# **Introduction to Machine Learning**

# Random Forest Basics





#### Learning goals

- Know how random forests are defined by extending the idea of bagging
- Understand general idea to decorrelate trees
- Understand effects of hyperparameters
- RFs and overfitting

#### **MOTIVATION**

CARTs offer several appealing features:

- Interpretability: Easy to understand and explain
- Invariance to rank-preserving transformations:
  E.g., unaffected by scaling or shifting of features
- Versatility: Work on categorical and numerical data
- Robustness to missing values: Can work with missings



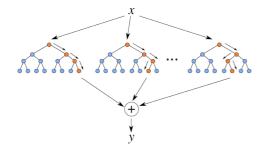
Despite these benefits, CARTs are not without drawbacks:

► Hastie, Tibshirani, and Friedman 2009

"Trees have one aspect that prevents them from being the ideal tool for predictive learning, namely inaccuracy."

# RANDOM FORESTS • Breiman 2001

- RFs use bagging with CARTs as BLs
- Random feature sampling decorrelates the base learners
- Fully expanded trees further increase variability of trees



Introduction to Machine Learning - 2 / 11



## INTUITION BEHIND DECORRELATION

- Since bootstrap samples are similar, models  $\hat{b}^{[m]}$  are correlated, affecting the variance of an ensemble  $\hat{f}$
- We would like variance to go down linearly with ensemble size, but because of correlation we cannot really expect that
- Assuming  $Var(\hat{b}^{[m]}) = \sigma^2$ ,  $Corr(\hat{b}^{[m]}, \hat{b}^{[j]}) = \rho$ , semi-formal analysis, without proper analysis of prediction error:

$$\operatorname{Var}\left(\hat{f}\right) = \operatorname{Var}\left(\frac{1}{M} \sum_{m=1}^{M} \hat{b}^{[m]}\right) = \frac{1}{M^{2}} \left(\sum_{m=1}^{M} \operatorname{Var}(\hat{b}^{[m]}) + 2\sum_{m < j} \operatorname{Cov}(\hat{b}^{[m]}, \hat{b}^{[j]})\right)$$
$$= \frac{1}{M^{2}} \left(M\sigma^{2} + 2\frac{M(M-1)}{2}\rho\sigma^{2}\right) = (1-\rho)\frac{\sigma^{2}}{M} + \rho\sigma^{2}$$

- Ensemble variance is "convex-combo of linear-reduction and no-reduction, controlled by  $\rho$ "
- Maybe we can decorrelate trees, to reduce ensemble variance?
  And get less prediction error?



#### RANDOM FEATURE SAMPLING

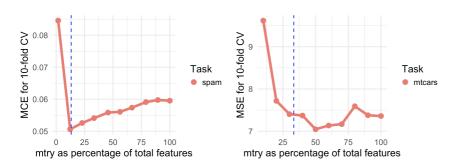
RFs decorrelate trees with a simple randomization:

- For each node of tree, randomly draw mtry ≤ p features (mtry = name in some implementations)
- Only consider these features for finding the best split
- Careful: Our previous analysis was simplified! The more we decorrelate by this, the more random the trees become! This also has negative effects!





## **EFFECT OF FEATURE SAMPLING**



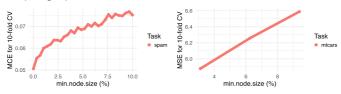


- Optimal mtry typically larger for regression than for classification
- Good defaults exist, but still most relevant tuning param
- Rule of thumb:
  - ullet Classification:  $\mathtt{mtry} = \lfloor \sqrt{p} \rfloor$
  - Regression:  $mtry = \lfloor p/3 \rfloor$

#### TREE SIZE

In addition to mtry, RFs have two other important HPs:

Min. nr. of obs. in each decision tree node
 Default (ranger): min.node.size = 5



× COO X

- Depth of each tree Default (ranger):  $maxDepth = \infty$
- There are more alternative HPs to control depth of tree: minimal risk reduction, size of terminal nodes, etc.

