



DAG/ workflow

ETC Matrix of 7 tasks against 3 VMs

	VM1	VM2	VM3
T1	7	9	8
T2	10	9	8
T3	6	5	9
T4	9	8	7
T5	6	7	5
T6	7	5	9
T7	8	9	7

Q8. Find the B-level Priority value of each tasks.

[1 Marks]

Q9. Find the t-level Priority value of each tasks.

[1 Marks]

Q10. Generate the overall schedule of all the 7 tasks on available 3 VMs as per the B-level priority value then calculate the **makespan** (overall workflow processing time) and **average VM utilization**.

[2+1+1 Marks]

Useful Formulas

I. $EST(T_i, VM_j) = 0$

II. $EST(T_i, VM_j) = \max \left\{ \underset{j \in \text{VM type}}{\text{avail } [j]}, \max_{T_p \in \text{pred}(T_i)} (AFT(T_i) + TT_{p,i}) \right\}$

Where, EST is the earliest start time of task T_i , T_p is the predecessor tasks set of T_i and $TT_{p,i}$ is the transfer time from T_p to T_i .

III. EFT is the earliest finish time which is defined as:

$EFT(T_i, VM_j) = ACC(T_i) + EST(T_i, VM_j)$

$makespan = \min \{ EFT (T_{exit}) \}$

Ans 8.

	t_1	t_2	t_3	t_4	t_5	t_6	t_7
Acc	8	9	6.66	8	6	7	8

$$B\text{-level}(t_1) = 8 + 0 = 8$$

$$B\text{-level}(t_6) = 7 + 11 + 8 = 26$$

$$B\text{-level}(t_5) = 6 + 9 + 8 = 23$$

$$B\text{-level}(t_4) = 8 + 26 + 8 = 42$$

$$B\text{-level}(t_3) = \max \left\{ \begin{array}{l} 6.66 + 6 + 23 \\ 6.66 + 9 + 26 \end{array} \right\} = 41.66$$

$$B\text{-level}(t_2) = 9 + 8 + 23 = 40$$

$$B\text{-level}(t_1) = \max \left\{ \begin{array}{l} 8 + 8 + 40 \\ 8 + 9 + 41.66 \\ 8 + 10 + 42 \end{array} \right\} = 56$$

B-level ~~priority~~ priority = $t_1, t_4, t_3, t_2, t_6, t_5, t_7$

ms9

	t_1	t_2	t_3	t_4	t_5	t_6	t_7
Acc	8	9	6.66	8	6	7	8

$$t \text{ level } (t_1) = 0$$

$$t \text{ level } (t_2) = 8 + 8 + 0 = 16$$

$$t \text{ level } (t_3) = 8 + 9 + 0 = 17$$

$$t \text{ level } (t_4) = 8 + 10 + 0 = 18$$

$$t \text{ level } (t_5) = \max \left\{ \begin{array}{l} 9 + 8 + 16 \\ 6.66 + 6 + 17 \end{array} \right\} = 33$$

$$t \text{ level } (t_6) = \max \left\{ \begin{array}{l} 6.66 + 9 + 17 \\ 8 + 8 + 18 \end{array} \right\} = 34$$

$$t \text{ level } (t_7) = \max \left\{ \begin{array}{l} 6 + 9 + 33 \\ 7 + 11 + 34 \end{array} \right\} = 52$$

$$\text{priority} = t_1, t_2, t_3, t_4, t_5, t_6, t_7$$

Ans 10. Priority level:-

$t_1, t_4, t_3, t_2, t_6, t_5, t_7$

$$EST(t_1) = VM_1 = 0$$

$$VM_2 = 0$$

$$VM_3 = 0$$

$$EFT(t_1) = \text{i) } 0 + 7 = \textcircled{7} - \text{Best possible}$$

$$\text{ii) } 0 + 9 = 9$$

$$\text{iii) } 0 + 8 = 8$$

Assign t_1 to VM_1

$$EST(t_4) = VM_1 = \max(7, 7+0) = 15$$

$$VM_2 = \max(0, 7+0) = \textcircled{7}$$

$$VM_3 = \max(0, 7+8) = 15$$

$$EFT(t_4) = \text{i) } 15 + 9 = 24$$

$$\text{ii) } 7 + 8 = \textcircled{15} \text{ Best possible}$$

$$\text{iii) } 15 + 7 = 22$$

Assign t_4 to VM

$$\begin{aligned} \text{EST}(t_4) &= \text{VM}_1 = \max(7, 7+0) = 7 \\ &\quad \text{VM}_2 = \max(0, 7+10) = 17 \\ &\quad \text{VM}_3 = \max(0, 7+10) = 17 \end{aligned}$$

$$\begin{aligned} \text{EFT}(t_4) &= \text{VM}_1 = 7+9 = 16 \quad \text{Best} \\ &\quad \text{VM}_2 = 17+8 = 25 \\ &\quad \text{VM}_3 = 17+7 = 24 \end{aligned}$$

