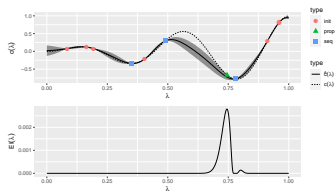


Introduction to Machine Learning

Hyperparameter Tuning - Advanced Tuning Techniques

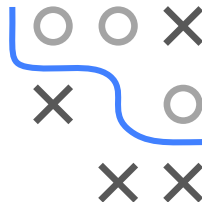
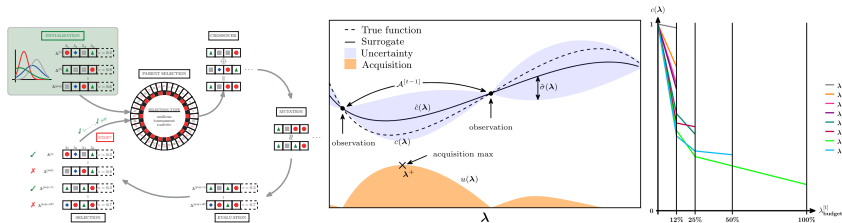


Learning goals

- Basic idea of evolutionary algorithms
- and Bayesian Optimization
- and hyperband

HPO – MANY APPROACHES

- Evolutionary algorithms
- Bayesian / model-based optimization
- Multi-fidelity optimization, e.g. Hyperband



HPO methods can be characterized by:

- how the exploration vs. exploitation trade-off is handled
- how the inference vs. search trade-off is handled

Further aspects: Parallelizability, local vs. global behavior, handling of noisy observations, multifidelity and search space complexity.

BAYESIAN OPTIMIZATION

BO sequentially iterates:

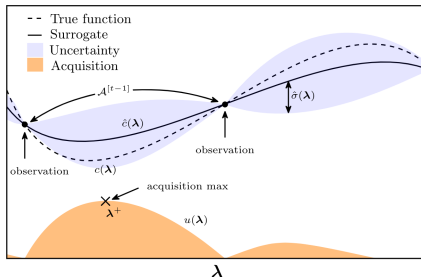
- 1 **Approximate** $\lambda \mapsto c(\lambda)$
by (nonlin) regression
model $\hat{c}(\lambda)$, from
evaluated configurations
(archive)

Important trade-off: **Exploration** (evaluate candidates in under-explored areas) vs. **exploitation** (search near promising areas)

BAYESIAN OPTIMIZATION

Surrogate Model:

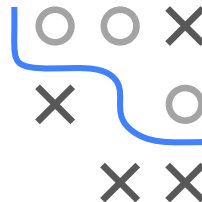
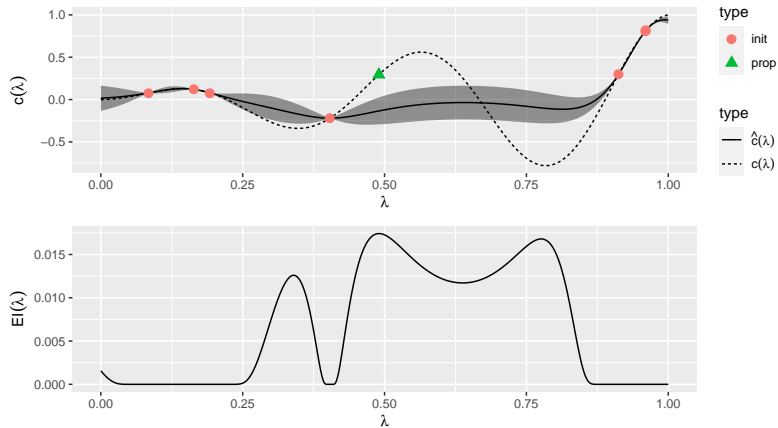
- Probabilistic modeling of $C(\lambda) \sim (\hat{c}(\lambda), \hat{\sigma}(\lambda))$ with posterior mean $\hat{c}(\lambda)$ and uncertainty $\hat{\sigma}(\lambda)$.
- Typical choices for numeric spaces are Gaussian Processes; random forests for mixed spaces



Acquisition Function:

- Balance exploration (high $\hat{\sigma}$) vs. exploitation (low \hat{c}).
- Lower confidence bound (LCB): $a(\lambda) = \hat{c}(\lambda) - \kappa \cdot \hat{\sigma}(\lambda)$
- Expected improvement (EI): $a(\lambda) = \mathbb{E} [\max \{c_{\min} - C(\lambda), 0\}]$
where (c_{\min} is best cost value from archive)
- Optimizing $a(\lambda)$ is still difficult, but cheap(er)

