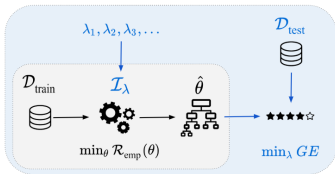
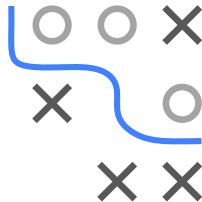


# Introduction to Machine Learning

## Hyperparameter Tuning - Problem Definition



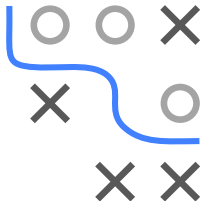
### Learning goals

- Definition of HPO objective and components
- Understand its properties
- What makes tuning challenging

# HYPERPARAMETER OPTIMIZATION

**Hyperparameters (HP)**  $\lambda$  are parameters that are *inputs* to learner  $\mathcal{I}$  which performs ERM on training data set to find optimal **model parameters**  $\theta$ . HPs can influence the generalization performance in a non-trivial and subtle way.

**Hyperparameter optimization (HPO) / Tuning** is the process of finding a well-performing hyperparameter configuration (HPC)  $\lambda \in \tilde{\Lambda}$  for an learner  $\mathcal{I}_\lambda$ .



# OBJECTIVE AND SEARCH SPACE

Search space  $\tilde{\Lambda} \subset \Lambda$  with all optimized HPs and ranges:

$$\tilde{\Lambda} = \tilde{\Lambda}_1 \times \tilde{\Lambda}_2 \times \cdots \times \tilde{\Lambda}_I$$

where  $\tilde{\Lambda}_i$  is a bounded subset of the domain of the  $i$ -th HP  $\Lambda_i$ , and can be either continuous, discrete, or categorical.



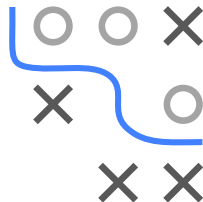
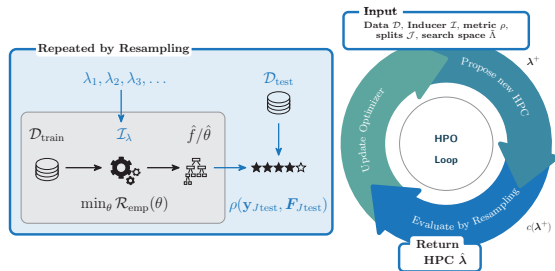
The general HPO problem is defined as:

$$\lambda^* \in \arg \min_{\lambda \in \tilde{\Lambda}} c(\lambda) = \arg \min_{\lambda \in \tilde{\Lambda}} \widehat{\text{GE}}(\mathcal{I}, \mathcal{J}, \rho, \lambda)$$

with  $\lambda^*$  as theoretical optimum, and  $c(\lambda)$  is short for estim. gen. error when  $\mathcal{I}$ , resampling splits  $\mathcal{J}$ , performance measure  $\rho$  are fixed.

# OBJECTIVE AND SEARCH SPACE

$$\lambda^* \in \arg \min_{\lambda \in \tilde{\Lambda}} c(\lambda) = \arg \min_{\lambda \in \tilde{\Lambda}} \widehat{GE}(\mathcal{I}, \mathcal{J}, \rho, \lambda)$$



- Evals are stored in **archive**

$\mathcal{A} = ((\lambda^{(1)}, c(\lambda^{(1)})), (\lambda^{(2)}, c(\lambda^{(2)})), \dots)$ , with  
 $\mathcal{A}^{[t+1]} = \mathcal{A}^{[t]} \cup (\lambda^+, c(\lambda^+))$ .

- We can define tuner as function  $\tau : (\mathcal{D}, \mathcal{I}, \tilde{\Lambda}, \mathcal{J}, \rho) \mapsto \hat{\lambda}$

# WHY IS TUNING SO HARD?

- Tuning is usually **black box**: No derivatives of the objective are available. We can only eval the performance for a given HPC via a computer program (CV of learner on data).
- Every evaluation can require multiple train and predict steps, hence it's **expensive**.
- Even worse: the answer we get from that evaluation is **not exact, but stochastic** in most settings, as we use resampling.
- **Categorical and dependent hyperparameters** aggravate our difficulties: the space of hyperparameters we optimize over can have non-metric, complicated structure.
- Many standard optimization algorithms cannot handle these properties.

