

Exercise 1: ROC metrics

Given are the results of a scoring algorithm and the associated *true* classes of 10 observations:

ID	True class	Score
1	0	0.33
2	0	0.27
3	0	0.11
4	1	0.38
5	1	0.17
6	1	0.63
7	1	0.62
8	1	0.33
9	0	0.15
10	0	0.57

- a) Create a confusion matrix assuming the decision boundary at 0.5.
- b) Calculate: PPV, TPR, NPV, TNR, ACC, MCE and $F1$ measure.
- c) Draw the ROC curve and interpret it. Feel free to use R for the drawing.
- d) Calculate the AUC.
- e) How would the ROC curve change if you had chosen a different threshold in a)?

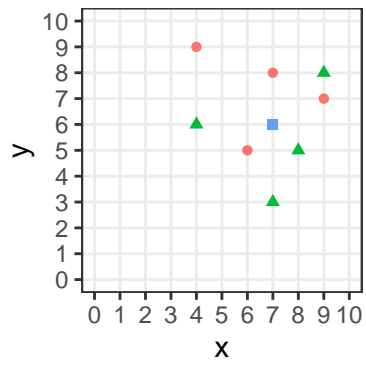
Exercise 2: k -NN

- a) Let the two-dimensional feature vectors in the following figure be instances of two different classes (triangles and circles). Classify the point (7, 6) – represented by a square in the picture – with a k -NN classifier using $L1$ norm (Manhattan distance):

$$d_{\text{Manhattan}}(\mathbf{x}, \tilde{\mathbf{x}}) = \sum_{j=1}^p |x_j - \tilde{x}_j|.$$

As a decision rule, use the unweighted number of the individual classes in the k -neighborhood, i.e., assign the point to the class that represents most neighbors.

- i) $k = 3$
- ii) $k = 5$
- iii) $k = 7$



- b) Now consider the same constellation but assume a regression problem this time, where the circle-shaped points have a target value of 2 and the triangles have a value of 4.

Again, predict for the square point (7, 9), using both the *unweighted* and the *weighted* mean in the neighborhood (still with Manhattan distance).

- i) $k = 3$
- ii) $k = 5$
- iii) $k = 7$