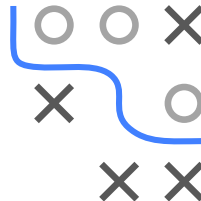
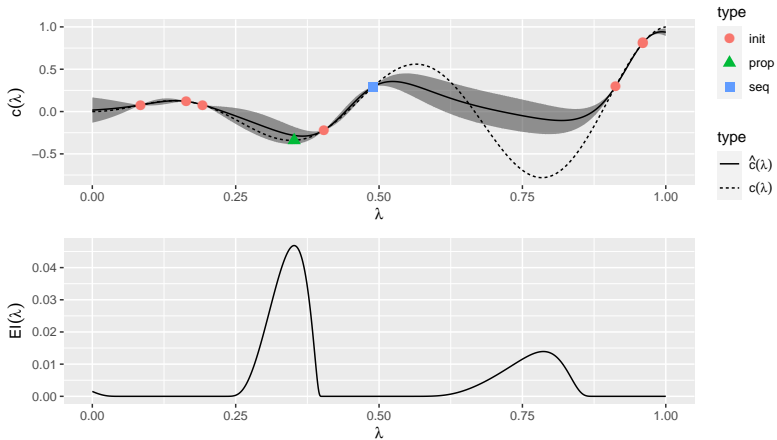
BAYESIAN OPTIMIZATION



Upper plot: The surrogate model (black, solid) models the *unknown* relationship between input and output (black, dashed) based on the initial design (red points).

Lower plot: Mean and variance of the surrogate model are used to derive the expected improvement (EI) criterion. The point that maximizes the EI is proposed (green point).

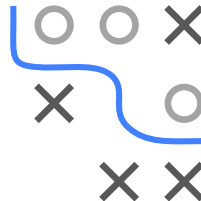
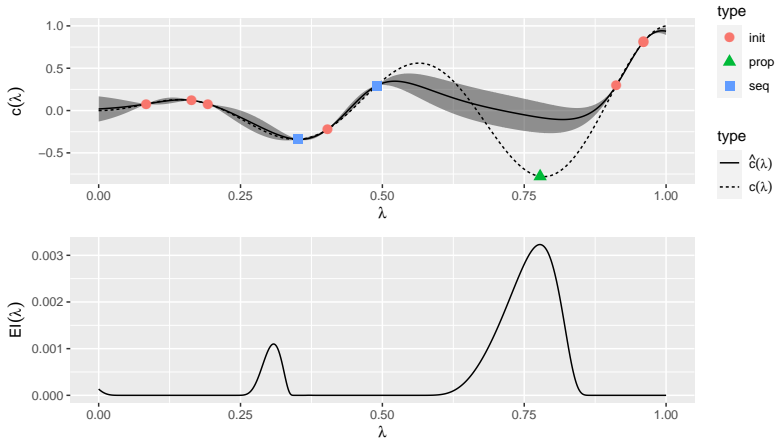
BAYESIAN OPTIMIZATION



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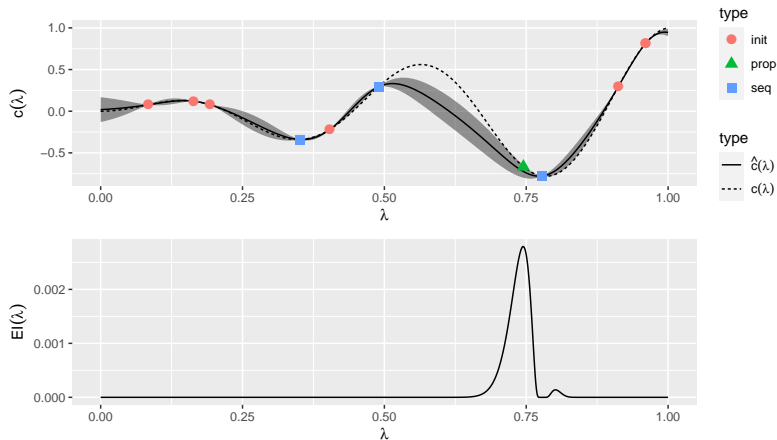
BAYESIAN OPTIMIZATION



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BAYESIAN OPTIMIZATION



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Lower plot: Mean and variance of the surrogate model are used to derive the expected improvement (EI) criterion. The point that maximizes the EI is proposed (green point).