Assign t_4 to VM_1

$$\begin{aligned} \text{EST}(t_5) &= \text{VM}_1 = \max(16, 7+0) = 16 \\ &\quad \text{VM}_2 = \max(0, 7+9) = 16 \\ &\quad \text{VM}_3 = \max(0, 7+9) = 16 \end{aligned}$$

$$\begin{aligned} \text{EFT}(t_5) &= \text{VM}_1 = 16+6 = 22 \\ &\quad \text{VM}_2 = 16+5 = 21 \quad \text{Best} \\ &\quad \text{VM}_3 = 16+9 = 25 \end{aligned}$$

Assign t_5 to VM_2

$$\begin{aligned} \text{EST}(t_6) &= \text{VM}_1 = \max(16, 7+0) = 16 \\ &\quad \text{VM}_2 = \max(21, 7+8) = 21 \\ &\quad \text{VM}_3 = \max(0, 7+8) = 15 \end{aligned}$$

$$\begin{aligned} \text{EFT}(t_6) &= \text{VM}_1 = 16+10 = 26 \\ &\quad \text{VM}_2 = 21+9 = 30 \\ &\quad \text{VM}_3 = 15+8 = 23 \quad \text{Best} \end{aligned}$$

Assign t_6 to VM_3

$$EST(t_6) \quad VM_1 = \max \left\{ \begin{array}{l} \max(16, 21+9) \\ \max(16, 16+8) \end{array} \right\} = 30$$

$$VM_2 = \max \left\{ \begin{array}{l} \max(21, 21+0) \\ \max(21, 16+8) \end{array} \right\} = 24$$

$$VM_3 = \max \left\{ \begin{array}{l} \max(23, 21+9) \\ \max(23, 16+8) \end{array} \right\} = 30$$

$$EFT(t_6) \quad VM_1 = 30 + 7 = 37$$

$$VM_2 = 24 + 5 = 29 - \text{Best}$$

$$VM_3 = 30 + 9 = 39$$

Assign VM_2 to t_6

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$$EST(t_5) \quad VM_1 = \max \left\{ \begin{array}{l} \max(16, 23+8) \\ \max(16, 21+6) \end{array} \right\} = 31$$

$$VM_2 = \max \left\{ \begin{array}{l} \max(29, 23+8) \\ \max(29, 21) \end{array} \right\} = 31$$

$$VM_3 = \max \left\{ \begin{array}{l} \max(23, 23) \\ \max(23, 21+6) \end{array} \right\} = 23$$

$$EFT(t_5) \quad VM_1 = 31 + 6 = 37$$

$$VM_2 = 31 + 7 = 38$$

$$VM_3 = 27 + 5 = 32$$

Assign VM_3 to t_5

Best

$$EST(t_7) = VM_1 = \max \left\{ \begin{array}{l} \max(16, 32+9) \\ \max(16, 29+11) \end{array} \right\} = 41$$

$$VM_2 = \max \left\{ \begin{array}{l} \max(29, 32+9) \\ \max(29, 29+0) \end{array} \right\} = 41$$

$$VM_3 = \max \left\{ \begin{array}{l} \max(32, 32+0) \\ \max(32, 29+11) \end{array} \right\} = 40$$

$$EST(t_7) = \begin{array}{l} 41 + 8 = 49 \\ 41 + 9 = 50 \\ 40 + 7 = 47 \end{array} \quad \text{Best}$$

assign VM_3 to t_7

makespan = 47 over all time.

Utilization $VM_1 = \frac{7+9}{47} \times 100 = 34.04\%$

$$VM_2 = \frac{10}{47} \times 100 = 21.27\%$$

$$VM_3 = \frac{8+5+7}{47} \times 100 = 42.25\%$$

$$\text{Average Utilisation} = \frac{34.04 + 21.27 + 42.25}{3}$$

$$= 32.62\%$$