

$$\lim_{x \rightarrow a} \frac{a^x - x^a}{\sqrt[3]{ax^2 - a \cos(x - a)}} =$$

4.

$$\begin{aligned} \lim_{x \rightarrow a} \frac{\log(x + \sqrt{x^2 - 4}) - \log(a + \sqrt{a^2 - 4})}{x - a} &= \lim_{x \rightarrow a} \left[\frac{\log\left(\frac{x + \sqrt{x^2 - 4}}{a + \sqrt{a^2 - 4}}\right)}{x - a} \right] \\ &= \frac{\log\left(1 + \frac{x + \sqrt{x^2 - 4} - a - \sqrt{a^2 - 4}}{a + \sqrt{a^2 - 4}}\right)}{x - a} = \frac{\log\left(1 + \frac{x - a}{a + \sqrt{a^2 - 4}} + \frac{x^2 - a^2}{(a + \sqrt{a^2 - 4})(\sqrt{a^2 - 4} + \sqrt{a^2 + 4})}\right)}{x - a} = \\ &= \frac{\frac{x - a}{\dots} + \frac{x - a}{\dots}(x + a) + 0(x - a)}{x - a} = \frac{1}{a + \sqrt{a^2 - 4}} \left(1 + \frac{2a}{2\sqrt{a^2 - 4}}\right) \end{aligned}$$

$$\left(\log(x + \sqrt{x^2 - 4})\right)' = \frac{1}{x + \sqrt{x^2 - 4}} \left(1 + \frac{2x}{2\sqrt{x^2 - 4}}\right)$$