## Introduction

This live script contains examples of reachable workspaces for 3D robots. For each example this includes:

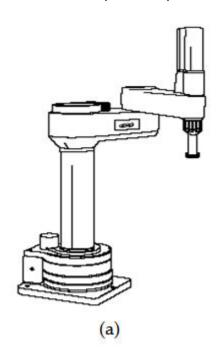
- DH Parameters
- Generated Workspace

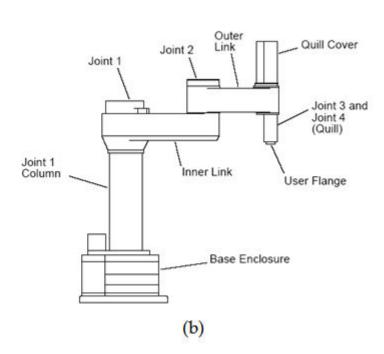
```
% Symbolic vars

syms thetal theta2 theta3 theta4 theta5 theta6 real
syms d1 d2 d3 d4 real
```

## Example 1 - AdeptThree Robot Arm

This is an example workspace search for the 4 DOF AdeptThree Robot Arm.

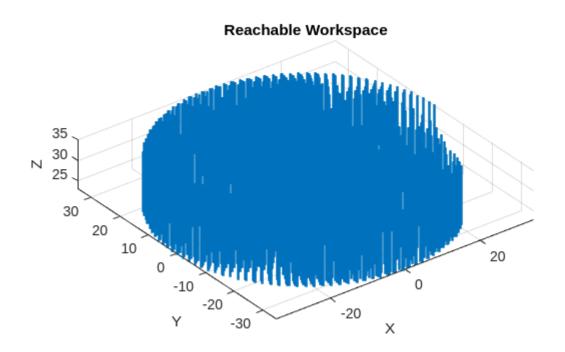




test\_dh =

```
\begin{pmatrix}
\frac{37}{2} & 0 & 42 & \theta_1 \\
16 & \pi & 0 & \theta_2 \\
0 & 0 & d_3 & 0 \\
0 & 0 & 7 & \theta_4
\end{pmatrix}
```

```
% Parameter ranges
theta1_range = arr2Rad(linspace(0,300, 50));
theta2_range = arr2Rad(linspace(0,300, 50));
d3_range = linspace(0,12, 50);
% Note the specification states 540°, but anything past 360° is redundant
theta4_range = arr2Rad(linspace(0,360, 50));
test_map = containers.Map({'theta1', 'theta2', 'd3','theta4'}, ...
    {theta1_range, theta2_range, d3_range, theta4_range});
% Workspace plotting function
plot3dworkspace(test_dh, test_map, @get_alternative_dh_transform)
```



## Example 2 - PUMA 560

This is an example using 6 DOF PUMA 560.

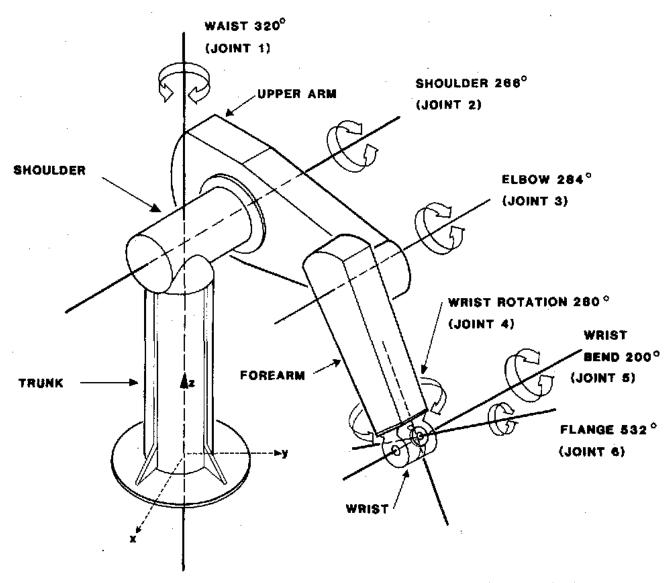


Fig. 1. PUMA 560 robot arm. Degrees of joint rotation and member identification.

test\_dh =

```
\begin{pmatrix}
0 & -\frac{\pi}{4} & 671 & \theta_1 \\
431 & 0 & 139 & \theta_2 \\
-20 & \frac{\pi}{4} & 0 & \theta_3 \\
0 & -\frac{\pi}{4} & 431 & \theta_4 \\
0 & \frac{\pi}{4} & 0 & \theta_5 \\
0 & 0 & 56 & \theta_6
\end{pmatrix}
```

% Parameter ranges

```
theta1_range = arr2Rad(linspace(-160,160,50));
theta2_range = arr2Rad(linspace(-225,45,50));
theta3_range = arr2Rad(linspace(-45,225,50));
theta4_range = arr2Rad(linspace(-110,170,5));
theta5_range = arr2Rad(linspace(-100,100,5));
theta6_range = arr2Rad(linspace(-180,180,5));
test_map = containers.Map({'theta1', 'theta2', 'theta3','theta4', 'theta5',
'theta6'}, ...
     {thetal_range, theta2_range, theta3_range, theta4_range, theta5_range,
theta6_range})
test_map =
 Map with properties:
      Count: 6
    KeyType: char
   ValueType: any
% Workspace plotting function + timing
```

plot3dworkspace(test\_dh, test\_map, @get\_alternative\_dh\_transform, true)

final transformation matrix from base to end-effector:

