunn(clusters = my_km, Data = ...)
```

- clusters: cluster partitioning vector
- Data: original dataset



Scale issues

Metrics are often scale dependent!

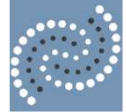
Which pair is most similar? (Age, Income, IQ)

- $X_1 = (28, 72000, 120)$
- $X_2 = (56, 73000, 80)$
- $X_3 = (29, 74500, 118)$



- Intuition: (X_1, X_3)
- Euclidean: (X_1, X_2)

Solution: Rescale income / 1000\$



Standardizing

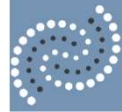
Problem: Multiple variables on different scales

Solution: Standardize your data

1. Subtract the mean
2. Divide by the standard deviation

```
> scale(data)
```

Note: Standardizing → Different interpretation



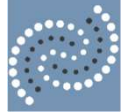
Hierarchical clustering

Hierarchy:

- Which objects cluster first?
- Which cluster pairs merge? When?

Bottom-up:

- Starts from the objects
- Builds a hierarchy of clusters

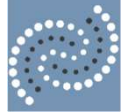


Linkage - methods

- Simple-Linkage: *minimal* distance between clusters
- Complete-Linkage: *maximal* distance between clusters
- Average-Linkage: *average* distance between clusters

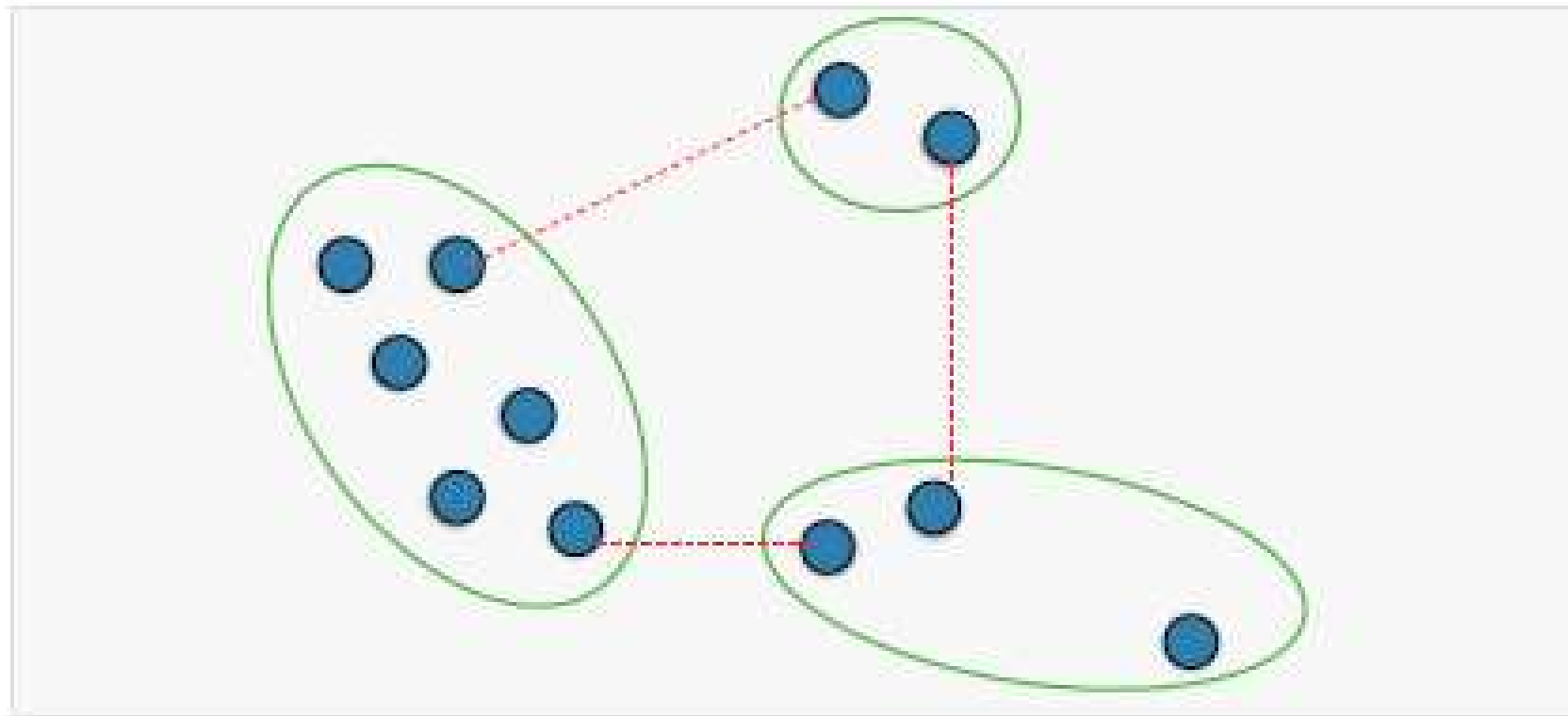


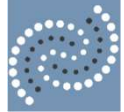
Different Clusterings



Simple - linkage

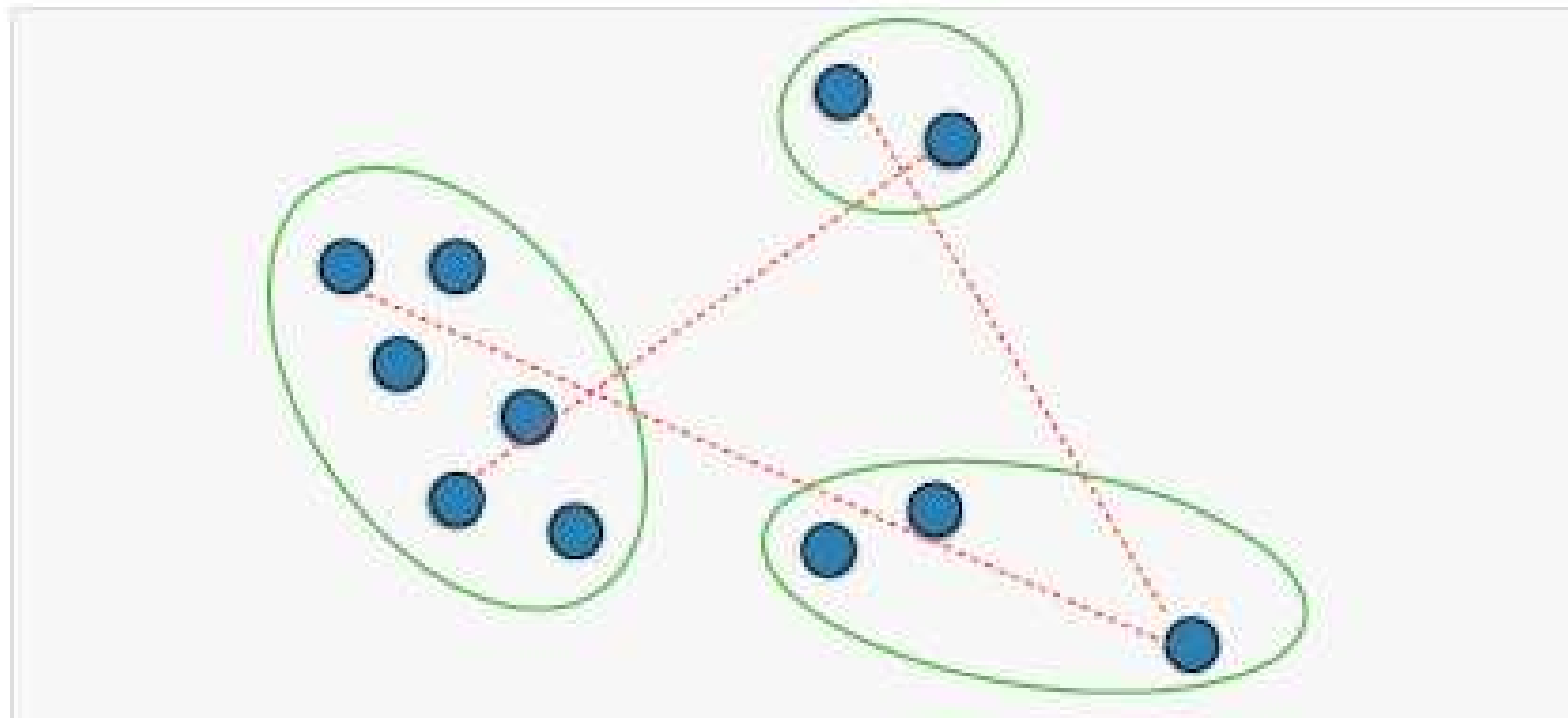
Minimal distance between objects in each clusters

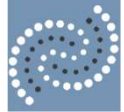




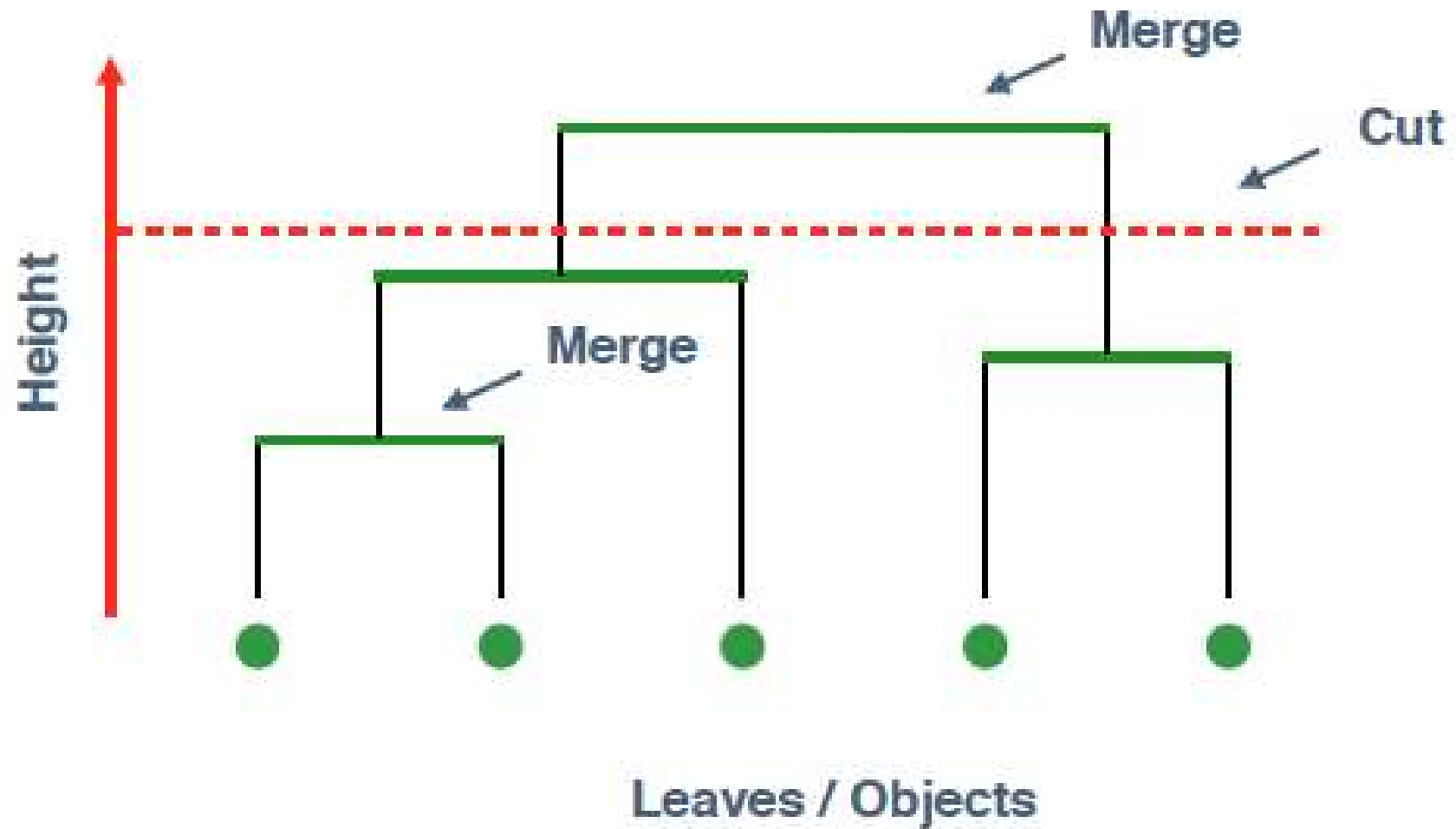
Complete - linkage

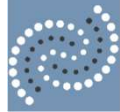
Maximal distance between objects in each cluster





Dendrogram





Hierarchical clustering in R

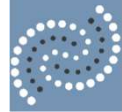
Library: stats

```
> dist(x, method)
```

- x: dataset
- method: distance

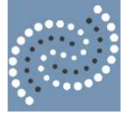
```
> hclust(d, method)
```

- d: distance matrix
- method: linkage



Hierarchical: Pro and Cons

- Pros
 - In-depth analysis
 - Linkage-methods → Different pattern
- Cons
 - High computational cost
 - Can never undo merges



k-means: Pro and Cons

- Pros
 - Can undo merges
 - Fast computations
- Cons
 - Fixed #Clusters
 - Dependent on starting centroids



Practise

clustering.R

Managed Independent Work

pr_clustering.R