RF usually use fully expanded trees, without aggressive early stopping or pruning, to further increase variability of each tree. • Louppe 2015

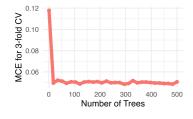
#### **ENSEMBLE SIZE**

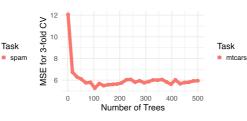
- RFs usually better if ensemble is large
- But: Increases computational costs, and diminishing returns

Task

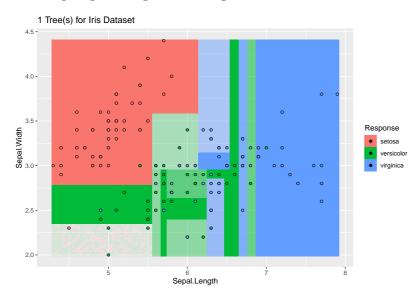
- 100 or 500 is a sensible default
- Can also inspect the OOB error (see later)





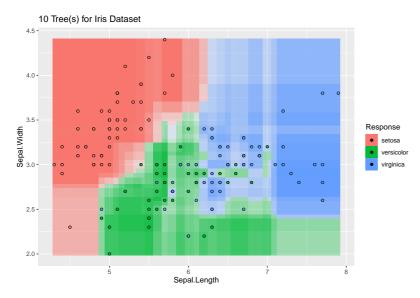


# **EFFECT OF ENSEMBLE SIZE**



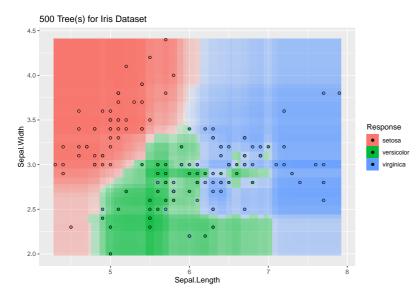


# **EFFECT OF ENSEMBLE SIZE**





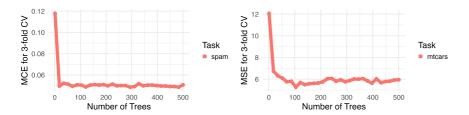
# **EFFECT OF ENSEMBLE SIZE**





# CAN RF OVERFIT? Probst and Boulesteix 2018

- Just like any other learner, RFs can overfit!
- However, RFs generally less prone to overfitting than individual CARTs.
- Overly complex trees can still lead to overfitting!
  If most trees capture noise, so does the RF.
- But randomization and averaging helps.

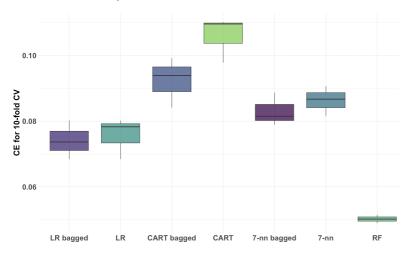


Since each tree is trained *individually* and without knowledge of previously trained trees, increasing ntrees generally reduces variance without increasing the chance of overfitting!



#### **RF IN PRACTICE**

Benchmarking bagged ensembles with 100 BLs each on spam versus RF (ntrees = 100, mtry =  $\sqrt{p}$ , minnode = 1), we see how well RF performs!





#### DISCUSSION

#### Advantages:

- Most advantages of trees also apply to RF: not much preprocessing required, missing value handling, etc.
- Easy to parallelize
- Often work well (enough)
- Works well on high-dimensional data
- Works well on data with irrelevant "noise" variables

#### Disadvantages:

- Same extrapolation problem as for trees
- Harder to interpret than trees (but many extra tools are nowadays available for interpreting RFs)
- Implementation can be memory-hungry
- Prediction can be computationally demanding for large ensembles

Introduction to Machine Learning - 11 / 11

