

	t_1	t_2	t_3	t_4	t_5	t_6	t_7
VM_1	10	11	5	11	9	5	6
VM_2	8	11	11	6	11	11	8
VM_3	10	5	7	11	10	11	9

$Acc(t_i)$	9.33	9	7.67	9.33	10	9	7.67
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$$B\text{-level}(t_7) = Acc(t_7) = 7.67$$

$$B\text{-level}(t_6) = 9 + 18 + 7.67 = 34.67$$

$$B\text{-level}(t_4) = 9.33 + 12 + 7.67 = 29$$

$$B\text{-level}(t_5) = 10 + 14 + 7.67 = 31.67$$

$$\begin{aligned}
 B\text{-level}(t_2) &= \max \{ 9 + 14 + B\text{-level}(t_5), 9 + 8 + B\text{-level}(t_4) \} \\
 &= \max \{ 23 + 31.67, 17 + 29 \} \\
 &= \max \{ 54.67, 46 \} \\
 &= 54.67
 \end{aligned}$$

$$\begin{aligned}
 B\text{-level of } (t_3) &= \max \{ 7.67 + 13 + b\text{level of } (t_6), \\
 &\quad 7.67 + 16 + b\text{level of } (t_5) \} \\
 &= \max \{ 20.67 + 34.67, 23.67 + 31.67 \} \\
 &= \max \{ 55.34, 55.34 \} \\
 &\approx 55.34
 \end{aligned}$$

$$\begin{aligned}
 B\text{-level of } (t_1) &= \max \{ 9 + 9.33 + b\text{level of } (t_2), 9.33 + 15 + \\
 &\quad b\text{level of } (t_3) \} \\
 &= \max \{ 18.33 + 54.67, 24.33 + 55.34 \} \\
 &= \max \{ 73.00, 79.67 \} \\
 &= 79.67
 \end{aligned}$$

Task (i)	t_1	t_2	t_3	t_4	t_5	t_6	t_7
	79.67	54.67	55.34	29	31.67	34.67	7.67

Arrange in non-increasing order

$$t_1 > t_3 > t_2 > t_6 > t_5 > t_4 > t_7$$

Mapping

Order of execution of task

$$\begin{aligned}
 EST(t_1, VM_1) &= 0, \quad EST(t_1, VM_2) = 0, \\
 EST(t_7, VM_3) &= 0
 \end{aligned}$$

EFT (t_1)

$$\begin{aligned}
 EFT(t_1, VM_1) &= 0 + 10 = 10 \\
 EFT(t_1, VM_2) &= 0 + 8 = 8 \quad (\text{Best suited VM}) \\
 VM_3 &= 0 + 10 = 10
 \end{aligned}$$

$$\begin{aligned}
 EST(t_3, VM_1) &= \max \{ 0, 8 + 15 \} = 23 \\
 VM_2 &= \max \{ 8, 8 + 0 \} = 8 - \text{Best suited} \\
 VM_3 &= \max \{ 0, 8 + 15 \} = 23
 \end{aligned}$$

