Data Cube Computation Practice

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Start-Up Task

Assume a base suboid of four dimensions (**student**, **course**, **semester**, **lecturer**), contains only two base cells:

```
1. (a1, d2, d3, d4)
2. (d1, d2, c3, d4), where a1 \neq d1 and c3 \neq d3.
```

The measure of the cube is **tally**.

Question 1

How many non-empty cuboids will a full data cube contain?

If there are no hierarchies associated with each dimension, then the number of cuboids for a n-dimensional cuboids is the same as the number of non-empty cuboids in a full data cube. Therefore, the number of non-empty cuboids in a full data cube is $2^n = 2^4 = 16$, where n is the number of dimensions.

Question 2

How many closed cells are in the full cube?

There are three (3) closed cells in the full cube - the two base cells and (*, d2, *, d4)

Recall and review quiz

Consider a data cube with four dimensions (**subject**, **lecturer**, **time** and **student**), and the measure **count**. Given the following four cells:

```
a = (CP5806, *, *, *, *, 480)
b = (CP5806, *, 2018, *, 120)
c = (CP5806, Ickjai Lee, 2018, *, 10)
d = (CP5806, Ickjai Lee, 2018, Michael Jordan, 2)
```

Question 1

```
Cell b is a ?
```

2-D cell as exactly two (2) out of the four dimensions are not * (aggregated).

Question 2

which is the base cell?

d, which is a 4-D cell as it doesn't contain any aggregation.

Question 3

The cell \mathbf{a} is of the cell \mathbf{c} .

Cell **a** is a 1-D cell and cell **c** is a 3-D cell, which means that cell **a** is higher up in the lattice of cuboids. Therefore, cell **a** is an **ancestor** of cell **c**. It cannot be a parent as there is a layer in the lattice separating the two cells.

Question 4

Which cell is the parent of cell **c**?

 \mathbf{b} , as it is a 2-D cell and \mathbf{c} is a 3-D cell.

Question 5

If the minimum support for iceberg cube materialisation is set to 10, then is cell \mathbf{c} materialised?

Yes, as the usual condition would be having count(*) >= min sup

Question 6

Is the cell \mathbf{c} a closed cell?

No.

A cell is a closed cell if there is no descendent such that a *-value can be replaced by a non-* value and the descendent has the same measure value.

Now consider a base cuboid of 10 dimensions that contains only three base cells:

- 1. $(a1, d2, d3, d4, \dots, d9, d10)$
- 2. $(d1, b2, d3, d4, \dots, d9, d10)$
- 3. (d1, d2, c3, d4, ..., d9, d10), where $a1 \neq d1, b2 \neq d2$ and $c3 \neq d3$.

The measure of the cube is **count**.

Question 7

How many non-empty cuboids will a full data cube contain?

If there are no hierarchies associated with each dimension, then the number of cuboids for a n-dimensional cuboids is the same as the number of non-empty cuboids in a full data cube. Therefore, the number of non-empty cuboids in a full data cube is $2^n = 2^{10} = 1024$, where n is the number of dimensions.

Question 8

How many non-empty aggregate cells will an iceberg cube contain if the condition of the iceberg cube is $count \ge 2$?

Aggregate cells are any cell from a non-base cuboid. Those cells aggregate over one or more dimensions, which are denoted by * in the cell notation. Each cell generates 2n-1 non-empty aggregate cells, so in this case there are $3 \times (2 \times 10 - 1) = 3(2 \times 10) - 3) = 3069$ non-aggregate cells.

 $2^{n-1} * (m+1)^{n+1}$ cells in a lattice of cuboids