$$\begin{pmatrix}
-\sin(\theta_{6}) \, \sigma_{3} - \cos(\theta_{6}) \, \sigma_{8} & \sin(\theta_{6}) \, \sigma_{8} - \cos(\theta_{6}) \, \sigma_{3} & \sigma_{10} - \sigma_{9} + \frac{\sqrt{2} \, \sin(\theta_{5}) \, \sigma_{17}}{2} & 431 \cos(\theta_{1}) \cos(\theta_{2}) - \sigma_{2} - 2 \\
-\sin(\theta_{6}) \, \sigma_{4} - \cos(\theta_{6}) \, \sigma_{7} & \sin(\theta_{6}) \, \sigma_{7} - \cos(\theta_{6}) \, \sigma_{4} & \sigma_{12} - \sigma_{11} + \frac{\sqrt{2} \, \sin(\theta_{5}) \, \sigma_{16}}{2} & \sigma_{2} + 431 \cos(\theta_{2}) \sin(\theta_{1}) - 2 \\
\sin(\theta_{6}) \, \sigma_{5} - \cos(\theta_{6}) \, \sigma_{6} & \sin(\theta_{6}) \, \sigma_{6} + \cos(\theta_{6}) \, \sigma_{5} & \sigma_{13} - \sigma_{14} - \frac{\sqrt{2} \, \sin(\theta_{5}) \, \sigma_{15}}{2} & \frac{431 \cos(\theta_{2}) \sin(\theta_{3})}{2} - \frac{431}{2} \\
0 & 0 & 0
\end{pmatrix}$$

where

$$\sigma_1 = \frac{139 \sqrt{2} \sin(\theta_1)}{2}$$

$$\sigma_2 = \frac{431 \sin(\theta_1)}{2}$$

$$\sigma_3 = \sigma_9 + \sigma_{10} + \frac{\sqrt{2} \cos(\theta_5) \, \sigma_{17}}{2}$$

$$\sigma_4 = \sigma_{11} + \sigma_{12} + \frac{\sqrt{2} \cos(\theta_5) \sigma_{16}}{2}$$

$$\sigma_5 = \sigma_{13} + \sigma_{14} + \frac{\sqrt{2} \cos(\theta_5) \sigma_{15}}{2}$$

$$\sigma_6 = \cos(\theta_5) \, \sigma_{23} - \sin(\theta_5) \, \sigma_{15}$$

$$\sigma_7 = \sin(\theta_5) \, \sigma_{16} - \cos(\theta_5) \, \sigma_{21}$$

$$\sigma_8 = \sin(\theta_5) \, \sigma_{17} - \cos(\theta_5) \, \sigma_{19}$$

$$\sigma_9 = \frac{\sqrt{2} \sigma_{18}}{2}$$

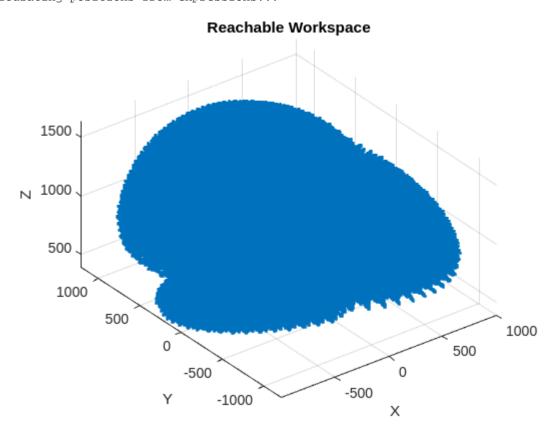
$$\sigma_{10} = \frac{\sqrt{2} \sin(\theta_5) \, \sigma_{19}}{2}$$

$$\sigma_{11} = \frac{\sqrt{2} \sigma_{20}}{2}$$

$$\sigma_{12} = \frac{\sqrt{2} \sin(\theta_5) \sigma_{21}}{2}$$

$$\sigma_{13} = \frac{\sqrt{2} \sigma_{22}}{2}$$

```
expressions for position:  x = 431*\cos(\text{theta1})*\cos(\text{theta2}) - (431*\sin(\text{theta1}))/2 - 20*\cos(\text{theta3})*(\cos(\text{theta1})*\cos(\text{theta2}) - (2^{(1/2)})/2 + (431*\sin(\text{theta1}))/2 + (431*\cos(\text{theta2})*\sin(\text{theta1}) - 20*\cos(\text{theta3})*(\cos(\text{theta2})*\sin(\text{theta1}) + (2^{(1/2)})/2 + (431*\cos(\text{theta3}))/2 + (139*2^{(1/2)})/2 - (431*2^{(1/2)})*\sin(\text{theta3})/2 + (139*2^{(1/2)})/2 - (431*2^{(1/2)})*\sin(\text{theta3})/2 + (139*2^{(1/2)})/2 - (131*2^{(1/2)})*\sin(\text{theta3})/2 + (139*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/2 - (131*2^{(1/2)})/
```



```
% A somewhat convoluted PDF export procedure to save a PDF of the .mlx file
% for github. You can ignore this.
file_name = 'plot3dworkspace_examples';
current_mlx = which(file_name);
[path_to_file, name, ext] = fileparts(current_mlx);
mlx_path = fullfile(path_to_file, (file_name + ".mlx"));
pdf_path = fullfile(path_to_file, (file_name + ".pdf"));
export(mlx_path, pdf_path);
```

```
function out = arr2Rad(A)
   out = arrayfun(@(angle) deg2rad(angle), A);
end

function T = get_alternative_dh_transform(a,alpha,d,theta)
T = [cos(theta) -cos(alpha)*sin(theta) sin(alpha)*sin(theta) a*cos(theta)
   sin(theta) cos(alpha)*cos(theta) -sin(alpha)*sin(theta) a*sin(theta)
   0 sin(alpha) cos(alpha) d
   0 0 0 1];
```