

Memory Size in the Prisoner's Dilemma

Nikoleta E. Glynatsi



Dr. Vincent KNIGHT

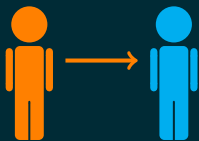
Dr. Jonathan GILLARD

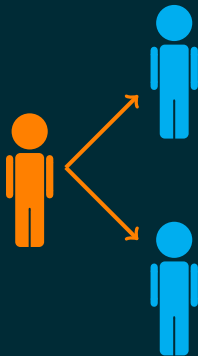
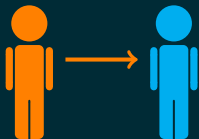


	C	D
C	3, 3	0, 5
D	5, 0	1, 1



William H. Press and Freeman J. Dyson. Iterated Prisoner's Dilemma contains strategies that dominate any evolutionary opponent. 2012





**WHICH IS THE BEST MEMORY ONE
STRATEGY?**

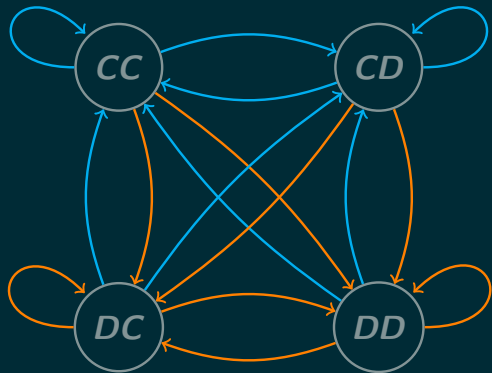
**ARE THERE LIMITATIONS TO MEMORY ONE
STRATEGIES?**

**WHICH IS THE BEST MEMORY ONE
STRATEGY?**

**ARE THERE LIMITATIONS TO MEMORY ONE
STRATEGIES?**



$$p = (p_1, p_2, p_3, p_4) \in \mathbb{R}_{[0,1]}^4$$



$$\max_p u_q(p) \text{ such that } p \in \mathbb{R}_{[0,1]}^4$$

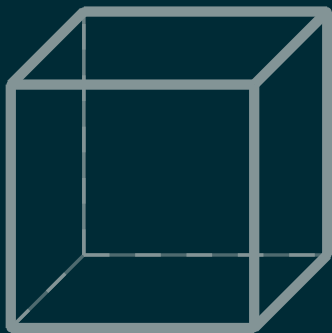
Theorem

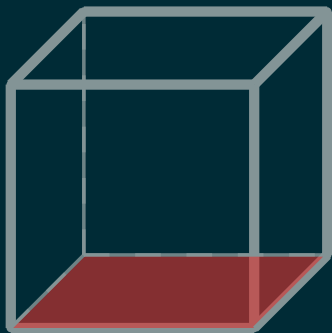
$$u_q(p) = \frac{\frac{1}{2}pQp^T + c^T p + a}{\frac{1}{2}p\bar{Q}p^T + \bar{c}^T p + \bar{a}}$$

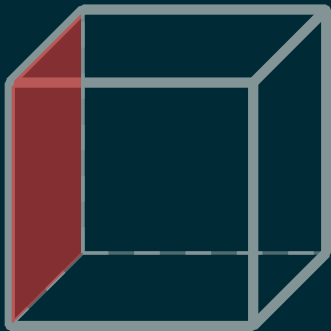
- ▶ $Q, \bar{Q} \in \mathbb{R}^{4 \times 4}$
- ▶ $c, \bar{c} \in \mathbb{R}^{4 \times 1}$
- ▶ $a, \bar{a} \in \mathbb{R}$

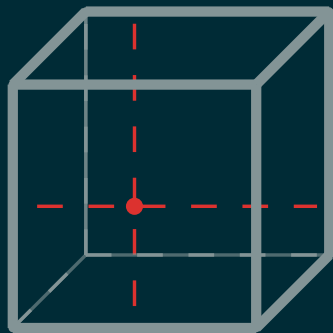










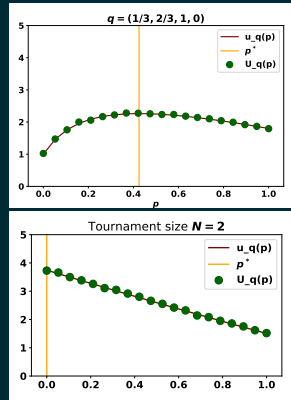


PURELY RANDOM

$$p = (p, p, p, p)$$

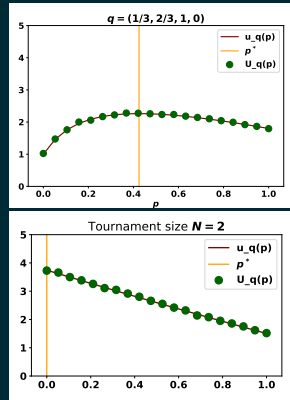
$$S_q = U_{i=1}^{2N} \lambda_i \cup \{0, 1\}$$

$$1 \leq |S_{q(i)}| \leq 2N + 2$$



$$S_q = U_{i=1}^{2N} \lambda_i \cup \{0, 1\}$$

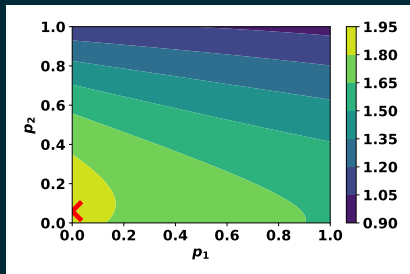
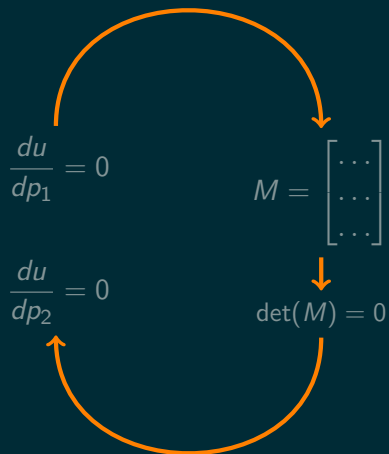
$$1 \leq |S_{q(i)}| \leq 2N + 2$$

