ETH Zurich Institut für Theoretische Informatik Prof. Dr. Angelika Steger

Prof. Dr. Emo Welzl Prof. Dr. Peter Widmayer

## **Algorithms Lab**

## **Exercise** – *Monkey Island*

Remember the old LucasArts adventure *The Secret of Monkey Island*? You have been elected as the new governor of Monkey Island<sup>TM</sup> and it is time to make good on your campaign promises. One of these promises was to finally rid the island of its severe piracy problem by building police stations at strategic locations.

However, this is complicated by the fact that some roads in the dense jungle on the island do not actually work both ways (those of you who actually played the game might remember this). Additionally, building police stations is not free, and for every location there is an associated cost for building a police station there.

Thus your goal is the following: choose locations at which to build police stations such that (1) every location is reachable from some police station by following the roads and (2) the total cost of building the police stations is minimized.

**Input** The first line of the input contains the number of test cases  $t \le 60$ . Each of the t test cases is described as follows.

- It starts with a line containing the number of locations  $n \le 1000$  and the number of roads  $m \le 5000$ .
- Then m lines follow, each containing two numbers  $1 \le i, j \le n$ , representing a directed road from the i-th to the j-th location.
- The last line contains costs  $c_1, \ldots, c_n$  of building a station in the respective locations. You may assume  $0 \le c_i \le 100$  for every  $i \in \{1, \ldots, n\}$ .

**Output** For every test case you should output the minimum cost needed to build police stations such that every location is reachable (via roads) from some police station.

**Points** There are three groups of test sets. The individual points are specified below; the total number of points is 100.

- 1. For the first group of test sets, worth 20 points, you may assume that  $n \le 50$ .
- 2. For the second group of test sets, worth 30 points, you may assume that  $n \leq 200$ .
- 3. For the third group of test sets, worth 50 points, there are no additional assumptions.

## **Sample Input**

1 1 1

## Sample Output

1 2