$$EFT(t_3, VM_1) = 23 + 5 = 28$$

$$EFT(t_3, VM_2) = 8 + 11 = 19 \quad \leftarrow \text{Best suited}$$

$$EFT(t_3, VM_3) = 23 + 7 = 30$$

$$EST(t_2, VM_1) = \max \{ 0, 8 + 9 \} = 17$$

$$= \max \{ 19, 8 + 0 \} = 19$$

$$= \max \{ 0, 8 + 9 \} = 17$$

$$EFT(t_2, VM_1) = 17 + 11 = 28$$

$$EFT(t_2, VM_2) = 19 + 11 = 30$$

$$EFT(t_2, VM_3) = 17 + 5 = 22 \quad \leftarrow \text{Best suit}$$

$$EST_1(t_6, VM_1) = \max \{ 0, 19 + 13 \} = 32$$

$$\max \{ 19, 19 + 0 \} = 19$$

$$\max \{ 22, 19 + 13 \} = 32$$

$$EFT(t_6, VM_1) = 32 + 5 = 37$$

$$EFT(t_6, VM_2) = 19 + 11 = 30 \quad \leftarrow \text{Best suited}$$

$$EFT(t_6, VM_3) = 32 + 11 = 43$$

$$EST(t_5, VM_1) = \max \{ 0, \max \{ 22 + 14, 19 + 16 \} \} = 36$$

$$= \max \{ 19, \max \{ 22 + 14, 19 + 0 \} \} = 36$$

$$= \max \{ 22, \max \{ 22 + 14, 19 + 16 \} \} = 36$$

$$EFT(t_5, VM_1) = 36 + 9 = 45 \quad \leftarrow \text{Best}$$

$$EFT(t_5, VM_2) = 36 + 11 = 47$$

$$EFT(t_5, VM_3) = 36 + 10 = 46$$

$$EST(t_4, VM_1) = \max \{ 45, 8 + 22 \} = 45$$

$$\max \{ 30, 8 + 22 \} = 30$$

$$\max \{ 22, 22 + 0 \} = 22$$

$$EFT(t_4, VM_1) = 45 + 11 = 56$$

$$EFT(t_4, VM_2) = 30 + 6 = 36$$

$$EFT(t_4, VM_3) = 22 + 11 = 33$$

Best suited
 t_5 t_4 t_3

$$EST(t_7, VM_1) = \max \begin{cases} 45, \max\{45+0, 33+12, 30+18\} \\ 30, \max\{45+14, 33+12, 30+0\} \\ 33, \max\{45+14, 33+0, 30+18\} \end{cases}$$

$$= \max \begin{cases} 45, \max\{45, 45, 48\} \\ 30, \max\{59, 45, 30\} \\ 33, \max\{59, 33, 48\} \end{cases}$$

$$EST(t_7, VM_1) = \max 48$$

$$EST(t_7, VM_2) = 59$$

$$EST(t_7, VM_3) = 59$$

$$EFT(t_7, VM_1) = 48 + 6 = 54$$

$$EFT(t_7, VM_2) = 59 + 8 = 67$$

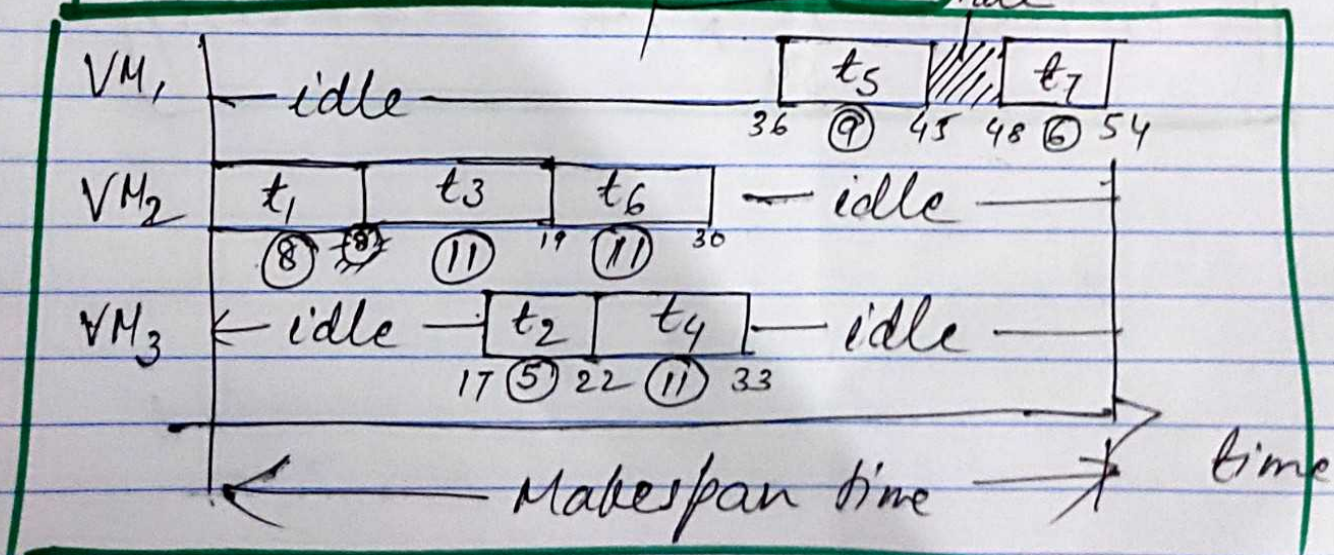
$$EFT(t_7, VM_3) = 59 + 9 = 68$$

Best suited

$$\text{Make span time} = \min \{ EFT(t_{exit}) \}$$

$$= 54$$

idle



GANTT Chart

$$U(VM_i) = \frac{\text{Working Hrs. of } VM_i}{\text{Makespan}} \times 100$$

$$\text{average utilization} = \frac{\text{Sum of all VM utilization}}{\text{Total No. of VM}}$$

$$\begin{aligned} \sum_{i=1}^n U(VM_i) &= U(VM_1) + U(VM_2) + U(VM_3) \\ \sum_{i=1}^n \frac{1}{VM_i} &= \frac{(9+6) + (8+11+11) + (5+11)}{54 \times 3} \\ &= \frac{15 + 30 + 16}{54 \times 3} \\ &= \frac{61}{162} \times 100 \end{aligned}$$

$$\text{Average Utilization} = \frac{61}{162} \times 100 = 37.65\%$$

$$U(VM_1) = \frac{15}{54} \times 100 = 27.78\%$$

$$U(VM_2) = \frac{30}{54} \times 100 = 55.55\%$$

$$U(VM_3) = \frac{16}{54} \times 100 = 29.63\%$$