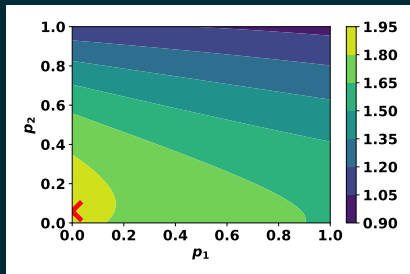
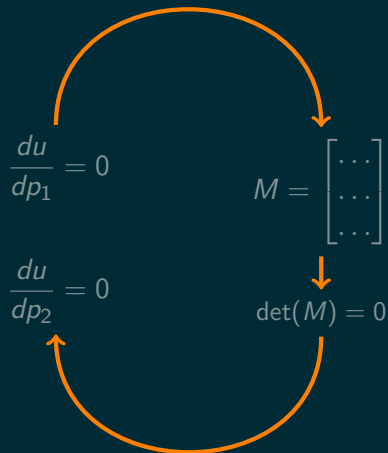


Result: optimal behaviour using eigenvalues of companion matrix

REACTIVE

$$p = (p_1, p_2, p_1, p_2)$$





**Result: optimal behaviour using Sylvester's resultant
(Sylvester 1840)**

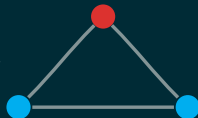
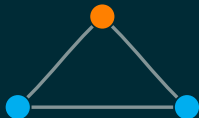
MEMORY ONE



	q_1	q_2	q_3	q_4	p_1	p_2	p_3	p_4	u_q	U_q
0	0.208	0.481	0.420	0.859	0.603	0.435	0.0	0.0	3.494	3.467
1	0.781	0.692	0.969	0.032	0.000	0.000	0.0	1.0	3.266	3.328
2	0.546	0.964	0.063	0.383	0.389	0.491	0.0	0.0	4.659	4.544
3	0.930	0.381	0.665	0.999	0.145	0.480	0.0	0.0	3.470	3.454
4	0.309	0.129	0.346	0.770	0.566	0.039	0.0	0.0	2.878	2.886

**WHICH IS THE BEST MEMORY ONE
STRATEGY?**

**ARE THEIR LIMITATIONS TO MEMORY ONE
STRATEGIES?**



— memory one strategy

— complex strategy

	q_1	q_2	q_3	q_4	\bar{q}_1	\bar{q}_2	\bar{q}_3	\bar{q}_4	ρ_1	ρ_2	ρ_3	ρ_4	u_q	U_q	U_G
1	0.548	0.715	0.602	0.544	0.545	0.171	0.852	0.180	0.0	0.0	0.0	0.317	2.694	2.662	2.723
3	0.548	0.715	0.602	0.544	0.545	0.171	0.852	0.180	0.0	0.0	0.0	0.427	2.692	2.662	2.796
5	0.548	0.715	0.602	0.544	0.545	0.171	0.852	0.180	0.0	0.0	0.0	0.427	2.692	2.662	2.915
7	0.548	0.715	0.602	0.544	0.545	0.171	0.852	0.180	0.0	0.0	0.0	0.427	2.692	2.662	2.915
9	0.548	0.715	0.602	0.544	0.545	0.171	0.852	0.180	0.0	0.0	0.0	0.427	2.692	2.662	2.915



This repository

Search

Pull requests

Issues

Marketplace

Explore



sympy / sympy

Unwatch

316

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4,837

Fork

2,285

< Code

Issues 2,763

Pull requests 560

Projects 0

Wiki

Insights

implementation of multivariate resultants. #14370

Edit

Merged

jksuom merged 19 commits into sympy:master from nikoleta-v3:multivariate-resultants on 30 Mar

Conversation 63

Commits 19

Checks 0

Files changed 6

+3,033 -0



Nikoleta-v3 commented on 2 Mar

Contributor



Brief description

Adds a new file `multivariate_resultants` that contains two classes.

These classes are implementations of the following multivariate resultants:

- Dixons
- Macaulay

They are a natural follow up from the resultants implemented withing the library:

- `subresultants_qq_zz.py`

Resultants are used to identify if polynomials have common roots. The multivariate version is for multivariate systems.

Other comments

Tests have been implemented and are currently passing. I added relevant literature and some notebooks with examples in the `example/notebooks/` directory.

References to other Issues or PRs

Reviewers

asmeurer

smichr

jksuom

normalhuman

Assignees

No one assigned

Labels

PR: sympy's turn

Projects

None yet

Milestone

No milestone

Limitations of memory size on the Iterated Prisoner's dilemma. (In preparation)

@NikoletaGlyn

<https://github.com/Nikoleta-v3>