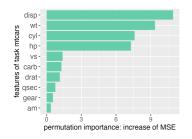
Introduction to Machine Learning

Random Forest Feature Importance





Learning goals

- Understand that the goal of feature importance is to enhance interpretability of RF
- Understand FI based on feature permutation
- Understand FI based on improvement in splits

PERMUTATION FEATURE IMPORTANCE

RFs improve accuracy by aggregating multiple decision trees but **lose interpretability** compared to a single tree. **Feature importance** mitigates this problem.

- How much does performance decrease, if feature is removed / rendered useless?
- We permute values of considered feature
- Removes association between feature and target, keeps marginal distribution
- Can obtain GE of RF (without and with permuted features) by predicting OOB data, to efficiently compute FI during training
- Avoids not only new models (if feature would be removed) but can already use "OOB test data" during training

ID	Color	Form	Origin	Length	Banana
1	yellow	round	domestic	10	no
2	brown	oblong	imported	11	yes
3	green	oblong	imported	19	yes
4	yellow	oblong	domestic	14	yes



PERMUTATION IMPORTANCE

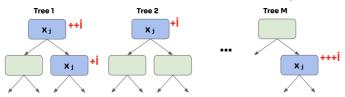
Tree 1	ID		Length	Banana	ĥ(x)	Tree 1	ID		Length	Banana	ĥ(x)
	1		10	no	1		1		11	no	1
	2		11	yes	yes		2		19	yes	no
	3		19	yes	1		3		14	yes	1
	4		14	yes	1	permutation of	4		10	yes	1
feature Length											
	ID		Length	Banana	ĥ(x)	/	ID		Length	Banana	ĥ(x)
Tree M	1		10	no	1	Tree M	1		11	no	1
	2		11	yes	1		2		19	yes	1
	3		19	yes	yes		3		14	yes	yes
	4		14	yes	yes		4		10	yes	no



- 1: Calculate $\widehat{\mathrm{GE}}_{\mathsf{OOB}}$ using set-based metric ho
- 2: **for** features x_j , $j = 1 \rightarrow p$ **do**
- 3: **for** Some statistical repetitions **do**
- 4: Distort feature-target relation: permute x_i with ψ_i
- 5: Compute all *n* OOB-predictions for permuted feature data, obtain all $\hat{f}_{OOB,\psi_i}^{(i)}$
- 6: Arrange predictions in $\hat{\mathbf{F}}_{OOB,\psi_i}$; Compute $\widehat{GE}_{OOB,j} = \rho(\mathbf{y}, \hat{\mathbf{F}}_{OOB,\psi_i})$
- 7: Estimate importance of *j*-th feature: $\widehat{\mathsf{Fl}_j} = \widehat{\mathrm{GE}}_{\mathsf{OOB},j} \widehat{\mathrm{GE}}_{\mathsf{OOB}}$
- 8: end for
- 9: Average obtained \widehat{FI}_j values over reps
- 10: end for

IMPURITY IMPORTANCE

Alternative: Add up all *improvements* in splits where feature x_i is used.

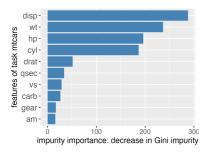


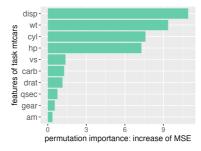


- 1: **for** features x_j , $j = 1 \rightarrow p$ **do**
- 2: **for** all models $\hat{b}^{[m]}$, $m=1 \rightarrow M$ **do**
- 3: Find all splits in $\hat{b}^{[m]}$ on x_i
- 4: Extract improvement / risk reduction for these splits
- 5: Sum them up
- 6: end for
- 7: Add up improvements over all trees for FI of x_i
- 8: end for

IN PRACTICE / OUTLOOK

Let's compare both FI variants on mtcars:







- Both methods are biased toward features with more levels (i.e., continuous or categoricals with many categories) ► Strobl et al. 2007
- More advanced versions exist
- PFI and FI have been generalized, see our lecture on IML!