BAYESIAN OPTIMIZATION / 2

Since we use the sequentially updated surrogate model predictions of performance to propose new configurations, we are guided to “interesting” regions of Λ and avoid irrelevant evaluations:

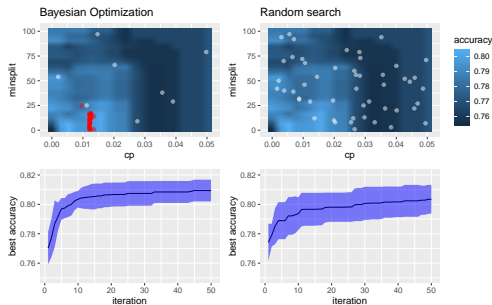
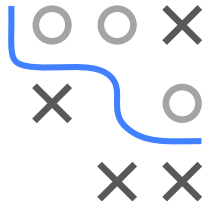
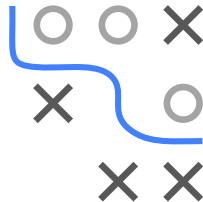


Figure: Tuning complexity and minimal node size for splits for CART on the titanic data (10-fold CV maximizing accuracy).

Left panel: BO, 50 configurations; right panel: random search, 50 iterations.

Top panel: one run (initial design of BO is white); bottom panel: mean \pm std of 10 runs.

BAYESIAN OPTIMIZATION / 3



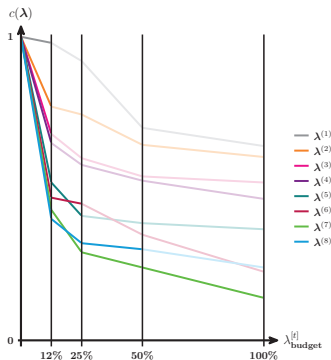
MULTIFIDELITY OPTIMIZATION

- Prerequisite: Fidelity HP λ_{fid} , i.e., a component of λ , which influences the computational cost of the fitting procedure in a monotonically increasing manner
- Methods of multifidelity optimization in HPO are all tuning approaches that can efficiently handle a \mathcal{I} with a HP λ_{fid}
- The lower we set λ_{fid} , the more points we can explore in our search space, albeit with much less reliable information w.r.t. their true performance.
- We assume to know box-constraints of λ_{fid} , so $\lambda_{\text{fid}} \in [\lambda_{\text{fid}}^{\text{low}}, \lambda_{\text{fid}}^{\text{upp}}]$, where the upper limit implies the highest fidelity returning values closest to the true objective value at the highest computational cost.



SUCCESSIVE HALVING

- Races down set of HPCs to the best
- Idea: Discard bad configurations early
- Train HPCs with fraction of full budget (SGD epochs, training set size); the control param for this is called **multi-fidelity HP**
- Continue with better $1/\eta$ fraction of HPCs (w.r.t \widehat{GE}); with η times budget (usually $\eta = 2, 3$)
- Repeat until budget depleted or single HPC remains



MULTIFIDELITY OPTIMIZATION – HYPERBAND

Problem with SH

- Good HPCs could be killed off too early, depends on evaluation schedule

Solution: Hyperband

- Repeat SH with different start budgets $\lambda_{\text{fid}}^{[0]}$ and initial number of HPCs $p^{[0]}$
- Each SH run is called bracket
- Each bracket consumes ca. the same budget

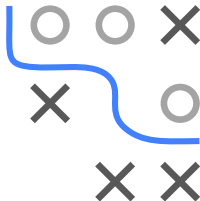
For $\eta = 4$

bracket 3		
t	$\lambda_{\text{fid}}^{[t]}$	$p_3^{[t]}$
0	1	82
1	4	20
2	16	5
3	64	1

	bracket 2	
t	$\lambda_{\text{fid}}^{[t]}$	$p_2^{[t]}$
0	4	27
1	16	6
2	64	1

bracket 1		
t	$\lambda_{\text{fid}}^{[t]}$	$p_1^{[t]}$
0	16	10
1	64	2

bracket 0		
t	$\lambda_{\text{fid}}^{[t]}$	$p_0^{[t]}$
0	64	5



MORE TUNING ALGORITHMS:

Other advanced techniques besides model-based optimization and the hyperband algorithm are:

- Stochastic local search, e.g., simulated annealing
- Genetic algorithms / CMAES
- Iterated F-Racing
- Many more . . .

For more information see *Hyperparameter Optimization: Foundations, Algorithms, Best Practices and Open Challenges*, Bischl (2021)

